Structure detection methods

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Outline

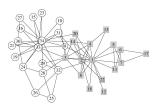
Overview

Methods

Hierarchy by aggregation Hierarchy by division Hierarchy by shuffling Spectral methods Hierarchies & Missing Links Overlapping communities Link-based methods General structure detection

References

Structure detection



▲ Zachary's karate club [19, 12]

Possible substructures: hierarchies, cliques, rings, ...

All combinations of substructures.

Much focus on hierarchies...



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The issue:

how do we

elucidate the

large networks

internal structure of

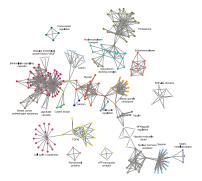
across many scales?

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Hierarchy by aggregati



"Community detection in graphs" 🗗 Santo Fortunato, Physics Reports, **486**, 75–174, 2010. [6]



Hierarchy by aggregation—Bottom up:

Idea: Extract hierarchical classification scheme for N objects by an agglomeration process.

Need a measure of distance between all pairs of objects.

& Example: Ward's method [7]

Procedure:

1. Order pair-based distances.

2. Sequentially add links between nodes based on closeness.

3. Use additional criteria to determine when clusters are meaningful.

Clusters gradually emerge, likely with clusters inside of clusters.

Call above property Modularity.

Works well for data sets where a distance between all objects can be specified (e.g., Aussie Rules [9]).

Hierarchy by aggregation

Bottom up problems:

Tend to plainly not work on data sets representing

Good at finding cores of well-connected (or similar) nodes... but fail to cope well with

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Top down:

Idea: Identify global structure first and recursively uncover more detailed structure.

Basic objective: find dominant components that have significantly more links within than without, as compared to randomized version.

We'll first work through "Finding and evaluating" community structure in networks" by Newman and Girvan (PRE, 2004). [12]

A See also

Hierarchy by division

Hierarchy by division

5 Record when

removed.

structure.

1. "Scientific collaboration networks. II. Shortest paths, weighted networks, and centrality" by Newman (PRE, 2001). [10, 11]

2. "Community structure in social and biological networks" by Girvan and Newman (PNAS, 2002). [7]



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Idea: Edges that connect communities have higher betweenness than edges within communities.

One class of structure-detection algorithms:

2. Remove edge with highest betweenness.

3. Recompute edge betweenness

components appear as a function of # edges

6 Generate dendogram

revealing hierarchical

1. Compute edge betweenness for whole network.

4. Repeat steps 2 and 3 until all edges are removed.



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Red line indicates appearance of four (4) components at a certain level.



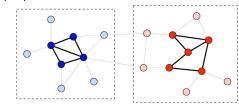
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networks with known modular structures.

peripheral, in-between nodes.



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Key element for division approach:

- Recomputing betweenness.
- links that connect large communities if other links carry majority of shortest paths.

When to stop?:

- A How do we know which divisions are meaningful?
- within component nodes to that expected for randomized version:

$$Q = \sum_{i} [e_{i\,i} - a_i^2]$$

where $e_{i,j}$ is the fraction of (undirected) edges and $a_i = \sum_i e_{ij}$ is the fraction of edges with at least one end in community i. \square

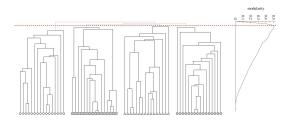
Hierarchy by division

Test case:

- Generate random community-based networks.
- N = 128 with four communities of size 32.
- Add edges randomly within and across communities.
- Example:

$$\langle k \rangle_{\text{in}} = 6 \text{ and } \langle k \rangle_{\text{out}} = 2.$$

Hierarchy by division



- Arr Maximum modularity $Q \simeq 0.5$ obtained when four communities are uncovered.
- Further 'discovery' of internal structure is somewhat meaningless, as any communities arise accidentally.

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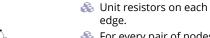
General structure References

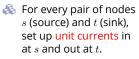


Rections in Zachary's karate club network. [19]

Betweenness for electrons:

Hierarchy by division





Measure absolute current along each edge ℓ , $|I_{\ell,st}|$.

- \Re Sum $|I_{\ell,st}|$ over all pairs of nodes to obtain electronic betweenness for edge ℓ .
- (Equivalent to random walk betweenness.)
- Contributing electronic betweenness for edge between nodes *i* and *i*:

$$B_{ij,\,st}^{\,\mathrm{elec}} = a_{ij} |V_{i,\,st} - V_{j,\,st}|. \label{eq:Beleen}$$

Electronic betweenness

- Define some arbitrary voltage reference.
- & Kirchhoff's laws: current flowing out of node i must balance:

$$\sum_{j=1}^N \frac{1}{R_{ij}}(V_j-V_i) = \delta_{is} - \delta_{it}.$$

- \Re Between connected nodes, $R_{ij} = 1 = a_{ij} = 1/a_{ij}$.
- \Re Between unconnected nodes, $R_{ij} = \infty = 1/a_{ij}$.
- We can therefore write:

$$\sum_{i=1}^N a_{ij}(V_i-V_j) = \delta_{is} - \delta_{it}.$$

Some gentle jiggery-pokery on the left hand side: $\sum_{j} a_{ij} (V_i - V_j) = \frac{V_i}{\sum_{j} a_{ij}} - \sum_{j} a_{ij} V_j$ $=V_{i}k_{i}-\sum_{j}a_{ij}V_{j}=\sum_{j}\left[k_{i}\delta_{ij}V_{j}-a_{ij}V_{j}\right]$ $= [(\mathbf{K} - \mathbf{A})\vec{V}]_i$

Electronic betweenness

& Write right hand side as $[I^{\text{ext}}]_{i,st} = \delta_{is} - \delta_{it}$, where I_{ext}^{ext} holds external source and sink currents.

Matrixingly then:

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Hierarchy by division

$$(\mathbf{K} - \mathbf{A})\vec{V} = I_{st}^{\mathsf{ext}}.$$

- & **L** = **K A** is a beast of some utility—known as the Laplacian.
- Solve for voltage vector \vec{V} by **LU** decomposition (Gaussian elimination).
- Do not compute an inverse!
- Note: voltage offset is arbitrary so no unique
- Presuming network has one component, null space of $\mathbf{K} - \mathbf{A}$ is one dimensional.
- \Re In fact, $\mathcal{N}(\mathbf{K} \mathbf{A}) = \{c\vec{1}, c \in R\}$ since $(\mathbf{K} \mathbf{A})\vec{1} = \vec{0}$.

Alternate betweenness measures:

Random walk betweenness:

- Asking too much: Need full knowledge of network to travel along shortest paths.
- One of many alternatives: consider all random walks between pairs of nodes i and j.
- Malks starts at node *i*, traverses the network randomly, ending as soon as it reaches *j*.
- Record the number of times an edge is followed by a walk.
- Consider all pairs of nodes.

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- Random walk betweenness of an edge = absolute difference in probability a random walk travels one way versus the other along the edge.
- Equivalent to electronic betweenness (see also diffusion).

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Factions in Zachary's karate club network. [19]



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Reason: Possible to have a low betweenness in

Modularity measure: difference in fraction of

$$Q = \sum_i [e_{i\,i} - a_i^2]$$

travelling between identified communities i and j,

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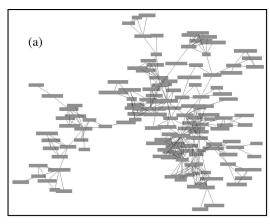
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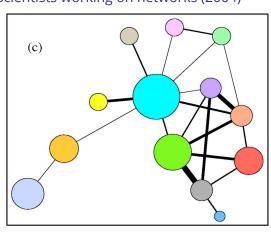
Hierarchy by division

Third column shows what happens if we don't recompute betweenness after each edge removal.

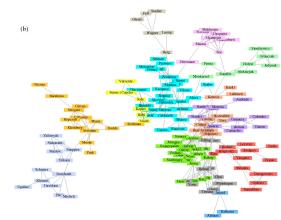
Scientists working on networks (2004)



Scientists working on networks (2004)



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Dolphins!

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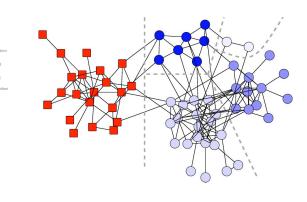
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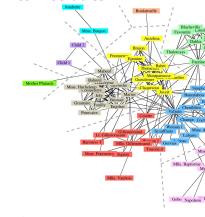
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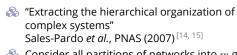
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PoCS @pocsvox Les Miserables Structure Hierarchy by divisio



More network analyses for Les Miserables here and here \square .

Shuffling for structure @pocsvox Structure detection



- & Consider all partitions of networks into m groups
- As for Newman and Girvan approach, aim is to find partitions with maximum modularity:

$$Q = \sum_i [e_{ii} - (\sum_j e_{ij})^2] = \mathrm{Tr} \mathbf{E} - ||\mathbf{E}^2||_1.$$



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Shuffling for structure

- & Consider partition network, i.e., the network of all possible partitions.
- Defn: Two partitions are connected if they differ only by the reassignment of a single node.
- & Look for local maxima in partition network.
- & Construct an affinity matrix with entries M_{ij}^{aff} .
- $\Re M_{ij}^{aff} = \mathbf{Pr}$ random walker on modularity network ends up at a partition with i and j in the same group.
- C.f. topological overlap between i and j =# matching neighbors for i and j divided by maximum of k_i and k_i .



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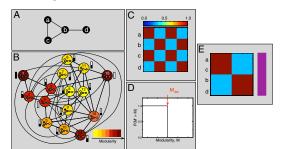
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A: Base network; B: Partition network; C: Coclassification matrix; **D:** Comparison to random networks (all the same!); E: Ordered

Shuffling for structure



coclassification matrix; Conclusion: no structure...

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- Method obtains a distribution of classification hierarchies.
- Note: the hierarchy with the highest modularity score isn't chosen.
- & Idea is to weight possible hierarchies according to their basin of attraction's size in the partition network.
- Next step: Given affinities, now need to sort nodes into modules, submodules, and so on.
- & Idea: permute nodes to minimize following cost

$$C = \frac{1}{N} \sum_{i=1}^N \sum_{j=1}^N M_{ij}^{\mathrm{aff}} |i-j|. \label{eq:constraint}$$

- Use simulated annealing (slow).
- where f is a strictly monotonically increasing function of 0, 1, 2, ...

 \clubsuit Define cost matrix as **T** with entries $T_{ij} = f(|i-j|)$.

 $\lambda_1 = -\frac{1}{6}n(n^2 - 1),$

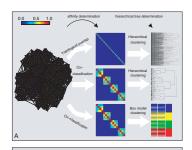
 $\lambda_2 = + \sqrt{nS_{n,4}} + S_{n,2}, \text{ and }$

 $\lambda_3 = -\sqrt{nS_{n,4}} + S_{n,2}.$

 $S_{n,2} = \frac{1}{12}n(n^2 - 1)$, and

 $S_{n,4} = \frac{1}{240}n(n^2 - 1)(3n^2 - 7).$

Shuffling for structure



Shuffling for structure

The eigenvalues are

where

rank 3, independent of N.

Discovered by numerical inspection ...

- N = 640,
- $\langle k \rangle = 16$,
- 🔏 3 tiered hierarchy.

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Eigenvectors

Shuffling for structure

$$\begin{split} \left(\vec{v}_1\right)_i &= \left(i - \frac{n+1}{2}\right), \\ \left(\vec{v}_2\right)_i &= \left(i - \frac{n+1}{2}\right)^2 + \sqrt{S_{n,4}/n}, \text{ and } \\ \left(\vec{v}_3\right)_i &= \left(i - \frac{n+1}{2}\right)^2 - \sqrt{S_{n,4}/n}. \end{split}$$

Remarkably,

$$T = \lambda_1 \hat{v}_1 \hat{v}_1^\mathsf{T} + \lambda_2 \hat{v}_2 \hat{v}_2^\mathsf{T} + \lambda_3 \hat{v}_3 \hat{v}_3^\mathsf{T}.$$

The next step: figure out how to capitalize on this...

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Table 1. Top-level structure of real-world networks

| Network | Nodes | Edges | Modules | Main module |
|-----------------------|-------|--------|---------|-------------|
| Air transportation | 3,618 | 28,284 | 57 | 8 |
| E-mail | 1,133 | 10,902 | 41 | 8 |
| Electronic circuit | 516 | 686 | 18 | 11 |
| Escherichia coli KEGG | 739 | 1,369 | 39 | 13 |
| E. coli UCSD | 507 | 947 | 28 | 17 |

Shuffling for structure

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|-----------------------|-------|--------|---------|-------------|--|
| Network | Nodes | Edges | Modules | Main module | |
| Air transportation | 3,618 | 28,284 | 57 | 8 | |
| E-mail | 1,133 | 10,902 | 41 | 8 | |
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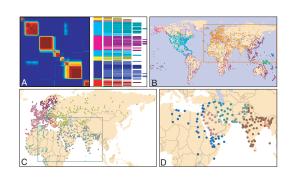
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Modules found match up with geopolitical units.

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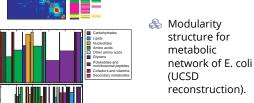
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Builds on Kleinberg's HITS algorithm.

"Detecting communities in large networks"

& Consider normal matrix $\mathbf{K}^{-1}A$, random walk

matrix $A^{\mathsf{T}}\mathbf{K}^{-1}$, Laplacian $\mathbf{K} - \mathbf{A}$, and AA^{T} .

Basic observation is that eigenvectors associated

with secondary eigenvalues reveal evidence of

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Example network:

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Capocci *et al.* (2005) [4]

structure.

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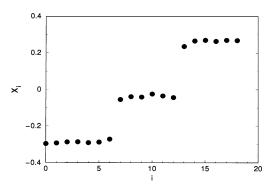
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General structure detection

Second eigenvector's components:



General structure detection

- Network of word associations for 10616 words.
- Average in-degree of 7.
- Using 2nd to 11th evectors of a modified version of AA^T :

Table 1 Words most correlated to science, literature and piano in the eigenvectors of $Q^{-1}WW^{T}$

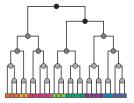
| Science | 1 | Literature | 1 | Piano | 1 | |
|-------------|-------|------------|-------|-----------|-------|--|
| Scientific | 0.994 | Dictionary | 0.994 | Cello | 0.993 | |
| Chemistry | 0.990 | Editorial | 0.990 | Fiddle | 0.992 | |
| Physics | 0.988 | Synopsis | 0.988 | Viola | 0.990 | |
| Concentrate | 0.973 | Words | 0.987 | Banjo | 0.988 | |
| Thinking | 0.973 | Grammar | 0.986 | Saxophone | 0.985 | |
| Test | 0.973 | Adjective | 0.983 | Director | 0.984 | |
| Lab | 0.969 | Chapter | 0.982 | Violin | 0.983 | |
| Brain | 0.965 | Prose | 0.979 | Clarinet | 0.983 | |
| Equation | 0.963 | Topic | 0.976 | Oboe | 0.983 | |
| Examine | 0.962 | English | 0.975 | Theater | 0.982 | |

Values indicate the correlation

Hierarchies and missing links

Clauset et al., Nature (2008) [5]





- & Idea: Shades indicate probability that nodes in left and right subtrees of dendogram are connected.
- & Handle: Hierarchical random graph models.
- Plan: Infer consensus dendogram for a given real
- Obtain probability that links are missing (big problem...).

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Model also predicts reasonably well

- - 1. average degree,
 - 2. clustering,
 - 3. and average shortest path length.

Table 1 | Comparison of original and resampled networks

| Network | $\langle k \rangle_{\rm real}$ | $\langle k \rangle_{\text{samp}}$ | C_{real} | C_{samp} | d_{real} | d_{samp} | |
|-------------|--------------------------------|-----------------------------------|-------------------|-------------------|-------------------|------------|--|
| T. pallidum | 4.8 | 3.7(1) | 0.0625 | 0.0444(2) | 3.690 | 3.940(6) | |
| Terrorists | 4.9 | 5.1(2) | 0.361 | 0.352(1) | 2.575 | 2.794(7) | |
| Grassland | 3.0 | 2.9(1) | 0.174 | 0.168(1) | 3.29 | 3.69(2) | |
| | | | | | | | |

Statistics are shown for the three example networks studied and for new networks generated by resampling from our hierarchical model. The generated networks closely match the average degree $\langle k \rangle$, clustering coefficient C and average vertex-vertex distance d in each case, suggesting that they capture much of the structure of the real networks. Parenthetical values indicate standard errors on the final digits.

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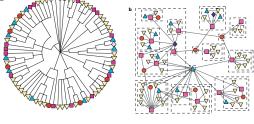
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- Consensus dendogram for grassland species.
- Copes with disassortative and assortative communities.



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From PoCS: Small-worldness and social searchability

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Social networks and identity:

Identity is formed from attributes such as:

- Geographic location
- Type of employment
- Religious beliefs
- Recreational activities.

Groups are formed by people with at least one similar attribute.

Attributes ⇔ Contexts ⇔ Interactions ⇔ Networks.

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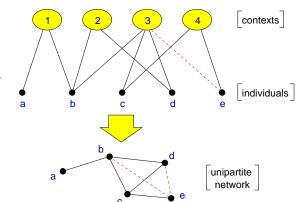
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Hierarchies & Missing Links

Social distance—Bipartite affiliation networks



occupation

Social distance—Context distance

kindergarter

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education

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Overlapping communities

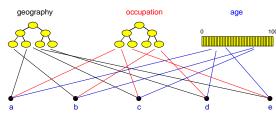
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Models

high school

teacher

Generalized affiliation networks



Blau & Schwartz [2], Simmel [16], Breiger [3], Watts et al. [18]; see also Google+ Circles.

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Dealing with community overlap:

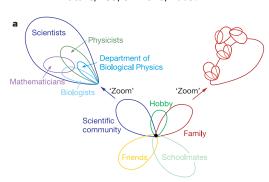
- & Earlier structure detection algorithms, agglomerative or divisive, force communities to be purely distinct.
- & Overlap: Acknowledge nodes can belong to multiple communities.
- Palla et al. [13] detect communities as sets of adjacent k-cliques (must share k-1 nodes).
- \triangle One of several issues: how to choose k?
- Four new quantities:
 - m, number of a communities a node belongs to.
 - $s_{\alpha,\beta}^{ov}$ number of nodes shared between two given communities, α and β .

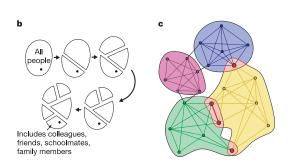
 - s_{α}^{com} , community α 's size.
- Associated distributions: $P_{>}(m)$, $P_{>}(s_{\alpha,\beta}^{ov})$, $P_{>}(d_{\alpha}^{com})$, and $P_{>}(s_{\alpha}^{com})$.



"Uncovering the overlapping community structure of complex networks in nature and society"

Palla et al.. Nature, **435**, 814–818, 2005. [13]





apping regions are emphasized in red. Notice that any k-clique ubgraph of size k) can be reached only from the k-cliques of the unity through a series of adjacent k-cliques. Two k-cliques are hey share k-1 nodes.

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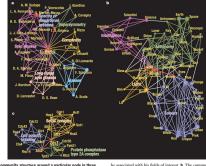
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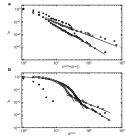
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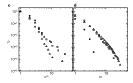
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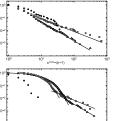


be associated with his fields of interest. **b**, The communities of the word 'bright' in the South Florida Free Association norms list (for $w^* = 0.025$ prepresent the different meanings of this word, c. The communities of the protein Zds1 in the DIP core list of the protein–protein interactions of S. corresions on the associated with either protein complexes or certain

& Two tunable parameters: w^* , the link weight threshold, and k, the clique size.







A link-based approach:

- What we know now: Many network analyses profit from focusing on links.
- & Idea: form communities of links rather than communities of nodes.
- & Observation: Links typically of one flavor, while nodes may have many flavors.
- Link communities induce overlapping and still hierarchically structured communities of nodes.
- (Applause.)

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"Link communities complexity in netw Ahn, Bagrow, and L Nature, 466, 761-7

Smart, intellect, scientists

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Note: See details of paper on how to choose link communities well based on partition density D.



networks were chosen for their varied sizes and topolog the different domains where network analysis is used. Sh number of nodes, N, and the average number of neighb Link clustering finds the most relevant community stru networks. APMS. affinity-unification/mass socretome

- & Comparison of structure detection algorithms using four measures over many networks.
- Revealed communities are matched against 'known' communities recorded in network metadata.
- Link approach particularly good for dense,

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overlapful networks.



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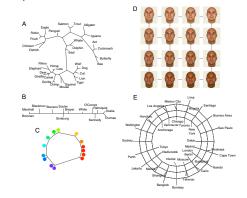
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ocial network within the largest community in c, with its largest ubcommunity highlighted. The highlighted subcommunity is she with its link dendrogram and partition density, D, as a function of t

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Example learned structures:



Biological features; Supreme Court votes; perceived color differences; face differences; & distances

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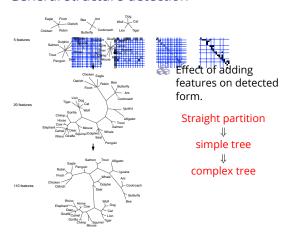
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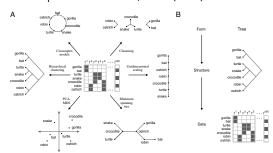
between cities.

General structure detection

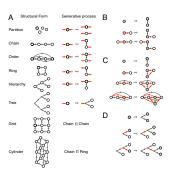


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"The discovery of structural form" Kemp and Tenenbaum, PNAS (2008)[8]



General structure detection

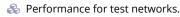


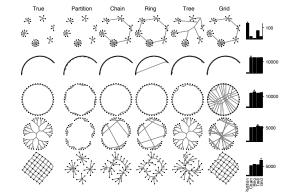
Top down description of form.

Node replacement graph grammar: parent node becomes two child nodes.

B-D: Growing chains, orders, and trees.

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