## Mechanisms for Generating Power-Law Size Distributions, Part 2

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Principles of Complex Systems, Vols. 1, 2, & 3D CSYS/MATH 6701, 6713, & a pretend number, 2023–2024| @pocsvox

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Variable transformation Basics Holtsmark's Distribution PLIPLO

References





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## Outline

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References

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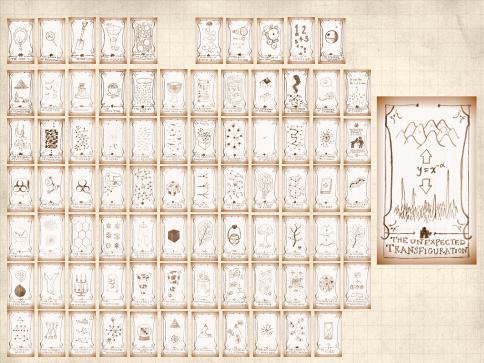
# The Boggoracle Speaks: 🖽 🖸



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## Outline

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References

### Variable transformation Basics

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Understand power laws as arising from

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### Understand power laws as arising from

1. Elementary distributions (e.g., exponentials).

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### Understand power laws as arising from

- 1. Elementary distributions (e.g., exponentials).
- 2. Variables connected by power relationships.

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### Understand power laws as arising from

- 1. Elementary distributions (e.g., exponentials).
- 2. Variables connected by power relationships.

 $\clubsuit$  Random variable X with known distribution  $P_x$ 

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### Understand power laws as arising from

- 1. Elementary distributions (e.g., exponentials).
- 2. Variables connected by power relationships.

Random variable *X* with known distribution  $P_x$ Second random variable *Y* with y = f(x). The PoCSverse Power-Law Mechanisms, Pt. 2 8 of 20

Variable transformation Basics

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### Understand power laws as arising from

- 1. Elementary distributions (e.g., exponentials).
- 2. Variables connected by power relationships.

Random variable X with known distribution  $P_x$ Second random variable Y with y = f(x).

$$\begin{array}{ll} & P_{Y}(y) \mathrm{d} y = \\ & \sum_{x \mid f(x) = y} P_{X}(x) \mathrm{d} x \\ = \\ & \sum_{y \mid f(x) = y} P_{X}(f^{-1}(y)) \frac{\mathrm{d} y}{|f'(f^{-1}(y))|} \end{array}$$

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### Understand power laws as arising from

- 1. Elementary distributions (e.g., exponentials).
- 2. Variables connected by power relationships.

Random variable *X* with known distribution  $P_x$ Second random variable *Y* with y = f(x).

$$P_{Y}(y)dy = \sum_{x|f(x)=y} P_{X}(x)dx = \sum_{y|f(x)=y} P_{X}(f^{-1}(y)) \frac{dy}{|f'(f^{-1}(y))|}$$
  
Often easier to do by hand...

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The PoCSverse Power-Law Mechanisms, Pt. 2 9 of 20

Variable transformation

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3 Assume relationship between *x* and *y* is 1-1.

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Variable transformation

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 $\bigotimes$  Assume relationship between x and y is 1-1.

Power-law relationship between variables:  $y = cx^{-\alpha}, \alpha > 0$  The PoCSverse Power-Law Mechanisms, Pt. 2 9 of 20

Variable transformation

Basics Holtsmark's Distribution PLIPLO



- & Assume relationship between x and y is 1-1.
- Power-law relationship between variables:  $y = cx^{-\alpha}, \alpha > 0$
- $\overset{\circ}{\underset{}_{\overset{\circ}{\overset{}}}}$  Look at y large and x small

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Variable transformation

Basics Holtsmark's Distribution PLIPLO



2

- & Assume relationship between x and y is 1-1.
- Power-law relationship between variables:  $y = cx^{-\alpha}, \alpha > 0$
- $\bigotimes$  Look at y large and x small

$$\mathsf{d}y = \mathsf{d}\left(cx^{-\alpha}\right)$$

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Variable transformation

Basics Holtsmark's Distribution PLIPLO



2

- & Assume relationship between x and y is 1-1.
- Power-law relationship between variables:  $y = cx^{-\alpha}, \alpha > 0$
- $\bigotimes$  Look at y large and x small

$$\mathsf{d}y = \mathsf{d}\left(cx^{-\alpha}\right)$$

$$= c(-\alpha)x^{-\alpha-1}\mathsf{d}x$$

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Variable transformation

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2

- $\bigotimes$  Assume relationship between x and y is 1-1.
- Power-law relationship between variables:  $y = cx^{-\alpha}, \alpha > 0$
- $\bigotimes$  Look at y large and x small

$$\mathrm{d} y = \mathrm{d} \left( c x^{-\alpha} \right)$$

$$= c(-\alpha)x^{-\alpha-1}\mathsf{d}x$$

invert: 
$$dx = \frac{-1}{c\alpha}x^{\alpha+1}dy$$

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Variable transformation

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2

- $\bigotimes$  Assume relationship between x and y is 1-1.
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$$\mathrm{d}x \,= \frac{-1}{c\alpha} \left(\frac{y}{c}\right)^{-(\alpha+1)/\alpha} \mathrm{d}y$$

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Variable transformation

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- $\bigotimes$  Assume relationship between x and y is 1-1.
- Power-law relationship between variables:  $y = cx^{-\alpha}, \alpha > 0$
- $\bigotimes$  Look at y large and x small

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$$\mathrm{d}x \,= \frac{-1}{c\alpha} \left(\frac{y}{c}\right)^{-(\alpha+1)/\alpha} \mathrm{d}y$$

$$\mathsf{d}x = \frac{-c^{1/\alpha}}{\alpha}y^{-1-1/\alpha}\mathsf{d}y$$

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Variable transformation

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$$P_y(y)\mathsf{d} y = P_x(x)\mathsf{d} x$$

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Variable transformation

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$$P_y(y)\mathsf{d} y = P_x(x)\mathsf{d} x$$

$$P_{y}(y)\mathsf{d}y = P_{x} \underbrace{\overline{\left(\left(\frac{y}{c}\right)^{-1/\alpha}\right)}}_{(\alpha)} \underbrace{\frac{\mathsf{d}x}{\alpha}}_{\alpha} \frac{\mathsf{d}x}{y^{-1-1/\alpha}\mathsf{d}y}$$

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Variable transformation

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$$P_y(y)\mathsf{d} y = P_x(x)\mathsf{d} x$$

$$P_y(y)\mathsf{d} y = P_x \overbrace{\left(\left(\frac{y}{c}\right)^{-1/\alpha}\right)}^{(x)} \overbrace{\frac{dx}{\alpha} y^{-1-1/\alpha} \mathsf{d} y}^{(x)}$$

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References

rightarrow If  $P_x(x) \rightarrow$  non-zero constant as  $x \rightarrow 0$  then

$$P_y(y) \propto y^{-1-1/lpha}$$
 as  $y o \infty$ .



$$P_y(y)\mathsf{d} y\,=P_x(x)\mathsf{d} x$$

$$P_y(y)\mathsf{d} y = P_x \underbrace{\left(\left(\frac{y}{c}\right)^{-1/\alpha}\right)}^{(x)} \underbrace{\frac{\mathsf{d} x}{c^{1/\alpha}}}_{\alpha} y^{-1-1/\alpha} \mathsf{d} y}$$

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References

$$\begin{split} & \& \quad \text{If } P_x(x) \to \text{non-zero constant as } x \to 0 \text{ then} \\ & \qquad P_y(y) \propto y^{-1-1/\alpha} \text{ as } y \to \infty. \\ & \& \quad \text{If } P_x(x) \to x^\beta \text{ as } x \to 0 \text{ then} \\ & \qquad P_y(y) \propto y^{-1-1/\alpha-\beta/\alpha} \text{ as } y \to \infty. \end{split}$$



### Example

Exponential distribution Given  $P_x(x) = \frac{1}{\lambda}e^{-x/\lambda}$  and  $y = cx^{-\alpha}$ , then

 $P(y) \propto y^{-1 - 1/\alpha} + O\left(y^{-1 - 2/\alpha}\right)$ 

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## Example

Exponential distribution Given  $P_x(x) = \frac{1}{\lambda}e^{-x/\lambda}$  and  $y = cx^{-\alpha}$ , then  $P(y) \propto y^{-1-1/\alpha} + O(y^{-1-2/\alpha})$ 

🙈 Exponentials arise from randomness (easy) ...

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Variable transformation Basics

Holtsmark's Distribution



## Example

Exponential distribution Given  $P_x(x) = \frac{1}{\lambda}e^{-x/\lambda}$  and  $y = cx^{-\alpha}$ , then  $P(y) \propto y^{-1-1/\alpha} + O(y^{-1-2/\alpha})$ 

Exponentials arise from randomness (easy) ...
 More later when we cover robustness.

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## Outline

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References

#### Variable transformation Basics Holtsmark's Distribution





🚳 Select a random point in the universe  $\vec{x}$ .

POLICE BOY

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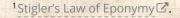
Basics

POLICE BOX

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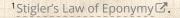
🚳 Select a random point in the universe  $\vec{x}$ .

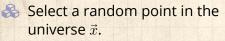
Measure the force of gravity  $F(\vec{x}).$ 



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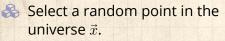
Variable transformation Basics Holtsmark's Distribution





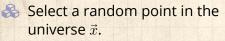
- Solution Measure the force of gravity  $F(\vec{x})$ .
- Observe that  $P_F(F) \sim F^{-5/2}.$



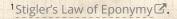


- Solution Measure the force of gravity  $F(\vec{x})$ .
  - Observe that  $P_F(F) \sim F^{-5/2}$ .
- Distribution named after Holtsmark who was thinking about electrostatics and plasma<sup>[1]</sup>.





- Solution Measure the force of gravity  $F(\vec{x})$ .
  - Observe that  $P_F(F) \sim F^{-5/2}$ .
- Distribution named after Holtsmark who was thinking about electrostatics and plasma<sup>[1]</sup>.
- Again, the humans naming things after humans, poorly.<sup>1</sup>





## Matter is concentrated in stars: <sup>[2]</sup> *F* is distributed unevenly

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Variable transformation Basics Holtsmark's Distribution

References

PLIPLO



🚓 F is distributed unevenly

Solution Probability of being a distance r from a single star at  $\vec{x} = \vec{0}$ :

 $P_r(r) {\rm d} r \propto r^2 {\rm d} r$ 

The PoCSverse Power-Law Mechanisms, Pt. 2 14 of 20

Variable transformation Basics Holtsmark's Distribution



 $rac{1}{8}$  F is distributed unevenly

Solution Probability of being a distance r from a single star at  $\vec{x} = \vec{0}$ :

 $P_r(r) {\rm d} r \propto r^2 {\rm d} r$ 

Assume stars are distributed randomly in space (oops?) The PoCSverse Power-Law Mechanisms, Pt. 2 14 of 20

Variable transformation Basics Holtsmark's Distribution PLIPLO

 $rac{1}{8}$  F is distributed unevenly

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 $P_r(r) \mathrm{d}r \propto r^2 \mathrm{d}r$ 

Assume stars are distributed randomly in space (oops?)

 $\mathfrak{B}$  Assume only one star has significant effect at  $\vec{x}$ .

The PoCSverse Power-Law Mechanisms, Pt. 2 14 of 20

Variable transformation Basics Holtsmark's Distribution PLIPLO

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Solution Probability of being a distance r from a single star at  $\vec{x} = \vec{0}$ :

 $P_r(r) \mathrm{d}r \propto r^2 \mathrm{d}r$ 

Assume stars are distributed randomly in space (oops?)

Solution Assume only one star has significant effect at  $\vec{x}$ . Assume only one star has significant effect at  $\vec{x}$ .

$$F \propto r^{-2}$$

The PoCSverse Power-Law Mechanisms, Pt. 2 14 of 20

Variable transformation Basics Holtsmark's Distribution PLIPLO

🗞 F is distributed unevenly

Probability of being a distance r from a single star at  $\vec{x} = \vec{0}$ :

 $P_r(r) \mathrm{d}r \propto r^2 \mathrm{d}r$ 

Assume stars are distributed randomly in space (oops?)

Assume only one star has significant effect at  $\vec{x}$ .

law of gravity:

$$F \propto r^{-2}$$

🚳 invert:

$$r \propto F^{-\frac{1}{2}}$$

The PoCSverse Power-Law Mechanisms, Pt. 2 14 of 20

Variable transformation Basics Holtsmark's Distribution PLIPLO

🗞 F is distributed unevenly

Probability of being a distance r from a single star at  $\vec{x} = \vec{0}$ :

 $P_r(r) {\rm d} r \propto r^2 {\rm d} r$ 

Assume stars are distributed randomly in space (oops?)

Solution Assume only one star has significant effect at  $\vec{x}$ . As Law of gravity:

$$F \propto r^{-2}$$

🚳 invert:

$$r \propto F^{-\frac{1}{2}}$$

 $\clubsuit$  Connect differentials: d $r \propto {\sf d} F^{-rac{1}{2}} \propto F^{-rac{3}{2}} {\sf d} F$ 

The PoCSverse Power-Law Mechanisms, Pt. 2 14 of 20

Variable transformation Basics Holtsmark's Distribution PLIPLO

Using 
$$\boxed{r\propto F^{-1/2}}$$
 ,  $\boxed{{\rm d}r\,\propto F^{-3/2}{\rm d}F}$  , and  $\boxed{P_r(r)\propto r^2}$ 

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Variable transformation Basics Holtsmark's Distribution



3

Using 
$$\boxed{r\propto F^{-1/2}}$$
 ,  $\boxed{{\rm d}r\,\propto F^{-3/2}{\rm d}F}$  , and  $\boxed{P_r(r)\propto r^2}$ 

 $P_F(F)\mathsf{d} F\,=P_r(r)\mathsf{d} r$ 

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Variable transformation Basics Holtsmark's Distribution



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Using 
$$\boxed{r\propto F^{-1/2}}$$
 ,  $\boxed{{\rm d}r\,\propto F^{-3/2}{\rm d}F}$  , and  $\boxed{P_r(r)\propto r^2}$ 

 $P_F(F)\mathsf{d} F = P_r(r)\mathsf{d} r$ 

 $\propto P_r({\rm const} imes F^{-1/2})F^{-3/2}{\rm d}F$ 

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Variable transformation Basics Holtsmark's Distribution



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Using 
$$\boxed{r\propto F^{-1/2}}$$
 ,  $\boxed{{\rm d}r\,\propto F^{-3/2}{\rm d}F}$  , and  $\boxed{P_r(r)\propto r^2}$ 

 $P_F(F)\mathsf{d} F = P_r(r)\mathsf{d} r$ 

 $\propto P_r({\rm const}\times F^{-1/2})F^{-3/2}{\rm d}F$ 

$$\propto \left(F^{-1/2}\right)^2 F^{-3/2} \mathsf{d} F$$

The PoCSverse Power-Law Mechanisms, Pt. 2 15 of 20

Variable transformation Basics Holtsmark's Distribution

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Using 
$$\boxed{r\propto F^{-1/2}}$$
 ,  $\boxed{{\rm d}r\,\propto F^{-3/2}{\rm d}F}$  , and  $\boxed{P_r(r)\propto r^2}$ 

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$$\propto \left(F^{-1/2}
ight)^2 F^{-3/2} \mathsf{d} F$$

 $= F^{-1-3/2} \mathsf{d} F$ 

The PoCSverse Power-Law Mechanisms, Pt. 2 15 of 20

Variable transformation Basics Holtsmark's Distribution

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2

Using 
$$\boxed{r\propto F^{-1/2}}$$
 ,  $\boxed{{\rm d}r\,\propto F^{-3/2}{\rm d}F}$  , and  $\boxed{P_r(r)\propto r^2}$ 

 $P_F(F)\mathsf{d} F = P_r(r)\mathsf{d} r$ 

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$$\propto \left(F^{-1/2}
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$$= F^{-1-3/2} \mathsf{d} F$$

 $= F^{-5/2} \mathrm{d}F$ .

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Variable transformation Basics Holtsmark's Distribution

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 $P_F(F) = F^{-5/2} \mathsf{d} F$ 

The PoCSverse Power-Law Mechanisms, Pt. 2 16 of 20

Variable transformation Basics Holtsmark's Distribution



-

 $P_F(F) = F^{-5/2} \mathsf{d} F$ 

 $\gamma = 5/2$ 

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Variable transformation Basics Holtsmark's Distribution



3

 $P_F(F)=F^{-5/2}\mathrm{d} F$ 

$$\gamma = 5/2$$

🚳 Mean is finite.

The PoCSverse Power-Law Mechanisms, Pt. 2 16 of 20

Variable transformation Basics Holtsmark's Distribution

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 $P_F(F)=F^{-5/2}\mathrm{d} F$ 

$$\gamma = 5/2$$

Solution  $\mathbf{k}$  Mean is finite. Solution  $\mathbf{k}$  Variance =  $\infty$ . The PoCSverse Power-Law Mechanisms, Pt. 2 16 of 20

Variable transformation Basics Holtsmark's Distribution

m

References

PLIPLO

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$$P_F(F)=F^{-5/2}\mathrm{d} F$$

$$\gamma = 5/2$$

lean is finite.

- $\clubsuit$  Variance =  $\infty$ .
- \lambda wild distribution.

The PoCSverse Power-Law Mechanisms, Pt. 2 16 of 20

Variable transformation Basics Holtsmark's Distribution PUPLO

III.

2

 $P_F(F) = F^{-5/2} \mathrm{d} F$ 

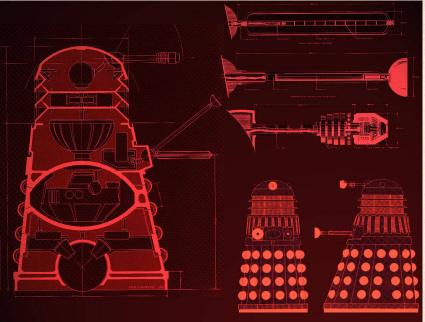
$$\gamma = 5/2$$

- 🚳 Mean is finite.
- $\clubsuit$  Variance =  $\infty$ .
- 🚳 A wild distribution.
- Upshot: Random sampling of space usually safe but can end badly...

The PoCSverse Power-Law Mechanisms, Pt. 2 16 of 20

Variable transformation Basics Holtsmark's Distribution

# □ Todo: Build Dalek army.



# Outline

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Variable transformation Basics Holtsmark's Distribution PLIPLO

References

### Variable transformation

Holtsmark's Distribution



#### PLIPLO = Power law in, power law out

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Variable transformation Basics Holtsmark's Distribution PLIPLO



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References

#### PLIPLO = Power law in, power law out

Explain a power law as resulting from another unexplained power law.



The PoCSverse Power-Law Mechanisms, Pt. 2 19 of 20

Variable transformation Basics Holtsmark's Distribution PLIPLO

References

- Explain a power law as resulting from another unexplained power law.
- Set another homunculus argument C...



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Variable transformation Basics Holtsmark's Distribution PLIPLO

References

- Explain a power law as resulting from another unexplained power law.
- 🗞 Yet another homunculus argument 🗹 ...
- \lambda Don't do this!!! (slap, slap)



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Variable transformation Basics Holtsmark's Distribution PLIPLO

References

- Explain a power law as resulting from another unexplained power law.
- 🚳 Yet another homunculus argument 🗹 ...
- \lambda Don't do this!!! (slap, slap)
- limits and a stuff. Mild out is the stuff.



#### The PoCSverse Power-Law Mechanisms, Pt. 2 19 of 20

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References

- Explain a power law as resulting from another unexplained power law.
- 🚳 Yet another homunculus argument 🗹 ...
- \lambda Don't do this!!! (slap, slap)
- MIWO = Mild in, Wild out is the stuff.
- 🚳 In general: We need mechanisms!



## **References** I

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References

[1] J. Holtsmark. Über die verbreiterung von spektrallinien. Ann. Phys., 58:577–630, 1919. pdf 🖸

[2] D. Sornette. <u>Critical Phenomena in Natural Sciences</u>. Springer-Verlag, Berlin, 1st edition, 2003.

