

How grading works:

Questions are worth 3 points according to the following scale:

- 3 = correct or very nearly so.
- 2 = acceptable but needs some revisions.
- 1 = needs major revisions.
- $0=$ way off.


## Schedule:

The course will mainly cover chapters 2 through 6 of the textbook. (You should know all about Chapter 1.)

| Week \# (dates) | Tuesday | Thursday |
| :--- | :--- | :--- |
| $1(8 / 31,9 / 2)$ | Lecture | Lecture + A1 |
| $2(9 / 7,9 / 9)$ | Lecture | Lecture + A2 |
| $3(9 / 14,9 / 16)$ | Lecture | Lecture + A3 |
| $4(9 / 21,9 / 23)$ | Lecture | Test 1 |
| $5(9 / 28,9 / 30)$ | Lecture | Lecture + A4 |
| $6(10 / 5,10 / 7)$ | Lecture | Lecture + A5 |
| $7(10 / 12,10 / 14)$ | Lecture | Lecture + A6 |
| $8(10 / 19,10 / 21)$ | Lecture | Test 2 |
| $9(10 / 26,10 / 29)$ | Lecture | Lecture + A7 |
| $10(11 / 2,11 / 4)$ | Lecture | Lecture + A8 |
| $11(11 / 9,11 / 11)$ | Lecture | Lecture + A9 |
| $12(11 / 16,11 / 18)$ | Lecture | Test 3 |
| $13(11 / 23,11 / 25)$ | Thanksgiving | Thanksgiving |
| $14(11 / 30,12 / 2)$ | Lecture | Lecture + A10 |
| $15(12 / 7,12 / 9)$ | Lecture | Lecture |

## Important dates:

1. Classes run from Monday, August 31 to Wednesday, December 9.
2. Add/Drop, Audit, Pass/No Pass deadline-Monday, September 14.
3. Last day to withdraw-Friday, November 6.
4. Reading and exam period-Thursday, December 10 to Friday, December 18.
Ch. 2: Lec. 1
Outline
Importance
Usages
Key problems
Three ways of
looking...
Colbert on
Equations
References
Ch. 2: Lec. 1
Outline
Importance
Usages
Key problems
Three ways of
looking...
Colbert on
Equations
References


## More stuff:

Do check your zoo account for updates regarding the course.

Academic assistance: Anyone who requires assistance in any way (as per the ACCESS program or due to athletic endeavors), please see or contact me as soon as possible.

## More stuff

Being good people:

1. In class there will be no electronic gadgetry, no cell phones, no beeping, no text messaging, etc. You really just need your brain, some paper, and a writing implement here (okay, and Matlab or similar).
2. Second, I encourage you to email me questions, ideas, comments, etc., about the class but request that you please do so in a respectful fashion.
3. Finally, as in all UVM classes, Academic honesty will be expected and departures will be dealt with appropriately. See http://www.uvm.edu/cses/ for guidelines.

## More stuff:

Late policy: Unless in the case of an emergency (a real one) or if an absence has been predeclared and a make-up version sorted out, assignments that are not turned in on time or tests that are not attended will be given 0\%.

Computing: Students are encouraged to use Matlab or something similar to check their work.

Note: for assignment problems, written details of calculations will be required.

| Ch. 2: Lec. 1 |
| :--- |
| Outline |
| Importance |
| Usages |
| Key problems |
| Three ways of <br> looking... <br> Colbert on <br> Equations |
| References |






What is going on here? We have 25 lectures to find out...

Is this your left nullspace?:

Broadly speaking, $A \vec{x}=\vec{b}$ translates as follows:

- $\vec{b}$ represents reality (e.g., music, structure)
- A contains building blocks (e.g., notes, shapes)
- $\vec{x}$ specifies how we combine our building blocks to make $\vec{b}$ (as best we can).

How can we disentangle an orchestra's sound?
What about pictures, waves, signals, ...?


Three ways to understand $A \vec{x}=\vec{b}$ :

- Way 1: The Row Picture
- Way 2: The Column Picture
- Way 3: The Matrix Picture

Example:

$$
\begin{aligned}
& -x_{1}+x_{2}=1 \\
& 2 x_{1}+x_{2}=4
\end{aligned}
$$

- Call this a 2 by 2 system of equations.
- 2 equations with 2 unknowns.

Standard method of simultaneous equations: solve above by adding and subtracting multiples of equations to each other $=$ Row Picture.

Three ways to understand $A \vec{x}=\vec{b}$ :
ow Picture-what we are doing:
(a) Finding intersection of two lines
(b) Finding the values of $x_{1}$ and $x_{2}$ for which both equations are satisfied (true/happy)
A splendid and deep connection:

Three possible kinds of solution:

1. Lines intersect at one point -One, unique solution
2. Lines are parallel and disjoint -No solutions
3. Lines are the same -Infinitely many solutions

Three ways to understand $A \vec{x}=\vec{b}$ :
The column picture:
See

$$
\begin{aligned}
& -x_{1}+x_{2}=1 \\
& 2 x_{1}+x_{2}=4
\end{aligned}
$$

as

$$
x_{1}\left[\begin{array}{c}
-1 \\
2
\end{array}\right]+x_{2}\left[\begin{array}{l}
1 \\
1
\end{array}\right]=\left[\begin{array}{l}
1 \\
4
\end{array}\right]
$$

General problem

$$
x_{1} \vec{a}_{1}+x_{2} \vec{a}_{2}=\vec{b}
$$

- Column vectors are our 'building blocks'
- Key idea: try to 'reach' $\vec{b}$ by combining (summing) multiples of column vectors $\vec{a}_{1}$ and $\vec{a}_{2}$.

Three ways to understand $A \vec{x}=\vec{b}$ :

We love the column picture:

- Intuitive.
- Generalizes easily to many dimensions.

Three possible kinds of solution:

1. $\vec{a}_{1} \nmid \vec{a}_{2}: 1$ solution
2. $\vec{a}_{1} \| \vec{a}_{2} \nmid \vec{b}$ : No solutions
3. $\vec{a}_{1}\left\|\vec{a}_{2}\right\| \vec{b}$ : infinitely many solutions
(assuming neither $\vec{a}_{1}$ or $\vec{a}_{1}$ are $\overrightarrow{0}$ )

Three ways to understand $A \vec{x}=\vec{b}$ :

Difficulties:

- Do we give up if $A \vec{x}=\vec{b}$ has no solution?
- No! We can still find the $\vec{x}$ that gets us as close to $\vec{b}$ as possible.
- Method of approximation-very important!
- We may not have the right building blocks but we can do our best.

[1] G. Strang. The fundamental theorem of linear algebra. The American Mathematical Monthly, 100(9):848-855, 1993. pdf ( $\boxplus$ )
[2] G. Strang.
Too much calculus, 2002.
SIAM Linear Algebra Activity Group Newsletter. pdf ( $\boxplus$ )
Ch. 2: Lec. 1
Outline
Importance
Usages
Key problems
Three ways of
looking...
Colbert on
Equations
References

