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Contagion

A confusion of contagions:

- Was Harry Potter some kind of virus?
- What about the Da Vinci Code?
- Did Sudoku spread like a disease?
- Language?
- Religion?
- Democracy...?

Social contagion

Optimism according to Ambrose Bierce: (⊞)

The doctrine that everything is beautiful, including what is ugly, everything good, especially the bad, and everything right that is wrong. ... It is hereditary, but fortunately not contagious.



Social contagion

Eric Hoffer, 1902–1983

There is a grandeur in the uniformity of the mass. When a fashion, a dance, a song, a slogan or a joke sweeps like wildfire from one end of the continent to the other, and a hundred million people roar with laughter, sway their bodies in unison, hum one song or break forth in anger and denunciation, there is the overpowering feeling that in this country we have come nearer the brotherhood of man than ever before.

► Hoffer (⊞) was an interesting fellow...

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The spread of fanaticism

Hoffer's acclaimed work: "The True Believer:

Thoughts On The Nature Of Mass Movements" (1951)^[3]

Quotes-aplenty:

Imitation

- "We can be absolutely certain only about things we do not understand."
- "Mass movements can rise and spread without belief in a God, but never without belief in a devil."
- "Where freedom is real, equality is the passion of the masses. Where equality is real, freedom is the passion of a small minority."



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Contagion

Definitions

- (1) The spreading of a quality or quantity between individuals in a population.
- (2) A disease itself: the plague, a blight, the dreaded lurgi, ...
- from Latin: con = 'together with' + tangere 'to touch.'
- Contagion has unpleasant overtones...
- Just Spreading might be a more neutral word
- But contagion is kind of exciting...



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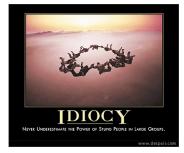
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The collective...

despair.com



JFORMI

despair.com

"Never Underestimate the Power of Stupid People in Large Groups."

"When people are free

to do as they please,

they usually imitate

each other." -Eric Hoffer "The Passionate State

of Mind"^[4]





del output

Two main classes of contagion 1. Infectious diseases: tuberculosis, HIV, ebola, SARS, influenza, ...

2. Social contagion: fashion, word usage, rumors, riots, religion, ...

► Viral get-out-the-vote video. (⊞)

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Examples of non-disease spreading:

Interesting infections:

- ► Spreading of buildings in the US... (⊞)















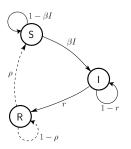
Mathematical Epidemiology

The standard SIR model^[8]

- = basic model of disease contagion
- Three states:
 - 1. S = Susceptible
 - 2. I = Infective/Infectious
 - 3. R = Recovered or Removed or Refractory
- ► S(t) + I(t) + R(t) = 1
- Presumes random interactions (mass-action principle)
- Interactions are independent (no memory)
- Discrete and continuous time versions

Mathematical Epidemiology

Discrete time automata example:



Transition Probabilities:

 β for being infected given contact with infected r for recovery ρ for loss of immunity

Mathematical Epidemiology

Original models attributed to

- ▶ 1920's: Reed and Frost
- ▶ 1920's/1930's: Kermack and McKendrick^[5, 7, 6]
- Coupled differential equations with a mass-action principle



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resulting from a single initial infective

 β , r, and ρ are now rates.

Reproduction Number R₀:

• Epidemic threshold: If $R_0 > 1$, 'epidemic' occurs.

 \triangleright R₀ = expected number of infected individuals



Reproduction Number R_0

Discrete version:

- Set up: One Infective in a randomly mixing population of Susceptibles
- At time t = 0, single infective random bumps into a Susceptible
- Probability of transmission = β
- At time t = 1, single Infective remains infected with probability 1 - r
- At time t = k, single Infective remains infected with probability $(1 - r)^k$

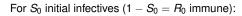
Reproduction Number R_0

Discrete version:

Expected number infected by original Infective:

$$R_0 = \beta + (1-r)\beta + (1-r)^2\beta + (1-r)^3\beta + .$$
$$= \beta \left(1 + (1-r) + (1-r)^2 + (1-r)^3 + ... \right)$$

$$=\beta\frac{1}{1-(1-r)}=\beta/r$$



$$R_0 = S_0 \beta / r$$

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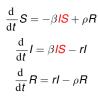




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Independent Interaction models

Differential equations for continuous model







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Independent Interaction models

For the continuous version

Second equation:

 $\frac{\mathrm{d}}{\mathrm{d}t}I = \beta SI - rI$ $\frac{\mathrm{d}}{\mathrm{d}t}I = (\beta S - r)I$

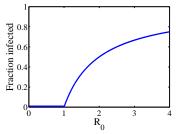
Number of infectives grows initially if

$$\beta S(0) - r > 0 \Rightarrow \beta S(0) > r \Rightarrow \beta S(0)/r > 1$$

Same story as for discrete model.

Independent Interaction models

Example of epidemic threshold:



- Continuous phase transition.
- Fine idea from a simple model.

Independent Interaction models

Many variants of the SIR model:

- SIS: susceptible-infective-susceptible
- SIRS: susceptible-infective-recovered-susceptible
- compartment models (age or gender partitions)
- more categories such as 'exposed' (SEIRS)
- recruitment (migration, birth)









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Size distributions

Disease spreading models

Can we predict the size of an epidemic?
 How important is the reproduction number *R*₀?

*R*₀ approximately same for all of the following:
1918-19 "Spanish Flu" ~ 500,000 deaths in US
1957-58 "Asian Flu" ~ 70,000 deaths in US

1968-69 "Hong Kong Flu" ~ 34,000 deaths in US
 2003 "SARS Epidemic" ~ 800 deaths world-wide

For novel diseases:

Size distributions are important elsewhere:

- earthquakes (Gutenberg-Richter law)
- city sizes, forest fires, war fatalities
- wealth distributions
- 'popularity' (books, music, websites, ideas)
- Epidemics?

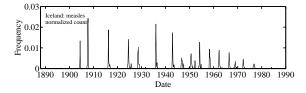
Power laws distributions are common but not obligatory...

Really, what about epidemics?

- Simply hasn't attracted much attention.
- Data not as clean as for other phenomena.

Feeling III in Iceland

Caseload recorded monthly for range of diseases in Iceland, 1888-1990



 Treat outbreaks separated in time as 'novel' diseases.



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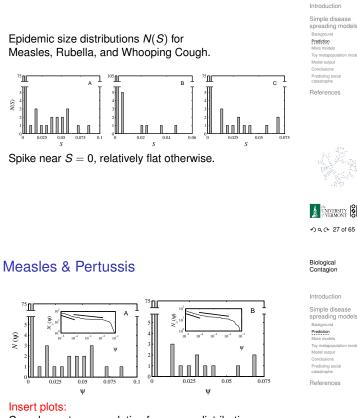
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Really not so good at all in Iceland



Complementary cumulative frequency distributions:

 $N(\Psi' > \Psi) \propto \Psi^{-\gamma+1}$

Limited scaling with a possible break.

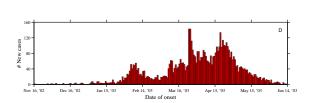
Power law distributions

Measured values of γ :

- measles: 1.40 (low Ψ) and 1.13 (high Ψ)
- pertussis: 1.39 (low Ψ) and 1.16 (high Ψ)
- Expect $2 \le \gamma < 3$ (finite mean, infinite variance)
- When $\gamma < 1$, can't normalize
- Distribution is quite flat.

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Epidemic slows... then an infective moves to a new context.

- Epidemic discovers new 'pools' of susceptibles: Resurgence.
- Importance of rare, stochastic events.



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The challenge

- So... can a simple model produce 1. broad epidemic distributions
- and
- 2. resurgence?



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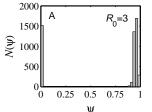
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Size distributions



This includes network models: random, small-world, scale-free, ...

- Exceptions:
 - 1. Forest fire models
 - 2. Sophisticated metapopulation models



Simple models

typically produce

size distributions.

bimodal or unimodal



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Burning through the population

Forest fire models: ^[9]

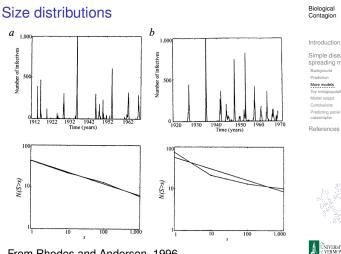
- Rhodes & Anderson, 1996
- ► The physicist's approach: "if it works for magnets, it'll work for people ... "

A bit of a stretch:

- 1. Epidemics \equiv forest fires spreading on 3-d and 5-d lattices.
- 2. Claim Iceland and Faroe Islands exhibit power law distributions for outbreaks.
- 3. Original forest fire model not completely understood.



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From Rhodes and Anderson, 1996.

Sophisticated metapopulation models

- Community based mixing: Longini (two scales).
- Eubank et al.'s EpiSims/TRANSIMS—city simulations.
- Spreading through countries—Airlines: Germann et al., Corlizza et al.
- Vital work but perhaps hard to generalize from...
- \blacktriangleright \Rightarrow Create a simple model involving multiscale travel
- Multiscale models suggested by others but not formalized (Bailey, Cliff and Haggett, Ferguson et al.)

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Size distributions

Very big question: What is N?

- Should we model SARS in Hong Kong as spreading in a neighborhood, in Hong Kong, Asia, or the world?
- For simple models, we need to know the final size • beforehand...



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Introduction

Improving simple models

Idea for social networks: incorporate identity.

Identity is formed from attributes such as:

- Geographic location
- Type of employment
- Age
- Recreational activities

Groups are crucial...

- formed by people with at least one similar attribute
- ► Attributes ⇔ Contexts ⇔ Interactions ⇔ Networks.^[11]



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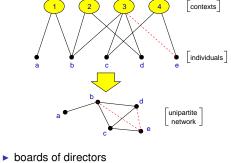




Simple disease spreading models

Improving simple models

Contexts and Identities-Bipartite networks





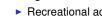




- movies
- transportation modes (subway)

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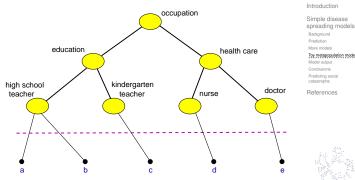
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Infer interactions/network from identities



Distance makes sense in identity/context space.

Generalized context space



Toy metapopulation mod

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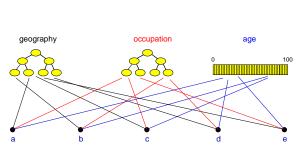
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(Blau & Schwartz^[1], Simmel^[10], Breiger^[2])

A toy agent-based model

Geography-allow people to move between

- Locally: standard SIR model with random mixing
- discrete time simulation

contexts:

- $\blacktriangleright \beta$ = infection probability
- γ = recovery probability
- P = probability of travel
- Movement distance: $Pr(d) \propto exp(-d/\xi)$
- ξ = typical travel distance



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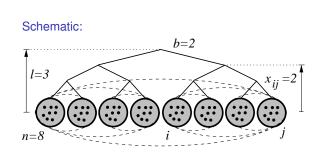
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A toy agent-based model



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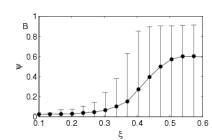
Define P₀ = Expected number of infected individuals

- Need $P_0 > 1$ for disease to spread (independent of R_0).
- Limit epidemic size by restricting frequency of travel and/or range



Model output

Varying ξ :



 Transition in expected final size based on typical movement distance (sensible)







leaving initially infected context.

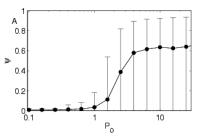


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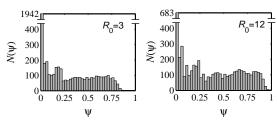
Model output

Varying P₀:



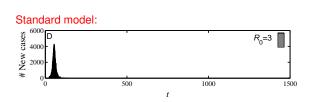
- Transition in expected final size based on typical number of infectives leaving first group (also sensible)
- Travel advisories: ξ has larger effect than P_0 .

Example model output: size distributions



- Flat distributions are possible for certain ξ and *P*.
- Different R₀'s may produce similar distributions
- Same epidemic sizes may arise from different R_0 's



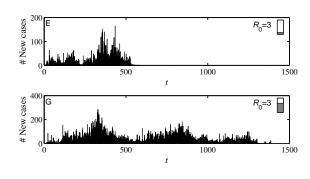






Model output—resurgence

Standard model with transport:



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The upshot

Simple multiscale population structure + stochasticity
leads to
resurgence + broad epidemic size distributions



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Conclusions

- For this model, epidemic size is highly unpredictable
- Model is more complicated than SIR but still simple
- We haven't even included normal social responses such as travel bans and self-quarantine.
- The reproduction number R_0 is not terribly useful.
- \triangleright R_0 , however measured, is not informative about 1. how likely the observed epidemic size was, 2. and how likely future epidemics will be.
- Problem: R₀ summarises one epidemic after the fact and enfolds movement, the price of bananas, everything.







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Conclusions

Disease spread highly sensitive to population structure

- Rare events may matter enormously (e.g., an infected individual taking an international flight)
- More support for controlling population movement (e.g., travel advisories, quarantine)

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Predicting social catastrophe isn't easy...

"Greenspan Concedes Error on Regulation"

- ...humbled Mr. Greenspan admitted that he had put too much faith in the self-correcting power of free markets ...
- "Those of us who have looked to the self-interest of lending institutions to protect shareholders' equity, myself included, are in a state of shocked disbelief"
- Rep. Henry A. Waxman: "Do you feel that your ideology pushed you to make decisions that you wish you had not made?"
- Mr. Greenspan conceded: "Yes, I've found a flaw. I don't know how significant or permanent it is. But I've been very distressed by that fact."

New York Times, October 23, 2008 (⊞)

Economics, Schmeconomics

"I've been dealing with these big

or changing to more euphoric,

mathematical models of forecasting the

If I could figure out a way to determine whether or not people are more fearful

Alan Greenspan (September 18, 2007):



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I could forecast the economy better than any way I know."



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Greenspan continues:

"The trouble is that we can't figure that out. I've been in the forecasting business for 50 years. I'm no better than I ever was, and nobody else is. Forecasting 50 years ago was as good or as bad as it is today. And the reason is that human nature hasn't changed. We can't improve ourselves."

▶ From the Daily Show (⊞) (September 18, 2007)

Jon Stewart:

"You just bummed the @*!# out of me."

► The full inteview is here (⊞).





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Valiant attempts to use SIR and co. elsewhere:

- Adoption of ideas/beliefs (Goffman & Newell, 1964)
- Spread of rumors (Daley & Kendall, 1965)
- Diffusion of innovations (Bass, 1969)
- Spread of fanatical behavior (Castillo-Chávez & Song, 2003)
- Spread of Feynmann diagrams (Bettencourt et al., 2006)

Need to separate movement from disease ▶ R₀ needs a friend or two.

• Need $R_0 > 1$ and $P_0 > 1$ and ξ sufficiently large for disease to have a chance of spreading

More wondering:

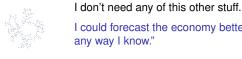
Conclusions

What to do:

- Exactly how important are rare events in disease spreading?
- ► Again, what is N?















economy ...

Economics, Schmeconomics

James K. Galbraith:

- NYT But there are at least 15,000 professional economists in this country, and you're saying only two or three of them foresaw the mortgage crisis? [JKG] Ten or 12 would be closer than two or three.
- NYT What does that say about the field of economics, which claims to be a science? [JKG] It's an enormous blot on the reputation of the profession. There are thousands of economists. Most of them teach. And most of them teach a theoretical framework that has been shown to be fundamentally useless.

From the New York Times, 11/02/2008 (\boxplus)

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