











Show $a > 0$ , $ac - b^2 > 0 \Leftrightarrow \lambda_1$ , $\lambda_2 > 0$ :	Positive Definite Matrices (PDMs)
<ul> <li>Show ":":</li> <li>Given ac - b<sup>2</sup> &gt; 0 then λ<sub>1</sub> · λ<sub>2</sub> &gt; 0, so both eigenvalues are positive or both are negative.</li> <li>Given a &gt; 0 then c &gt; 0 b/c otherwise ac - b<sup>2</sup> &lt; 0.</li> <li>This means a + c = λ<sub>1</sub> + λ<sub>2</sub> &gt; 0 → both eigenvalues</li> </ul>	Lecture 26 Molivation What a PDM is Identifying PDMs Completing the square 4-5 Gaussian elimination Principle Avia Theorem Nutshell Optional readerial
are positive. Show " $\Leftarrow$ ": Given $\lambda_1$ , $\lambda_2 > 0$ , then $ac - b^2 = \lambda_1 \cdot \lambda_2 > 0$	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
<ul> <li>Know a + c = λ<sub>1</sub> + λ<sub>2</sub> &gt; 0, so either a, c &gt; 0, or one is negative.</li> <li>But again, ac - b<sup>2</sup> &gt; 0 implies a, c must have same</li> </ul>	N.
sign, $\rightarrow a > 0$ .	UNIVERSITY O

## Finding PDMs...

 Upshot: We can compute determinants instead of eigenvalues to find signs.

- But: Computing determinants still isn't a picnic either...
- A much better way is to use the connection between pivots and eigenvalues.
- Another weird connection.



Positive Definite Matrices (PDMs)

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Optional material



References I



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