Data from our man Zipf

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Principles of Complex Systems, Vols. 1, 2, & 3D CSYS/MATH 6701, 6713, & a pretend number, 2024-2025

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From the Preface—

Nearly twenty-five years ago it occurred to me that we might gain considerable insight into the mainsprings of human behavior if we viewed it purely as a natural phenomenon like everything else in the universe, ...

Human Behavior/Principle of Least Effort:

And-

... the expressed purpose of this book is to establish The Principle of Least Effort as the primary principle that governs our entire individual and collective behavior ...

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(f = frequency, r = rank).

TABLE 2-1 Arbitrary Ranks with Frequencies in James Joyce's Ulysses (Hanley Index) Product of I and II
(r × f = C) 265,500 262,200 277,800 286,800 278,800 2,653 1,311 926 717 556 265 133 84 62 50 26,530 26,220 27,780 28,680 27,800 26,500 26,600 25,200 24,800 25,000 26,000 265,000 266,000 252,000 248,000 250,000 260,000 24,000 24,000 24,000 25,000 20,000 20,000 29,899 2,000 3,000 4,000 5,000 10,000 240,000 240,000 240.000 200,000 200,000 298,990

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 $f \sim r^{-1}$ for word frequency:

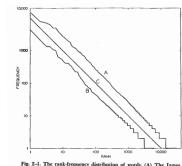


Fig. 2-1. The rank-frequency distribution of words. (A) The James Joyce data; (B) the Eldridge data; (C) ideal curve with slope of nega-tive unity.

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The Principle of Least Effort:

Zipf's framing (p. 1):

- "... a person in solving his immediate problems will view these against the background of his probable future problems as estimated by himself."
- "... he will strive ... to minimize the total work that he must expend in solving both his immediate problems and his probable future problems."
- "[he will strive to] minimize the probable average rate of his work-expenditure..."

George Kingsley Zipf:

In brief:

- & Zipf ☑ (1902–1950) was a linguist at Harvard, specializing in Chinese languages.
- Unusual passion for statistical analysis of texts.
- Studied human behavior much more generally ...

Zipf's masterwork:

- Human Behavior and the Principle of Least Effort" Addison-Wesley, 1949 Cambridge, MA [2]
- & Bonus field of study: Glottometrics.
- 🙈 Bonus 'word' word: Glossolalia. 🗹

Rampaging research Data from our mar

Within Human Behavior and the Principle of Least Effort:

& City sizes

retail stores in cities

services (barber shops, beauty parlors, cleaning, ...)

people in occupations

one-way trips in cars and trucks vs. distance

new items by dateline

& weight moved between cities by rail

telephone messages between

people moving vs. distance

marriages vs. distance

& Observed general dependency of 'interactions' between cities A and B on $P_A P_B / D_{AB}$ where P_A and P_B are population size and D_{AB} is distance between A and B. \Rightarrow 'Gravity Law.'

Zipf's basic idea:

Zipf in brief Forces of Unification and Diversification: Zipfian empirics

Easiest for the speaker to use just one word. Encoding is simple but decoding is hard

Zipf uses the analogy of tools: one tool for all tasks.

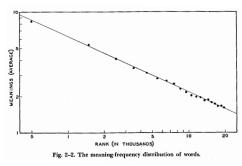
- Optimal for listener if all pieces of information correspond to different words (or morphemes).
- Analogy: a specialized tool for every task.
 - Decoding is simple but encoding is hard
- Zipf thereby argues for a tension that should lead to an uneven distribution of word usage.
- No formal theory beyond this... (more later [1])

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 $\red{solution}$ Number of meanings $m_r \propto f_r^{1/2}$ where r is rank and f_r is frequency.



Zipfian empirics:

Article length in the Encyclopedia Britannica:

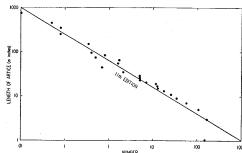


Fig. 5-3. The number of different articles of like length in samples of the 11th edition of the Encyclopaedia Britannica. Lengths in inches.

Not a rank-ordered plot; flipped frequency distribution.

 $\mbox{\&}$ (?) slope of -3/5 corresponds to $\gamma = 5/3$.

Zipfian empirics:

Population size of districts:

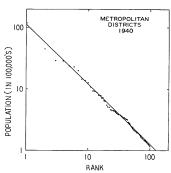


Fig. 9-2. Metropolitan districts. One hundred largest in the U. S. A. in 1940, ranked in the order of decreasing population size.

 $\alpha = 1$ corresponds to $\gamma = 1 + 1/\alpha = 2$.

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Number of employees in organizations

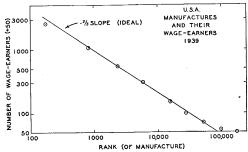


Fig. 9-8. Manufactures and their wage earners in the U. S. A. in 1939, with the manufactures ranked in the order of their decreasing number of wage earners.

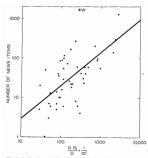
 $\alpha = 2/3$ corresponds to $\gamma = 1 + 1/\alpha = 5/2$.

Zipfian empirics:

 \clubsuit # news items as a function of population P_2 of location in the Chicago Tribune

 $D = distance, <math>P_1 = Chicago's population$

Solid line = +1 exponent.



Zipfian empirics:

obituaries in the New York Times for locations with population P_2 .

D = distance, $P_1 =$ New York's population

Solid line = +1 exponent.

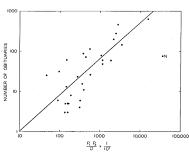


Fig. 9-11. Number of obituaries in The New York Times (N represents Newark, New Jersey).

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Movement of stuff between cities

 $Arr D = \text{distance}, P_1 \text{ and } P_2 = \text{city populations}.$

Solid line = +1 exponent.

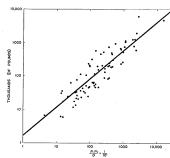


Fig. 9–14. Railway express. The movement by weight (less carload lots) between 13 arbitrary cities in the U. S. A., May 1939.

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Length of trip versus frequency of trip.

Not a rank-ordered plot; flipped frequency distribution. Solid line = -1/2 exponent corresponds to $\gamma=2$.

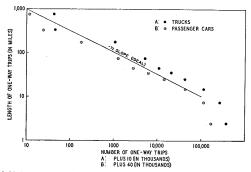


Fig. 9-19. Trucks and passenger cars: the number of one-way trips of like length.

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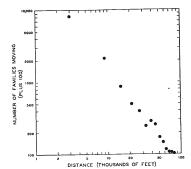


Fig. 9-23. Number of families (plus 100) moving varying distances within or between separated areas in Cleveland during 1933-1935 (adapted from the data of S. A. Stouffer).

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The probability of marriage?

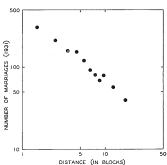


Fig. 9-22. Number of marriage licenses issued to 5,000 pairs of applicants living within Philadelphia in 1931 and separated by varying distances (the data of J. H. S. Bossard).

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100 NUMBER Fig. 2-3. The number-frequency relationship of words. (A) Homer's Iliad; (B) James Joyce's Ulysses.

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TABLE 2-4

The dispersion of single-page intervals between the f-1 repetitions of all words that occur with ten arbitrarily selected frequencies of occurrence, f_i in Joyce's Ubyster (Hanley's Index).

No. of	1	f - 1	Intervals between Repetitions in Order of Appearan										
Sample			1	2	3	4	5	6	7	8	9	10	11
1	6	5	62	55	62	58	52		_				Т
2	12	11	7	19	15	16	9	12	18	16	12	15	14
3	16	15	6	10	10	13	18	11	16	11	11	1 0	11
4	17	16	4	3	5	6	4	8	5	10	111	9	14
5	18	17	9	11	6	5	6	7	7	6	9	6	1 2
6	19	18	3	8	5	11	5	6	13	0	6	5	1 6
7	21	20	3	4 1	10	5	8	9	3	10	8	11	1 2
8	22	21	7	5	8	12	- 6	9	5	0	6	1 7	
9	23	22	3	5	6	4	8	4	3	2	7	3	4
10	24	23	3	5	2	1	3 /	3	3	3	l á.	5	2

			_ 11	he Int	etvals	from	13 th	ough	23					
No. of	,		Intervals between Repetitions in Order of Appearance											
Sample	Ľ		1.5	14	15	16	17	18	19	20	21	22	23	
3	16	15	6	8	12							-		
4 .	17	16	8	6	7	8			1					
5	18	17	5	6	6	5	4					l		
6	19	18	2	- 7	10	5	7	4	1					
7	21	20	6	6	2	1	7	8	4	2	í			
8	22	21	6	6	7	10	7	10	9	1 5	2			
9	23	22	5	7	3	6	2	7	2	1 3	ĩ	3	l	
10	24	23	7	3	2	2	0	Ιí	2	2	2	8	1 3	

Comment #60 in Math and the City by Strogatz, NYT:

60. May 20, 2009 9:26 am

Link

George Kingsley Zipf was my teacher at Harvard...He had given a class project where we were to see if Chemical Companies when ranked by the number of different chemicles they produced, followed his Law of Least Effort. I missed turning in my assignment due to the accidental death of my father....When I returned from the funeral I was given a message to call Dr. Zipf immediately. I did and when I explained why I was late turning in the data. He said, "Well, your father's gone and I (Zipf) have no pipeline to God. I expect the data will be on my desk tomorrow morning!".....My mother, sister and extended family spread huge books of trade magazines on the kitchen and dining room tables and furiously went to work....We worked until late in the night and finished the project..... I drove to Harvard the next morning and angrily gave the hundreds of 'three by five cards' to Zipf. All he said was, "Thank you." Years later, I wondered whether his'meaness' had really been his way of helping me and my family to take our minds of our grief that day and concentrate on finishing my assignment. In my youth I thought not, but now as I approach 80, I like to think his seemingly hurtful attitude was really an act of kindness,,,,,

 $-Jim\ Terry$

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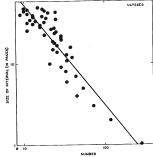


Fig. 2-4. The interval-frequency relationship. The number of dif-ferent intervals of like size (in pages) between the repetitions of words occurring five times in Joyce's *Ulysses*.

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ORDER OF INTERVAL IN TIME Fig. 2-5. The distribution of intervals between repetitions among the words occurring twenty-four times in James Joyce's Ulysses

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TABLE 2_2

The Number-Frequency Relationship, $N(f^p-1/4)=C$, of (I) some Arbitrary Lower Frequencies of (II) Joyce's Ulysses and (III) four Latin plays of Plautus.

1	Calculated N(f ² - 1/2)				
Frequency (f)	II Ulysses	III Plautus			
1	12,324	4,075			
2	15,410	4,490			
3	19,193	4,280			
4	20,239	4,750			
5	22,424	3,985			
6	22,773	4,504			
7	23,546	4,241			
8	23,651	4,399			
9	24,063	4,366			
10	22,145	4,289			
15	21,576	2,922			
20	27,844	5,996			
30	18,000	3,600			
40	25,600	4,800			
50	22,500	5,000			

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Calculated values of negative slopes, errors, and Y-intercepts of the number, N, of interval-sizes, I_p between the repetition of words in 14 frequency-classes, f, as fitted to the equation aX + Y = C where $X = \log N$ and Y = C= $\log I_p$ and where I_r has integral values from 1 through 21 inclusive.

I No. of Analysis	II Frequency of Occur. (f)	III No. of Different Words of like f	Slope of Best Line of Y's (negative) (Y = log I _l)	V Error (root-mean- square)	VI Y-intercept (antilog thereof)
1	5	906	1.21	.151	716
2	6	637	1.20	.169	666
3	10	222	1.27	.106	677
4	12	155	1.24	.111	491
5	15	96	1.15	.096	328
6	16	86	.96	.124	153
7	17	79	1.22	.174	422
8	18	62	1.20	.120	264
9	19	63	1.21	.148	350
10	20	69	1.29	.124	944
11	21	52	1.05	.138	212
12	22	50	1.10	.117	264
13	23	44	1.24	.113	352
14F	24	34	1.01	.158	136
15Z	24	34	1.05	.147	153

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The Frequencies and Average Lengths of Words (A) in terms of the number of phonemes, and (B) in terms of the number of syllables in (A) American newspaper English and in (B) the Latin of Plautus.

			ERICAN NEW According to R.				(B) LATIN OF PLAUTUS						
	fumber of Occur- rences	Number of Words	Average Number of Phonemes	Number of Occur- rences	Number of Words	Average Number of Phonemes	Number of Occur- rences	Number of Words	Average Number of Syllables	Number of Occur- rences	Number of Words	Averag Numbe of Syllable	
64	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	2976 1079 516 294 212 151 105 84 86 45 40 37 25 28 26 17 18	(6.656) (6.151) (6.015) (6.081) (5.589) (5.768) (5.333) (5.654) (3.174) (5.377) (4.825) (3.499) (5.00) (4.897) (5.008) (4.166) (6.100) (4.735)	31 32 33 34 35 36 37 39 40 41 42 43 44 45 46 47 48	6 4 6 2 5 5 5 2 2 4 1 7 1 4 1 2 2 5 1 3 3	(5,903)	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19	5429 1198 492 299 161 126 87 69 54 43 44 36 33 31 13 25 21 21	(3.23) (2.92) (2.77) (2.05) (2.53) (2.53) (2.39) (2.44) (2.35) (2.30) (2.30) (2.30) (2.09) (2.07) (2.40) (2.04) (2.04)	31 32 33 34 35 36 37 38 39 40 41 43 44 45 46 47 48 49 50	8 3 4 6 3 5 7 2 2 4 3 3 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(2.05)	
	20 21 22 23 24 25 26 27 28 29	16 13 11 6 8 10 9 6 5	(3.455)	51 52 54 55 56 58 60 61–4290	1 3 1 1 1 2 2 1 71	(3.333)	20 21 22 23 24 25 26 27 28 29	15 10 8 8 9 11 7 9	(2.08)	51 53 54 55 56 58 61 62-514 33,094	2 4 1 1 2 1 3 71 8,437	(1.40)	

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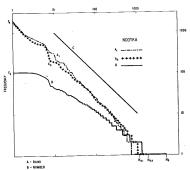


Fig. 3–1. Nootka. The rank-frequency distribution of (A_1) "varimorphs," (A_2) morphemes, and (B) holophrases.

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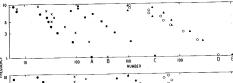
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IOO NUMBER Fig. 3-9. English and German morphemes. The number-frequency distributions of nine different authors.

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TABLE 6-1

The X Number of Different Genera of Like Y Number of Different Species of the Flora of Ceylon (After J. C. Willis)

No. of Genera X	No. of Specie			
573	1			
176	2			
85	3			
49	4			
36	5			
20	6			
etc.				

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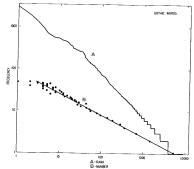
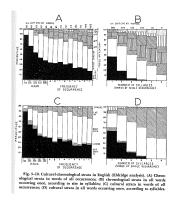


Fig. 3-7. Gothic words. (A) Rank-frequency distribution; (B) number-frequency distribution.

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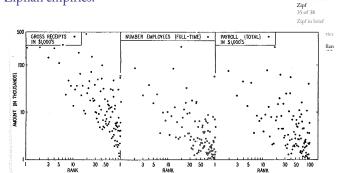
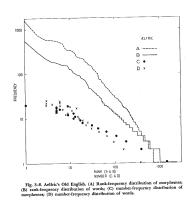


Fig. 9-9. Gross receipts, number of full-time employees, and total payroll of service establishments in the U. S. A. in 1939 when the service establishments are ranked in the order of their decreasing number of members as in Fig. 9-4 supra.

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Zipfian empirics (p. 176):

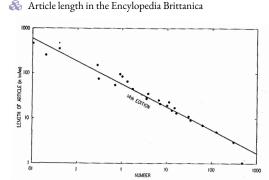


Fig. 5-2. The number of different articles of like length in samples of the 14th edition of the Encyclopaedia Britannica. Lengths in inches.

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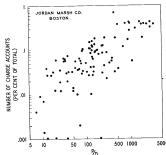


Fig. 9-13. Charge accounts of Jordan Marsh Co., Boston, in 96 cities and towns in Massachusetts, New Hampshire, and Maine, with their percentages of total charge accounts plotted against the communities values of T/D.

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species per genera:

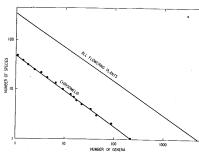


Fig. 6–1. The number of different genera of like number of different species for all flowering plants and for Chrysomelid heetles (from the J. C. Willis data, after reversing the co-ordinates).



 $\alpha = 1$ corresponds to $\gamma = 1 + 1/\alpha = 2$.

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References I

[1] R. Ferrer-i-Cancho and R. V. Solé. Least effort and the origins of scaling in human language. Proc. Natl. Acad. Sci, 100:788–791, 2003. pdf

[2] G. K. Zipf. Human Behaviour and the Principle of Least-Effort. Addison-Wesley, Cambridge, MA, 1949. The PoCSverse Data from our man Zipf 38 of 38 Zipf in brief Zipfian empirics

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References