Overview of Complex Networks Santa Fe Institute Summer School, 2009

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Lecture 1: Overview; Background

 Lecture 2: Random, Scale-free, and Small-World networks

Lecture 3: Models of Contagion

Lecture 4: Transportation networks; Discovering structure

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- Three versions (all in pdf):
 - 1. Presentation,
 - 2. Flat Presentation,
 - 3. Handout (2x2).
- Presentation versions are navigable and hyperlinks are clickable.
- Web links look <u>like this</u> (\boxplus) .
- References in slides link to full citation at end.^[1]
- Citations contain links to papers in pdf (if available).
- ▶ 50 hours of lectures \rightarrow 5 hours.
- Brought to you by a concoction of LaTEX, Beamer, and perl.

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Complex System—Some ingredients:

- Distributed system of many interrelated parts
- No centralized control
- Nonlinear relationships
- Existence of feedback loops
- Complex systems are open (out of equilibrium)
- Presence of Memory
- Modular (nested)/multiscale structure
- Opaque boundaries
- Emergence—'More is Different'^[1]

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Complex: (Latin = with + fold/weave (com + plex)) Adjective

- Made up of multiple parts; intricate or detailed.
- Not simple or straightforward.



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net•work |'net_iwərk|

noun

1 an arrangement of intersecting horizontal and vertical lines.

• a complex system of roads, railroads, or other transportation routes : a network of railroads.

2 a group or system of interconnected people or things : a trade network.

• a group of people who exchange information, contacts, and experience for professional or social purposes : a *support network*.

• a group of broadcasting stations that connect for the simultaneous broadcast of a program : the introduction of a second TV network | [as adj.] network television.

• a number of interconnected computers, machines, or operations : *specialized computers that manage multiple outside connections to a network* | *a local cellular phone network.*

• a system of connected electrical conductors.

verb [trans.]

connect as or operate with a network : the stock exchanges have proven to be resourceful in networking these deals.

• link (machines, esp. computers) to operate interactively : [as adj.] (**networked**) *networked workstations*.

• [intrans.] [often as n.] (**networking**) interact with other people to exchange information and develop contacts, esp. to further one's career *: the skills of networking, bargaining, and negotiation.*

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Thesaurus deliciousness:

network

noun

1 *a network of arteries* WEB, lattice, net, matrix, mesh, crisscross, grid, reticulum, reticulation; Anatomy plexus.

2 a network of lanes MAZE, labyrinth, warren, tangle.

3 *a network of friends* SYSTEM, complex, nexus, web, webwork.

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From Keith Briggs's excellent etymological investigation: (⊞)

- Opus reticulatum:
- A Latin origin?



[http://serialconsign.com/2007/11/we-put-net-network]

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First known use: Geneva Bible, 1560

'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

- 1658–: reticulate structures in animals
- 1839—: rivers and canals
- 1869–: railways
- 1883–: distribution network of electrical cables
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Net and Work are venerable old words:

- 'Net' first used to mean spider web (King Ælfréd, 888).
- 'Work' appear to have long meant purposeful action.



- 'Network' = something built based on the idea of natural, flexible lattice or web.
- c.f., ironwork, stonework, fretwork.

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- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998...
- In largely due to your typical theoretical physicist:

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Piranha physicus

- Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)

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Popularity (according to ISI)

"Collective dynamics of 'small-world' networks" [19]

- Watts and Strogatz Nature, 1998
- 3752 citations (as of June 5, 2009)
- Over 1100 citations in 2008 alone.

"Emergence of scaling in random networks"^[2]

- Barabási and Albert Science, 1999
- 3860 citations (as of June 5, 2009)
- Over 1100 citations in 2008 alone.

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Popularity according to books:



The Tipping Point: How Little Things can make a Big Difference—Malcolm Gladwell^[8]



Nexus: Small Worlds and the Groundbreaking Science of Networks—Mark Buchanan

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Popularity according to books:

Haw Europhing Is Connected to Everything Else and What Is Means for Dations, Science, and Decryday Ufe



Linked: How Everything Is Connected to Everything Else and What It Means—Albert-Laszlo Barabási



Six Degrees: The Science of a Connected Age—Duncan Watts^[18]

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Numerous others:

- Complex Social Networks—F. Vega-Redondo^[17]
- Fractal River Basins: Chance and Self-Organization—I. Rodríguez-Iturbe and A. Rinaldo^[14]
- Random Graph Dynamics—R. Durette
- Scale-Free Networks—Guido Caldarelli
- Evolution and Structure of the Internet: A Statistical Physics Approach—Romu Pastor-Satorras and Alessandro Vespignani
- Complex Graphs and Networks—Fan Chung
- Social Network Analysis—Stanley Wasserman and Kathleen Faust
- Handbook of Graphs and Networks—Eds: Stefan Bornholdt and H. G. Schuster^[4]
- Evolution of Networks—S. N. Dorogovtsev and J. F. F. Mendes^[7]

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But surely networks aren't new...

- Graph theory is well established..
- Study of social networks started in the 1930's...
- So why all this 'new' research on networks?
- Answer: Oodles of Easily Accessible Data.
- We can now inform (alas) our theories with a much more measurable reality.*
- A worthy goal: establish mechanistic explanations.

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* If this is upsetting, maybe string theory is for you...

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Web-scale data sets can be overly exciting.

Witness:

- ► The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired) (⊞
- "The Unreasonable Effectiveness of Data," Halevy et al.^[9].

But:

- For scientists, description is only part of the battle.
- ▶ We still need to understand.

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- ► The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired) (⊞)
- "The Unreasonable Effectiveness of Data," Halevy et al.^[9].

But:

- For scientists, description is only part of the battle.
- We still need to understand.

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Nodes = A collection of entities which have properties that are somehow related to each other

 e.g., people, forks in rivers, proteins, webpages, organisms,...

Links = Connections between nodes

- Links may be directed or undirected.
- Links may be binary or weighted.

Other spiffing words: vertices and edges.

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Node degree = Number of links per node

- Notation: Node *i*'s degree = k_i .
- ▶ $k_i = 0, 1, 2, ...$
- ▶ Notation: the average degree of a network = $\langle k \rangle$
- Connection between number of edges m and average degree:

$$\langle k \rangle = \frac{2m}{N}.$$

• Defn: N_i = the set of *i*'s k_i neighbors

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Adjacency matrix:

▶ e.q.,

- We represent a directed network by a matrix A with link weight a_{ij} for nodes i and j in entry (i, j).
 - $A = \begin{bmatrix} 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{bmatrix}$
- (n.b., for numerical work, we always use sparse matrices.)

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Adjacency matrix:

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So what passes for a complex network?

- Complex networks are large (in node number)
- Complex networks are sparse (low edge to node ratio)
- Complex networks are usually dynamic and evolving
- Complex networks can be social, economic, natural, informational, abstract, ...

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- Airline networks
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- Snogging
- Friendships
- Acquaintances
- Boards and directors
- Organizations
- ► myspace.com (⊞) facebook.com (⊞)



Each circle represents a student and lines connecting students represent remaintic relations occuring within the 6 months preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

 'Remotely sensed' by: email activity, instant messaging, phone logs (*cough*).

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The Structure of Romantic and Sexual Relations at "Jefferson High School"



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- Knowledge/Databases/Ideas
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common tags cloud | list

community daily dictionary education **encyclopedia** english free imported info information internet knowledge learning news **reference** research resource resources search tools useful web web2.0 **Wiki wikipedia**

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Clickworthy Science:



Bollen et al. [3]

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Graphical renderings are often just a big mess.

And even when renderings somehow look good:

We need to extract digestible, meaningful aspects.

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Graphical renderings are often just a big mess.



- ← Typical hairball
- number of nodes N = 500
- number of edges m = 1000
- average degree $\langle k \rangle = 4$

And even when renderings somehow look good:

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- We need to extract digestible, meaningful aspects.

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Some key features of real complex networks:

- Degree distribution
- Assortativity
- Homophily
- Clustering
- Motifs
- Modularity
- Coevolution of network structure and processes on networks.

- Concurrency
- Hierarchical scaling
- Network distances
- Centrality
- Efficiency
- Robustness

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1. Degree distribution P_k

- *P_k* is the probability that a randomly selected node has degree k
- Big deal: Form of P_k key to network's behavior
- ex 1: Erdős-Rényi random networks have a Poisson distribution:

 $P_k = e^{-\langle k
angle} \langle k
angle^k / k!$

- ex 2: "Scale-free" networks: $P_k \propto k^{-\gamma} \Rightarrow$ 'hubs'
- We'll come back to this business soon...

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2. Assortativity/3. Homophily:

- Social networks: Homophily (⊞) = birds of a feather
- e.g., degree is standard property for sorting: measure degree-degree correlations.
- Assortative network: ^[12] similar degree nodes connecting to each other.
- Disassortative network: high degree nodes connecting to low degree nodes.

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 - Often social: company directors, coauthors, actors.
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- e.g., degree is standard property for sorting: measure degree-degree correlations.
- Assortative network: ^[12] similar degree nodes connecting to each other.
 - Often social: company directors, coauthors, actors.
- Disassortative network: high degree nodes connecting to low degree nodes.
 - Often techological or biological: Internet, protein interactions, neural networks, food webs.

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4. Clustering:

- > Your friends tend to know each other.
- ► Two measures:

$$C_1 = \left\langle \frac{\sum_{j_1, j_2 \in \mathcal{N}_i} a_{j_1, j_2}}{k_i (k_i - 1)/2} \right\rangle_i \text{ due to Watts & Strogatz}$$

 $C_2 = \frac{3 \times \# \text{triangles}}{\# \text{triples}}$ due to Newman^[13]

- C₁ is the average fraction of pairs of neighbors who are connected.
- Interpret C₂ as probability two of a node's friends know each other.

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5. Motifs:

Small, recurring functional subnetworks

e.g., Feed Forward Loop:

Shen-Orr, Uri Alon, *et al.* ^[15]

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5. Motifs:

- Small, recurring functional subnetworks
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Shen-Orr, Uri Alon, et al. [15]

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6. modularity:



Clauset et al., 2006^[5]: NCAA football

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7. Concurrency:

- Transmission of a contagious element only occurs during contact^[11]
- Rather obvious but easily missed in a simple model
- Dynamic property—static networks are not enough
- Knowledge of previous contacts crucial
- Beware cumulated network data!

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8. Horton-Strahler stream ordering:

- Metrics for branching networks:
 - Method for ordering streams hierarchically
 - Reveals fractal nature of natural branching networks
 - Hierarchy is not pure but mixed (Tokunaga).^[1]
 - Major examples: rivers and blood networks



Beautifully described but poorly explained.

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9. Network distances:

(a) shortest path length d_{ij} :

- Fewest number of steps between nodes i and j.
- (Also called the chemical distance between i and j

(b) average path length $\langle d_{ij} \rangle$:

- Average shortest path length in whole network.
- Good algorithms exist for calculation.
- Weighted links can be accommodated.

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9. Network distances:(a) shortest path length *d_{ij}*:

- ▶ Fewest number of steps between nodes *i* and *j*.
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9. Network distances:

(c) Network diameter d_{\max} :

Maximum shortest path length in network.

(d) Closeness $d_{cl} = [\sum_{ij} d_{ij}^{-1} / {n \choose 2}]^{-1}$:

- Average 'distance' between any two nodes.
- ► Closeness handles disconnected networks (d_{ii} = ∞)
- $d_{cl} = \infty$ only when all nodes are isolated.

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10. Centrality:

- Many such measures of a node's 'importance.'
- ex 1: Degree centrality: k_i .
- ex 2: Node *i*'s betweenness
 = fraction of shortest paths that pass through *i*.
- ► ex 3: Edge ℓ's betweenness
 = fraction of shortest paths that travel along ℓ.
- ex 4: Recursive centrality: Hubs and Authorities (Jon Kleinberg^[10])

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Overview Key Points:

- The field of complex networks came into existence in the late 1990s.
- Explosion of papers and interest since 1998/99.
- ► Hardened up much thinking about complex systems.
- Specific focus on networks that are large-scale, sparse, natural or man-made, evolving and dynamic, and (crucially) measurable.
- Three main (blurred) categories:
 - 1. Physical (e.g., river networks),
 - 2. Interactional (e.g., social networks),
 - 3. Abstract (e.g., thesauri).

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Overview Key Points (cont.):

- Obvious connections with the vast extant field of graph theory.
- But focus on dynamics is more of a physics/stat-mech/comp-sci flavor.
- Two main areas of focus:
 - 1. Description: Characterizing very large networks
 - Explanation: Micro story ⇒ Macro features
- Some essential structural aspects are understood: degree distribution, clustering, assortativity, group structure, overall structure,...
- Still much work to be done, especially with respect to dynamics...

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