

# George Kingsley Zipf:

#### In brief:

- Zipf (⊞) (1902–1950) was a linguist at Harvard, specializing in Chinese languages.
- Unusual passion for statistical analysis of texts.
- Studied human behavior much more generally...

#### Zipf's masterwork:

- "Human Behavior and the Principle of Least Effort" Addison-Wesley, 1949 Cambridge, MA<sup>[2]</sup>
- ► Bonus field of study: <u>Glottometrics.</u> (⊞)
- ► Bonus 'word' word:  $\underline{Glossolalia.}$  ( $\boxplus$ )



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Zipf in brief

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Zipfian empirics

# Human Behavior/Principle of Least Effort:

#### From the Preface—

Nearly twenty-five years ago it occurred to me that we might gain considerable insight into the mainsprings of human behavior if we viewed it purely as a natural phenomenon like everything else in the universe, ...

#### And—

... the expressed purpose of this book is to establish The Principle of Least Effort as the primary principle that governs our entire individual and collective behavior ...

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#### The Principle of Least Effort:



#### Zipf's framing (p. 1):

"... a person in solving his immediate problems will view these against the background of his probable future problems *as estimated by himself*."

"... he will strive ... to minimize the *total work* that he must expend in solving *both* his immediate problems *and* his probable future problems."

"[he will strive to] minimize the *probable average rate of his work-expenditure...*"

# Zipfian empirics:

▶ vocabulary balance:  $f \sim r^{-1} \rightarrow r \cdot f \sim \text{constant}$ (*f* = frequency, *r* = rank).

TABLE 2-1 Arbitrary Ranks with Frequencies in James Joyce's Ulysses (Hanley Index)			
10	2,653	26,530	265,500
20	1,311	26,220	262,200
30	926	27,780	277,800
40	717	28,680	286,800
50	556	27,800	278,800
100	265	26,500	265,000
200	133	26,600	266,000
300	84	25,200	252,000
400	62	24,800	248,000
500	50	25,000	250,000
1,000	26	26,000	260,000
2,000	12	24,000	240,000
3,000	8	24,000	240,000
4,000	6	24,000	240,000
5,000	5	25,000	250,000
10,000	2	20,000	200,000
20,000	1	20,000	200,000
29,899	1	29,899	298,990

# Rampaging research

Within Human Behavior and the Principle of Least Effort:

- City sizes
- # retail stores in cities
- # services (barber shops, beauty parlors, cleaning, ...)
- # people in occupations
- # one-way trips in cars and trucks vs. distance

- # new items by dateline
- weight moved between cities by rail
- # telephone messages between cities
- # people moving vs. distance
- # marriages vs. distance
- Observed general dependency of 'interactions' between cities A and B on P<sub>A</sub>P<sub>B</sub>/D<sub>AB</sub> where P<sub>A</sub> and P<sub>B</sub> are population size and D<sub>AB</sub> is distance between A and B.

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# Zipfian empirics:

#### • $f \sim r^{-1}$ for word frequency:

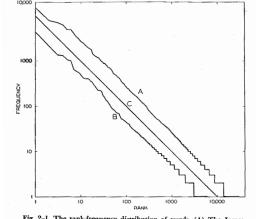


Fig. 2-1. The rank-frequency distribution of words. (A) The James Joyce data; (B) the Eldridge data; (C) ideal curve with slope of negative unity.

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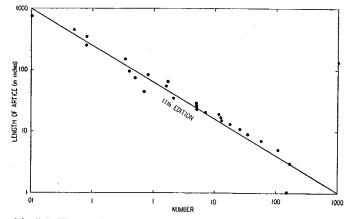
# Zipf's basic idea:

Forces of Unification and Diversification:

- Easiest for the speaker to use just one word.
  - Encoding is simple but decoding is hard
- Zipf uses the analogy of tools: one tool for all tasks.
- Optimal for listener if all pieces of information correspond to different words (or morphemes).
- Analogy: a specialized tool for every task.
  - Decoding is simple but encoding is hard
- Zipf thereby argues for a tension that should lead to an uneven distribution of word usage.
- No formal theory beyond this...



Article length in the Encyclopedia Britannica:



- Fig. 5-3. The number of different articles of like length in samples of the 11th edition of the Encyclopaedia Britannica. Lengths in inches.
- (?) slope of -3/5 corresponds to  $\gamma = 5/3$ .



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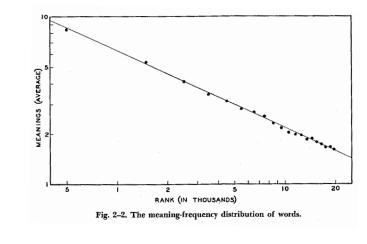
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# Zipfian empirics:

Number of meanings  $m_r \propto f_r^{1/2}$  where *r* is rank and  $f_r$  is frequency.



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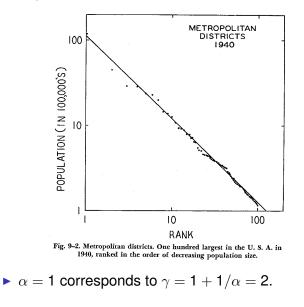
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Zipfian empirics:

Population size of districts:



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#### Zipfian empirics:

Number of employees in organizations

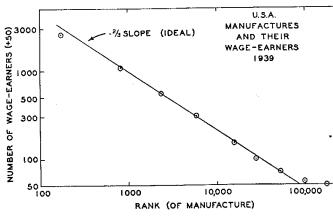


Fig. 9-8. Manufactures and their wage earners in the U. S. A. in 1939, with the manufactures ranked in the order of their decreasing number of wage earners.

• 
$$\alpha = 2/3$$
 corresponds to  $\gamma = 1 + 1/\alpha = 5/2$ .

#### Zipfian empirics:

- # obituaries in the New York Times for locations with population P<sub>2</sub>.
- D = distance,  $P_1$  = New York's population
- Solid line = +1 exponent.

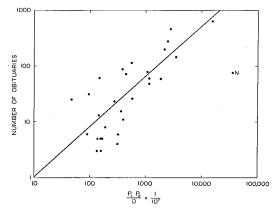
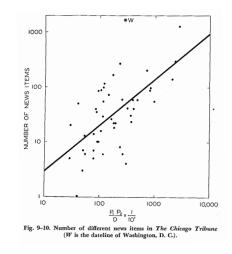


Fig. 9-11. Number of obituaries in *The New York Times* (N represents Newark, New Jersey).

# Zipfian empirics:

- # news items as a function of population P<sub>2</sub> of location in the Chicago Tribune
- D = distance,  $P_1$  = Chicago's population
- Solid line = +1 exponent.



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#### Zipfian empirics:

- Movement of stuff between cities
- D = distance,  $P_1$  and  $P_2$  = city populations.
- ► Solid line = +1 exponent.

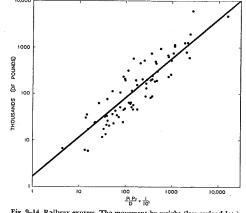
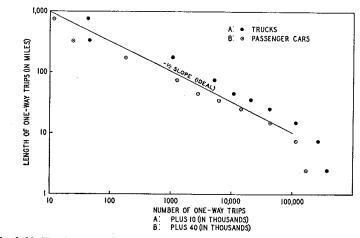


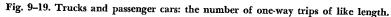
Fig. 9-14. Railway express. The movement by weight (less carload lots) between 13 arbitrary cities in the U. S. A., May 1939.

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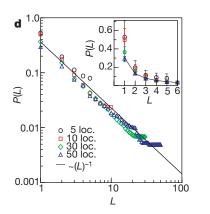
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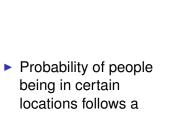
- Length of trip versus frequency of trip.
- Solid line = -1/2 exponent corresponds to  $\gamma = 2$ .





**Recent Zipf action:** 





- being in certain locations follows a Zipfish law...
- ► From Gonzàlez et al., Nature (2008) "Understanding individual human mobility patterns"<sup>[1]</sup>

#### Zipfian empirics:

- The probability of marriage?
- $\triangleright \gamma = 1?$

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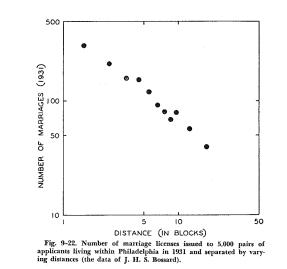
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M. C. González, C. A. Hidalgo, and A.-L. Barabási. Understanding individual human mobility patterns. Nature, 453:779–782, 2008. pdf (⊞)

#### G. K. Zipf.

Human Behaviour and the Principle of Least-Effort. Addison-Wesley, Cambridge, MA, 1949.

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