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Social Search

A small slice of the pie:

- Q. Can people pass messages between distant individuals using only their existing social connections?
- ► A. Apparently yes...

Handles:

The problem

- The Small World Phenomenon
- or "Six Degrees of Separation."

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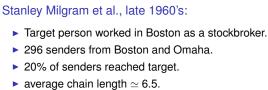
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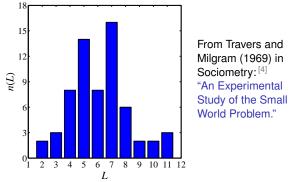






The problem

Lengths of successful chains:



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Some problems for people thinking about people?:

How are social networks structured?

- How do we define connections?
- How do we measure connections?
- (remote sensing, self-reporting)

What about the dynamics of social networks?

- How do social networks evolve?
- How do social movements begin?
- How does collective problem solving work?
- How is information transmitted through social networks?









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The problem



Two features characterize a social 'Small World':

- 1. Short paths exist
 - and
- 2. People are good at finding them.



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Social search-the Columbia experiment

- Milgram's participation rate was roughly 75%
- Email version: Approximately 37% participation rate.
- Probability of a chain of length 10 getting through:

$$.37^{10}\simeq 5 imes 10^{-5}$$

ightarrow 384 completed chains (1.6% of all chains).



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Social Search

Milgram's small world experiment with e-mail^[2]



Social search—the Columbia experiment

- 60,000+ participants in 166 countries
- 18 targets in 13 countries including
 - a professor at an Ivy League university,
 - an archival inspector in Estonia,
 - a technology consultant in India,
 - a policeman in Australia,
 - and
 - a veterinarian in the Norwegian army.
- > 24,000+ chains



- Motivation/Incentives/Perception matter.
- If target seems reachable \Rightarrow participation more likely.
- Small changes in attrition rates
- ▶ e.g., \ 15% in attrition rate \Rightarrow \nearrow 800% in completion rate







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Social search—the Columbia experiment

Successful chains disproportionately used

- weak ties (Granovetter)
- professional ties (34% vs. 13%)
- ties originating at work/college
- target's work (65% vs. 40%)

... and disproportionately avoided

- hubs (8% vs. 1%) (+ no evidence of funnels)
- family/friendship ties (60% vs. 83%)

Geography → Work



- \Rightarrow large changes in completion rates















Social search-the Columbia experiment

Senders of successful messages showed little absolute dependency on

- ▶ age, gender
- country of residence
- ▶ income
- religion
- relationship to recipient

Range of completion rates for subpopulations: 30% to 40%

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Social search-the Columbia experiment

Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- L_{*} = Estimated 'true' median chain length (zero attrition)
- ▶ Intra-country chains: $L_* = 5$
- ▶ Inter-country chains: $L_* = 7$

Previous work-short paths

Connected random networks have short average

 d_{AB} = distance between nodes A and B.

But: social networks aren't random...

 $\langle d_{AB} \rangle \sim \log(N)$

- All chains: $L_* = 7$
- Milgram: $L_* \simeq 9$

path lengths:

N = population size,

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Need "clustering" (your

friends are likely to

know each other):



Nevertheless, some weak discrepencies do exist...

Social search—the Columbia experiment

An above average connector:

Norwegian, secular male, aged 30-39, earning over \$100K, with graduate level education working in mass media or science, who uses relatively weak ties to people they met in college or at work.

A below average connector:

Italian, Islamic or Christian female earning less than \$2K, with elementary school education and retired, who uses strong ties to family members.

Social search—the Columbia experiment

Mildly bad for continuing chain:

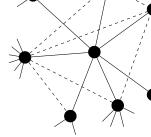
choosing recipients because "they have lots of friends" or because they will "likely continue the chain."

Why:

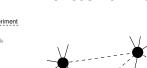
- Specificity important
- Successful links used relevant information. (e.g. connecting to someone who shares same profession as target.)

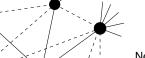


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Previous work—short paths







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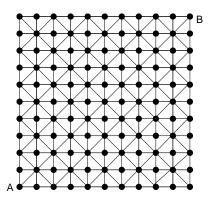
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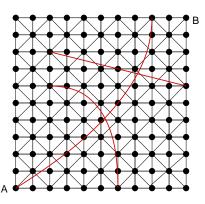
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Non-randomness gives clustering



 $d_{AB} = 10 \rightarrow$ too many long paths.

Randomness + regularity



Now have $d_{AB} = 3$

 $\langle d \rangle$ decreases overall

Small-world networks

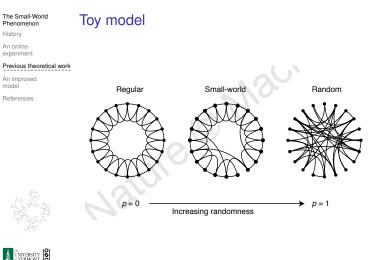
Introduced by Watts and Strogatz (Nature, 1998)^[6] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

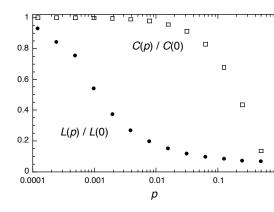
- neural network of C. elegans,
- semantic networks of languages,
- actor collaboration graph,
- food webs,
- social networks of comic book characters,...

Very weak requirements:

local regularity + random short cuts



The structural small-world property



Previous work-finding short paths

But are these short cuts findable?

No.

Nodes cannot find each other quickly with any local search method.



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Previous work-finding short paths

- What can a local search method reasonably use?
- How to find things without a map?
- Need some measure of distance between friends and the target.

Some possible knowledge:

- Target's identity
- Friends' popularity
- Friends' identities
- Where message has been



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Previous work-finding short paths

Jon Kleinberg (Nature, 2000)^[3] "Navigation in a small world."

Allowed to vary:

- 1. local search algorithm and
- 2. network structure.

Previous work—finding short paths

Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice.
- 2. Add local links so nodes know all nodes within a distance q.
- 3. Add m short cuts per node.
- 4. Connect *i* to *j* with probability

 $p_{ii} \propto d_{ii}^{-\alpha}$.

- $\triangleright \alpha = 0$: random connections.
- α large: reinforce local connections.
- $\sim \alpha = d$: same number of connections at all scales.

Previous work-finding short paths

But: social networks aren't lattices plus links.

Previous work-finding short paths

Theoretical optimal search:

"Greedy" algorithm.

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If networks have hubs can also search well: Adamic et al. (2001)^[1]

Same number of connections at all scales: $\alpha = d$.

Search time grows slowly with system size (like $\log^2 N$).

$$P(k_i) \propto k_i^{-\gamma}$$

where k = degree of node i (number of friends).

- Basic idea: get to hubs first (airline networks).
- But: hubs in social networks are limited.





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If there are no hubs and no underlying lattice, how can

to the target b?

What does 'closest' mean?

What is 'social distance'?





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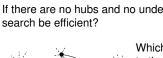
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Which friend of a is closest



The model

One approach: incorporate identity. (See "Identity and Search in Social Networks." Science, 2002, Watts, Dodds, and Newman^[5])

Identity is formed from attributes such as:

- Geographic location
- Type of employment
- Religious beliefs
- Recreational activities.

Groups are formed by people with at least one similar attribute.

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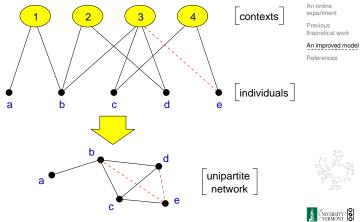
 $\mathsf{Attributes} \Leftrightarrow \mathsf{Contexts} \Leftrightarrow \mathsf{Interactions} \Leftrightarrow \mathsf{Networks}.$



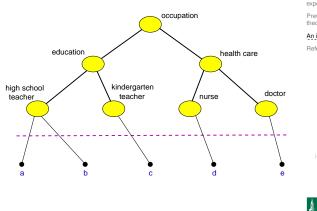
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Social distance—Context distance



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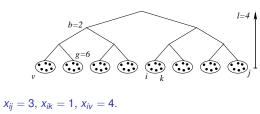




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The model

Distance between two individuals x_{ij} is the height of lowest common ancestor.



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Construct z connections for each node using

closer they are within a hierarchy.

Individuals are more likely to know each other the

 $p_{ij} = c \exp\{-\alpha x_{ij}\}.$

- $\alpha = 0$: random connections.
- α large: local connections.





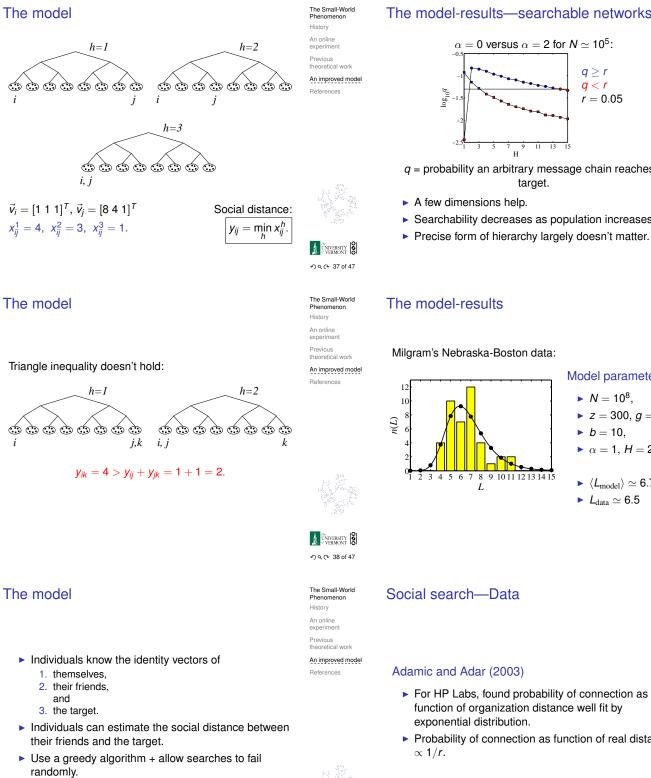
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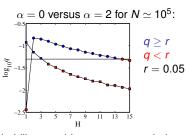
(Blau & Schwartz, Simmel, Breiger)



The model



The model-results—searchable networks



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- q = probability an arbitrary message chain reaches a target.
- A few dimensions help.
- Searchability decreases as population increases.

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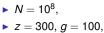


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Model parameters:



- ▶ *b* = 10,
- $\alpha = 1, H = 2;$

 \blacktriangleright $\langle L_{\rm model} \rangle \simeq 6.7$

• $L_{\rm data} \simeq 6.5$

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▶ For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.

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Probability of connection as function of real distance $\propto 1/r$.



- Individuals can estimate the social distance between their friends and the target.
- Use a greedy algorithm + allow searches to fail randomly.



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- Tags create identities for objects
- Website tagging: http://www.del.icio.us
- ► (e.g., Wikipedia)
- Photo tagging: http://www.flickr.com
- Dynamic creation of metadata plus links between information objects.
- Folksonomy: collaborative creation of metadata

Search in power-law networks. Phys. Rev. E, 64:046135, 2001. pdf (⊞)

References I

References II

B. Huberman.

[2] [2] P. S. Dodds, R. Muhamad, and D. J. Watts. An experimental study of search in global social networks. Science, 301:827–829, 2003. pdf (⊞)

[1] [1] L. Adamic, R. Lukose, A. Puniyani, and

- [3] [3] J. Kleinberg. Navigation in a small world. Nature, 406:845, 2000. pdf (⊞)
- [4] [4] J. Travers and S. Milgram. An experimental study of the small world problem. Sociometry, 32:425–443, 1969. pdf (⊞)

[5] [5] D. J. Watts, P. S. Dodds, and M. E. J. Newman.

Collective dynamics of 'small-world' networks.

Identity and search in social networks.

Nature, 393:440–442, 1998. pdf (⊞)

[6] [6] D. J. Watts and S. J. Strogatz.

Science, 296:1302–1305, 2002. pdf (⊞)

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Social Search-Real world uses

Recommender systems:

- Amazon uses people's actions to build effective connections between books.
- Conflict between 'expert judgments' and tagging of the hoi polloi.

Conclusions

- Bare networks are typically unsearchable.
- > Paths are findable if nodes understand how network is formed.
- Importance of identity (interaction contexts).
- Improved social network models.
- Construction of peer-to-peer networks.
- Construction of searchable information databases.





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