Biological Contagion

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A confusion of contagions:

- Is Harry Potter some kind of virus?
- What about the Da Vinci Code?
- Does Sudoku spread like a disease?
- ▶ Religion?
- Democracy...?

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Naturomorphisms

- "The feeling was contagious."
- "The news spread like wildfire."
- "Freedom is the most contagious virus known to man."
 - —Hubert H. Humphrey, Johnson's vice president
- "Nothing is so contagious as enthusiasm."
 - —Samuel Taylor Coleridge

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Optimism according to Ambrose Bierce: (H)

The doctrine that everything is beautiful, including what is ugly, everything good, especially the bad, and everything right that is wrong. ... It is hereditary, but fortunately not contagious.

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Social contagion

Eric Hoffer, 1902-1983

There is a grandeur in the uniformity of the mass. When a fashion, a dance, a song, a slogan or a joke sweeps like wildfire from one end of the continent to the other, and a hundred million people roar with laughter, sway their bodies in unison, hum one song or break forth in anger and denunciation, there is the overpowering feeling that in this country we have come nearer the brotherhood of man than ever before.

► Hoffer (⊞) was an interesting fellow...

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Thoughts On The Nature Of Mass Movements" (1951) $^{[3]}$

Quotes-aplenty:

- "We can be absolutely certain only about things we do not understand."
- "Mass movements can rise and spread without belief in a God, but never without belief in a devil."
- "Where freedom is real, equality is the passion of the masses. Where equality is real, freedom is the passion of a small minority."

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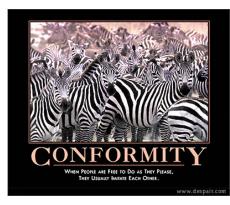
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Simple disease



"When people are free to do as they please, they usually imitate each other."

-Eric Hoffer "The Passionate State of Mind" [4]

despair.com

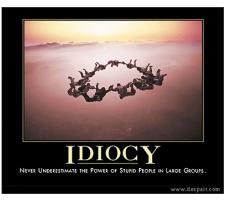
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"Never Underestimate the Power of Stupid People in Large Groups."

despair.com

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Definitions

- (1) The spreading of a quality or quantity between individuals in a population.
- (2) A disease itself: the plague, a blight, the dreaded lurgi, ...
- from Latin: con = 'together with' + tangere 'to touch.'
- Contagion has unpleasant overtones...
- Just Spreading might be a more neutral word
- But contagion is kind of exciting...

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Interesting infections:

- Spreading of buildings in the US. (⊞)
- Viral get-out-the-vote video. (⊞)

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Two main classes of contagion

- Infectious diseases: tuberculosis, HIV, ebola, SARS, influenza, ...
- 2. Social contagion: fashion, word usage, rumors, riots, religion, ...

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The standard SIR model [5]

- = basic model of disease contagion
- Three states:
 - 1. S = Susceptible
 - 2. I = Infective/Infectious
 - 3. R = Recovered or Removed or Refractory
- ightharpoonup S(t) + I(t) + R(t) = 1
- Presumes random interactions (mass-action principle)
- Interactions are independent (no memory)
- Discrete and continuous time versions

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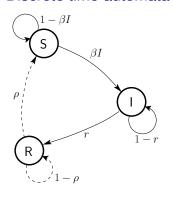
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Discrete time automata example:



Transition Probabilities:

 β for being infected given contact with infected r for recovery ρ for loss of immunity

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Original models attributed to

- ▶ 1920's: Reed and Frost
- 1920's/1930's: Kermack and McKendrick [?, ?, ?]
- Coupled differential equations with a mass-action principle

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Differential equations for continuous model

$$\frac{d}{dt}S = -\beta IS + \rho R$$

$$\frac{d}{dt}I = \beta IS - rI$$

$$\frac{d}{dt}R = rI - \rho R$$

 β , r, and ρ are now rates.

Reproduction Number R_0 :

- ▶ R₀ = expected number of infected individuals resulting from a single initial infective
- ▶ Epidemic threshold: If *R*₀ > 1, 'epidemic' occurs.

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Discrete version:

- Set up: One Infective in a randomly mixing population of Susceptibles
- At time t = 0, single infective random bumps into a Susceptible
- ▶ Probability of transmission = β
- At time t = 1, single Infective remains infected with probability 1 r
- At time t = k, single Infective remains infected with probability $(1 r)^k$

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Discrete version:

Expected number infected by original Infective:

$$R_0 = \beta + (1 - r)\beta + (1 - r)^2\beta + (1 - r)^3\beta + \dots$$
$$= \beta \left(1 + (1 - r) + (1 - r)^2 + (1 - r)^3 + \dots \right)$$
$$= \beta \frac{1}{1 - (1 - r)} = \beta/r$$

For S_0 initial infectives (1 – $S_0 = R_0$ immune):

$$R_0 = S_0 \beta / r$$

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Independent Interaction models

For the continuous version

Second equation:

$$\frac{\mathrm{d}}{\mathrm{d}t}I = \beta SI - rI$$

$$\frac{\mathrm{d}}{\mathrm{d}t}I = (\beta S - r)I$$

Number of infectives grows initially if

$$\beta S(0) - r > 0 \Rightarrow \beta S(0) > r \Rightarrow \frac{\beta S(0)}{r} > 1$$

Same story as for discrete model.

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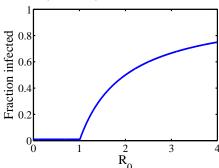
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Independent Interaction models

Example of epidemic threshold:



- Continuous phase transition.
- Fine idea from a simple model.

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Many variants of the SIR model:

- SIS: susceptible-infective-susceptible
- SIRS: susceptible-infective-recovered-susceptible
- compartment models (age or gender partitions)
- more categories such as 'exposed' (SEIRS)
- recruitment (migration, birth)

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For novel diseases:

- 1. Can we predict the size of an epidemic?
- 2. How important is the reproduction number R_0 ?

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R_0 approximately same for all of the following:

- ightharpoonup 1918-19 "Spanish Flu" \sim 500,000 deaths in US
- ightharpoonup 1957-58 "Asian Flu" \sim 70,000 deaths in US
- ightharpoonup 1968-69 "Hong Kong Flu" \sim 34,000 deaths in US
- ightharpoonup 2003 "SARS Epidemic" \sim 800 deaths world-wide

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Size distributions are important elsewhere:

- earthquakes (Gutenberg-Richter law)
- city sizes, forest fires, war fatalities
- wealth distributions
- 'popularity' (books, music, websites, ideas)
- Epidemics?

Power laws distributions are common but not obligatory...

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Really, what about epidemics?

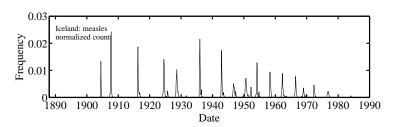
- Simply hasn't attracted much attention.
- Data not as clean as for other phenomena.

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Feeling III in Iceland

Caseload recorded monthly for range of diseases in Iceland, 1888-1990



Treat outbreaks separated in time as 'novel' diseases. Introduction

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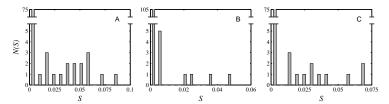
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Epidemic size distributions N(S) for Measles, Rubella, and Whooping Cough.



Spike near S = 0, relatively flat otherwise.

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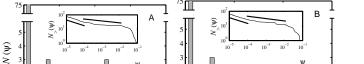
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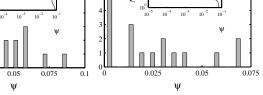
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Insert plots:

0.025

Complementary cumulative frequency distributions:

$$N(\Psi' > \Psi) \propto \Psi^{-\gamma+1}$$

Limited scaling with a possible break.

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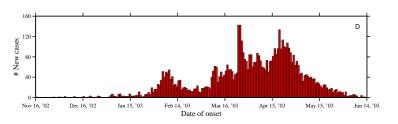


- measles: 1.40 (low Ψ) and 1.13 (high Ψ)
- pertussis: 1.39 (low Ψ) and 1.16 (high Ψ)
- ▶ Expect $2 \le \gamma < 3$ (finite mean, infinite variance)
- ▶ When γ < 1, can't normalize
- Distribution is quite flat.

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Resurgence—example of SARS



- Epidemic slows... then an infective moves to a new context.
- ► Epidemic discovers new 'pools' of susceptibles: Resurgence.
- Importance of rare, stochastic events.

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So... can a simple model produce

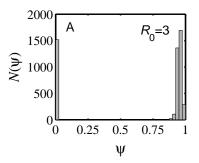
- 1. broad epidemic distributions and
- 2. resurgence?

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Size distributions



Simple models typically produce bimodal or unimodal size distributions.

- This includes network models: random, small-world, scale-free, ...
- Exceptions:
 - 1. Forest fire models
 - 2. Sophisticated metapopulation models

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Forest fire models: [6]

- Rhodes & Anderson, 1996
- The physicist's approach: "if it works for magnets, it'll work for people..."

A bit of a stretch:

- Epidemics ≡ forest fires spreading on 3-d and 5-d lattices.
- Claim Iceland and Faroe Islands exhibit power law distributions for outbreaks.
- 3. Original forest fire model not completely understood.

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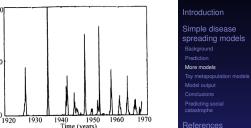
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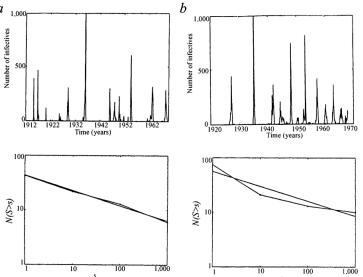
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From Rhodes and Anderson, 1996.

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- Community based mixing: Longini (two scales).
- Eubank et al.'s EpiSims/TRANSIMS—city simulations.
- Spreading through countries—Airlines: Germann et al.. Corlizza et al.
- Vital work but perhaps hard to generalize from...
- ➤ ⇒ Create a simple model involving multiscale travel
- Multiscale models suggested by others but not formalized (Bailey, Cliff and Haggett, Ferguson et al.)

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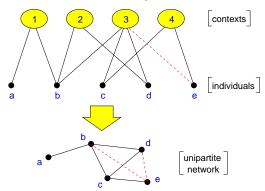
- Very big question: What is N?
- Should we model SARS in Hong Kong as spreading in a neighborhood, in Hong Kong, Asia, or the world?
- ► For simple models, we need to know the final size beforehand...

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Improving simple models

Contexts and Identities—Bipartite networks



- boards of directors
- movies
- transportation modes (subway)

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Improving simple models

Idea for social networks: incorporate identity.

Identity is formed from attributes such as:

- Geographic location
- Type of employment
- Age
- Recreational activities

Groups are crucial...

- formed by people with at least one similar attribute
- ▶ Attributes ⇔ Contexts ⇔ Interactions ⇔ Networks. [8]

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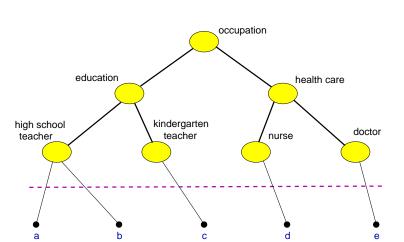
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Infer interactions/network from identities



Distance makes sense in identity/context space.

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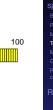
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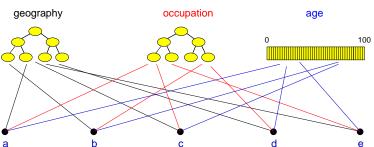


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(Blau & Schwartz [1], Simmel [7], Breiger [2])

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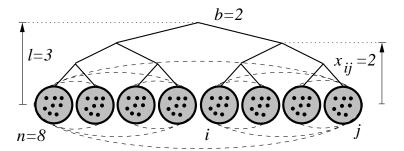
Geography—allow people to move between contexts:

- Locally: standard SIR model with random mixing
- discrete time simulation
- \triangleright β = infection probability
- $ightharpoonup \gamma$ = recovery probability
- ► *P* = probability of travel
- ▶ Movement distance: $Pr(d) \propto exp(-d/\xi)$
- \blacktriangleright ξ = typical travel distance

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Schematic:



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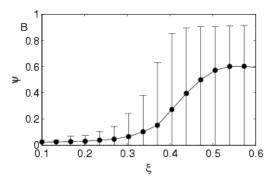


- ▶ Define P₀ = Expected number of infected individuals leaving initially infected context.
- Need $P_0 > 1$ for disease to spread (independent of R_0).
- Limit epidemic size by restricting frequency of travel and/or range

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Varying ξ :



 Transition in expected final size based on typical movement distance (sensible) Introduction

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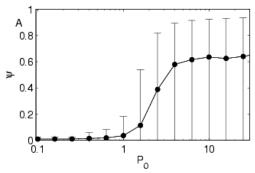
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Varying P_0 :



- Transition in expected final size based on typical number of infectives leaving first group (also sensible)
- ▶ Travel advisories: ξ has larger effect than P_0 .

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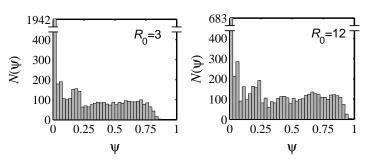
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- Flat distributions are possible for certain ξ and P.
- ▶ Different R₀'s may produce similar distributions
- Same epidemic sizes may arise from different R₀'s

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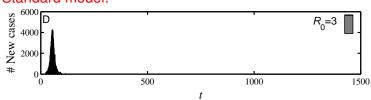
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Standard model:



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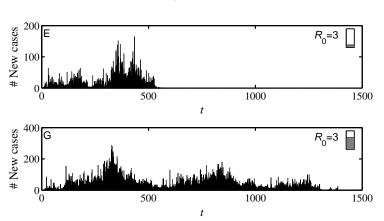
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Model output—resurgence

Standard model with transport:



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stochasticity

leads to

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broad epidemic size distributions

Simple multiscale population structure

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- For this model, epidemic size is highly unpredictable
- Model is more complicated than SIR but still simple
- We haven't even included normal social responses such as travel bans and self-quarantine.
- ▶ The reproduction number R_0 is terribly useful.
- ▶ *R*₀, however measured, is not informative about
 - 1. how likely the observed epidemic size was,
 - 2. and how likely future epidemics will be.
- ► Problem: R_0 summarises one epidemic after the fact and enfolds movement, the price of bananas, everything.

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- Rare events may matter enormously (e.g., an infected individual taking an international flight)
- More support for controlling population movement (e.g., travel advisories, quarantine)

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- Need to separate movement from disease
- R₀ needs a friend or two.
- Need R₀ > 1 and P₀ > 1 and ξ sufficiently large for disease to have a chance of spreading

More wondering:

- Exactly how important are rare events in disease spreading?
- ▶ Again, what is N?

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Valiant attempts to use SIR and co. elsewhere:

- Adoption of ideas/beliefs (Goffman & Newell, 1964)
- Spread of rumors (Daley & Kendall, 1965)
- ▶ Diffusion of innovations (Bass, 1969)
- Spread of fanatical behavior (Castillo-Chávez & Song, 2003)

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"Greenspan Concedes Error on Regulation"

- ... humbled Mr. Greenspan admitted that he had put too much faith in the self-correcting power of free markets...
- "Those of us who have looked to the self-interest of lending institutions to protect shareholders' equity, myself included, are in a state of shocked disbelief"
- Rep. Henry A. Waxman: "Do you feel that your ideology pushed you to make decisions that you wish you had not made?"
- Mr. Greenspan conceded: "Yes, I've found a flaw. I don't know how significant or permanent it is. But I've been very distressed by that fact."

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New York Times, October 23, 2008 (⊞)

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Alan Greenspan (September 18, 2007):

"I've been dealing with these big mathematical models of forecasting the economy ...

If I could figure out a way to determine whether or not people are more fearful or changing to more euphoric,

I don't need any of this other stuff.

I could forecast the economy better than any way I know."



http://wikipedia.org

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"The trouble is that we can't figure that out. I've been in the forecasting business for 50 years. I'm no better than I ever was, and nobody else is. Forecasting 50 years ago was as good or as bad as it is today. And the reason is that human nature hasn't changed. We can't improve ourselves."

Jon Stewart:

"You just bummed the @*!# out of me."



wildbluffmedia.com

- ► From the Daily Show (⊞) (September 18, 2007)
- ▶ The full inteview is $\underline{\text{here}}$ ($\underline{\boxplus}$).

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Economics, Schmeconomics

James K. Galbraith:

NYT But there are at least 15,000 professional economists in this country, and you're saying only two or three of them foresaw the mortgage crisis?

[JKG] Ten or 12 would be closer than two or three.

NYT What does that say about the field of economics, which claims to be a science? [JKG] It's an enormous blot on the reputation of the profession. There are thousands of economists. Most of them teach. And most of them teach a theoretical framework that has been shown to be fundamentally useless.

From the New York Times, 11/02/2008 (⊞)

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References I

P. M. Blau and J. E. Schwartz.

Crosscutting Social Circles.

Academic Press, Orlando, FL, 1984.

R. L. Breiger. The duality of persons and groups. Social Forces, 53(2):181–190, 1974. pdf (⊞)

E. Hoffer. The True Believer: On The Nature Of Mass Movements.

Harper and Row, New York, 1951.

E. Hoffer.

The Passionate State of Mind: And Other Aphorisms.

Buccaneer Books, 1954.

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References II

J. D. Murray.Mathematical Biology.Springer, New York, Third edition, 2002.

C. J. Rhodes and R. M. Anderson.

Power laws governing epidemics in isolated populations.

Nature, 381:600–602, 1996. pdf (⊞)

G. Simmel.
The number of members as determining the sociological form of the group. I.

American Journal of Sociology, 8:1–46, 1902.

D. J. Watts, P. S. Dodds, and M. E. J. Newman. Identity and search in social networks.

Science, 296:1302–1305, 2002. pdf (⊞)

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