Overview of Complex Networks

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Principles of Complex Systems, Vols. 1, 2, & 3D CSYS/MATH 6701, 6713, & a pretend number, 2024-2025

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net-work | 'net, wərk |

noun

1 an arrangement of intersecting horizontal and vertical lines.

- a complex system of roads, railroads, or other transportation routes : a network of railroads.
- 2 a group or system of interconnected people or things: a trade network.
 - a group of people who exchange information, contacts, and experience for professional or social purposes : a support network.
 - a group of broadcasting stations that connect for the simultaneous broadcast of a program : the introduction of a second TV network | [as adj.] network television.
 - a number of interconnected computers, machines, or operations: specialized computers that manage multiple outside connections to a network | a local cellular phone network.
 - a system of connected electrical conductors.

verb [trans.]

connect as or operate with a network: the stock exchanges have proven to be resourceful in networking these deals.

- link (machines, esp. computers) to operate interactively : [as adj.] (**networked**) networked workstations.
- [intrans.] [often as n.] (**networking**) interact with other people to exchange information and develop contacts, esp. to further one's career: the skills of networking, bargaining, and negotiation.

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Thesaurus deliciousness:

network

noun

- 1 a network of arteries WEB, lattice, net, matrix, mesh, crisscross, grid, reticulum, reticulation; Anatomy plexus.
- 2 a network of lanes MAZE, labyrinth, warren, tangle.
- 3 a network of friends SYSTEM, complex, nexus, web, webwork.

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Ancestry:

From Keith Briggs's etymological investigation:



[http://serialconsign.com/2007/11/we-put-net-network]

Opus reticulatum: A Latin origin?



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Ancestry:

First known use: Geneva Bible, 1560

'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

3 1658-: reticulate structures in animals

3 1839-: rivers and canals

<page-header> 1869-: railways

1883-: distribution network of electrical cables

4 1914–: wireless broadcasting networks

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Ancestry:

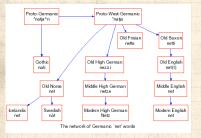
Net and Work are venerable old words:

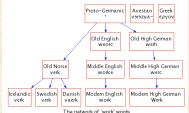


Net' first used to mean spider web (King Ælfréd, 888).



Work' appear to have long meant purposeful action.





'Network' = something built based on the idea of natural, flexible lattice or web.



& c.f., ironwork, stonework, fretwork.

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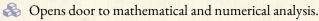
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Key Observation:

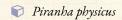
Many complex systems can be viewed as complex networks of physical or abstract interactions.



Dominant approach of the first decade was of a theoretical-physics/stat-mechish flavor.

Mindboggling amount of work published on complex networks since 1998...

🚓 ... largely due to your typical theoretical physicist:





- Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)
 - See also: https://xkcd.com/793/

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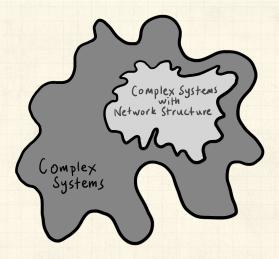
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Complex Systems is the Big Story:



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Only a bit networky: Fluids-at-large (the atmosphere, oceans, ...), organism cells, ...



Popularity (according to Google Scholar)



"Collective dynamics of 'small-world' networks"

Watts and Strogatz,

Nature, **393**, 440–442, 1998. [20]

Times cited: $\sim 27,184$ \Box (as of October 8, 2015)



"Emergence of scaling in random networks"

Barabási and Albert,
Science, **286**, 509–511, 1999. [2]

Times cited: $\sim 23,532$ (as of October 8, 2015)

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Review articles:



"Complex Networks: Structure and Dynamics" Boccaletti et al.,
Physics Reports, **424**, 175–308, 2006. [3]

Times cited: $\sim 5,791$ (as of October 8, 2015)



"The structure and function of complex networks"

M. E. J. Newman,

Times cited: $\sim 13,156$ (as of October 8, 2015)

SIAM Rev., 45, 167-256, 2003. [15]



"Statistical mechanics of complex networks"

Albert and Barabási,
Rev. Mod. Phys., 74, 47–97, 2002. [1]

Times cited: $\sim 26,636$ (as of May 9, 2023)

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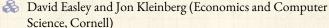
Popularity according to textbooks:

Textbooks:



Mark Newman (Physics, Michigan)

"Networks: An Introduction"



Science, Cornell)

"Networks, Crowds, and Markets: Reasoning About a Highly Connected World"

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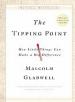
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Popularity according to popular books:



The Tipping Point: How Little Things can make a Big Difference—Malcolm Gladwell [9]



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Nexus: Small Worlds and the Groundbreaking Science of Networks—Mark Buchanan



Popularity according to popular books:



Linked: How Everything Is Connected to Everything Else and What It Means—Albert-Laszlo Barabási



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Six Degrees: The Science of a Connected Age—Duncan Watts [19]



Numerous others ...

- & Complex Social Networks—F. Vega-Redondo [18]
- Fractal River Basins: Chance and Self-Organization—I. Rodríguez-Iturbe and A. Rinaldo [16]
- & Random Graph Dynamics—R. Durette
- & Scale-Free Networks—Guido Caldarelli
- Evolution and Structure of the Internet: A Statistical Physics Approach—Romu Pastor-Satorras and Alessandro Vespignani
- & Complex Graphs and Networks—Fan Chung
- 🙈 Social Network Analysis—Stanley Wasserman and Kathleen Faust
- Handbook of Graphs and Networks—Eds: Stefan Bornholdt and H. G. Schuster [5]
- & Evolution of Networks—S. N. Dorogovtsev and J. F. F. Mendes [8]

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More observations

But surely networks aren't new ...



Graph theory was well established ...



Study of social networks started in the 1930's ...



So why all this 'new' research on networks?



Answer: Oodles of Easily Accessible Data.



We can now inform (alas) our theories with a much more measurable reality.*



Graph theory missed "becoming": Stories = Characters + Time



A worthy goal: establish mechanistic explanations.

*If this is upsetting, maybe string theory is for you ...

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More observations

Internet-scale data sets can be overly exciting.

Witness:

The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired)

The Unreasonable Effectiveness of Data," Halevy et al. [10].

🗞 c.f. Wigner's "The Unreasonable Effectiveness of Mathematics in the Natural Sciences" [21]

But:

For scientists, description is only part of the battle.

We still need to understand.

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Super Basic definitions

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Nodes = A collection of entities which have properties that are somehow related to each other



🍰 e.g., people, forks in rivers, proteins, webpages, organisms, ...

Links = Connections between nodes

Links may be directed or undirected.



Links may be binary or weighted.

Other spiffing words: vertices and edges.



Super Basic definitions

Node degree = Number of links per node

 \aleph Notation: Node *i*'s degree = k_i .

 $k_i = 0,1,2,...$

Notation: the average degree of a network = $\langle k \rangle$ (and sometimes z)

& Connection between number of edges m and average degree:

$$\langle k \rangle = \frac{2m}{N}.$$

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Super Basic definitions

Adjacency matrix:

We can represent a network by a matrix A with link weight a_{ij} for nodes i and j in entry (i,j).

ቆ e.g.,

$$A = \left[\begin{array}{ccccc} 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \end{array} \right]$$

For numerical work, we always use sparse matrices.

For many real networks, A is a function of time.

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So what passes for a complex network?



Complex networks are large (in node number)



Complex networks are sparse (low edge to node ratio)



Complex networks are usually dynamic and evolving



Complex networks can be social, economic, natural, informational, abstract, ...

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Physical networks

River networks

Neural networks

Trees and leaves

Blood networks

The Internet (pipes)

Road networks

Power grids









Distribution (branching) versus redistribution (cyclical)

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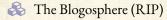
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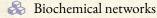
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Interaction networks





Gene-protein networks

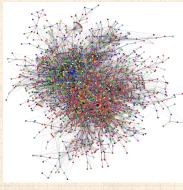
Food webs: who eats whom

Airline networks

Call networks (AT&T)

备 The Media

The internet (World Wide Web)



datamining.typepad.com

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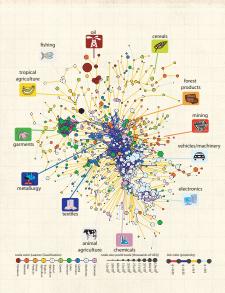


topics:

Hidalgo et al.'s "The Product Space Conditions the Development of Nations" [11]

How do products depend on each other, and how does this network evolve?

How do countries depend on each other for water, energy, people (immigration), investments?



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Interaction networks: social networks

Snogging

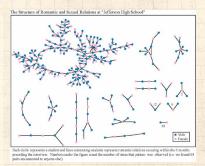
Friendships

Acquaintances

Boards and directors

🗞 Organizations

facebook twitter,



(Bearman et al., 2004)

Remotely sensed' by: email activity, instant messaging, phone logs (*cough*).



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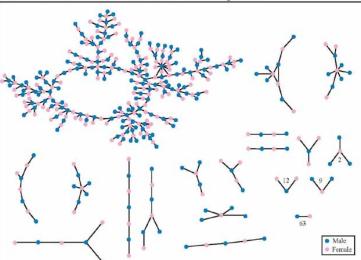
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The Structure of Romantic and Sexual Relations at "Jefferson High School"



Each circle represents a student and lines connecting students represent romantic relations occuring within the 6 months preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone clse).

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Relational networks

- Consumer purchases (Walmart, Target, Amazon, ...)
- A Thesauri: Networks of words generated by meanings
- Knowledge/Databases/Ideas
- & Large Language Models

common tags cloud | list

community daily dictionary education encyclopedia english free imported info information internet knowledge learning news reference research resource resources search tools useful web web2.0 wiki wikipedia

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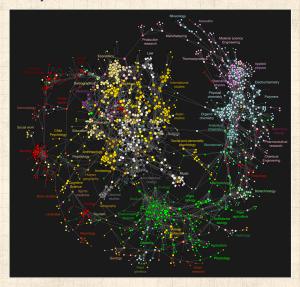
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Clickworthy Science:



"Clickstream Data Yields High-Resolution Maps of Science", Bollen et al. [4], 2009.

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HE MISREADING



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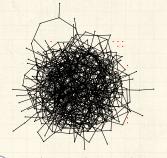
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A notable feature of large-scale networks:



Graphical renderings are often just a big mess.



← Typical hairball

- number of nodes N = 500
- number of edges m = 1000
- \bigcirc average degree $\langle k \rangle = 4$

And even when renderings somehow look good:

"That is a very graphic analogy which aids understanding wonderfully while being, strictly speaking, wrong in every possible way"

said Ponder [Stibbons] — Making Money, T. Pratchett.



We need to extract digestible, meaningful aspects.

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Some key aspects of real complex networks:

& degree distribution*

assortativity

A homophily

clustering

amotifs ...

modularity

concurrency

hierarchical scaling

network distances

centrality

efficiency

interconnectedness

robustness

Plus coevolution of network structure and processes on networks.

* Degree distribution is the elephant in the room that we are now all very aware of ...

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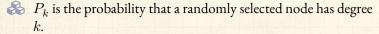
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Properties

1. degree distribution P_k



& k = node degree = number of connections.

ex 1: Pure (Erdős-Rényi) random networks have Poisson degree distributions:

Insert assignment question

$$P_k = e^{-\langle k \rangle} \frac{\langle k \rangle^k}{k!}$$

 \Leftrightarrow ex 2: "Scale-free" networks: $P_k \propto k^{-\gamma} \Rightarrow$ 'hubs'.

link cost controls skew.

A hubs may facilitate or impede contagion.

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Properties

Note:

- Pure (Erdős-Rényi) random networks are a mathematical construct.
- Scale-free' networks are growing networks that form according to a plausible mechanism.
- Randomness is out there, just not to the degree of a completely random network.
- "Becoming": Stories = Characters + Time

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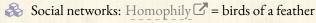
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2. Assortativity/3. Homophily:



e.g., degree is standard property for sorting: measure degree-degree correlations.

Assortative network: [14] similar degree nodes connecting to each other.

Often social: company directors, coauthors, actors.

Disassortative network: high degree nodes connecting to low degree nodes.

Often techological or biological: Internet, WWW, protein interactions, neural networks, food webs.

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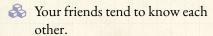
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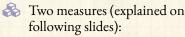


Local socialness:

4. Clustering:







1. Watts & Strogatz [20]

$$C_1 = \left\langle \frac{\sum_{j_1 j_2 \in N_i} a_{j_1 j_2}}{k_i (k_i - 1)/2} \right\rangle_i$$

2. Newman [15]

$$C_2 = \frac{3 \times \text{\#triangles}}{\text{\#triples}}$$

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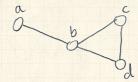
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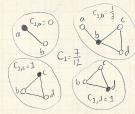
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Example network:



Calculation of C_1 :





 C_1 is the average fraction of pairs of neighbors who are connected.



Fraction of pairs of neighbors who are connected is

$$\frac{\sum_{j_1 j_2 \in N_i} a_{j_1 j_2}}{k_i (k_i - 1)/2}$$

where k_i is node i's degree, and N_i is the set of i's neighbors.



Averaging over all nodes, we have:

$$C_1 = \frac{1}{n} \sum_{i=1}^n \frac{\sum_{j_1 j_2 \in N_i} a_{j_1 j_2}}{k_i (k_i - 1)/2} = \left\langle \frac{\sum_{j_1 j_2 \in N_i} a_{j_1 j_2}}{k_i (k_i - 1)/2} \right\rangle_i$$

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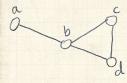
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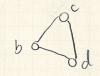


Triples and triangles

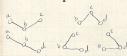
Example network:



Triangles:



Triples:



Nodes i_1 , i_2 , and i_3 form a triple around i_1 if i_1 is connected to i_2 and i_3 .

- Nodes i_1 , i_2 , and i_3 form a triangle if each pair of nodes is connected
- $\text{The definition } C_2 = \frac{3 \times \text{\#triangles}}{\text{\#triples}}$ measures the fraction of closed triples
- The '3' appears because for each triangle, we have 3 closed triples.
- Social Network Analysis (SNA): fraction of transitive triples.

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Clustering:

Sneaky counting for undirected, unweighted networks:

 \Leftrightarrow If the path $i-j-\ell$ exists then $a_{ij}a_{j\ell}=1$.

 \clubsuit We want $i \neq \ell$ for good triples.

 $\text{In general, a path of } n \text{ edges between nodes } i_1 \text{ and } i_n \\ \text{travelling through nodes } i_2, i_3, ... i_{n-1} \text{ exists } \Longleftrightarrow \\ a_{i_1 i_2} a_{i_2 i_3} a_{i_3 i_4} \cdots a_{i_{n-2} i_{n-1}} a_{i_{n-1} i_n} = 1.$

8

$$\# \text{triples} = \frac{1}{2} \left(\sum_{i=1}^{N} \sum_{\ell=1}^{N} \left[A^2 \right]_{i\ell} - \text{Tr} A^2 \right)$$



$$\#$$
triangles $=\frac{1}{6}$ Tr A^3

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 $\ref{eq:constraints}$ For sparse networks, C_1 tends to discount highly connected nodes.

 $\begin{cases} \&\begin{cases} \&\begin{cases} C_2 \end{cases} is a useful and often preferred variant \end{cases}$

 \clubsuit In general, $C_1 \neq C_2$.

 $\ensuremath{\mathfrak{S}}$ C_1 is a global average of a local ratio.

 $\ensuremath{\mathfrak{S}} C_2$ is a ratio of two global quantities.

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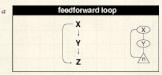
5. motifs:



small, recurring functional subnetworks



& e.g., Feed Forward Loop:



Shen-Orr, Uri Alon, et al. [17]

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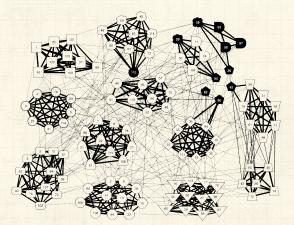
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6. modularity and structure/community detection:



Clauset et al., 2006 [7]: NCAA football

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7. concurrency:

- transmission of a contagious element only occurs during contact
- nather obvious but easily missed in a simple model
- 🙈 dynamic property—static networks are not enough
- & knowledge of previous contacts crucial
- beware cumulated network data
- & Kretzschmar and Morris, 1996 [13]
- "Temporal networks" become a concrete area of study for Piranha Physicus in 2013.

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8. Horton-Strahler ratios:



Metrics for branching networks:

- Method for ordering streams hierarchically
- Number: $R_n = N_\omega/N_{\omega+1}$
- Segment length: $R_l = \langle l_{\omega+1} \rangle / \langle l_{\omega} \rangle$
- ightharpoonup Area/Volume: $R_a = \langle a_{\omega+1} \rangle / \langle a_{\omega} \rangle$



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9. network distances:

(a) shortest path length d_{ij} :

- \Leftrightarrow Fewest number of steps between nodes i and j.
- (Also called the chemical distance between i and j.)

(b) average path length $\langle d_{ij} \rangle$:

- & Average shortest path length in whole network.
- Good algorithms exist for calculation.
- Weighted links can be accommodated.

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9. network distances:

 \clubsuit network diameter d_{\max} :

Maximum shortest path length between any two nodes.

 $\mbox{\ensuremath{\&}}$ closeness $d_{\rm cl} = [\sum_{ij} d_{ij}^{-1}/\binom{n}{2}]^{-1}$:

Average 'distance' between any two nodes.

- \Leftrightarrow Closeness handles disconnected networks $(d_{ij} = \infty)$
- $d_{\rm cl} = \infty$ only when all nodes are isolated.
- Closeness perhaps compresses too much into one number

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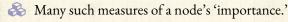
Examples of Complex Networks

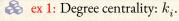
Properties of Complex Networks

Nutshell



10. centrality:





ex 2: Node i's betweenness = fraction of shortest paths that pass through i.

ex 3: Edge ℓ 's betweenness = fraction of shortest paths that travel along ℓ .

ex 4: Recursive centrality: Hubs and Authorities (Jon Kleinberg [12]) The PoCSverse Overview of Complex Networks 50 of 59

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Interconnected networks and robustness (two for one deal):

"Catastrophic cascade of failures in interdependent networks" [6]. Buldyrev et al., Nature 2010.

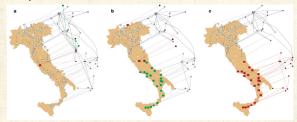


Figure 1 [Modelling a blackout in laby. Illustration of an iterative process of a cascade of failure using real-world date from a power network (located on the map of laby) and an internet network (shifted above the map) that were 1000°C. The network of the map of laby) and an internet network (shifted above the map) that were 1000°C. The networks are drawn using the real geographical locations and every internet server is connected to the geographically nearest power station. A tone power station is removed (red node on map) from the power network and na result the Internet nodes depending on it are removed from the power network and na result the Internet nodes depending on it are removed indications.

at the next step are marked in green. b, Additional nodes that were disconnected from the Internet communication network gain component are removed (red nodes above map). As a result the power stations depending on them are removed from the power network (feel nodes on map). Again, the nodes that will be disconnected from the gaint cluster at the next step are marked in green. C, Additional nodes that were disconnected may be a seen as the proper seal of the property of the

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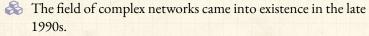
Properties of Complex Networks

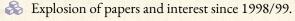
Nutshell



Nutshell:

Overview Key Points:





Hardened up much thinking about complex systems.

Specific focus on networks that are large-scale, sparse, natural or people-made, evolving and dynamic, and (crucially) measurable.

Three main (blurred) categories:

- 1. Physical (e.g., river networks),
- 2. Interactional (e.g., social networks),
- 3. Abstract (e.g., thesauri).

To solve network problems: "Follow the edges."

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