

Semester projects

Principles of Complex Systems
CSYS/MATH 300, Spring, 2013

Prof. Peter Dodds
@peterdodds

Department of Mathematics & Statistics | Center for Complex Systems |
Vermont Advanced Computing Center | University of Vermont



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Narrative hierarchy

Presenting at many scales:

- ▶ 1 to 3 word encapsulation, a soundbite,
- ▶ a sentence/title,
- ▶ a few sentences,
- ▶ a paragraph,
- ▶ a short paper,
- ▶ a long paper,
- ▶ ...

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Outline

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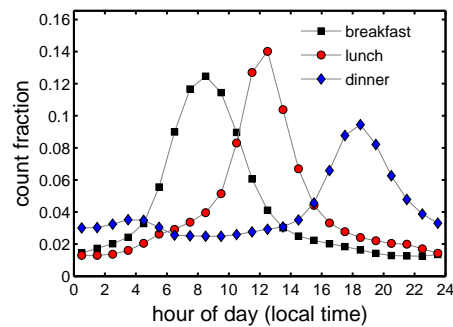
Requirements:

1. 3 minute introduction to project (5th week).
2. 5-10 minute final presentation.
3. Report: ≥ 5 pages (single space), journal-style

Goals:

- ▶ Understand, critique, and communicate published work.
- ▶ Seed research papers or help papers along.

Twitter—living in the now:



- ▶ Research opportunity: be involved in our socio-info-algorithmic-econo-geo-technico-physical systems research group studying Twitter and other wordful large data sets.

topics:

- ▶ Develop and elaborate an **online experiment** to study some aspect of **social phenomena**
- ▶ e.g., collective search, cooperation, cheating, influence, creation, decision-making, etc.
- ▶ Part of the PLAY project.

topics:

Rummage round in the [papers](#) (田) we've covered in our weekly Complex Systems Reading Group at UVM.

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Sociotechnical phenomena—Foldit:

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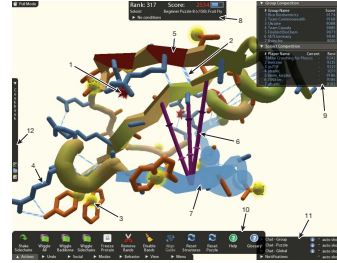


Figure 1 **Foldit** screenshot illustrating tools and visualizations. The visualizations include a chain representing atoms that are too close (arrow 1); a hydrogen bond (arrow 2); a hydrophobic side chain with a yellow blob because it is exposed (arrow 3); a hydrophilic side chain (arrow 4); and a segment of the backbone that is red due to high residue energy (arrow 5). The players can make modifications including "rubber bands" (arrow 6), which add constraints to guide automated tools, and "freezing" (arrow 7), which

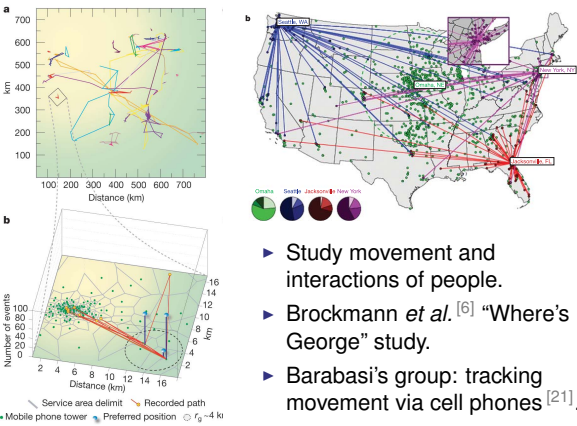
prevents degrees of freedom from changing. The user interface includes information about the player's current status, including score (arrow 8); a leader board (arrow 9), which shows the scores of other players and groups; toolbars for accessing tools and options (arrow 10); chat for interacting with other players (arrow 11) and a "cookbook" for making new automated tools or "recipes" (arrow 12).

- ▶ "Predicting protein structures with a multiplayer online game." Cooper et al., *Nature*, 2010. [14]
- ▶ Also: [zooniverse](#) (田), [ESP game](#) (田), [captchas](#) (田).



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topics:



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topics:

Explore "Catastrophic cascade of failures in interdependent networks" [7]. Buldyrev et al., *Nature* 2010.

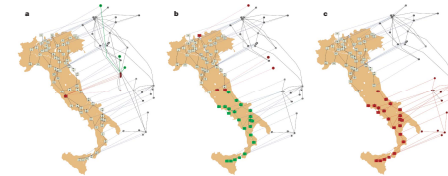


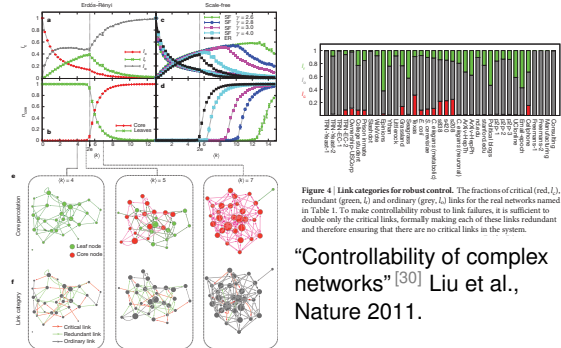
Figure 1 **Modeling a blackout in Italy**. Illustration of an iterative process of a cascade of failures using real-world data from a power network (located on the map of Italy) and an Internet network (sketched above the map) that were implicated in an electrical blackout that occurred in Italy in September 2009. The networks are drawn using the real geographical locations and every Internet server is connected to the geographically nearest power station. **a** One power station is removed (red node on map) from the power network and as a result the Internet nodes depending on it are removed (red nodes on map) as well as the nodes in the Internet network that depend on them (red nodes above map).

at the next step are marked in green. **b**. Additional nodes that were disconnected from the Internet communication network giant component are removed (red nodes above map). As a result the power stations depending on them are removed from the power network (red nodes on map). Again, the nodes that will be disconnected from the giant cluster at the next step are marked in green. **c**. Additional nodes that were disconnected from the giant component of the power network are removed (red nodes on map) as well as the nodes in the Internet network that depend on them (red nodes above map).



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topics:



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Voting

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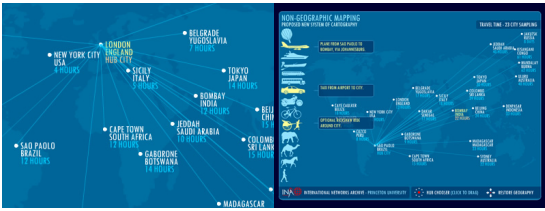
Score-based voting versus rank-based voting:

- ▶ Balinski and Laraki [2] "A theory of measuring, electing, and ranking" *Proc. Natl. Acad. Sci.*, pp. 8720–8725 (2007)



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The madness of modern geography:



- ▶ Explore distances between points on the Earth as travel times.
- ▶ See Jonathan Harris's work [here](#) (田) and [here](#) (田).

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topics:

- ▶ Explore general theories on system robustness.
- ▶ Are there **universal signatures** that presage system failure?
- ▶ See "Early-warning signals for critical transitions" Scheffer et al., Nature 2009. [35]
- ▶ "Although predicting such critical points before they are reached is extremely difficult, work in different scientific fields is now suggesting the existence of generic early-warning signals that may indicate for a wide class of systems if a critical threshold is approaching."
- ▶ Later in class: Doyle et al., robust-yet-fragile systems

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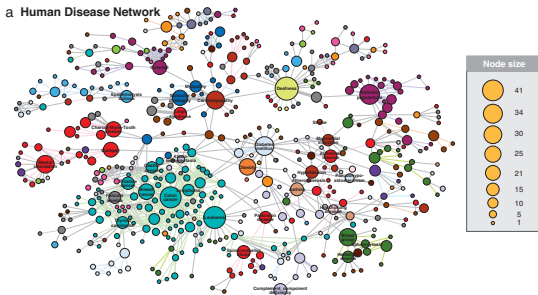
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topics:

- ▶ Study the human disease and disease gene networks (Goh et al., 2007):



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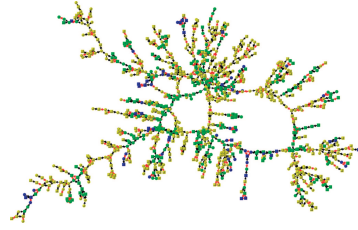
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topics:

Explore and critique Fowler and Christakis et al. work on social contagion of:



- ▶ Obesity [10]
- ▶ Smoking cessation [11]
- ▶ Happiness [19]
- ▶ Loneliness [8]

Figure 1. Contagion clusters in the Framingham Social Network. The graph shows the largest component of friends, spouses, and siblings at Fram 7 centered on the year 2000. There are 1079 individuals shown. Each node represents an individual, and the edges represent dyads (i.e. two individuals) who are friends, spouses or siblings. Nodes indicate relationships and the edges represent (i.e. two individuals) who are friends, spouses or siblings. Node color denotes the mean number of days the focal participant and all directly connected (degree 1) social participants felt lonely in the past week, with colors being 0-1 days, green being 2 days, and blue being greater than 7 days or more. The graph regions showing no contagion and a relationship between being perceived and feeling lonely, both of which are confirmed by statistical models discussed in the main text.

One of many questions:

How does the (very) sparse sampling of a real social network affect their findings?

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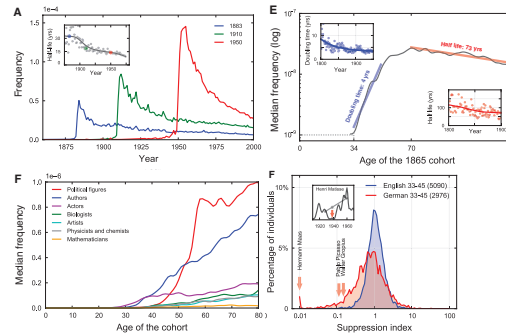
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Culturomics:

"Quantitative analysis of culture using millions of digitized books" by Michel et al., Science, 2011 [31]



<http://www.culturomics.org/> (田)
Google Books ngram viewer (田)

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topics:

The problem of missing data in networks:

- ▶ Clauset et al. (2008)
"Hierarchical structure and the prediction of missing links in networks" [12]
- ▶ Kossinets (2006)
"Effects of missing data in social networks" [28]

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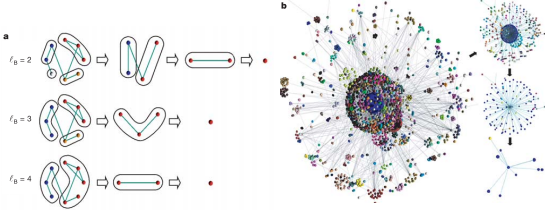
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topics:

- ▶ Explore “self-similarity of complex networks” [36, 37]
First work by Song *et al.*, Nature, 2005.
- ▶ See accompanying comment by Strogatz [38]
- ▶ See also “Coarse-graining and self-dissimilarity of complex networks” by Itzkovitz *et al.* [2]



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topics:

“Looking at Gielen’s work, it’s tempting to propose a new branch of the human sciences: geometric sociology, a study of nothing but the shapes our inhabited spaces make. Its research agenda would ask why these forms, angles and geometries emerge so consistently, from prehistoric settlements to the fringes of exurbia. Are sites like these an aesthetic pursuit, a mathematical accident, a calculated bending of property lines based on glitches in the local planning code or an emergent combination of all these factors? Or are they the expression of something buried deep in human culture and the unconscious, something only visible from high above?”

<http://opinionator.blogs.nytimes.com/2011/05/12/the-geometry-of-sprawl/> (田)

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topics:

Related papers:

- ▶ “Origins of fractality in the growth of complex networks”
Song *et al.* (2006a) [37]
- ▶ “Skeleton and Fractal Scaling in Complex Networks”
Go *et al.* (2006a) [20]
- ▶ “Complex Networks Renormalization: Flows and Fixed Points”
Radicchi *et al.* (2008a) [34]

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topics:

- ▶ Study collective creativity arising out of social interactions
- ▶ Productivity, wealth, creativity, disease, etc. appear to increase superlinearly with population
- ▶ Start with Bettencourt *et al.*’s “Growth, innovation, scaling, and the pace of life in cities” [4]

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topics:

- ▶ Explore patterns, designed and undesigned, of cities and suburbs.



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topics:

- ▶ **Physics/Society—Wars:** Study work that started with Lewis Richardson’s “Variation of the frequency of fatal quarrels with magnitude” in 1949.
- ▶ Specifically explore Clauset *et al.* and Johnson *et al.*’s work [13, 25, 5] on terrorist attacks and civil wars
- ▶ Richardson bonus: Britain’s coastline, turbulence, weather prediction, ...

$$\frac{M_x}{M} = \frac{1}{N} + \frac{(1-x)}{N^2} \sum_{j=1}^{x-1} j^2 N_j$$

$$= \frac{2(1-x)}{N^2} \sum_{j=1}^{x-1} j N_j$$

$$= \frac{2(1-x)}{N^2} \sum_{j=1}^{x-1} j^2 N_j$$

$$= \frac{2(1-x)}{N^2} \sum_{j=1}^{x-1} j^2 N_j$$

$$R_x \sim x^{D-2}$$

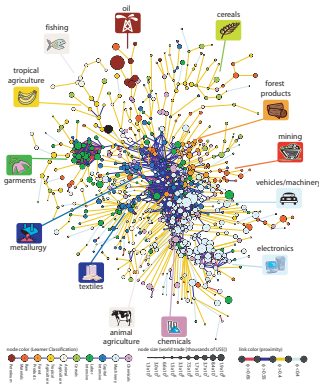
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topics:

- ▶ Study Hidalgo et al.'s "The Product Space Conditions the Development of Nations" [23]
- ▶ How do products depend on each other, and how does this network evolve?
- ▶ How do countries depend on each other for water, energy, people (immigration), investments?



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topics:

- ▶ Study scientific collaboration networks.
- ▶ Mounds of data + good models.
- ▶ See seminal work by De Solla Price [33], plus modern work by Redner, Newman, et al.
- ▶ We will study some of this in class...

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topics:

- ▶ Explore Dunbar's number (田)
- ▶ See here (田) and here (田) for some food for thought regarding large-scale online games and Dunbar's number. [http://www.lifewithalacrity.com (田)]
- ▶ Recent work: "Network scaling reveals consistent fractal pattern in hierarchical mammalian societies" Hill et al. (2008) [24].

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topics:

- ▶ Study Kearns et al.'s experimental studies of people solving classical graph theory problems [27]
- ▶ "An Experimental Study of the Coloring Problem on Human Subject Networks"
- ▶ (Possibly) Run some of these experiments for our class.

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Study networks and creativity:

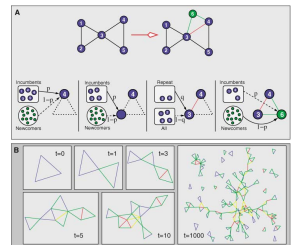


Fig. 2. Modeling the emergence of collaboration networks in creative enterprises. (A) Creation of a team with $m = 3$ agents. Consider, at time zero, a collaboration network comprising five agents, all incumbents (black circles). Along with the incumbents, there is a large pool of newcomers (green circles) available to participate in new teams. Each agent in a team has a probability of being drawn from the pool of newcomers and a probability $1 - p$ of being drawn from the pool of newcomers already in the team. (B) Observations, in order, of the evolution of the network. For convenience, let us assume that incumbent 4 is selected as the first agent in the new team (bottom box). Let us also assume that the second agent in an incumbent team (bottom-left box) is, in this example, the second agent in a past collaborator of agent 4, specifically agent 3 (center-right box). Lastly, the third agent is selected from the pool of newcomers; the agent becomes incumbent 2 (rightmost box). In these boxes and in the following panels and figures, blue lines indicate mesostructure-mesomorph collaboration, green lines indicate mesomorph-incident collaboration, yellow lines indicate new incumbent-incident collaborations, and red lines indicate repeat collaborations. (C) Time evolution of the network of collaborations according to the model for $p = 0.5$, $\alpha = 0.5$, and $m = 3$.

- ▶ Guimerà et al., Science 2005: [22] "Team Assembly Mechanisms Determine Collaboration Network Structure and Team Performance"
- ▶ Broadway musical industry
- ▶ Scientific collaboration in Social Psychology, Economics, Ecology, and Astronomy.

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topics:

- ▶ Study collective tagging (or folksonomy)
- ▶ e.g., del.icio.us, flickr
- ▶ See work by Bernardo Huberman et al. at HP labs.

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topics:

- ▶ Study games (as in game theory) on networks.
- ▶ For cooperation: Review Martin Nowak's piece in Science, "Five rules for the evolution of cooperation."^[32] and related works.
- ▶ Much work to explore: voter models, contagion-type models, etc.

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topics:

- ▶ Critically explore Bejan's Constructal Theory.
- ▶ See Bejan's book "Shape and Structure, from Engineering to Nature."^[3]
- ▶ Bejan asks why we see branching network flow structures so often in Nature—trees, rivers, etc.
- ▶ Read and critique "Historical Dynamics: Why States Rise and Fall" by Peter Turchin.^[39]
- ▶ Can history [Clyodynamics](#) (田), [Psychohistory](#) (田), ...
- ▶ "[Big History](#)" (田)
- ▶ Arbesman: "The life-spans of Empires"^[1]
- ▶ Also see "[Secular Cycles](#)" (田).

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topics:

- ▶ **Semantic networks**: explore word-word connection networks generated by linking semantically related words.
- ▶ Also: Networks based on morphological or phonetic similarity.
- ▶ More general: Explore [language evolution](#)
- ▶ One paper to start with: "The small world of human language" by Ferrer i Cancho and Solé^[18]
- ▶ Study spreading of neologisms.
- ▶ Examine new words relative to existing words—is there a pattern? Phonetic and morphological similarities.
- ▶ **Crazy**: Can new words be predicted?
- ▶ Use Google Books n-grams as a data source.

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topics:

- ▶ Explore work by Doyle, Alderson, et al. as well as Pastor-Satorras et al. on the structure of the [Internet\(s\)](#).

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topics:

- ▶ Explore proposed measures of system complexity.
- ▶ Study Stuart Kauffman's ***nk* boolean networks** which model regulatory gene networks^[26]

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topics:

- ▶ Review: Study Castronova's and others' work on massive multiplayer online games. How do social networks form in these games?^[9]
- ▶ See work by Johnson et al. on gang formation in the real world and in World of Warcraft (really!).

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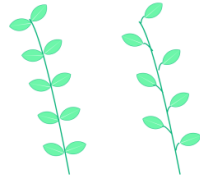
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topics:

- ▶ Study phyllotaxis (田), how plants grow new buds and branches.
- ▶ Some delightful mathematics appears involving the Fibonacci series.
- ▶ Excellent work to start with: "Phyllotaxis as a Dynamical Self Organizing Process: Parts I, II, and III" by Douady and Couder [15, 16, 17]



<http://andbug.blogspot.com/> (田)



Wikipedia (田)

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topics:

Vague/Large:

- ▶ Study how the Wikipedia's content is interconnected.



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topics:

Social networks:

- ▶ Study social networks as revealed by email patterns, Facebook connections, tweets, etc.
- ▶ "Empirical analysis of evolving social networks" Kossinets and Watts, Science, Vol 311, 88-90, 2006. [29]
- ▶ "Inferring friendship network structure by using mobile phone data" Eagle, et al., PNAS, 2009.
- ▶ "Community Structure in Online Collegiate Social Networks" Traud et al., 2008. <http://arxiv.org/abs/0809.0690> (田)

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topics:

More Vague/Large:

- ▶ How do countries depend on each other for water, energy, people (immigration), investments?
- ▶ How is the media connected? Who copies whom?
- ▶ (Problem: Need to be able to measure interactions.)
- ▶ Investigate memetics, the 'science' of memes.
- ▶ <http://memetracker.org/> (田)
- ▶ Sport...

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topics:

Vague/Large:

- ▶ Study amazon's recommender networks.

Customers Who Bought This Item Also Bought



See work by Sornette *et al.*

- ▶ Vague/Large: Study Netflix's open data (movies and people form a bipartite graph).

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topics:

More Vague/Large:

- ▶ How does **advertising** work collectively?
- ▶ Does one car manufacturers' ads indirectly help other car manufacturers?
- ▶ Ads for junk food versus fruits and vegetables.
- ▶ Ads for cars versus bikes versus walking.

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topics:

More Vague/Large:

- ▶ Study spreading of anything where influence can be measured (very hard).
- ▶ Study any interesting micro-macro story to do with evolution, biology, ethics, religion, history, food, international relations, ...
- ▶ Data is key.

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Alone in the crowd: The structure and spread of loneliness in a large social network.
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Synthetic Worlds: The Business and Culture of Online Games.
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- [5] J. C. Bohorquez, S. Gourley, A. R. Dixon, M. Spagat, and N. F. Johnson.
Common ecology quantifies human insurgency.
[Nature](#), 462:911–914, 2009. pdf (田)
- [6] D. Brockmann, L. Hufnagel, and T. Geisel.
The scaling laws of human travel.
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