

# Social Contagion

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Principles of Complex Systems, Vols. 1, 2, & 3D  
CSYS/MATH 6701, 6713, & a pretend number,  
2023–2024 | @pocsvox

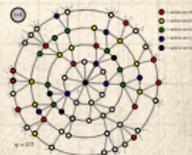
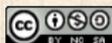
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- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center  
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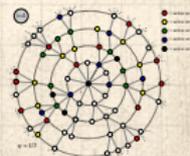
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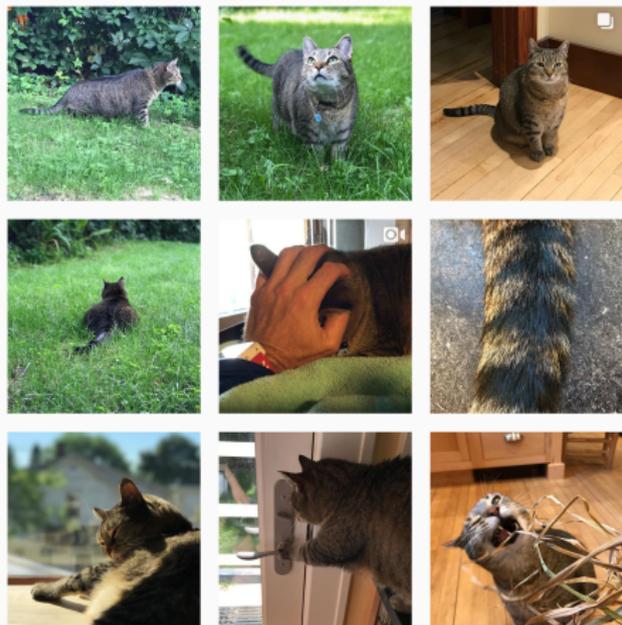
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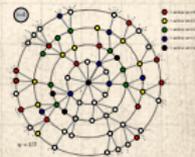
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# Outline

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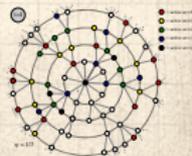
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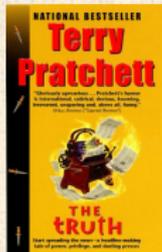
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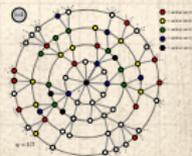




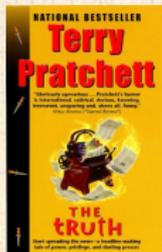
'The rumor spread through the city like wildfire



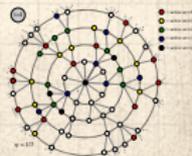
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by Terry Pratchett (2000). [22]



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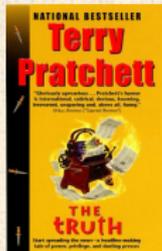


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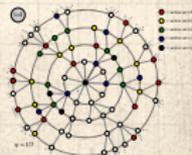
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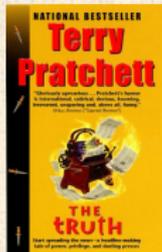


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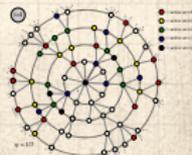
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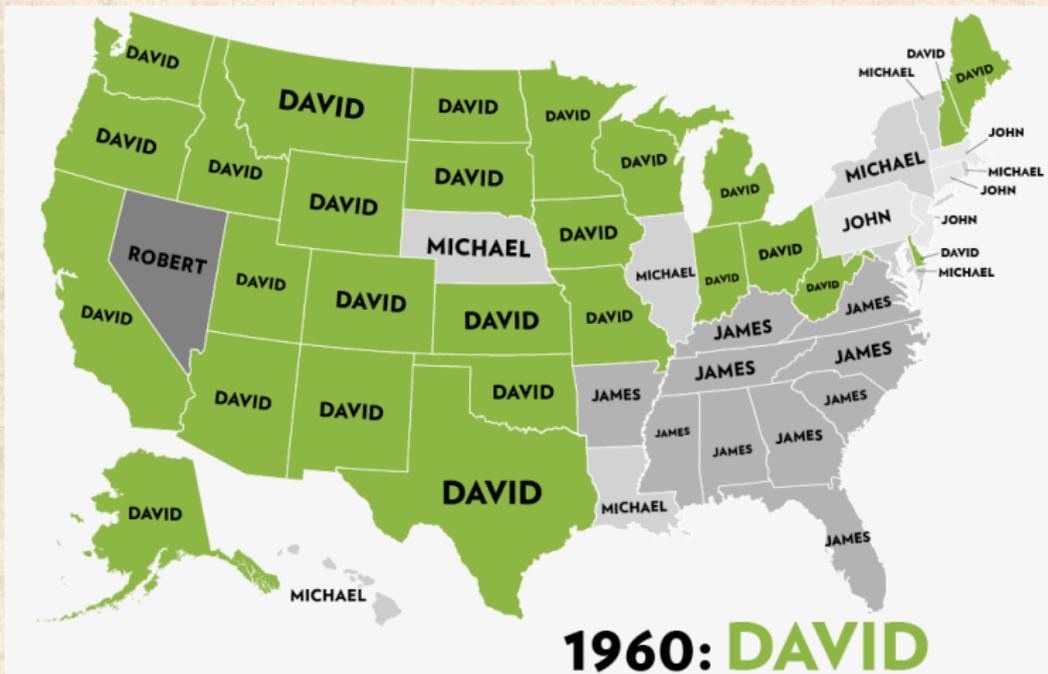
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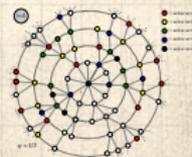
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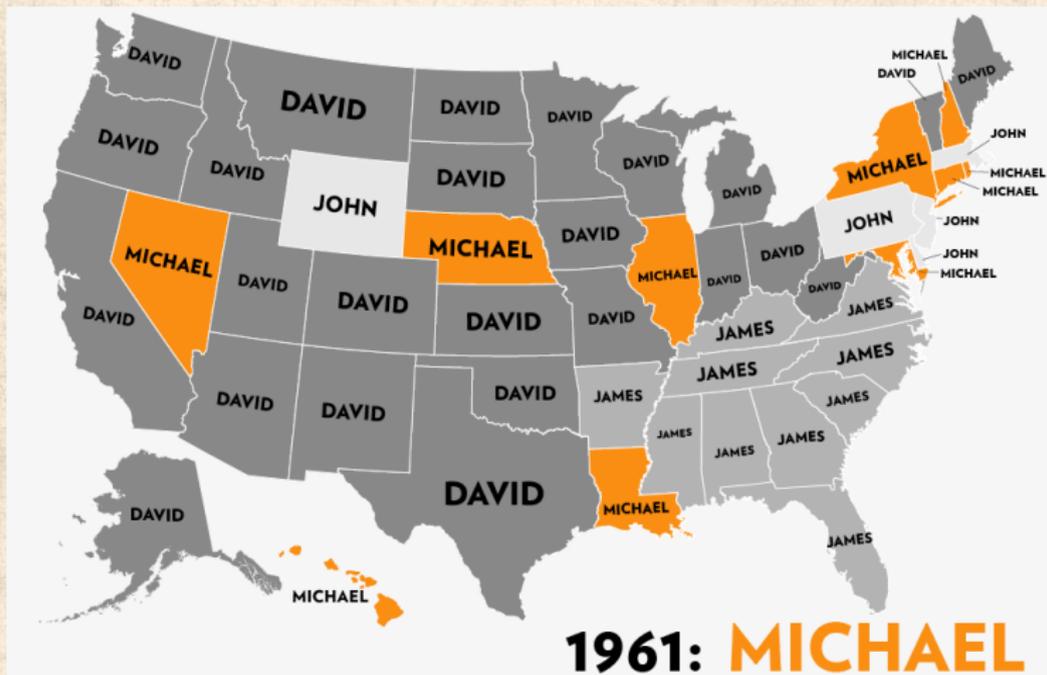
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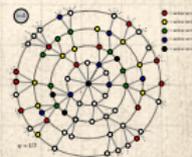
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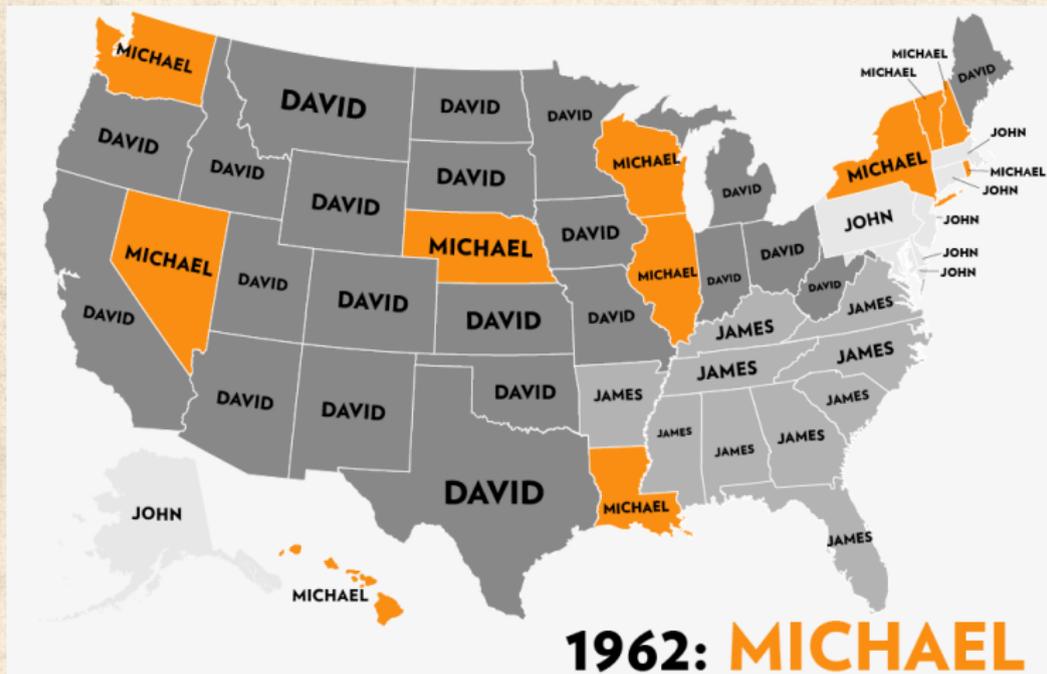
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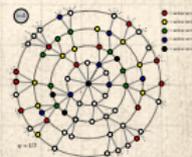
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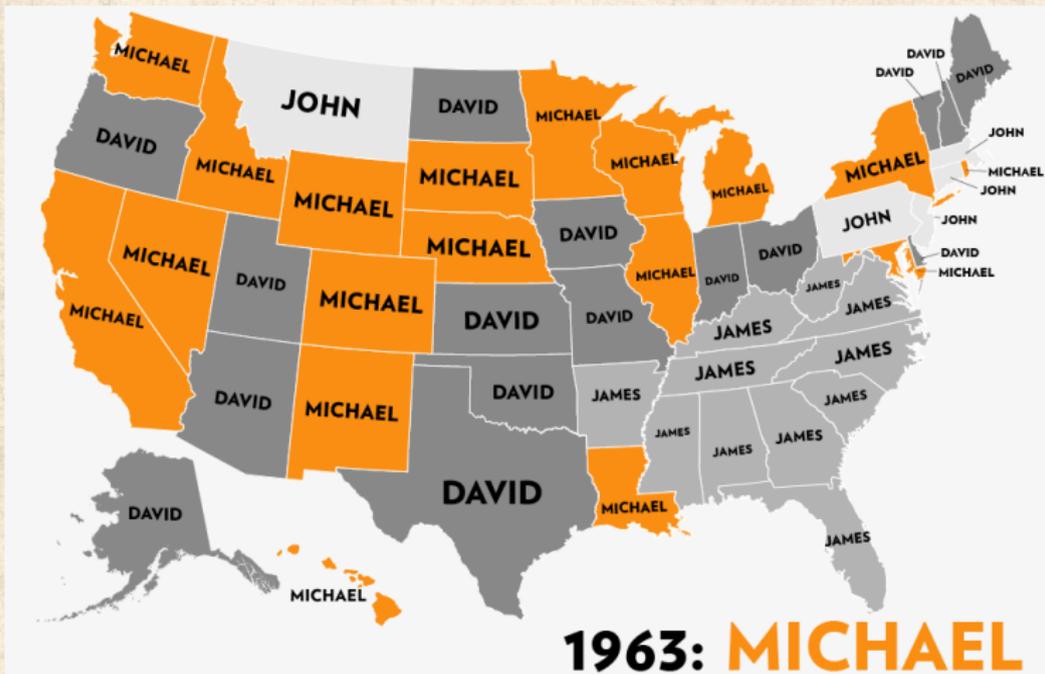
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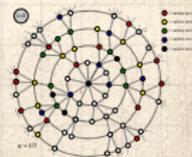
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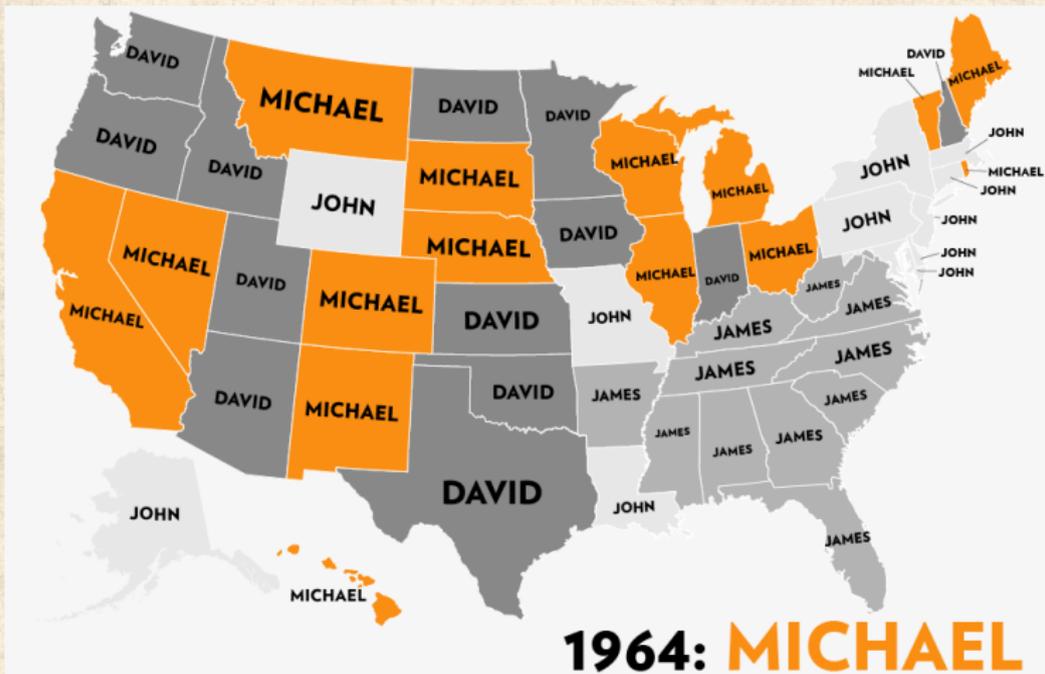
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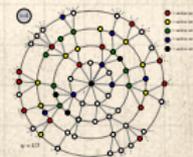
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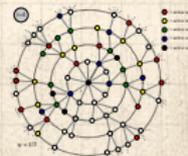
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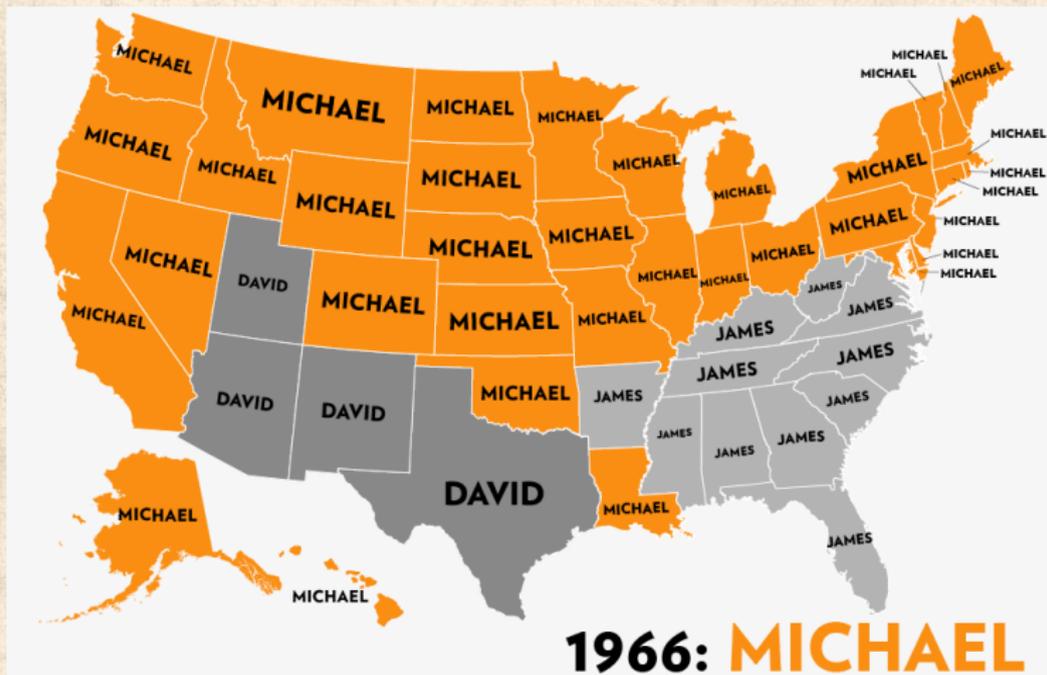
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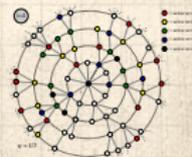
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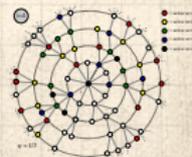
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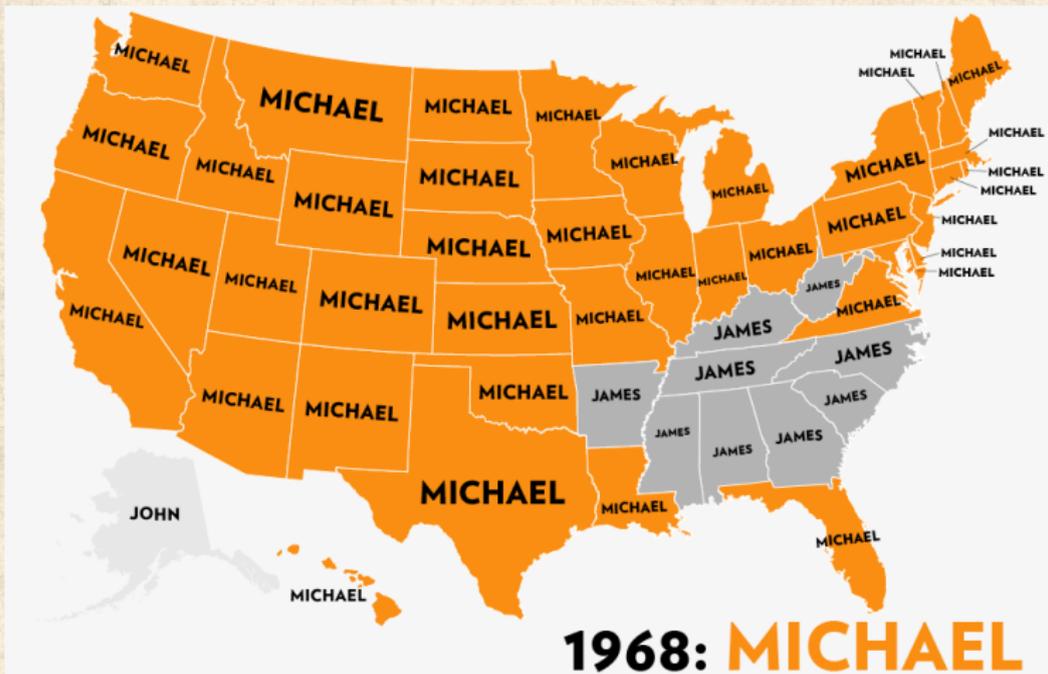
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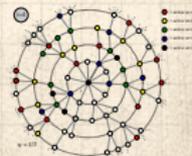
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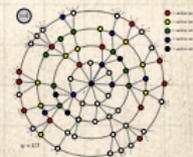
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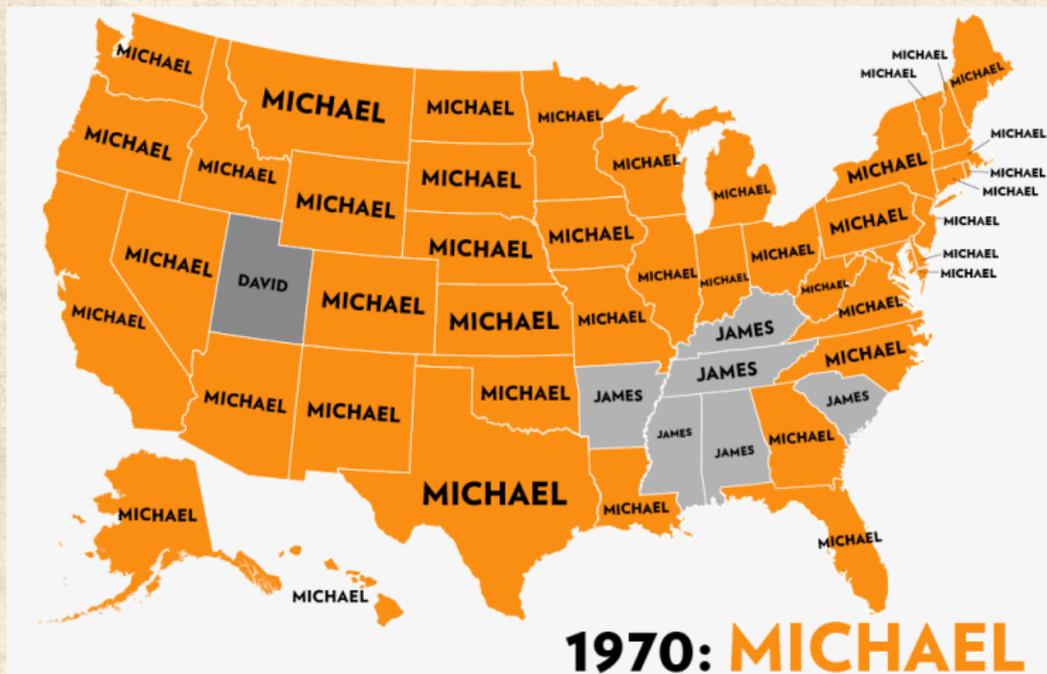
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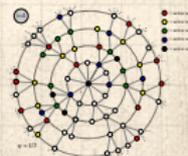
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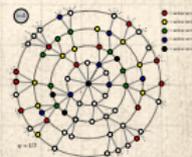
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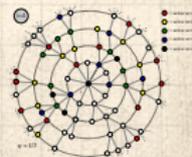
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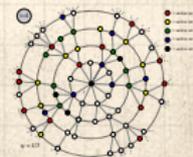
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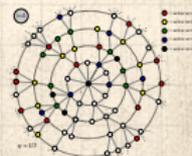
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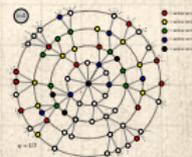
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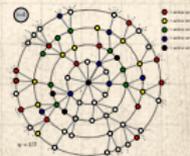
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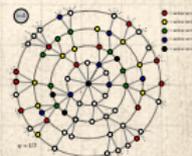
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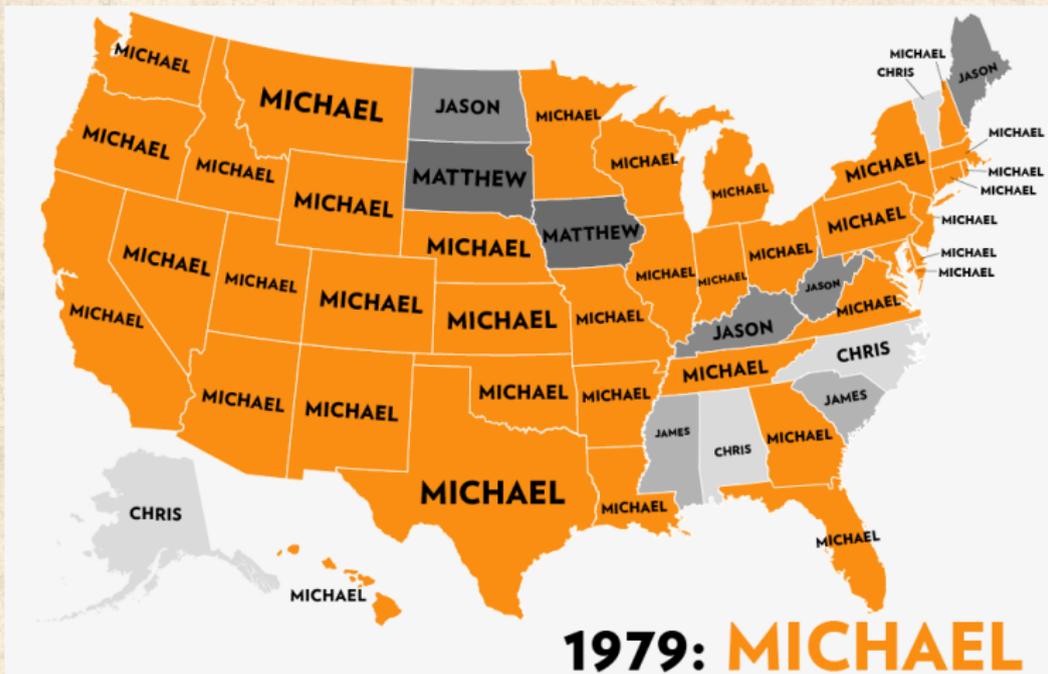
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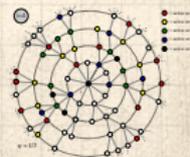
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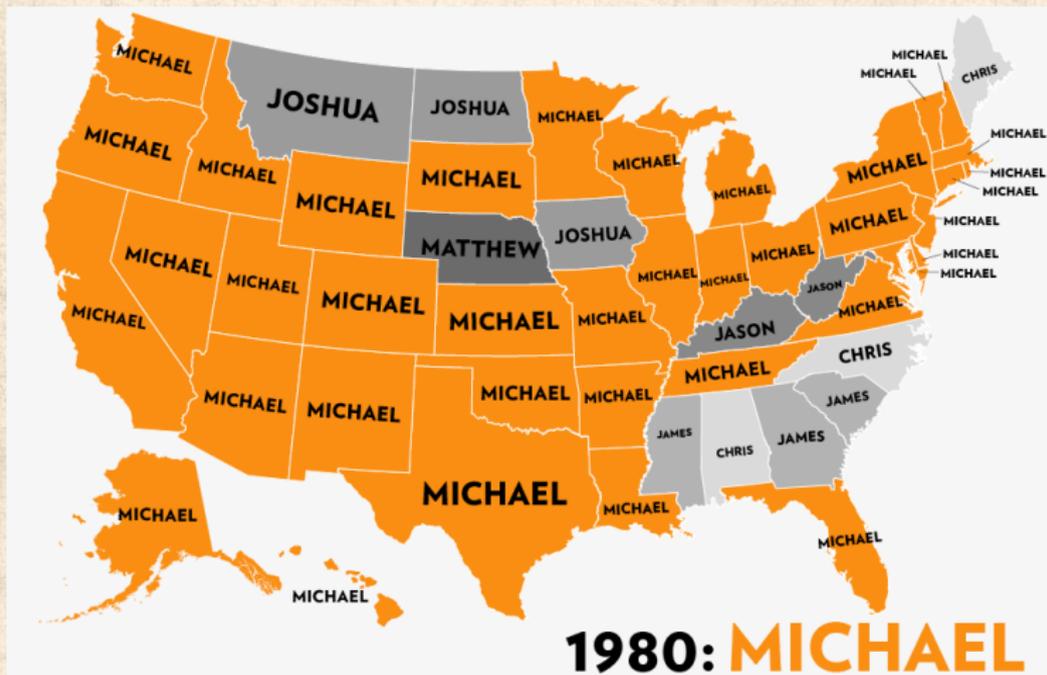
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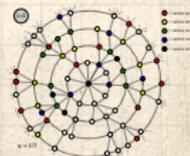
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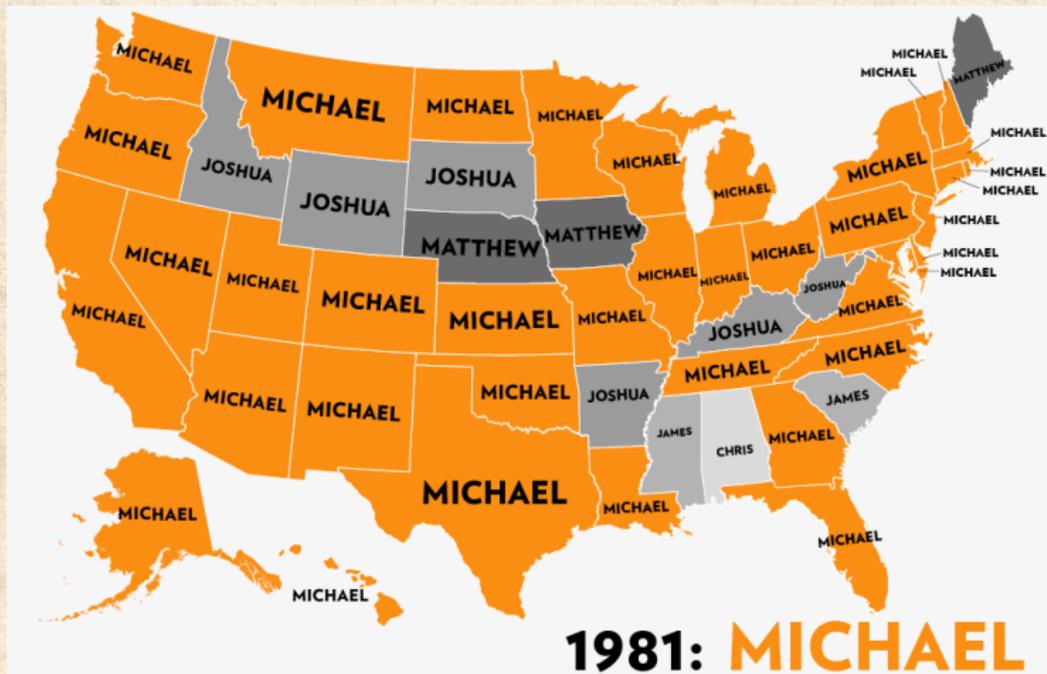
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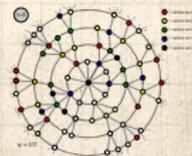
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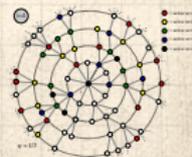
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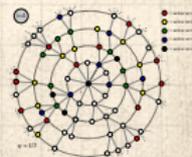
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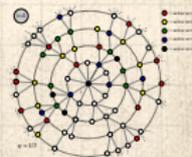
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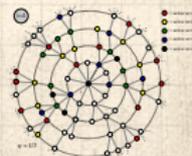
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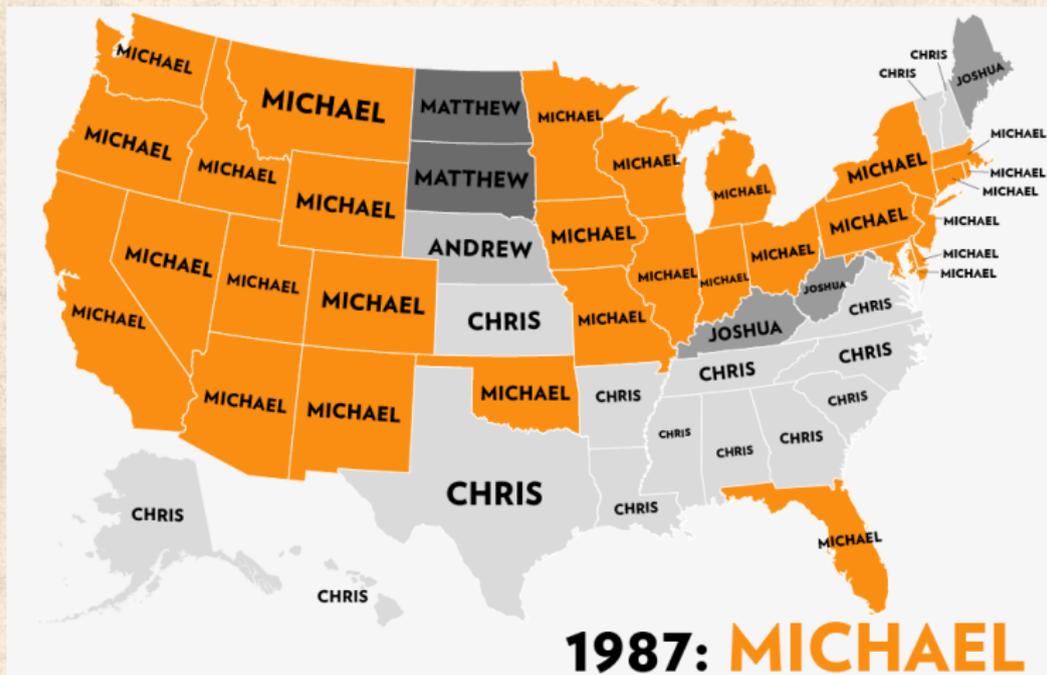
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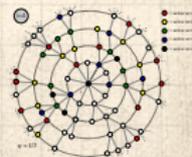
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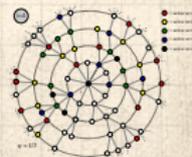
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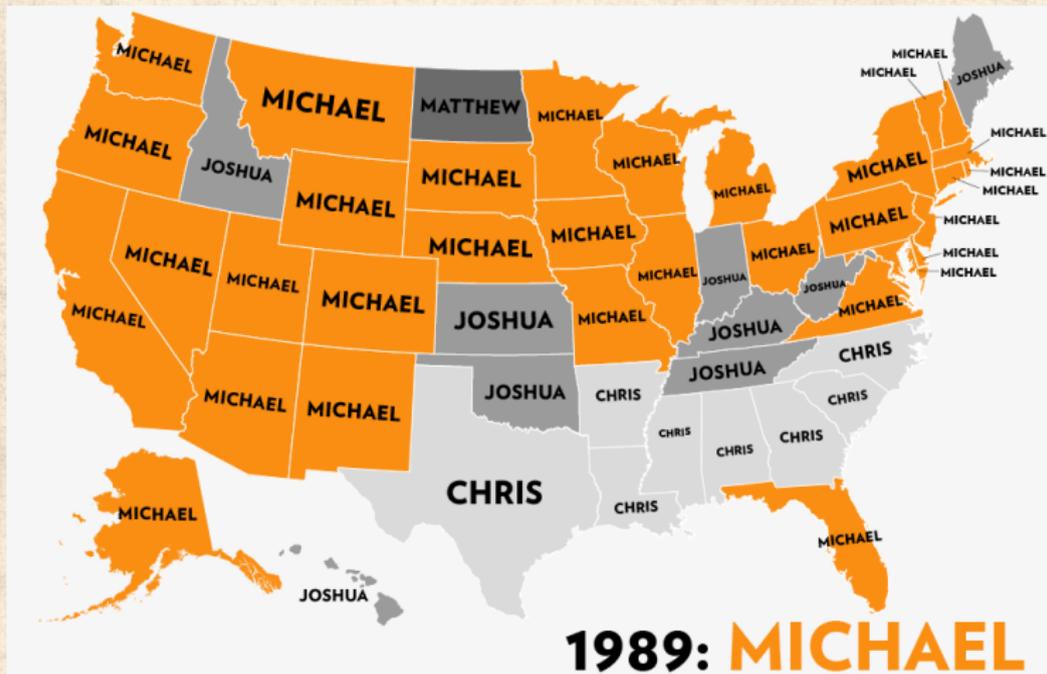
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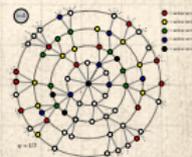
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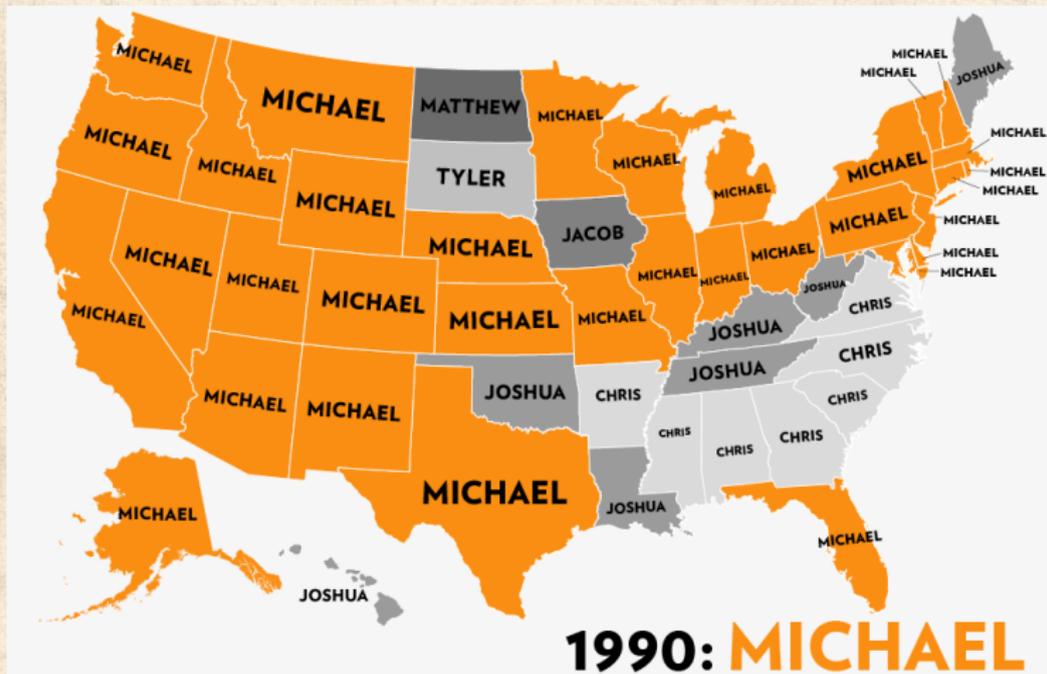
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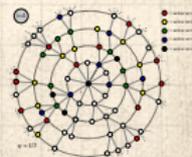
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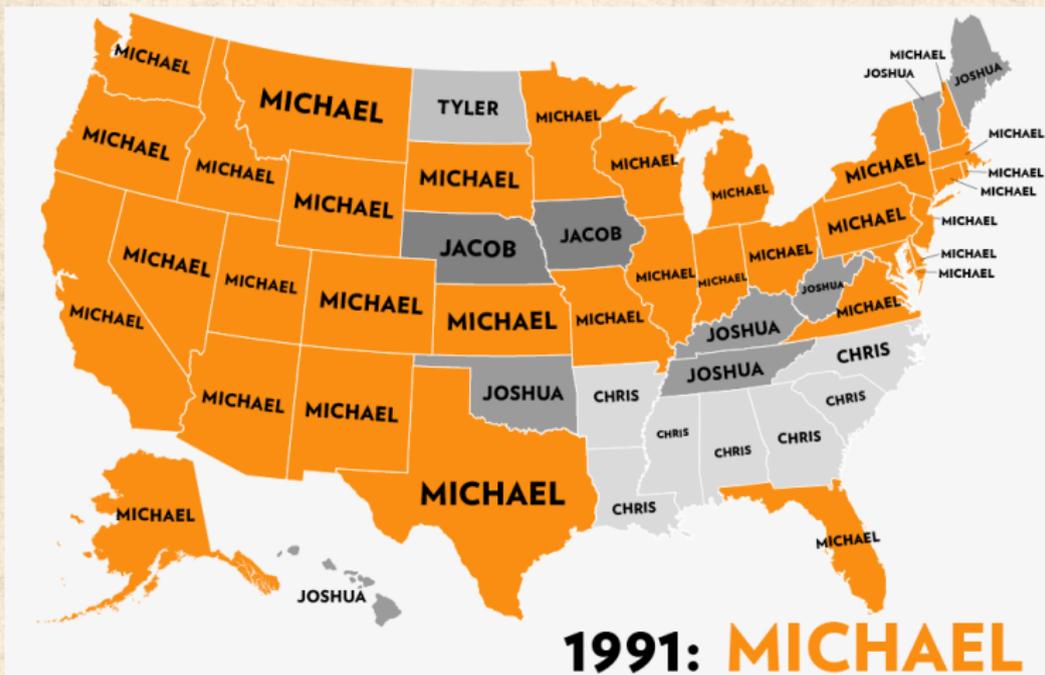
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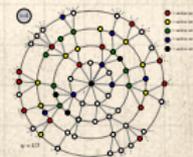
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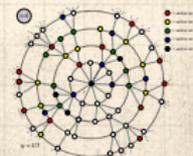
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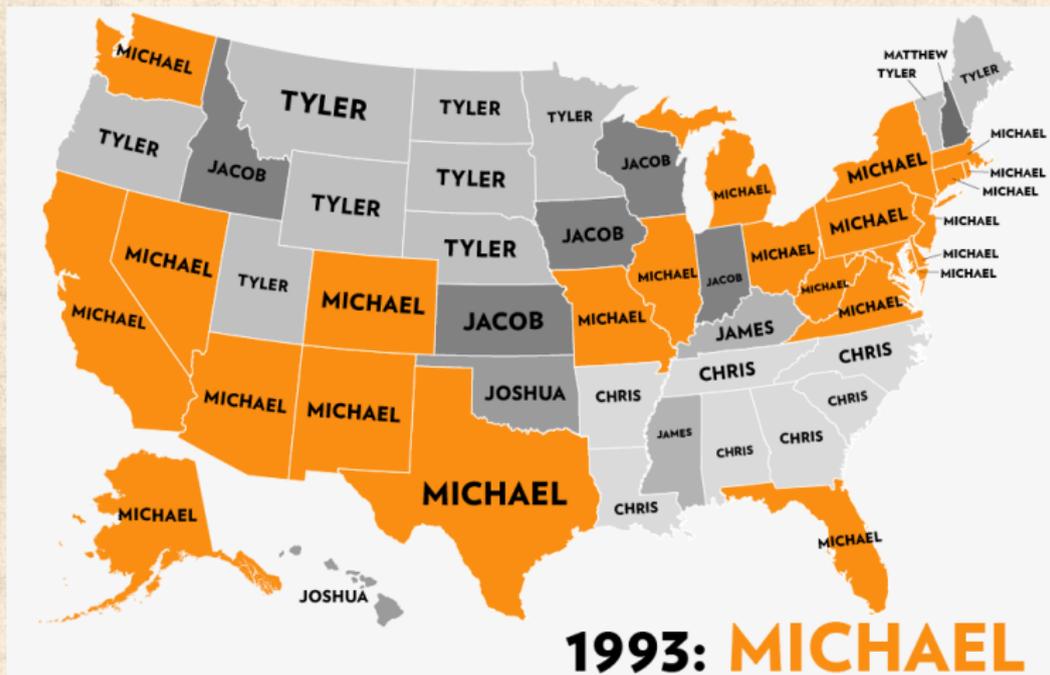
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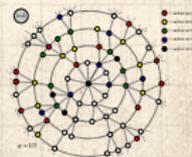
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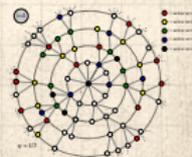
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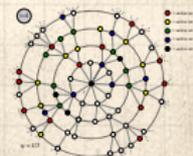
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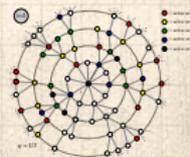
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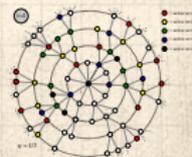
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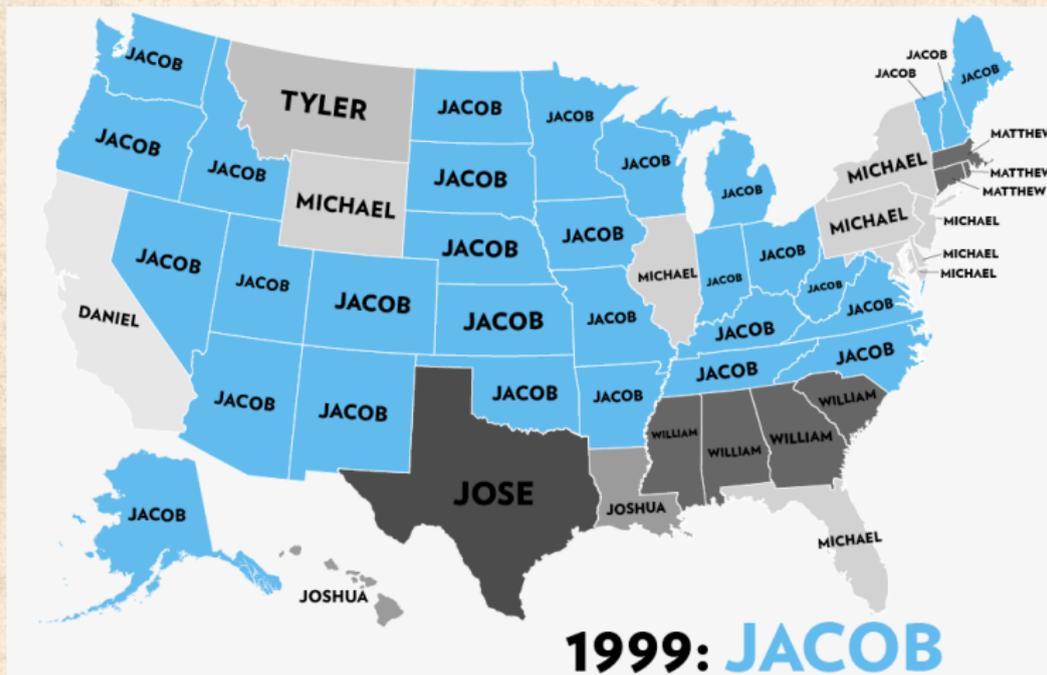
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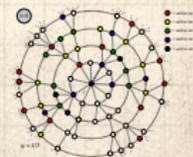
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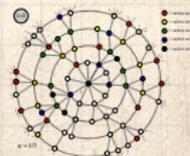
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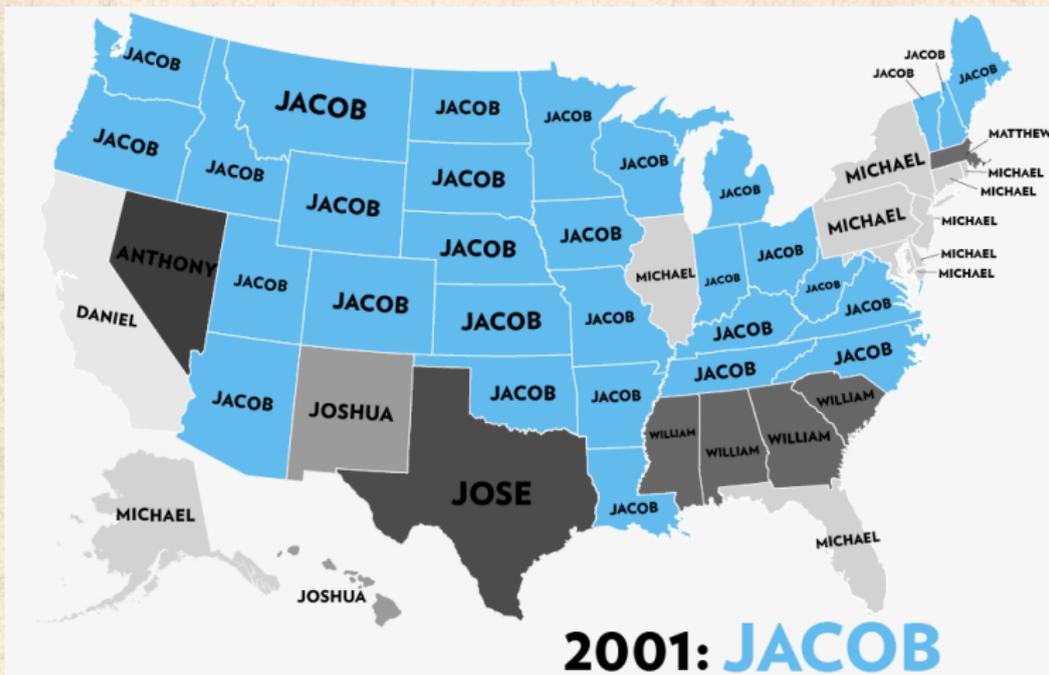
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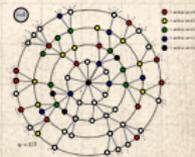
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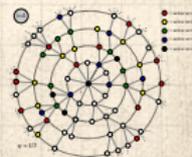
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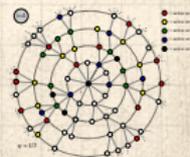
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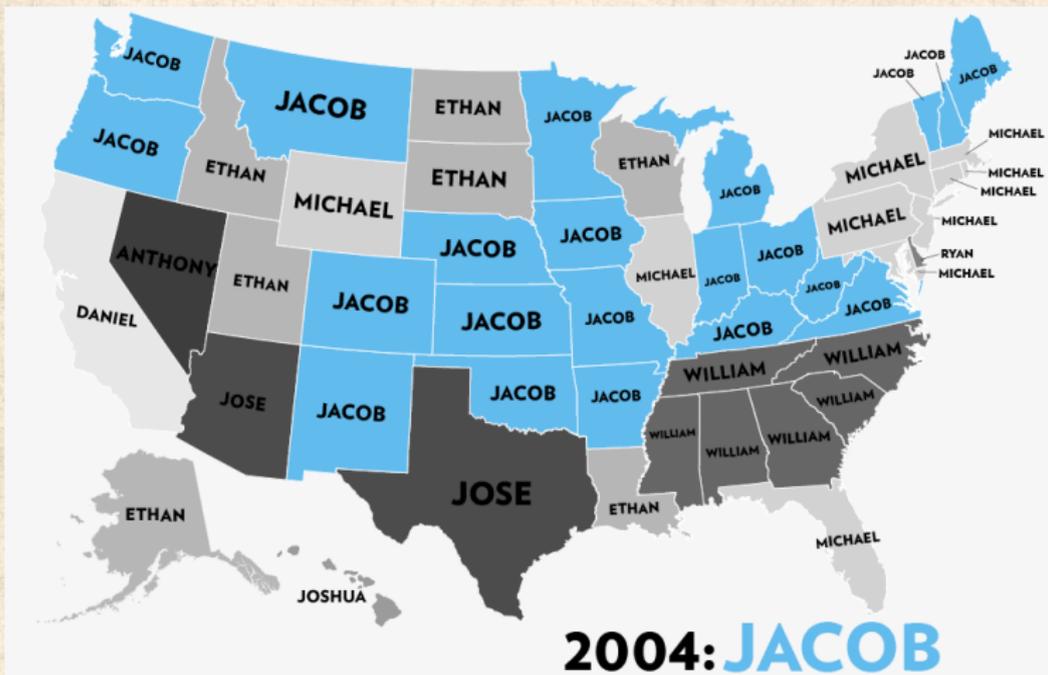
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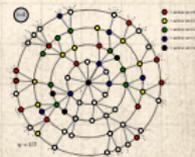
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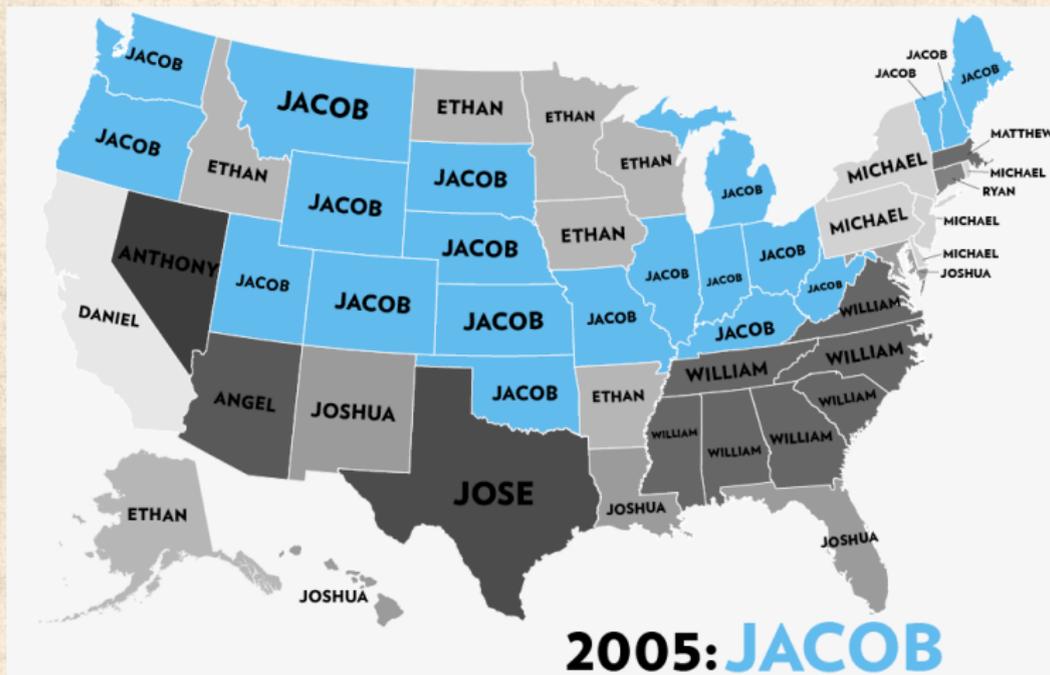
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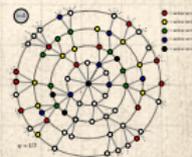
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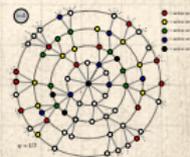
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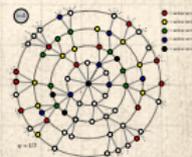
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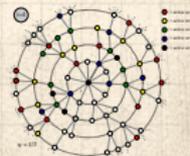
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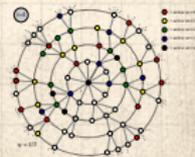
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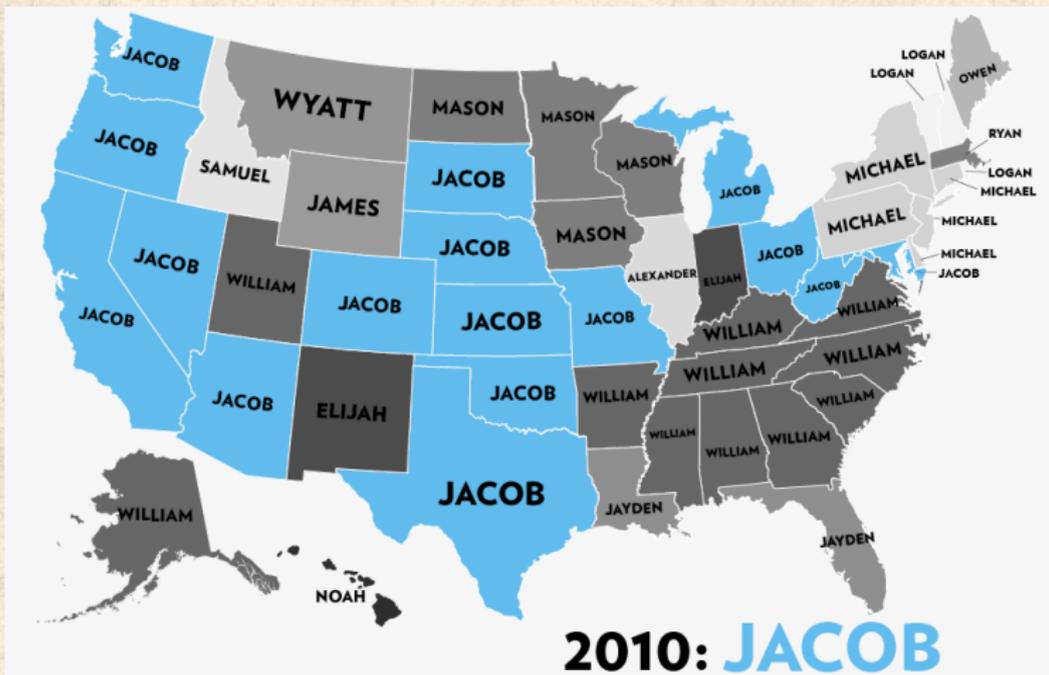
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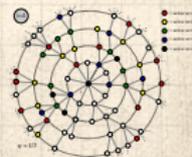
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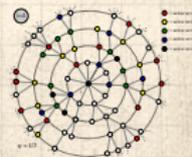
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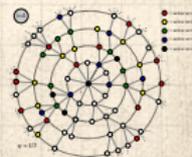
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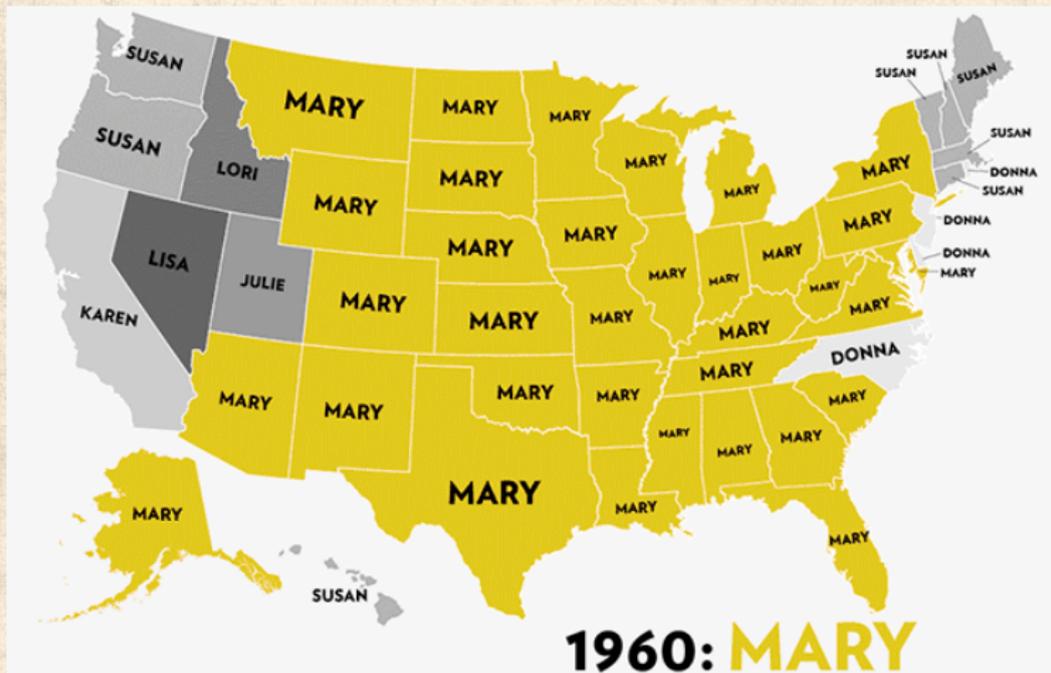
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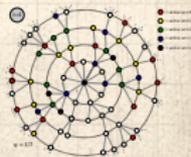
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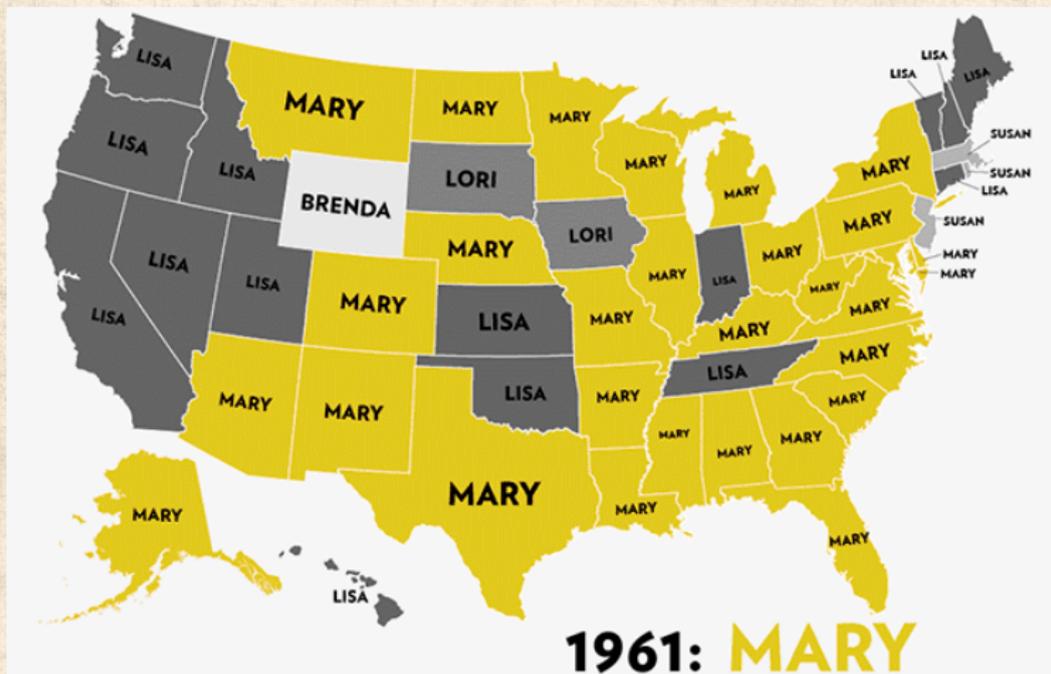
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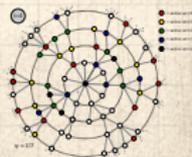
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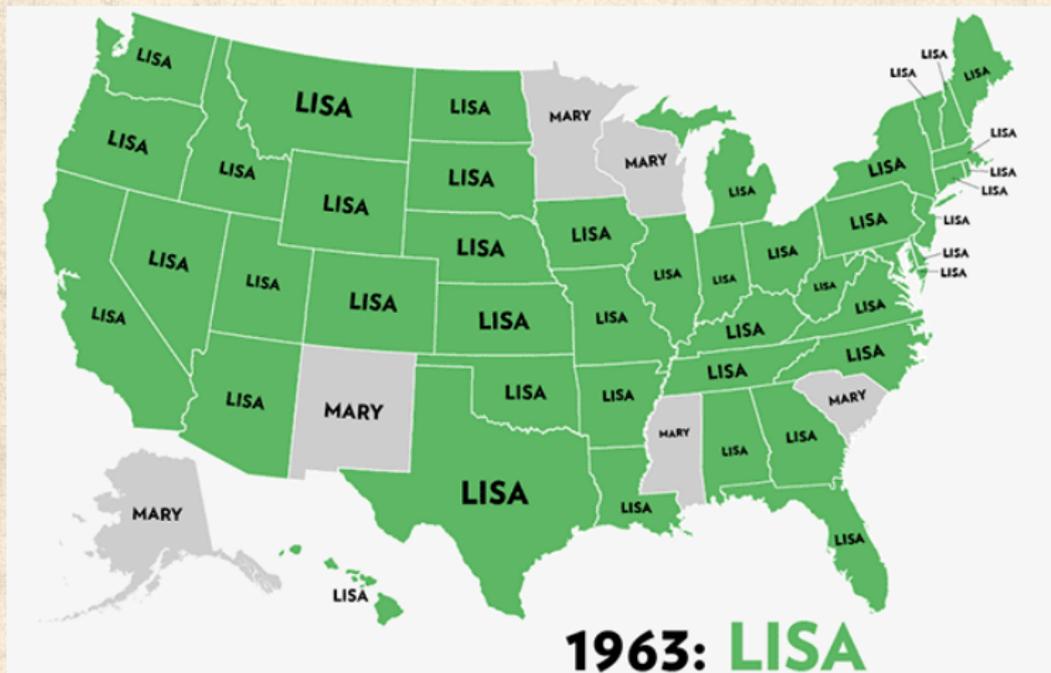




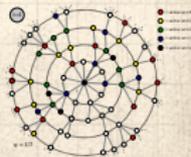
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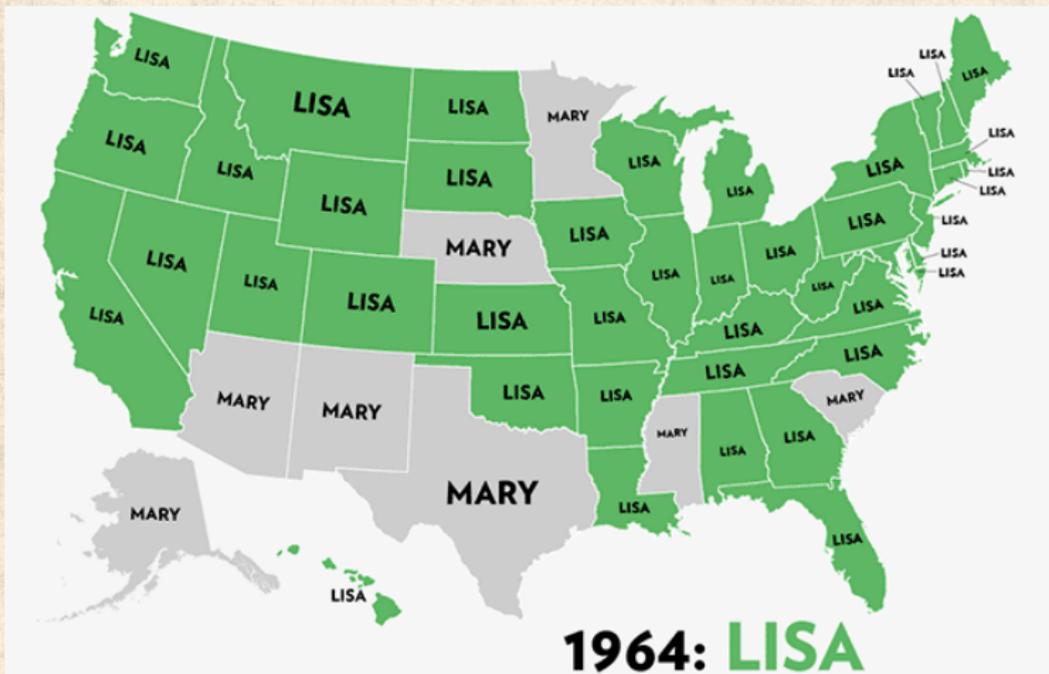
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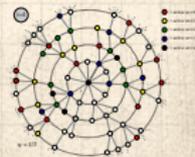
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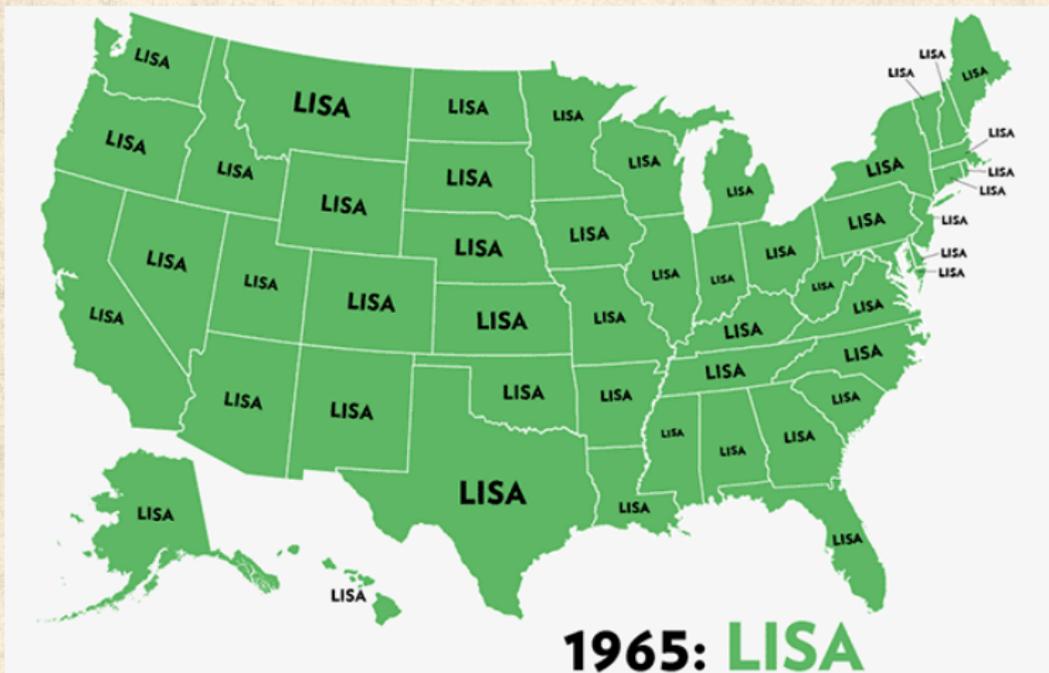
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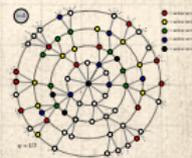
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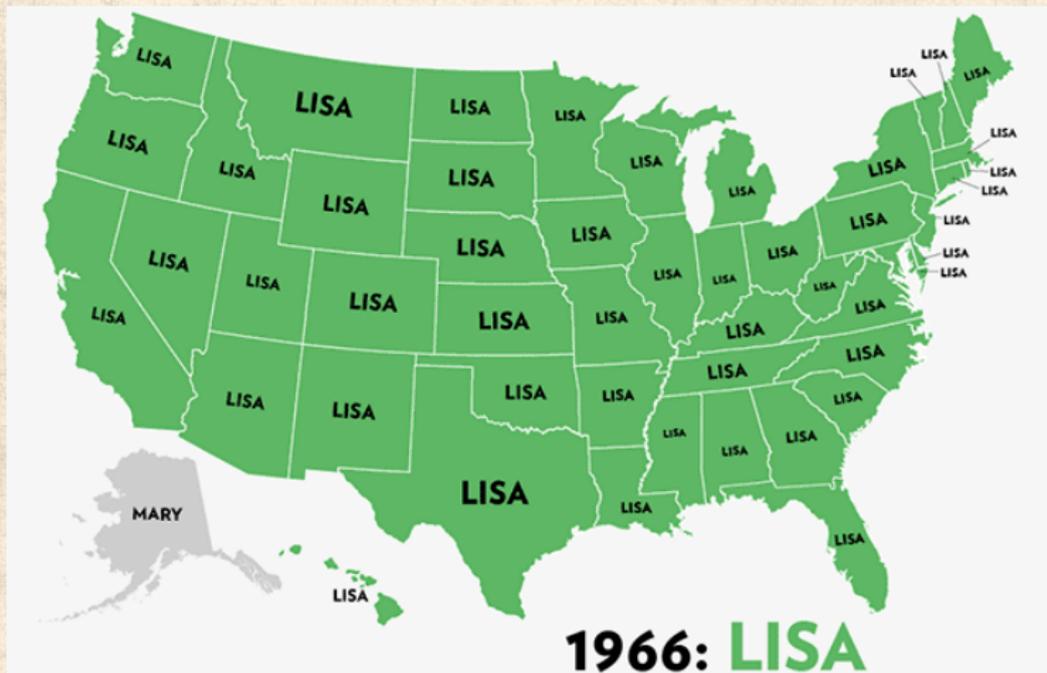
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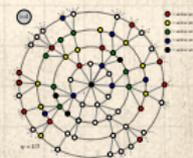
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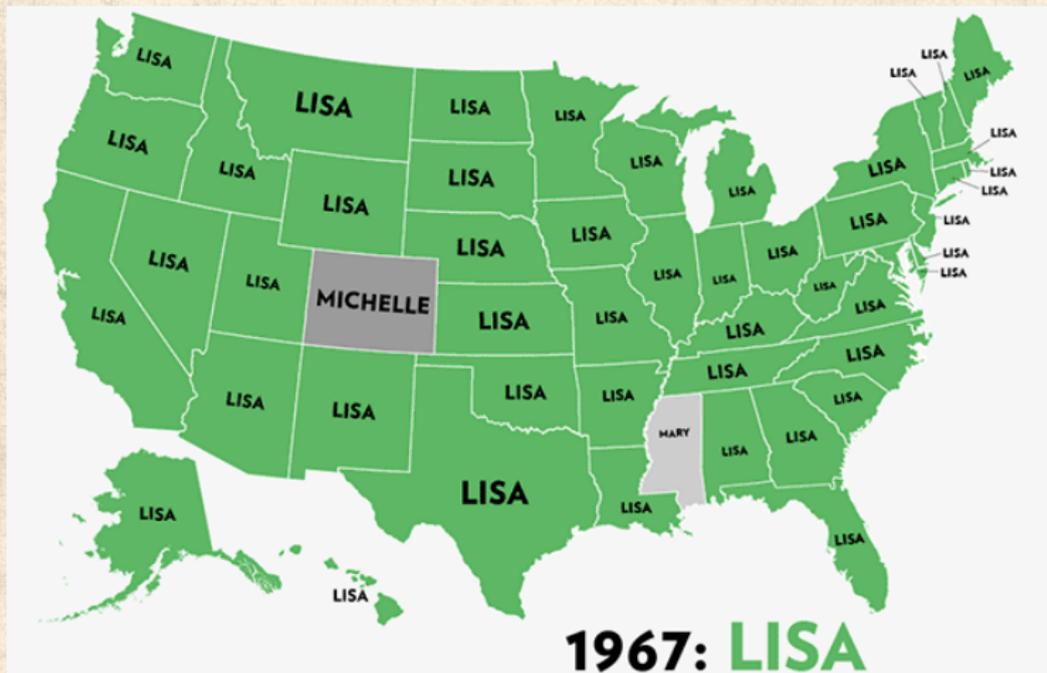
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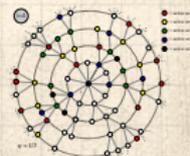
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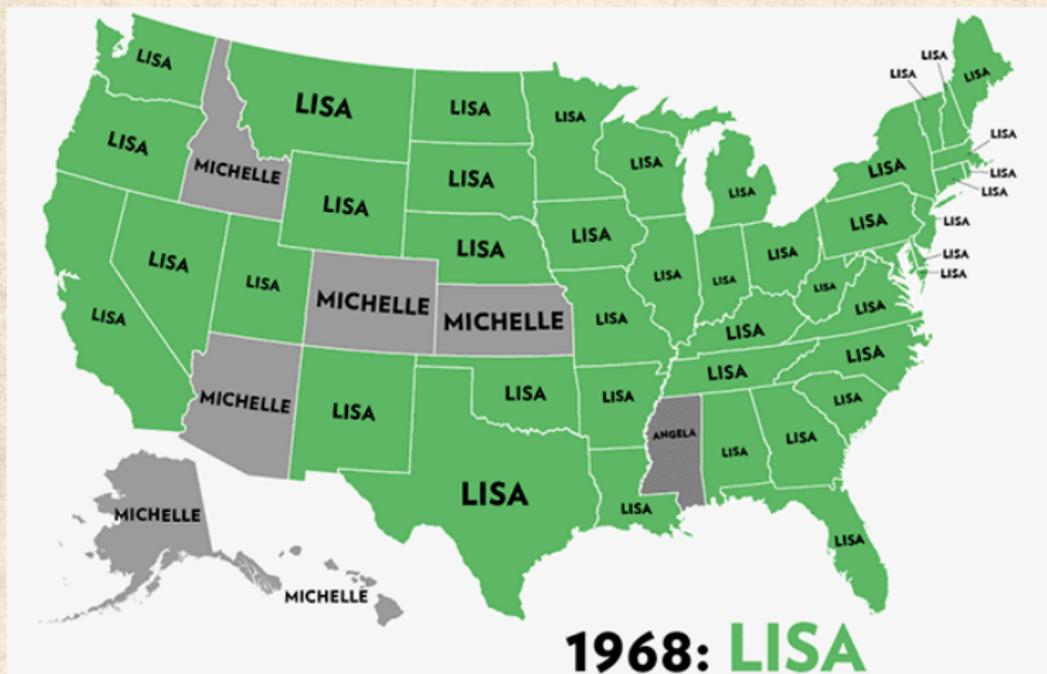
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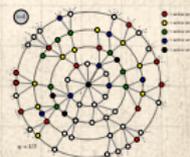
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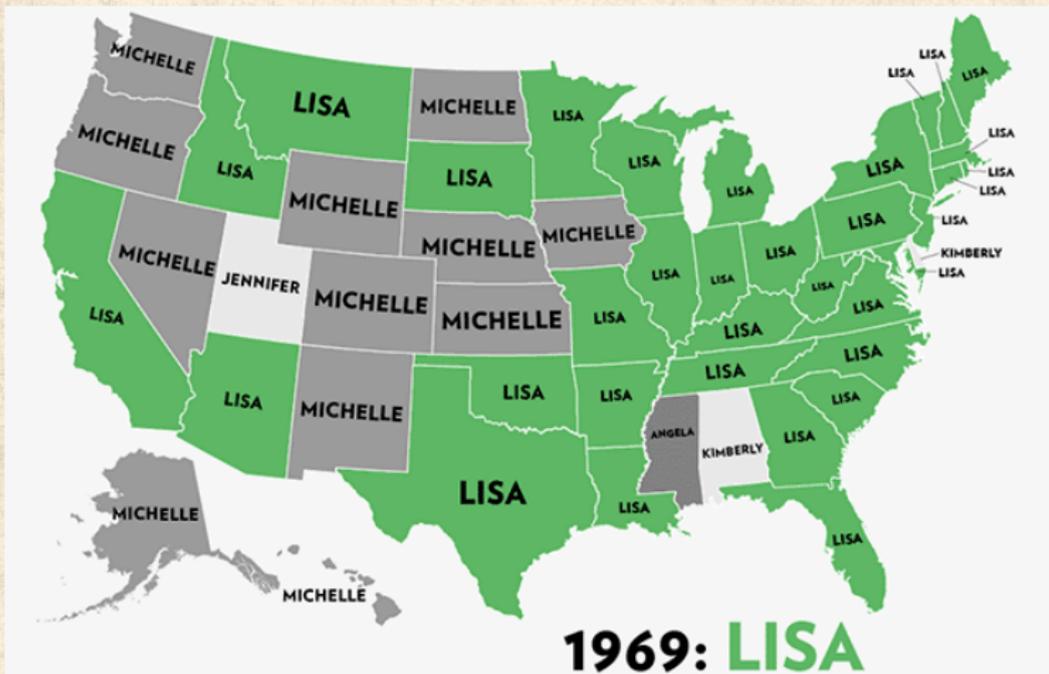
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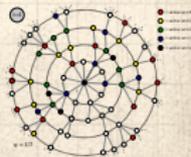
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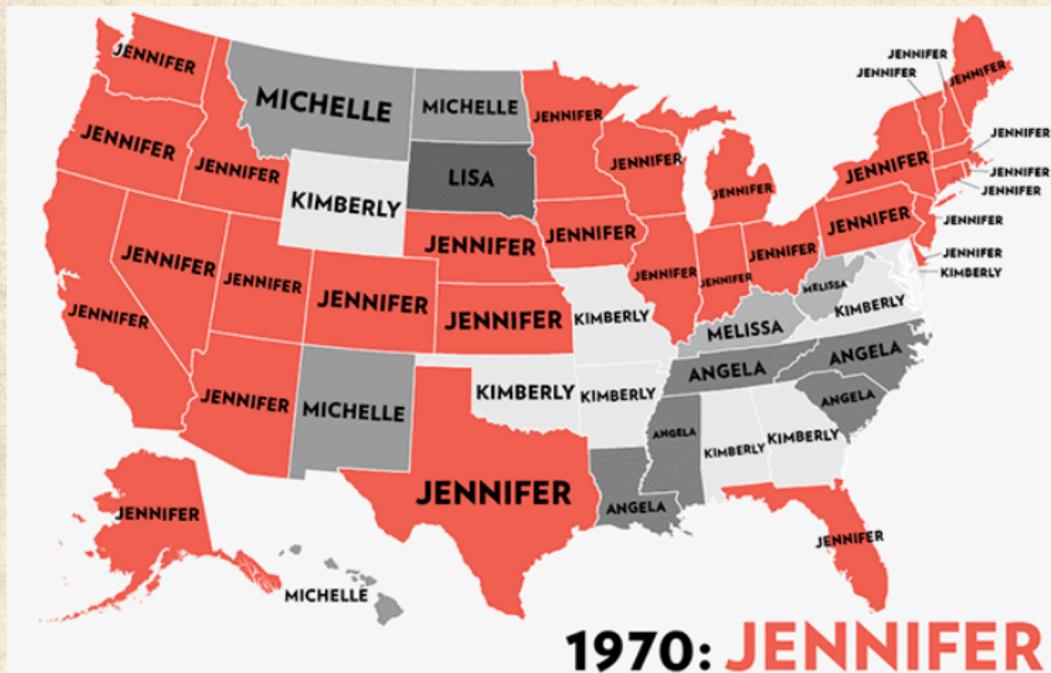
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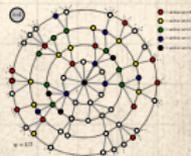
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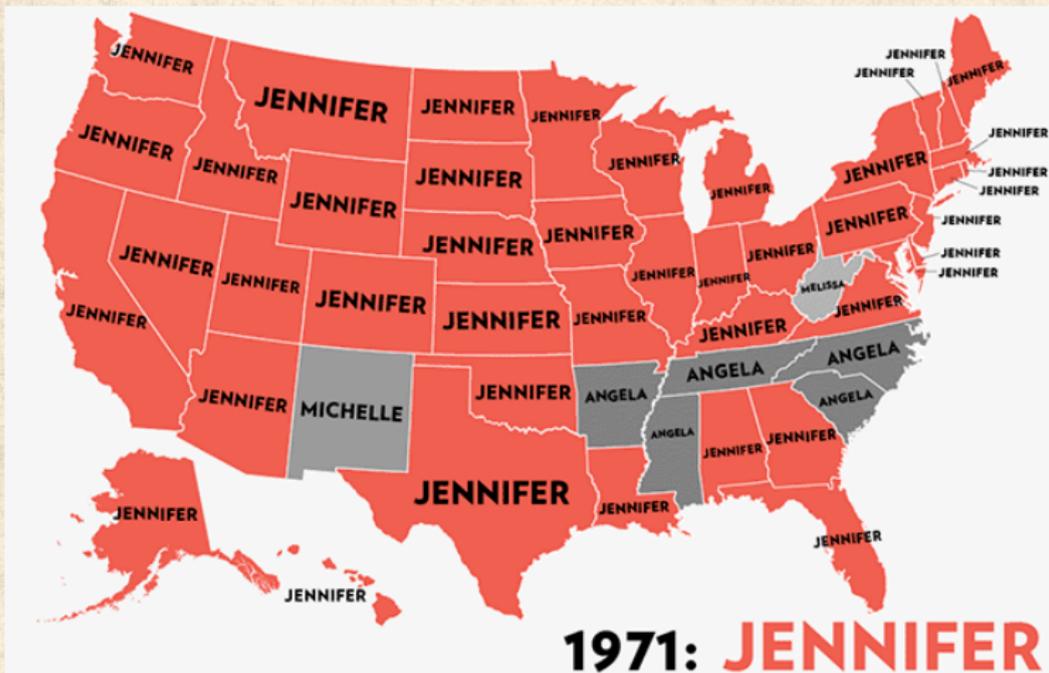
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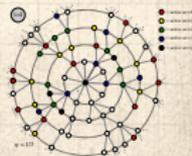
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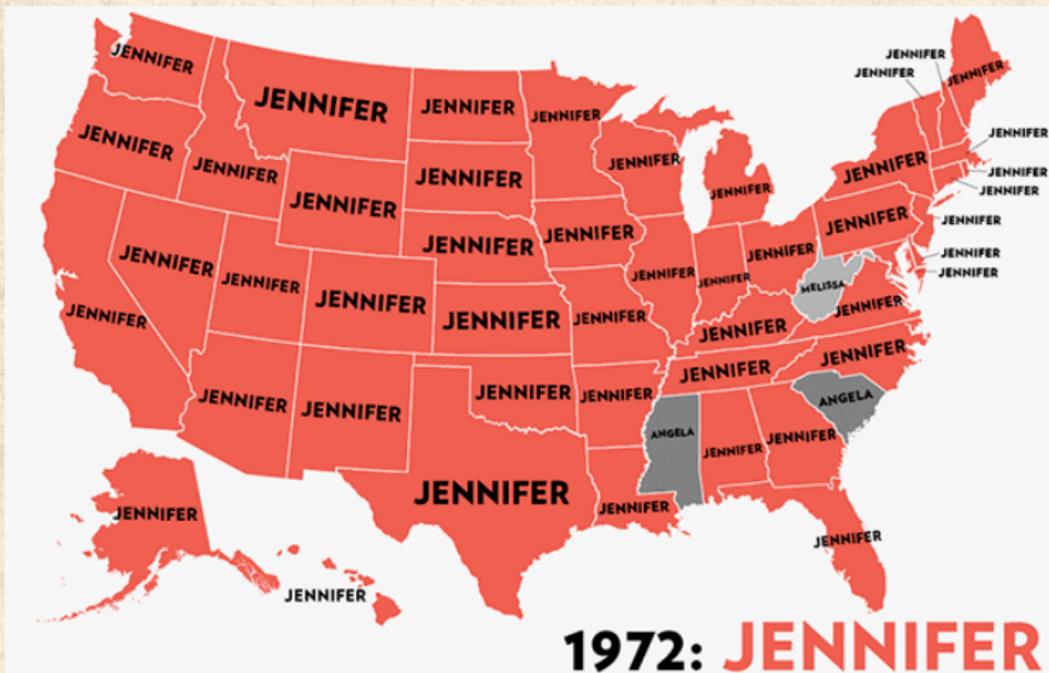
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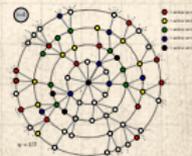
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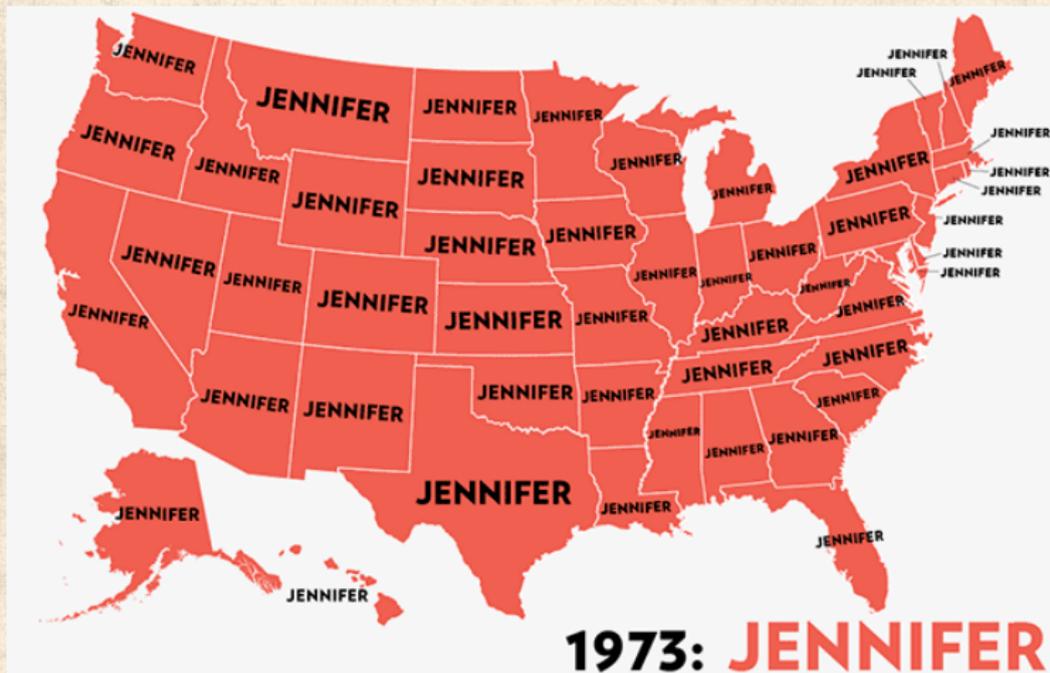
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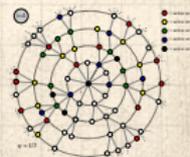
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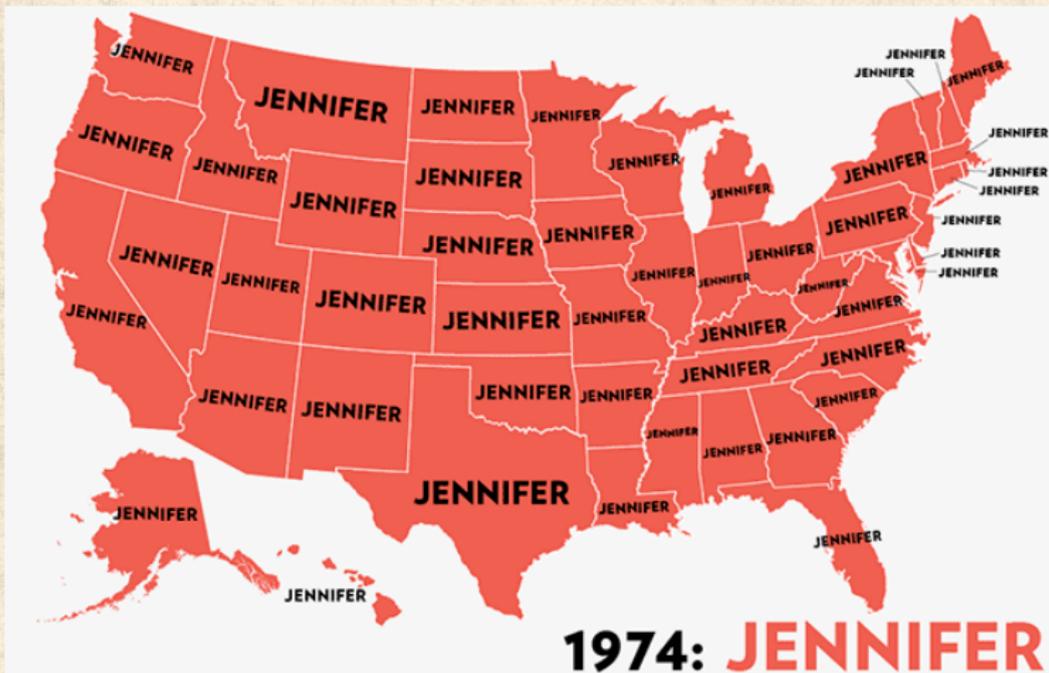
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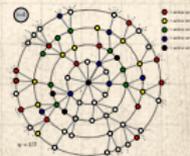
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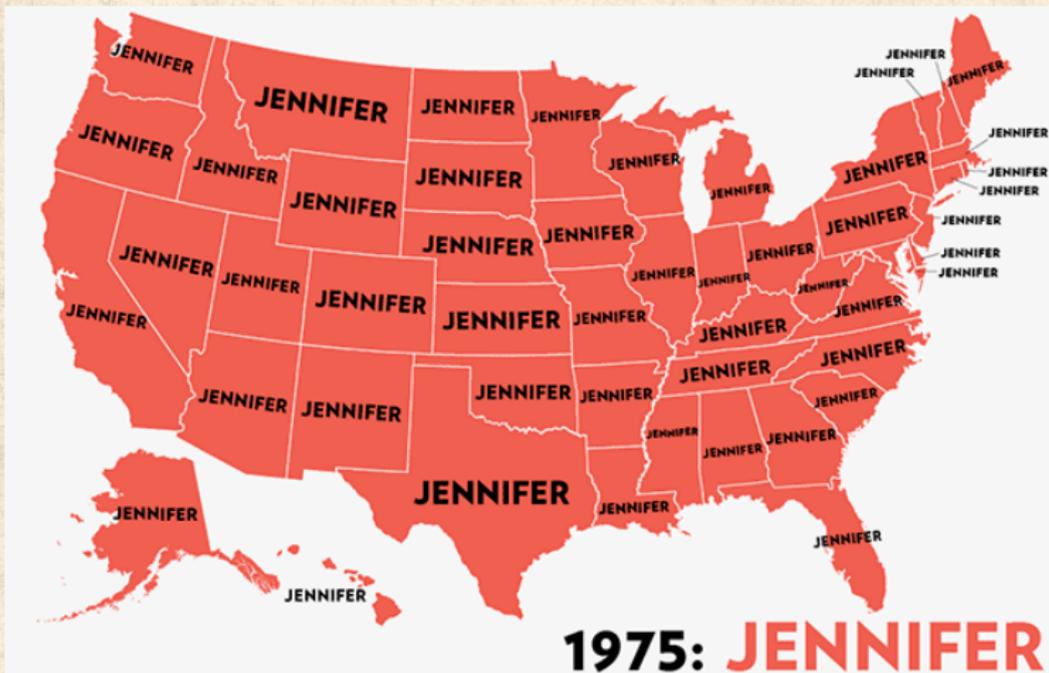
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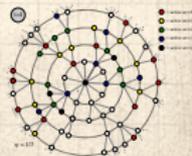
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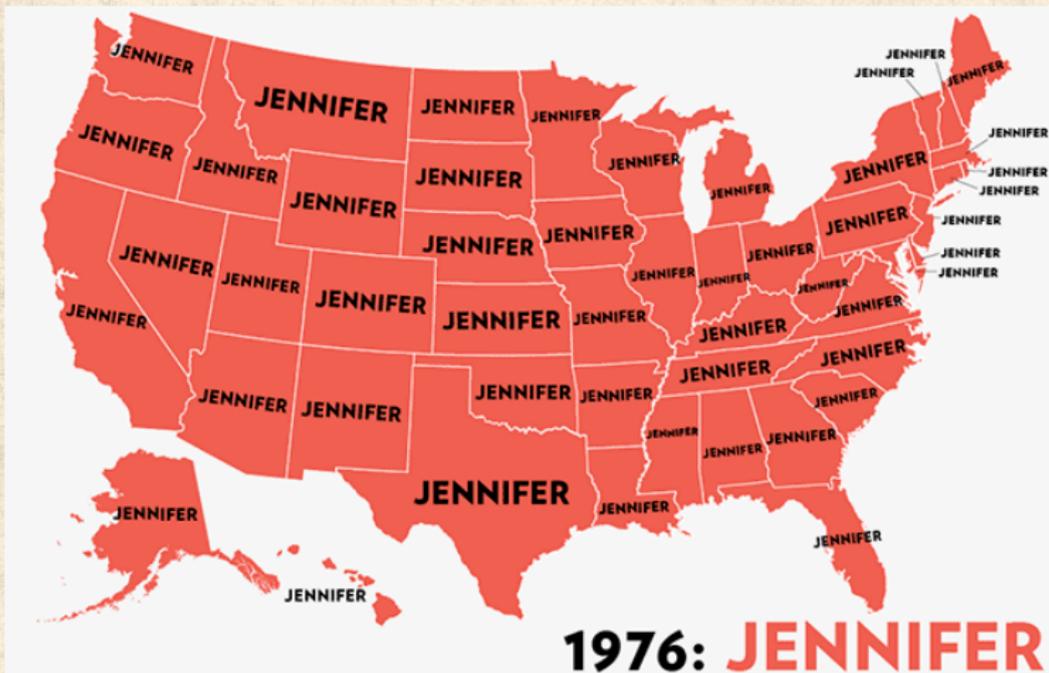
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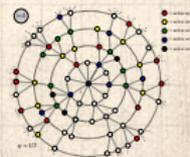
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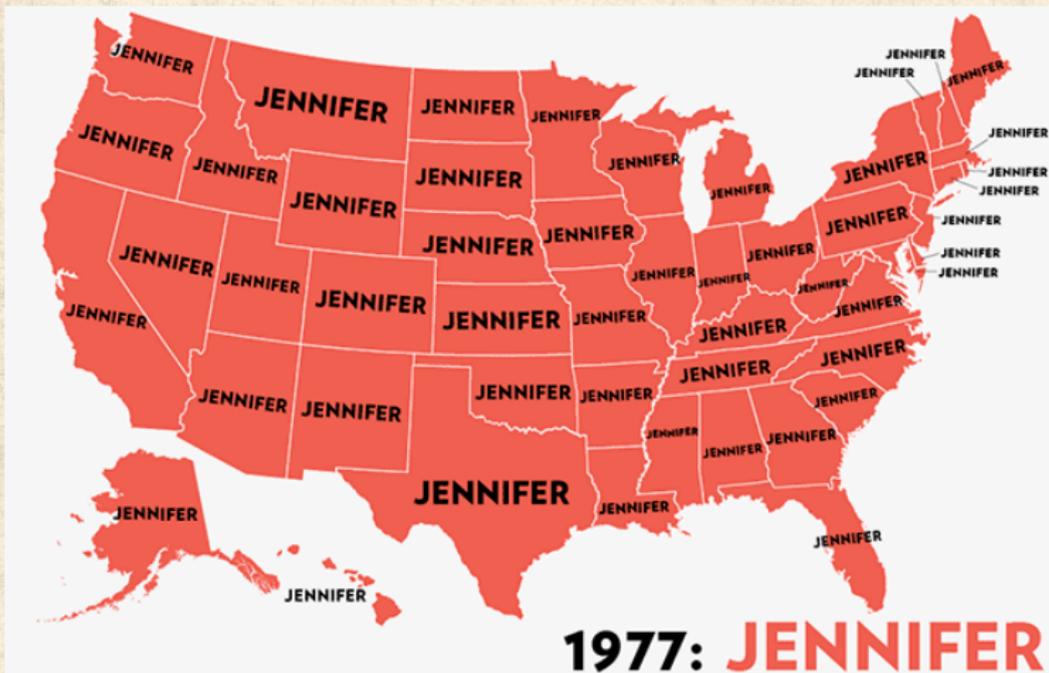
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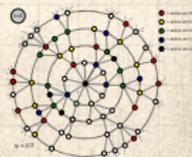
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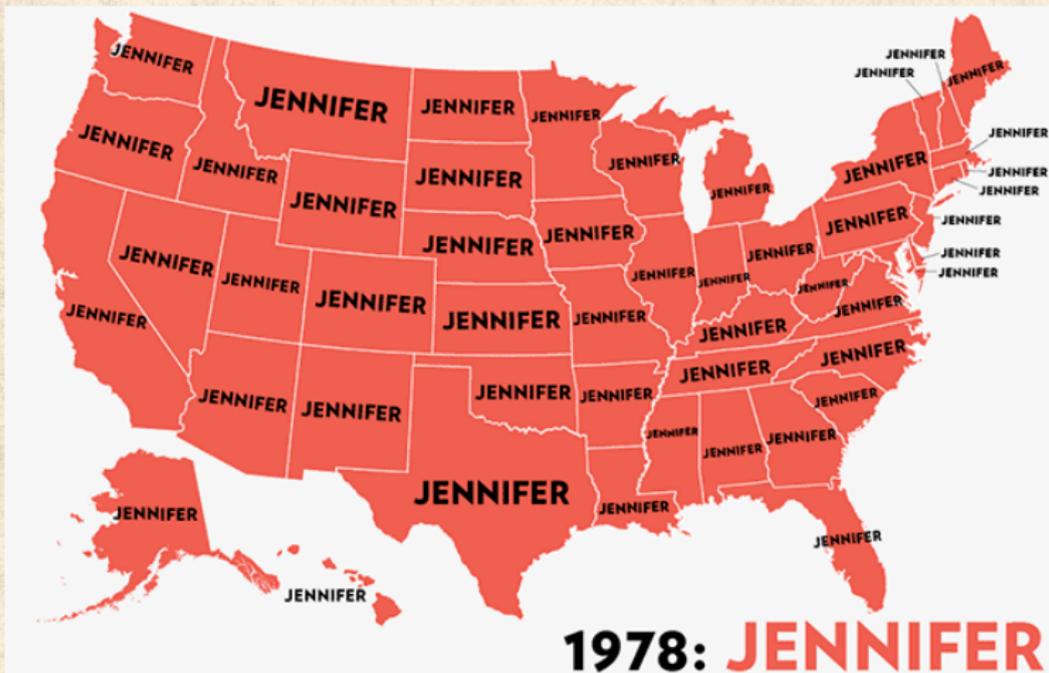
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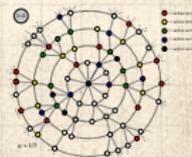
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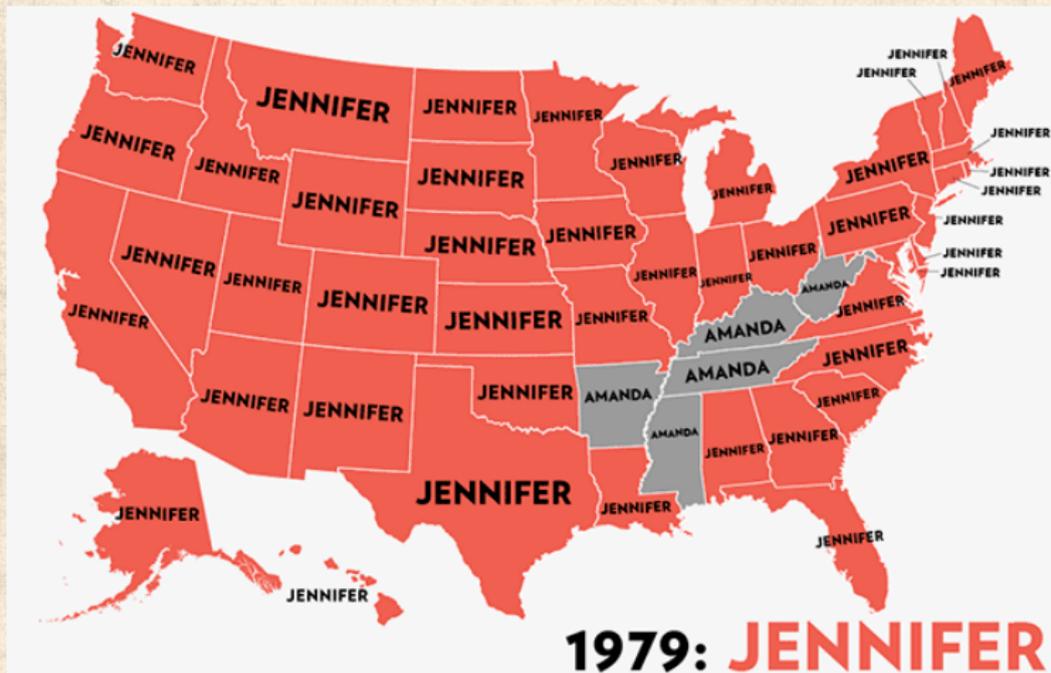
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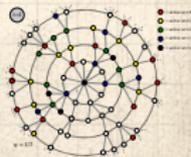
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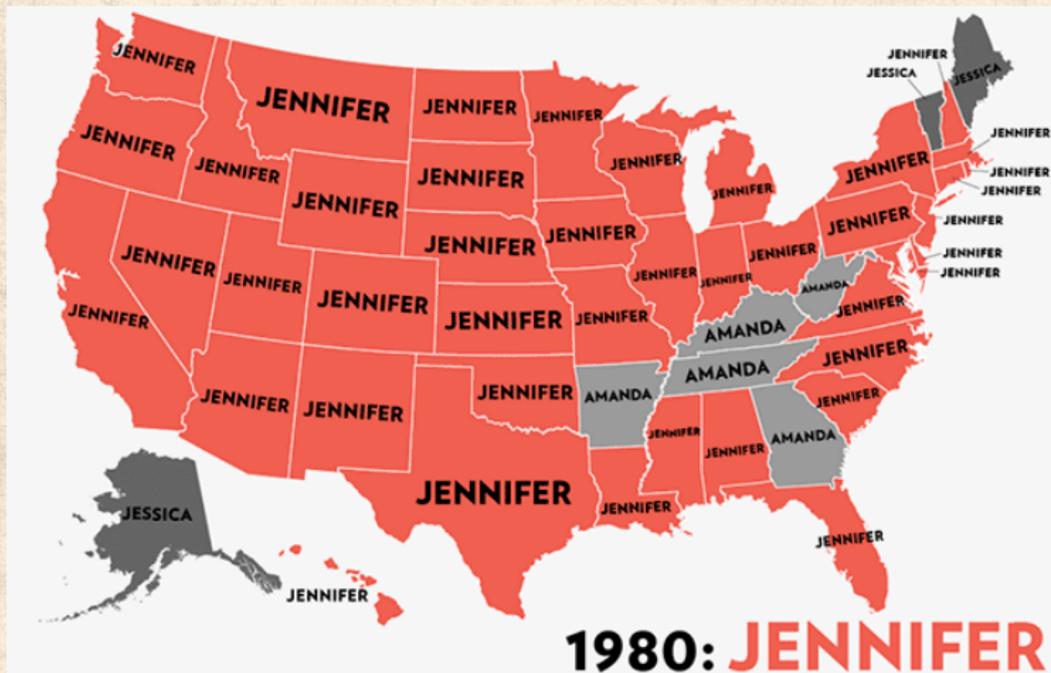
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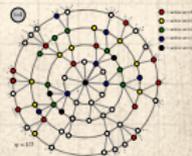
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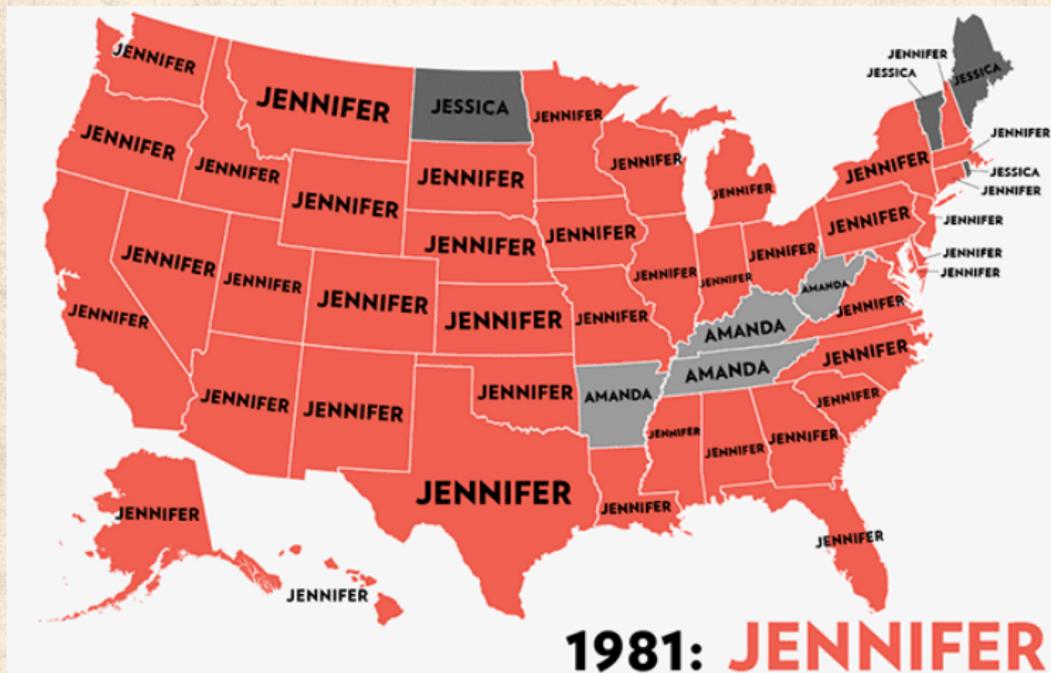
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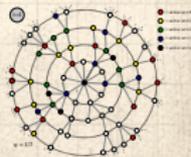
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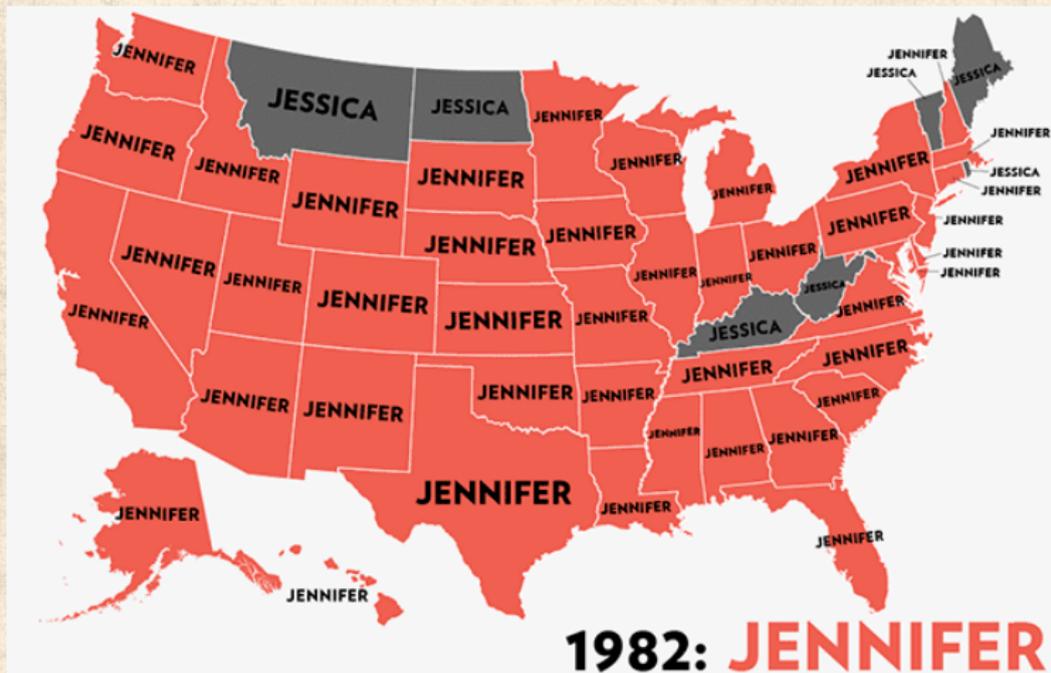
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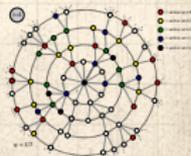
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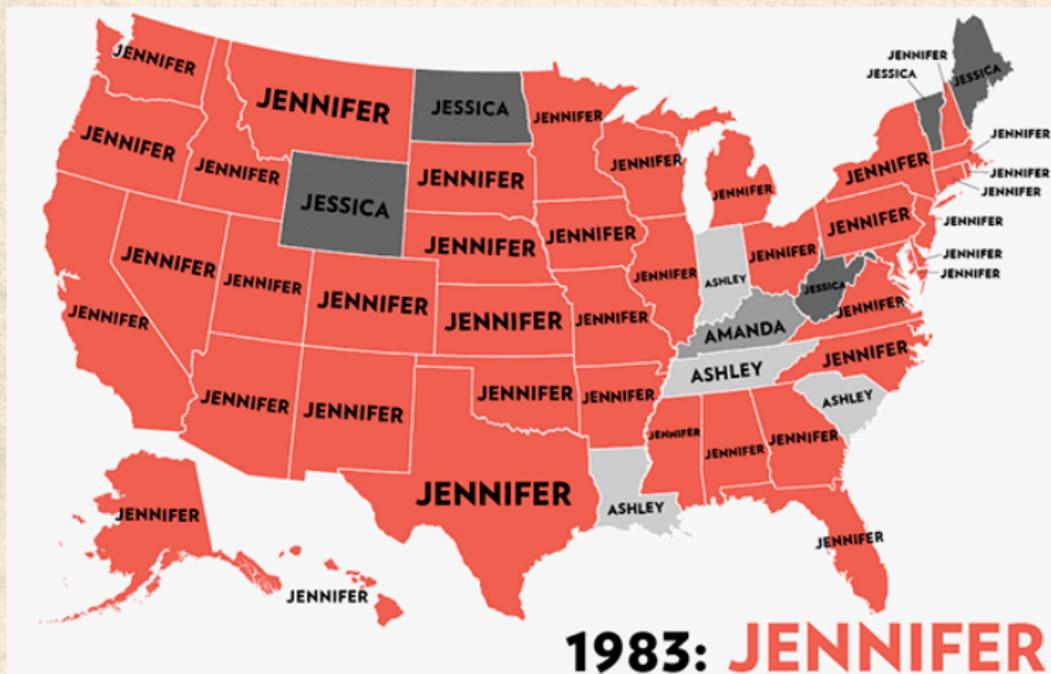
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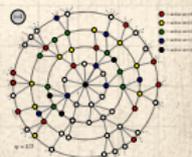
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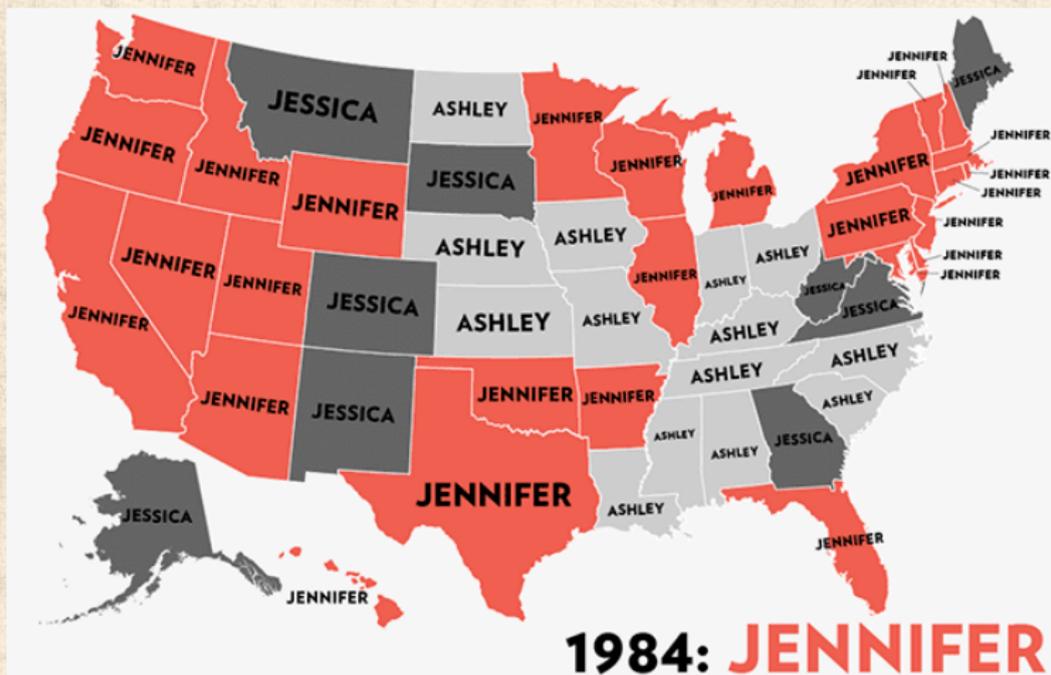
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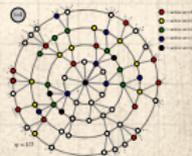
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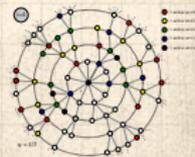
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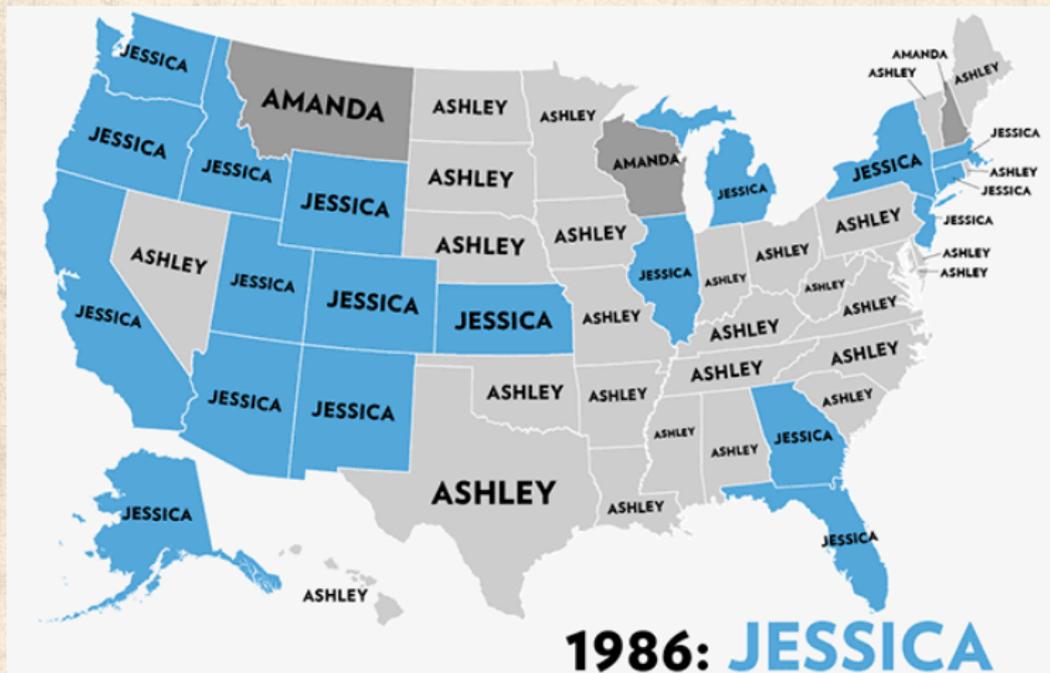
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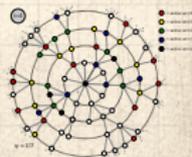
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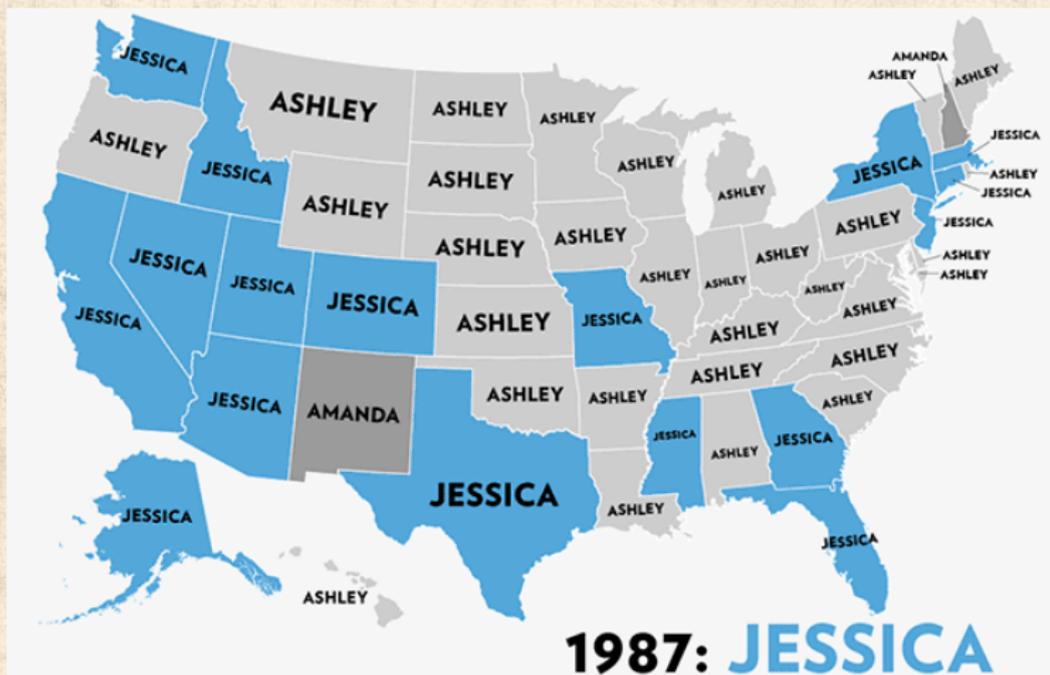
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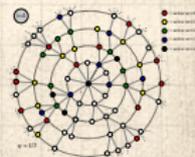
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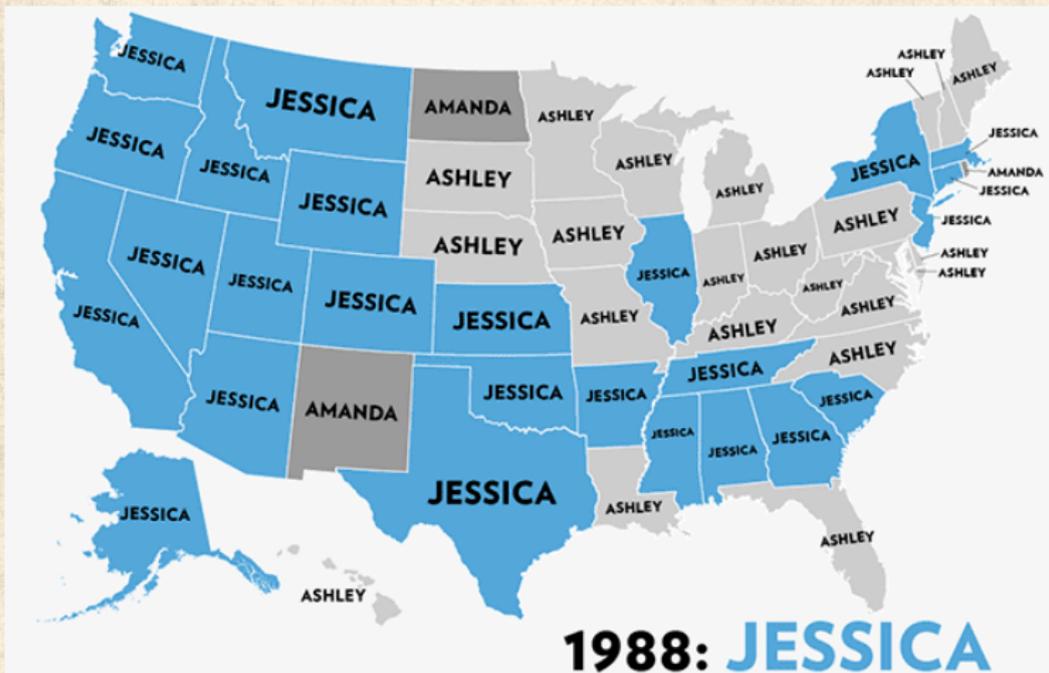
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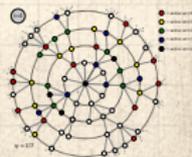
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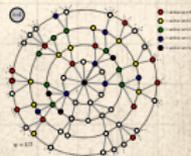
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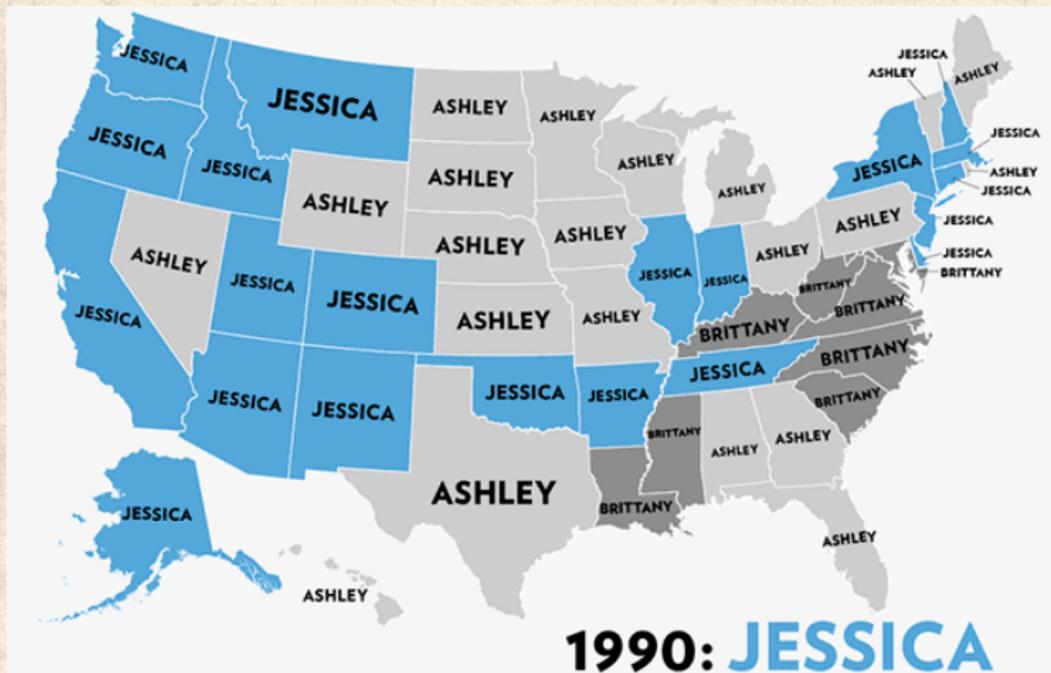
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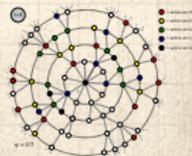
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic ↗



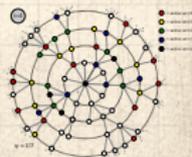
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From the Atlantic ↗



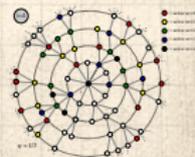
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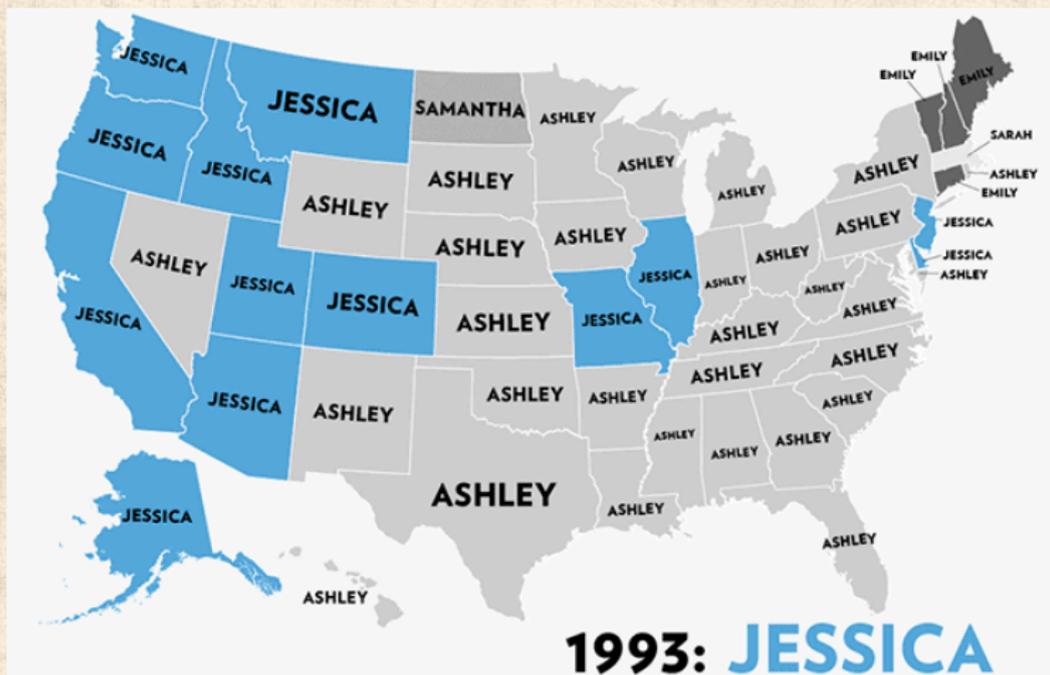
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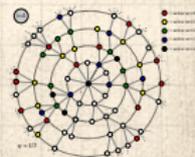
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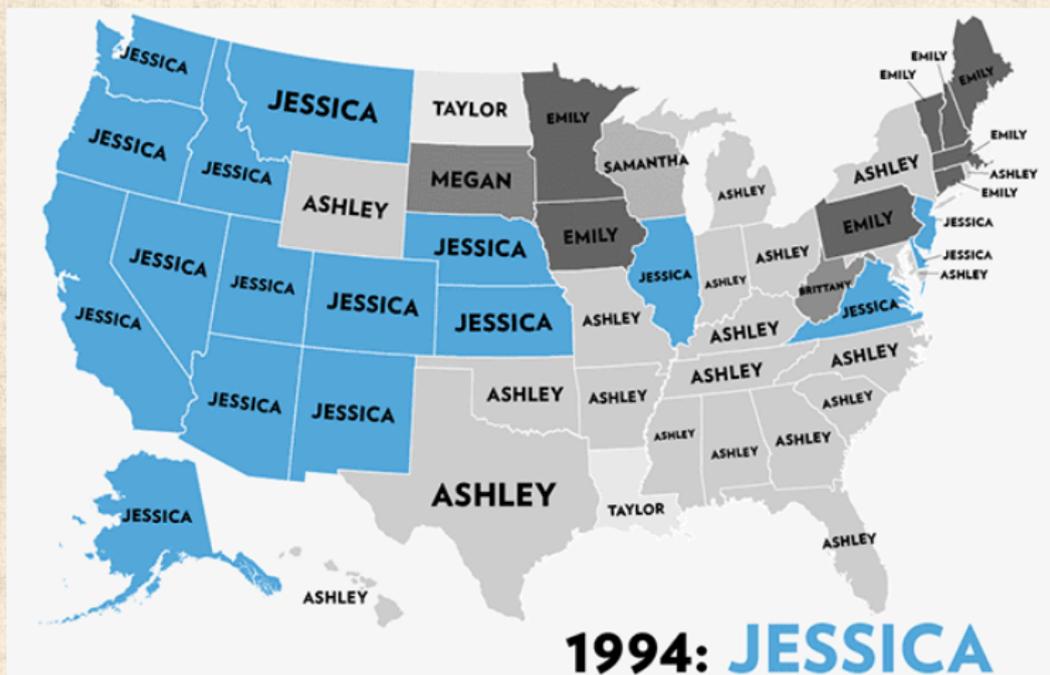
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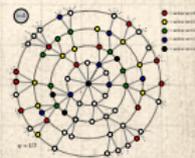
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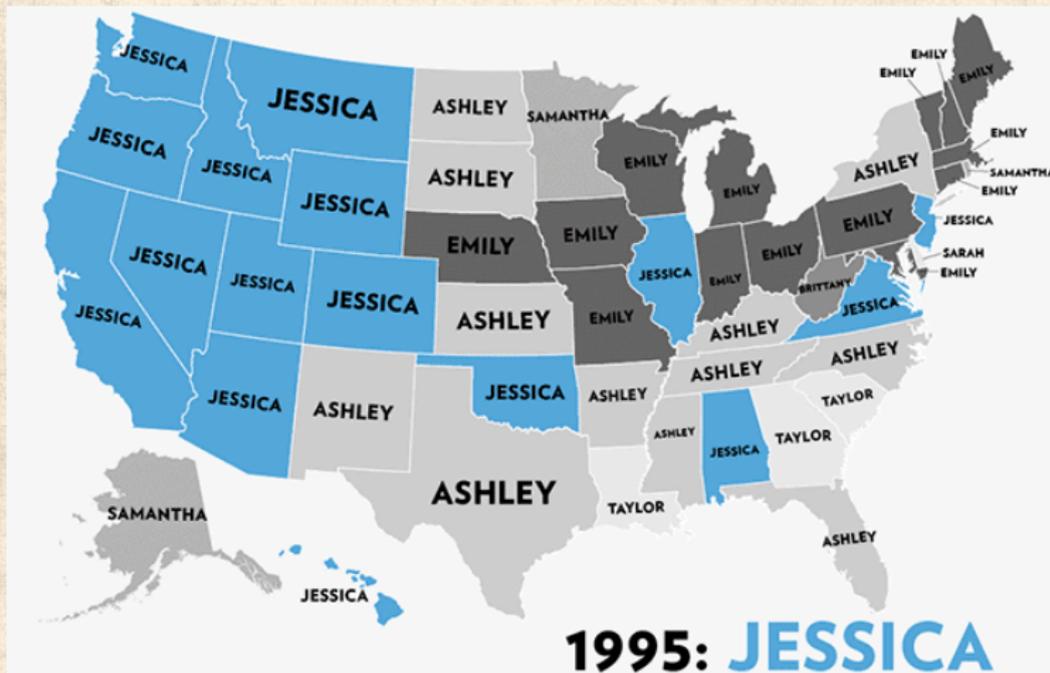
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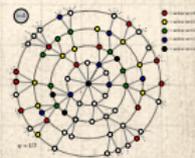
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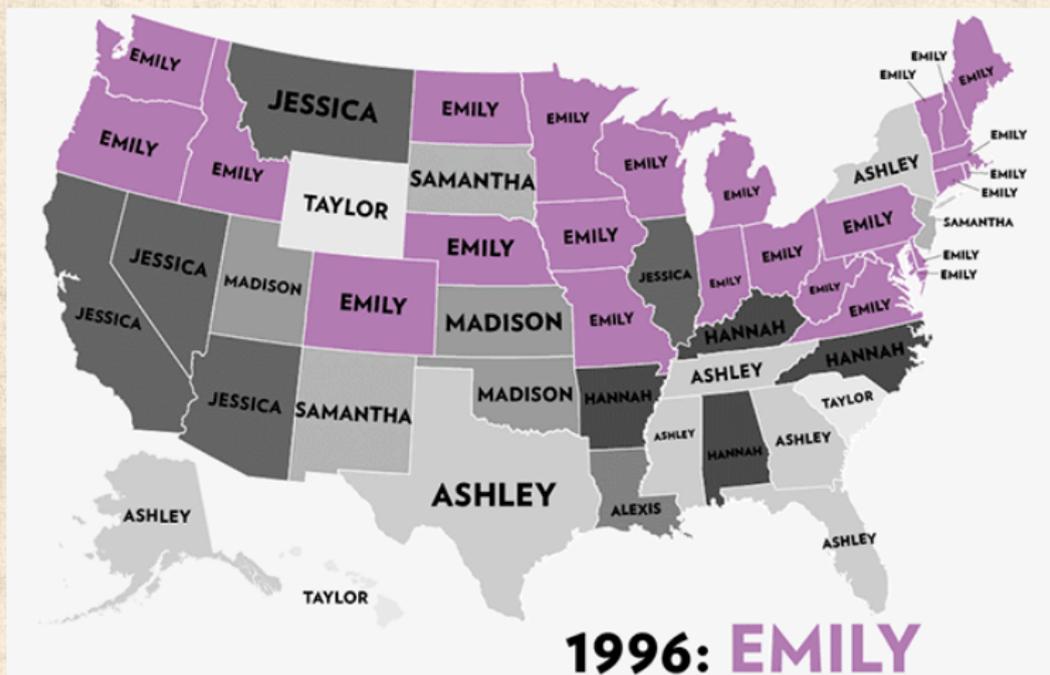
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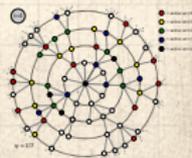
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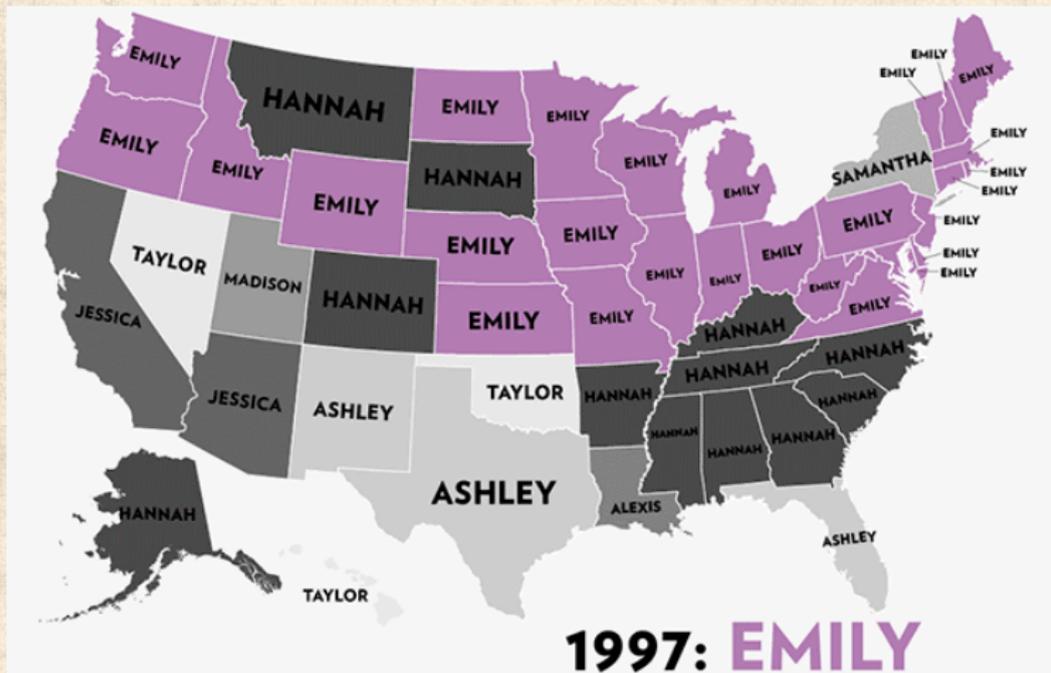
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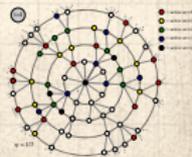
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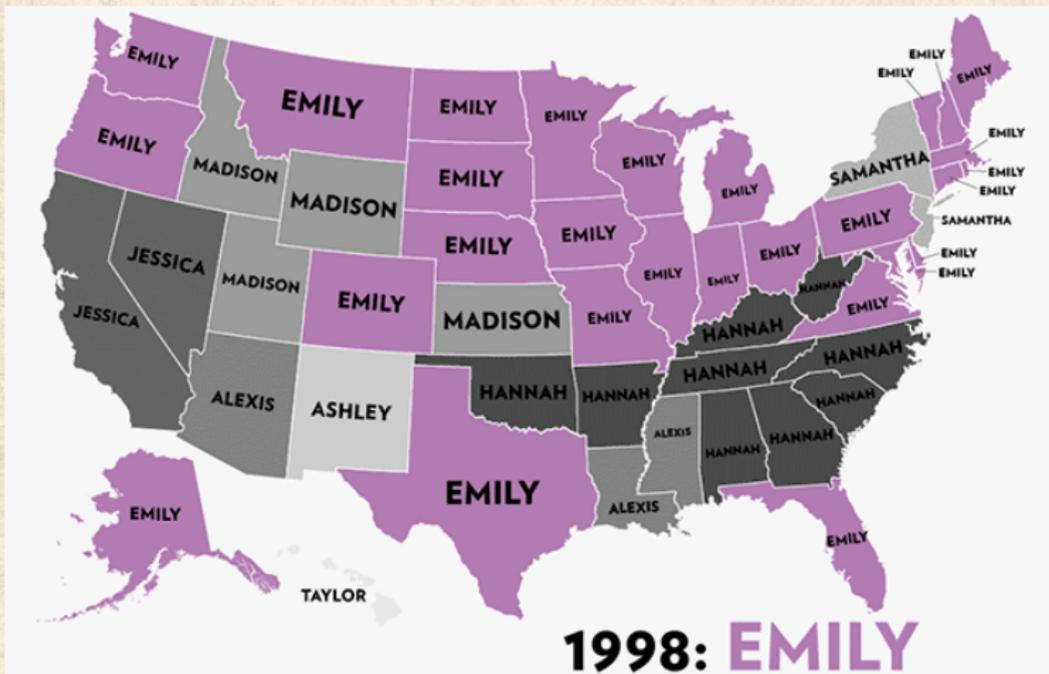
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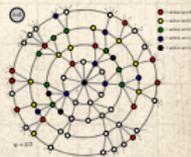
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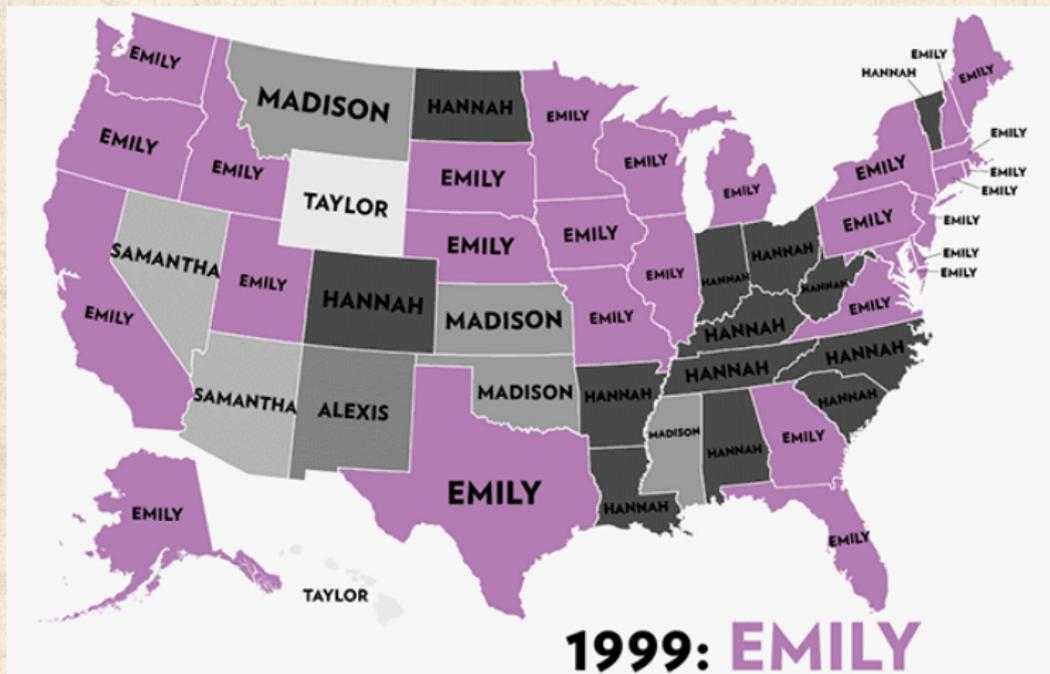
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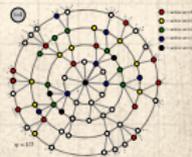
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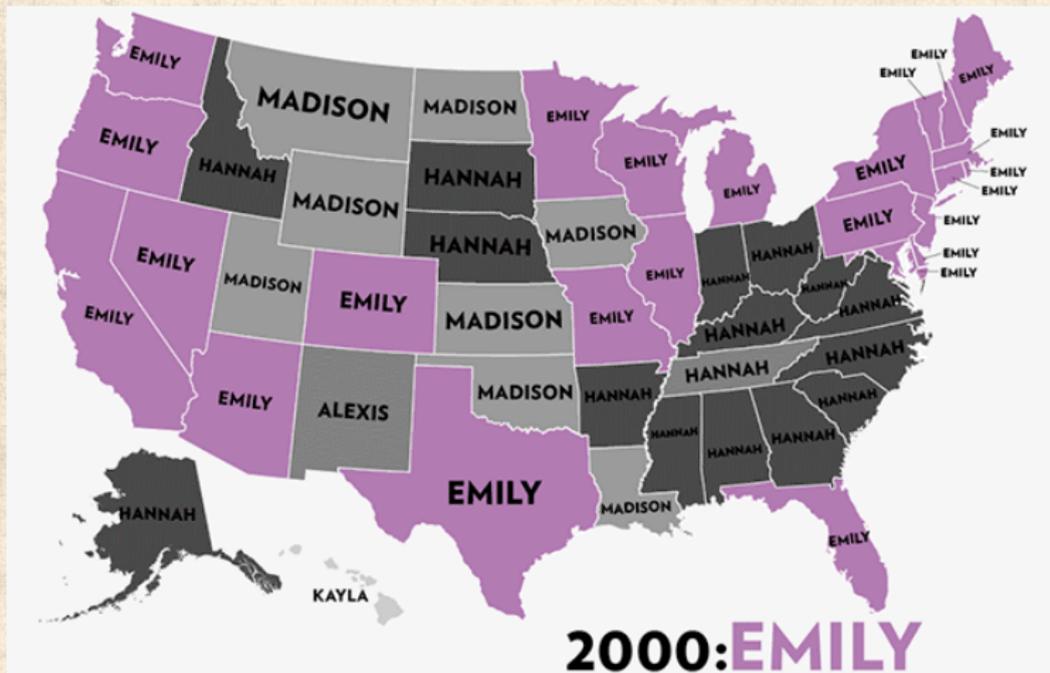
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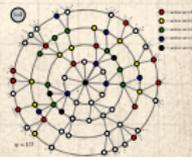
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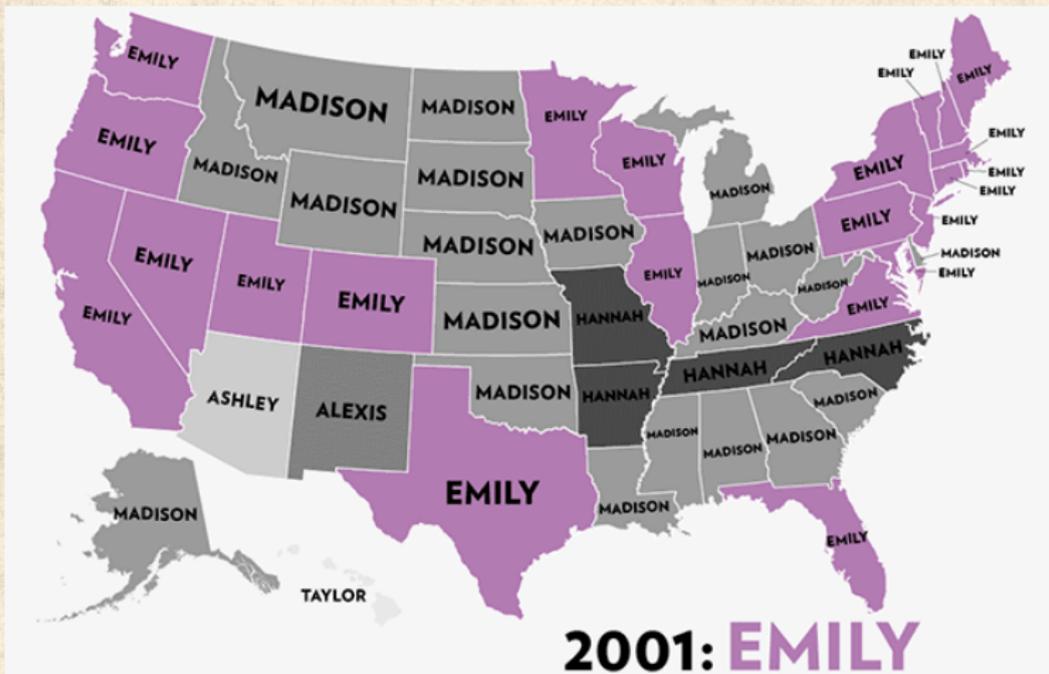
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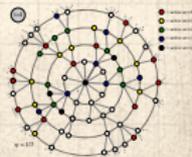
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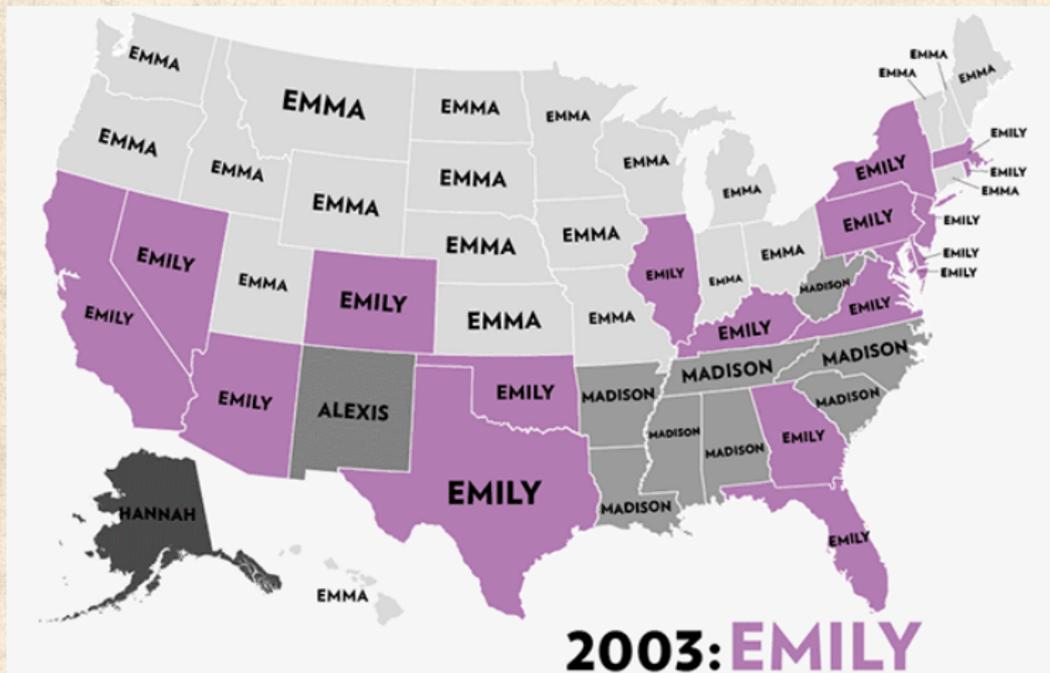




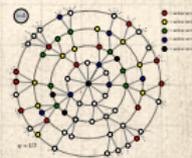
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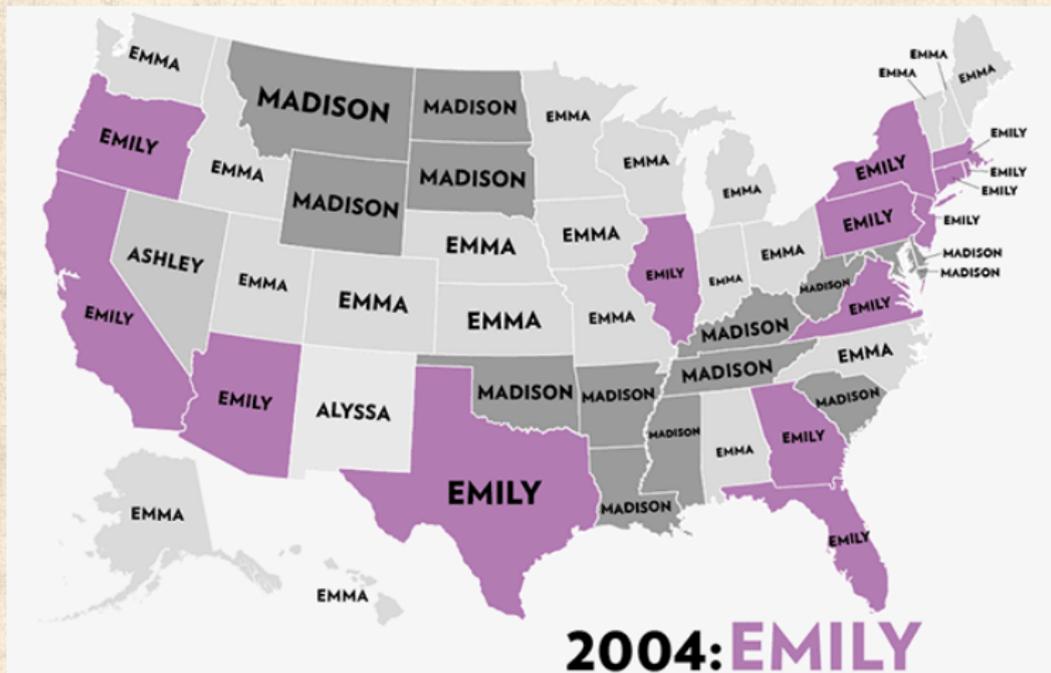
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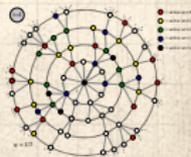
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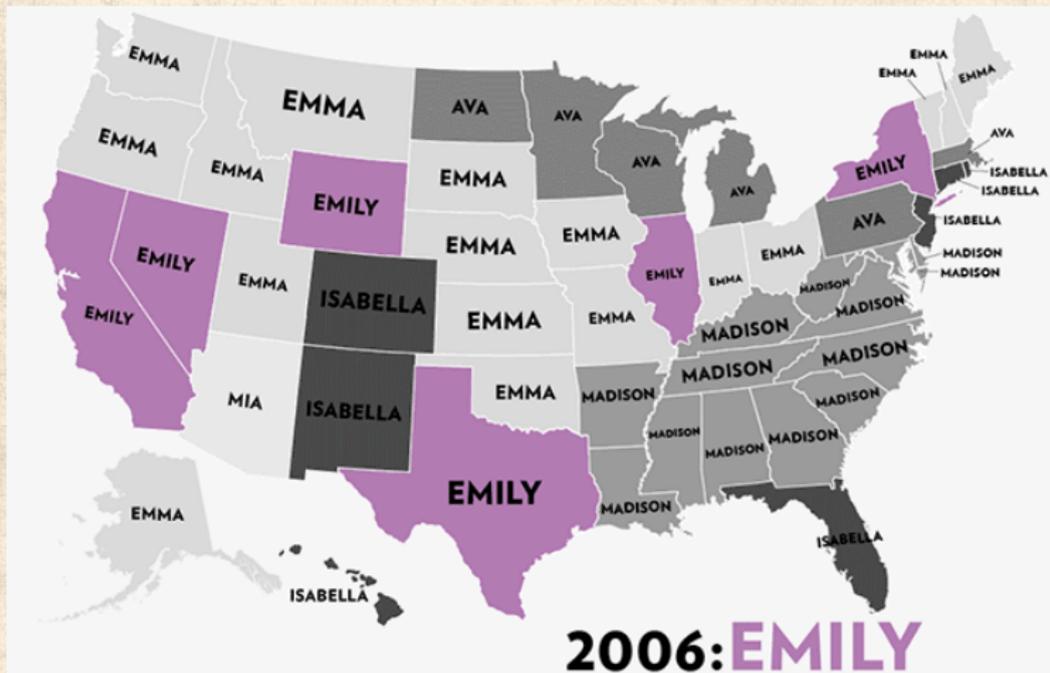




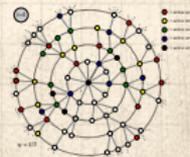
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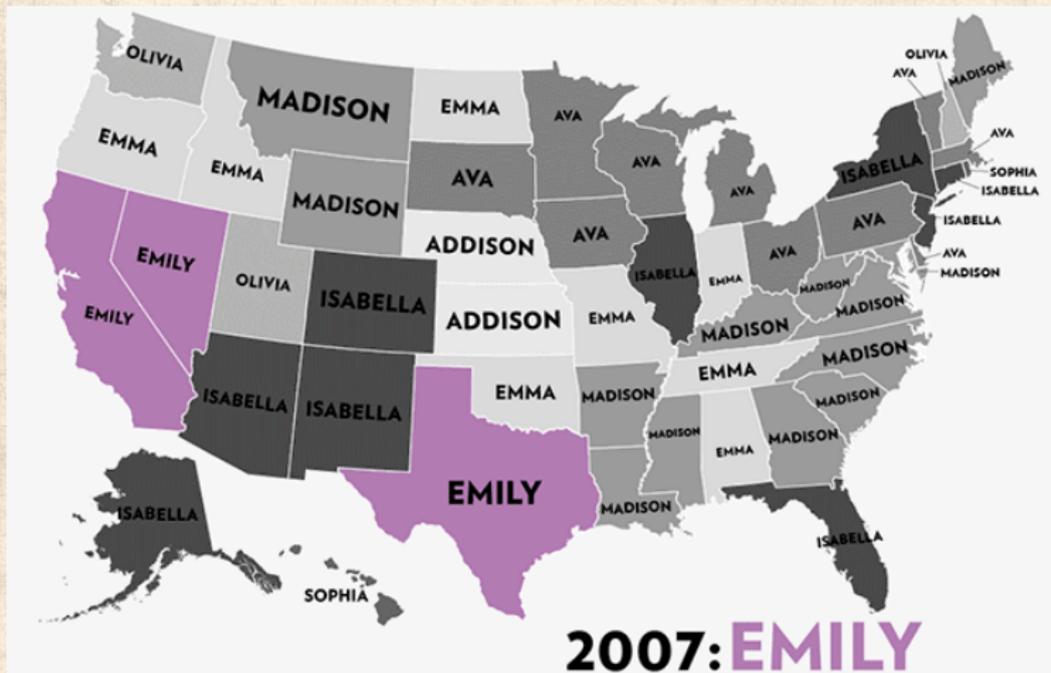
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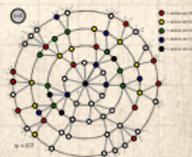
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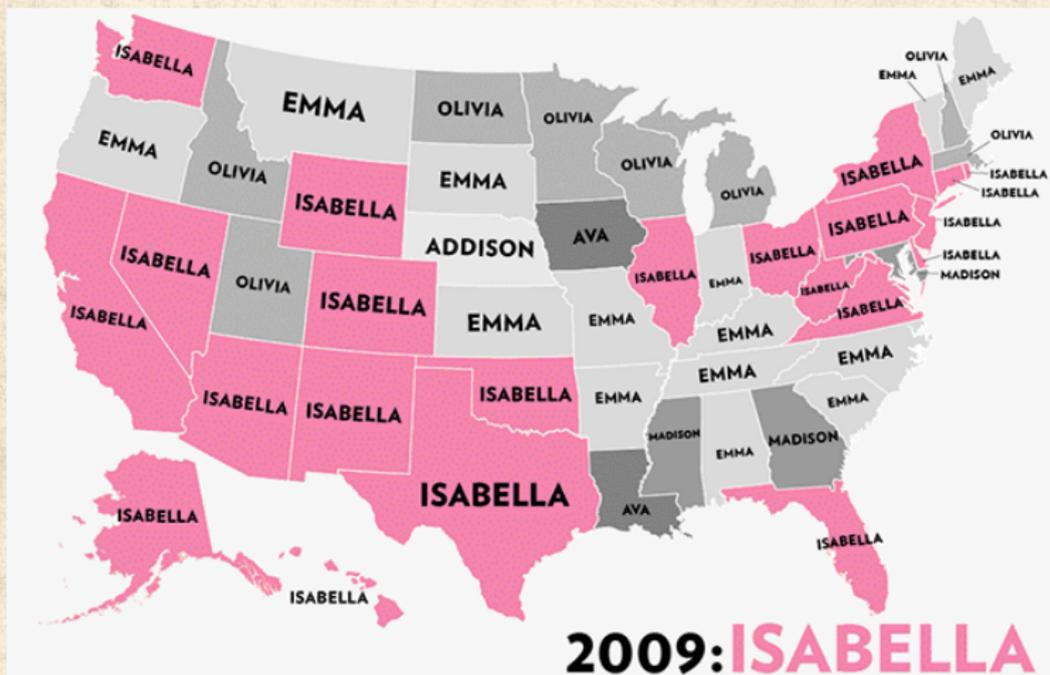




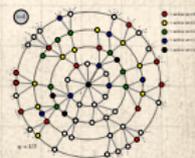
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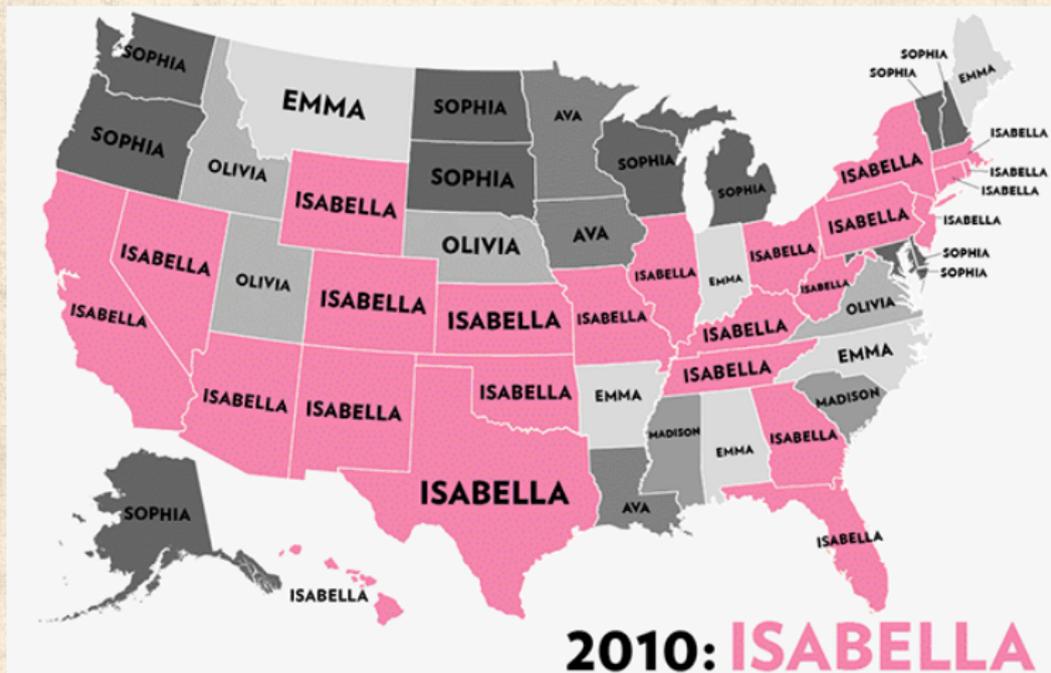
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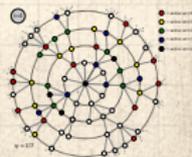
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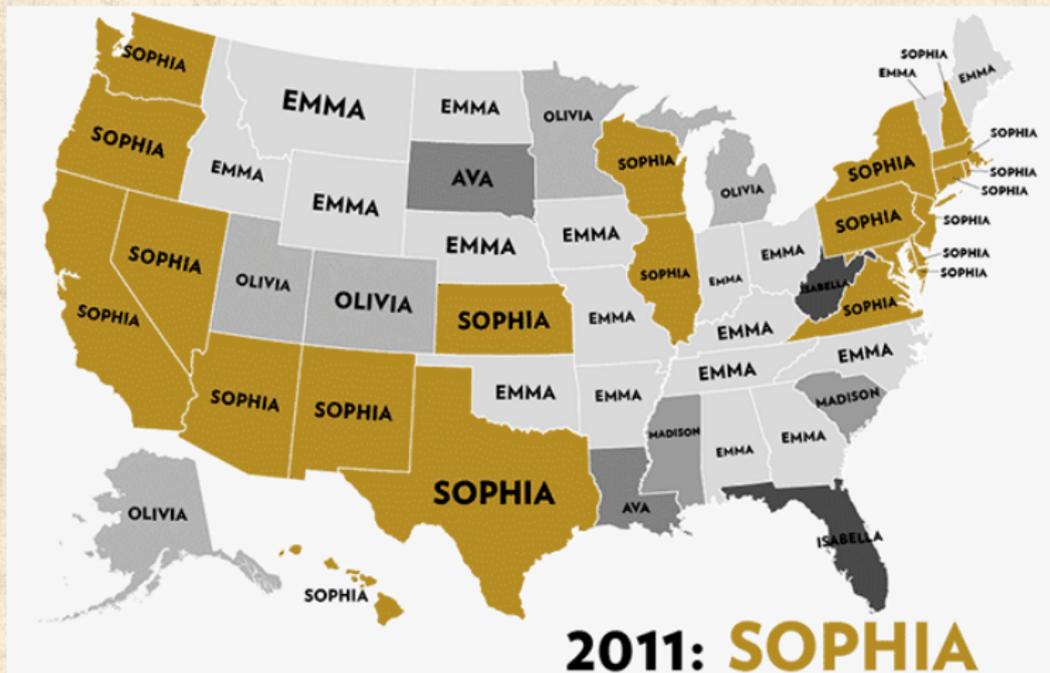
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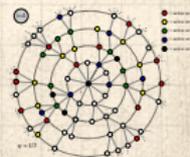
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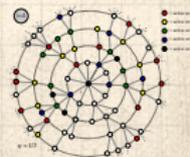
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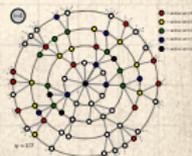


# Richard Feynmann on the Social Sciences:

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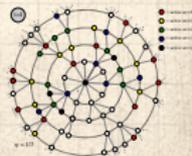


# Sheldon Cooper on the Social Sciences:

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# Things that spread well:

[buzzfeed.com](http://buzzfeed.com) 



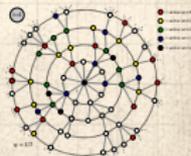
 Dangerously self aware: [11 Elements that make a perfect viral video.](#) 

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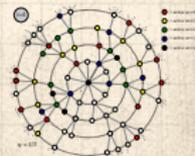
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[buzzfeed.com](http://buzzfeed.com) 



 Dangerously self aware: [11 Elements that make a perfect viral video.](#) 

+ News ...



LOL + cute + fail + wtf:

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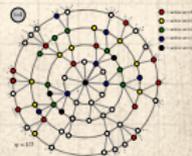
References

# Oopsie!



**BUZZFEED FELL DOWN AND WENT BOOM.**

Please try reloading this page. If the problem persists [let us know](#).



# The whole lolcats thing:

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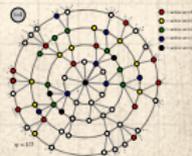
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:-p



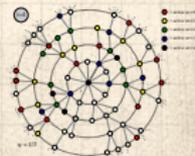
# Some things really stick:

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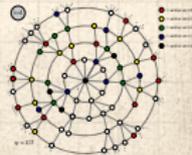
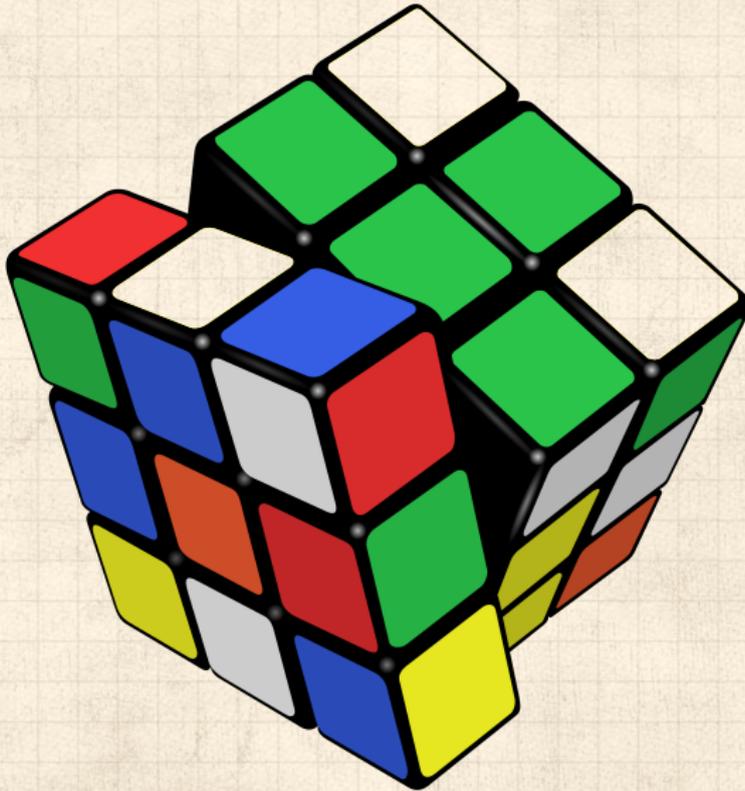
wtf + geeky + omg:

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## Social Contagion Models

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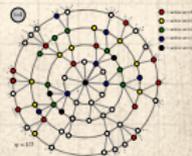
Final size

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## References



# Why social contagion works so well:

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Granovetter's model

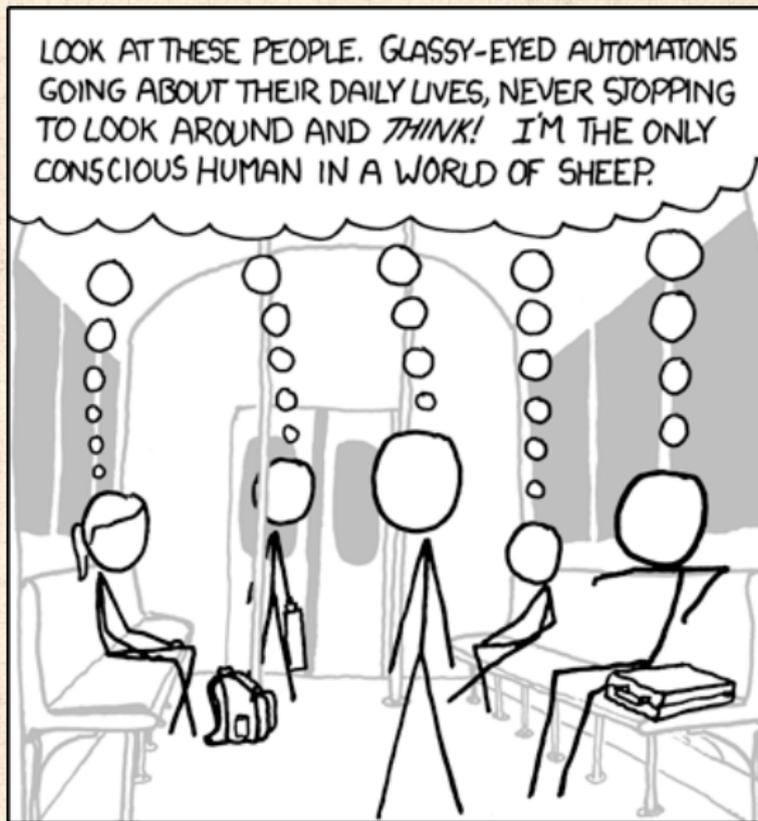
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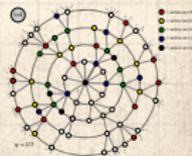
Spreading success

Groups

References



<http://xkcd.com/610/>



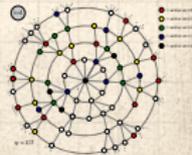
# Social Contagion

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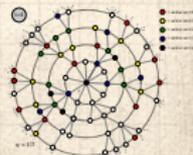
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# Social Contagion

Examples are claimed to abound:

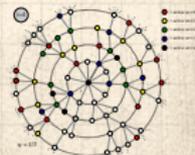
-  Fashion
-  Striking
-  smoking  [7]
-  Residential segregation [23]
-  iPhones and iThings
-  obesity  [6]
-  Stupidity
-  Harry Potter
-  voting
-  gossip
-  Rubik's cube 
-  religious beliefs
-  school shootings



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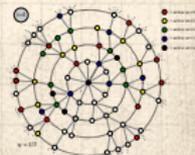
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-  school shootings
-  yawning 
-  **leaving lectures**



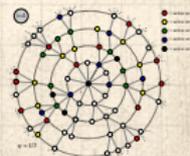
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SIR and SIRS type contagion possible

 Classes of behavior versus specific behavior



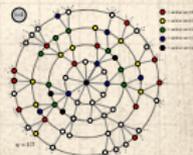
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-  Rubik's cube 
-  religious beliefs
-  school shootings
-  yawning 
-  **leaving lectures**

SIR and SIRS type contagion possible

-  Classes of behavior versus specific behavior :  
**dieting, horror movies, getting married, invading countries, ...**



# Mixed messages: Please copy, but also, don't copy ...

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## Background

Granovetter's model

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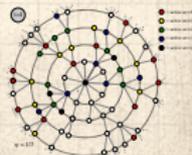
Final size

Spreading success

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References

<https://www.youtube.com/watch?v=TgDxWNV4wWY?rel=0>



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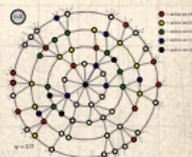
Groups

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<https://www.youtube.com/watch?v=TgDxWNV4wWY?rel=0>



Cindy Harrell appeared in the (terrifying) music video for Ray Parker Jr.'s Ghostbusters.



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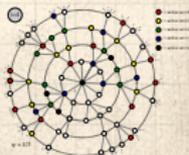
Groups

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<https://www.youtube.com/watch?v=TgDxWNV4wWY?rel=0>

 [Cindy Harrell appeared](#) in the (terrifying) music video for Ray Parker Jr.'s [Ghostbusters](#).

 In [Stranger Things 2](#), Steve Harrington reveals his Fabergé secret.



# Market much?

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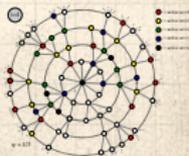
Groups

## References

<https://www.youtube.com/watch?v=FEaCflp9qR4?rel=0>



Advertisement enjoyed during "Herstory of  
Dance" , Community S4E08, April 2013.



# Framingham heart study:

## Evolving network stories (Christakis and Fowler):

 The spread of quitting smoking  [7]

 The spread of spreading  [6]

Background

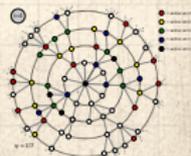
Granovetter's model

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Groups



# Framingham heart study:

## Evolving network stories (Christakis and Fowler):

 The spread of quitting smoking  <sup>[7]</sup>

 The spread of spreading  <sup>[6]</sup>

 Also: happiness  <sup>[11]</sup>, loneliness, ...

## Social Contagion Models

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Granovetter's model

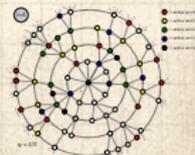
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# Framingham heart study:

## Evolving network stories (Christakis and Fowler):

-  The spread of quitting smoking  <sup>[7]</sup>
-  The spread of spreading  <sup>[6]</sup>
-  Also: happiness  <sup>[11]</sup>, loneliness, ...
-  The book: Connected: The Surprising Power of Our Social Networks and How They Shape Our Lives 

## Social Contagion Models

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Granovetter's model

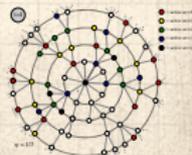
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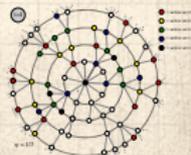
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## Controversy:

-  Are your friends making you fat?  (Clive Thomson, NY Times, September 10, 2009).



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## Evolving network stories (Christakis and Fowler):

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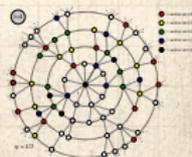
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-  Are your friends making you fat?  (Clive Thomson, NY Times, September 10, 2009).
-  Everything is contagious  —Doubts about the social plague stir in the human superorganism (Dave Johns, Slate, April 8, 2010).



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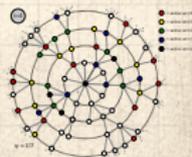
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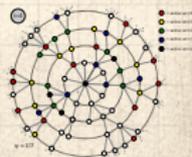
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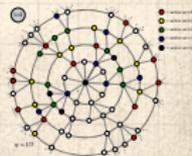
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We need to understand influence

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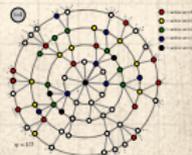
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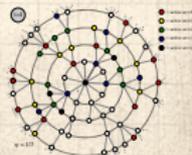
## Two focuses for us

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 Who influences whom?



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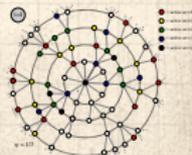
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 Who influences whom? Very hard to measure...



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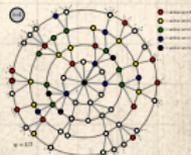
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- Who influences whom? Very hard to measure...
- What kinds of influence response functions are there?



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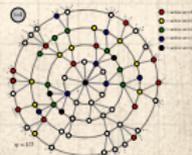
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- Are some individuals super influencers?



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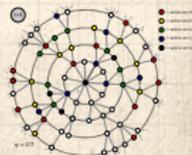
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Highly popularized by Gladwell<sup>[12]</sup> as 'connectors'



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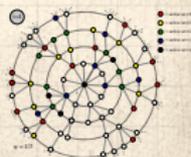
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- Who influences whom? Very hard to measure...
- What kinds of influence response functions are there?
- Are some individuals super influencers?  
Highly popularized by Gladwell<sup>[12]</sup> as 'connectors'
- The infectious idea of opinion leaders (Katz and Lazarsfeld)<sup>[19]</sup>



# The hypodermic model of influence

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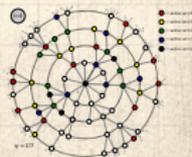
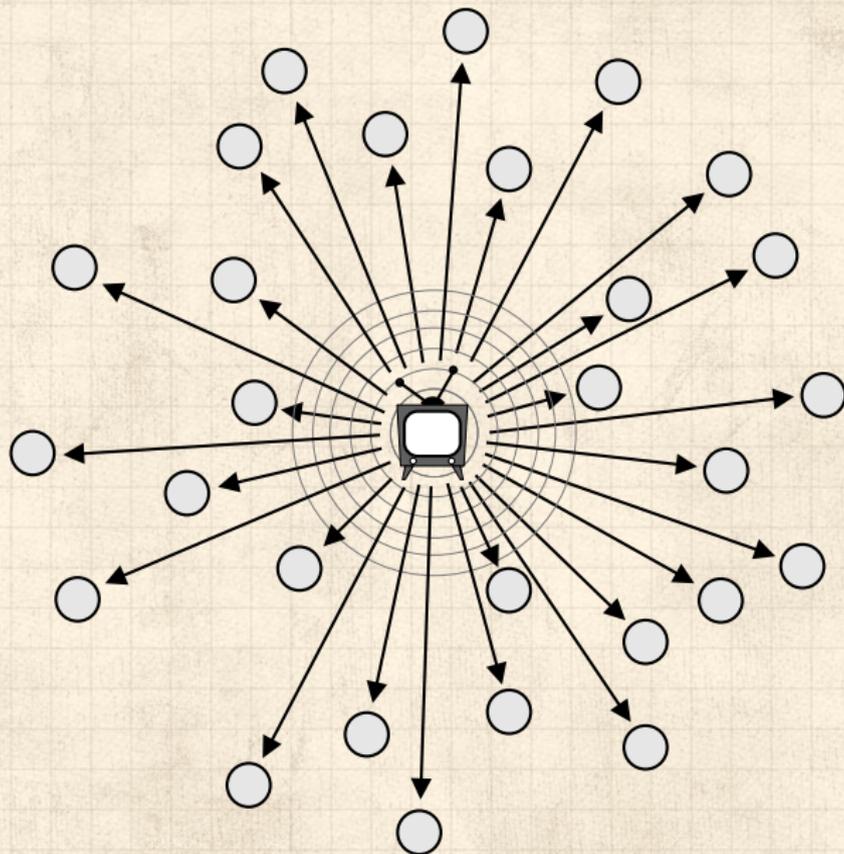
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# The two step model of influence <sup>[19]</sup>

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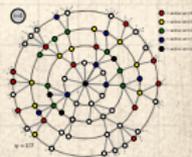
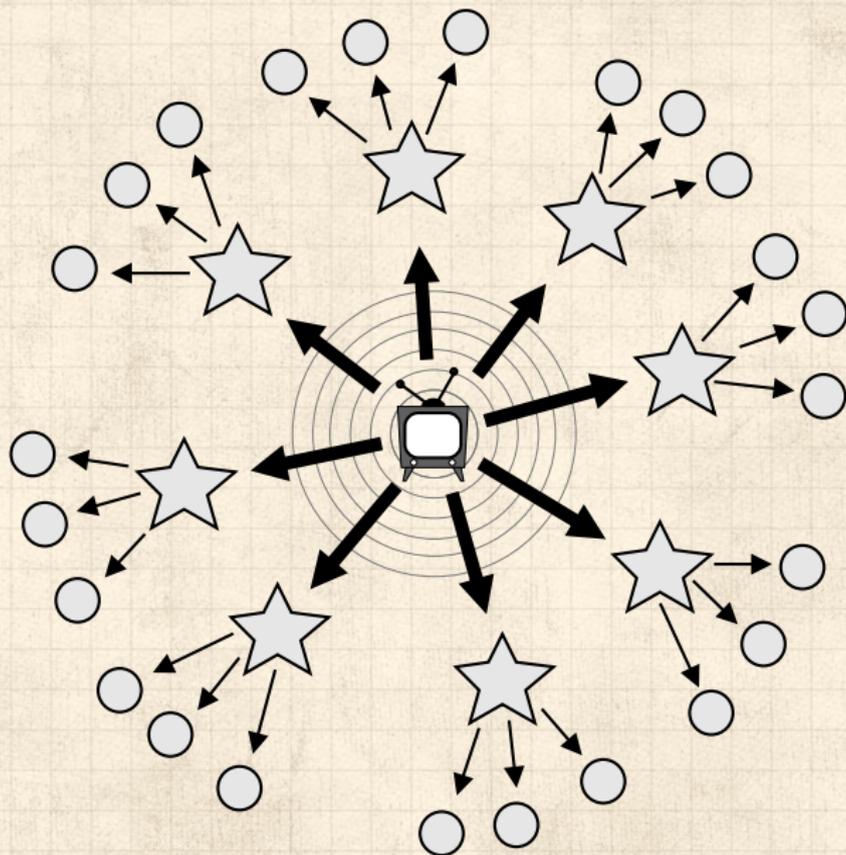
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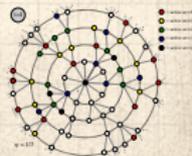
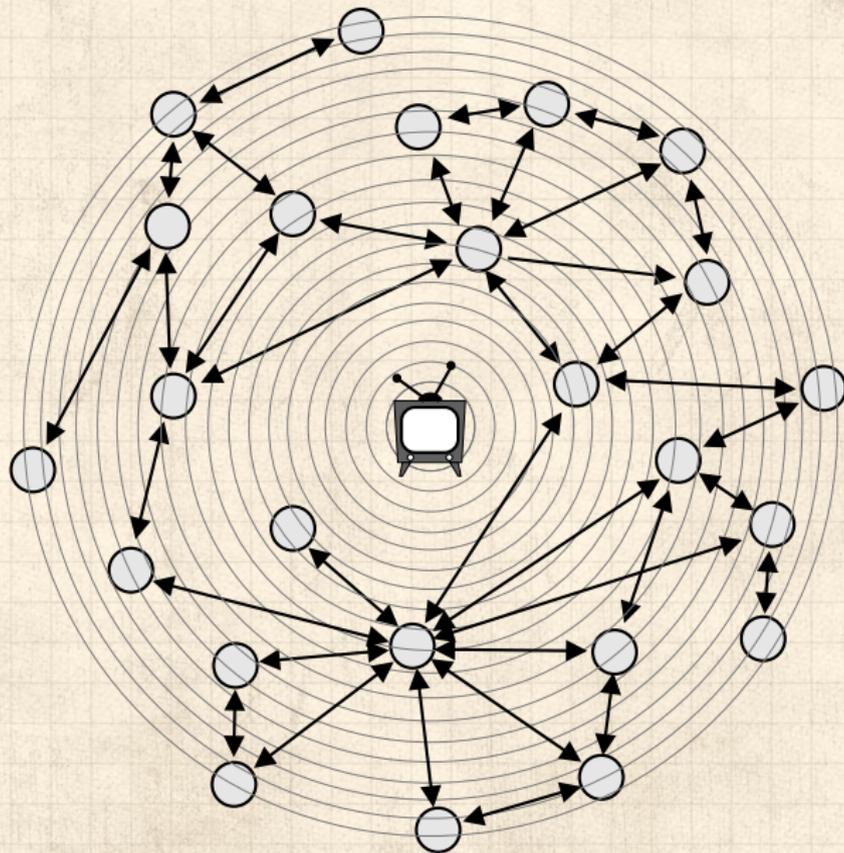
# The general model of influence: the Social Wild

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## Talking about the social wild:

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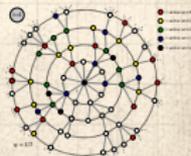
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# Why do things spread socially?

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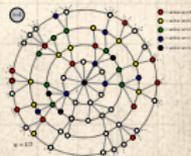
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# Why do things spread socially?

 Because of properties of special individuals?

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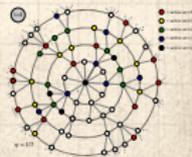
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# Why do things spread socially?

 Because of properties of special individuals?

 Or system level properties?

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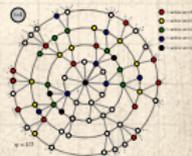
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- Because of properties of special individuals?
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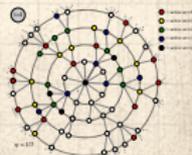
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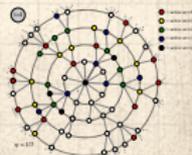
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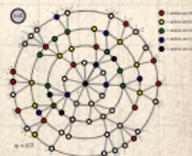
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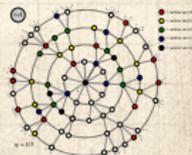
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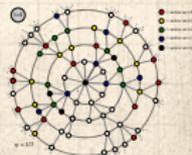
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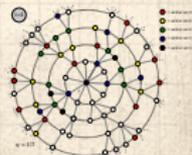
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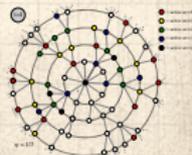
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- System/group dynamics harder to understand because most of our stories are built around individuals.
- Always good to examine what is said before and after the fact ...



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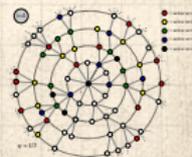
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“Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon



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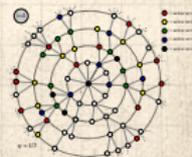
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 “Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon

 Not the world's greatest painting from the start...



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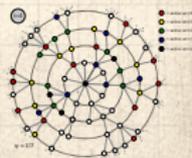
References



🧱 “Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon

🧱 Not the world’s greatest painting from the start...

🧱 Escalation through theft, vandalism,



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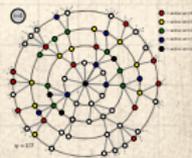
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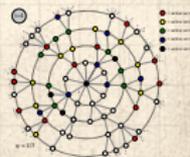
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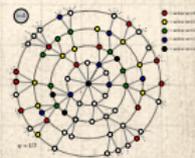
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# 'Tattooed Guy' Was Pivotal in Armstrong Case

[nytimes] 



"... LeGrande's doping sparked a series of events  
..."

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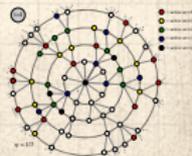
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# The completely unpredicted fall of Eastern Europe:



Timunr Kuran: <sup>[20, 21]</sup> "Now Out of Never: The Element of Surprise in the East European Revolution of 1989"

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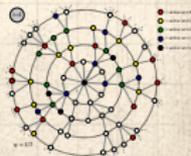
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From a 2013 Believer Magazine [↗](#) interview with Maurice Sendak [↗](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

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WHERE THE WILD THINGS ARE



STORY AND PICTURES BY MAURICE SENDAK

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MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then. Everyone wanted another Tahitian book, a beach book. But then he kept writing deeper and deeper and then came Moby-Dick and people hated it. The only ones who liked it were Mr. and Mrs. Nathaniel Hawthorne.

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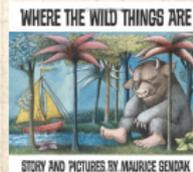
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 Sendak named his dog Herman.

 The essential Colbert interview: [Pt. 1](#) [↗](#) and [Pt. 2](#) [↗](#).



# Drafting success in the NFL: ↗

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### Top Players by Round, 1995-2012



1ST ROUND  
**Peyton Manning**  
1ST OVER ALL, 1998



2ND ROUND  
**Drew Brees**  
32ND PICK, 2001



3RD ROUND  
**Terrell Owens**  
89TH PICK, 1996



4TH ROUND  
**Jared Allen**  
126TH PICK, 2004



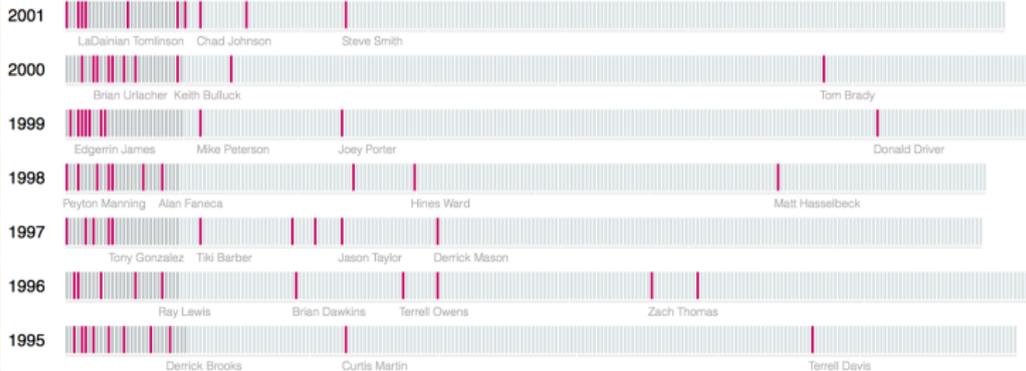
5TH ROUND  
**Zach Thomas**  
154TH PICK, 1996



6TH ROUND  
**Tom Brady**  
199TH PICK, 2000



7TH ROUND  
**Donald Driver**  
213TH PICK, 1999



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## Messing with social connections

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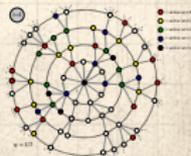
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# Social Contagion

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## Messaging with social connections

 Ads based on message content

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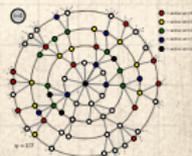
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## Messaging with social connections

- 📦 Ads based on message content  
(e.g., Google and email)

### Social Contagion Models

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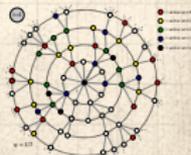
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## Messing with social connections

 Ads based on message content  
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 BzzAgent 

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-  Generally: BzzAgents did not reveal their BzzAgent status and did not want to be paid.
-  NYT, 2004-12-05: "The Hidden (in Plain Sight) Persuaders" 

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### Background

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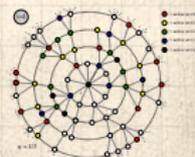
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 One of Facebook's early advertising attempts:  
Beacon 

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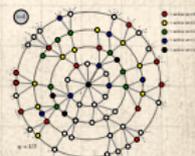
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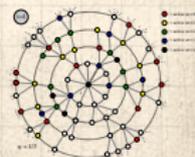
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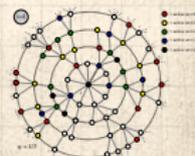
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- 📦 One of Facebook's early advertising attempts: Beacon 
- 📦 All of Facebook's advertising attempts.
- 📦 Seriously, Facebook. What could go wrong?

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# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by Robert Cialdini 

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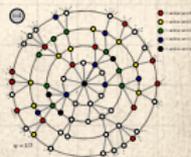
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Six modes of influence:

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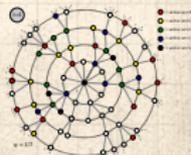
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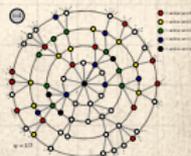
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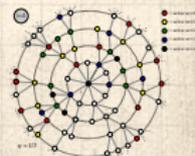
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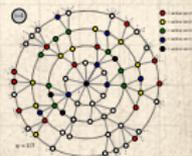
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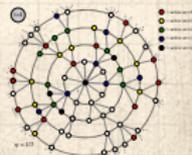
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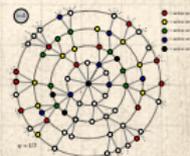
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6. **Scarcity**: *The Rule of the Few*; e.g., Prohibition.

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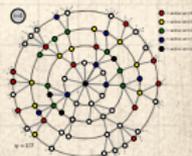
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## Social proof:

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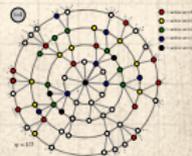
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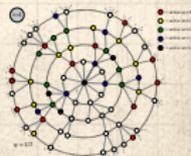
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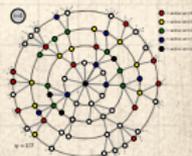
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Cialdini's modes are heuristics that help up us get through life.



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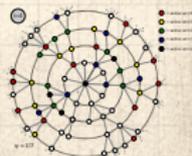
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 Useful but can be leveraged...



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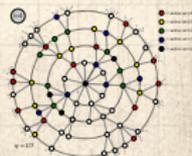
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Other acts of influence:



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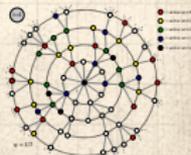
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Other acts of influence:

 Conspicuous Consumption (Veblen, 1912)



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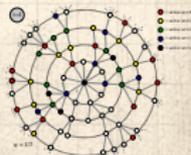
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Other acts of influence:

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 Conspicuous Destruction (Potlatch)





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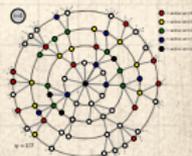
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Some important models:

 Tipping models—Schelling (1971) [23, 24, 25]



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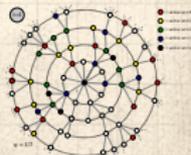
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 Simulation on checker boards



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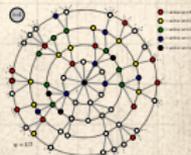
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-  Idea of thresholds



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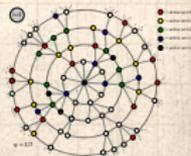
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-  Idea of thresholds
-  Polygon-themed online visualization. (Includes optional diversity-seeking proclivity.) 



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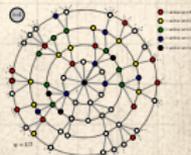
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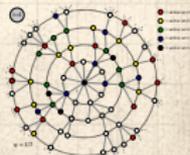
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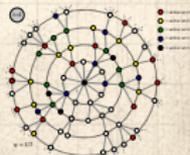
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-  Threshold models—Granovetter (1978) [15]
-  Herding models—Bikhchandani, Hirschleifer, Welch (1992) [2, 3]
  -  Social learning theory, Informational cascades,...



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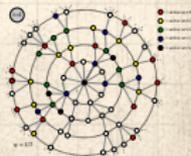
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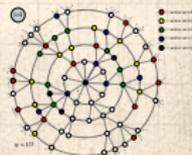
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## Thresholds



Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted



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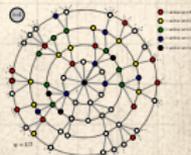
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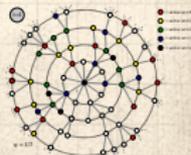
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# Social contagion models

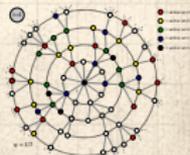
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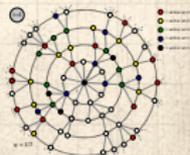
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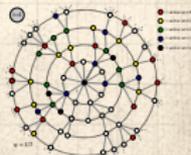
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- Individual thresholds can vary
- Assumption: order of others' adoption does not matter...



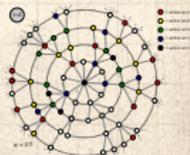
## Thresholds

- Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted
- 'Others' may be everyone in a population, an individual's close friends, any reference group.
- Response can be probabilistic or deterministic.
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- Assumption: order of others' adoption does not matter... **(unrealistic)**.



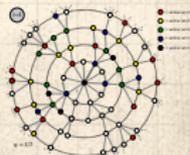
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Some possible origins of thresholds:

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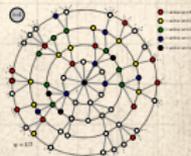
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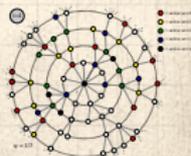
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Some possible origins of thresholds:

-  Inherent, evolution-devised inclination to coordinate, to conform, to imitate. [1]



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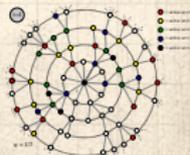
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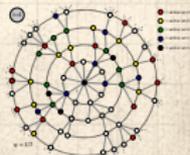
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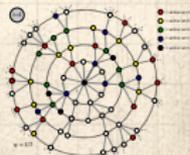
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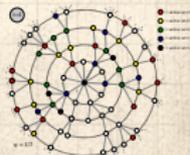
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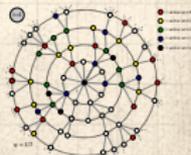
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-  Economics: **Network effects** or **network externalities**
  -  Externalities = Effects on others not directly involved in a transaction
  -  Examples: telephones, fax machine, TikTok, operating systems
  -  An individual's utility increases with the adoption level among peers and the population in general



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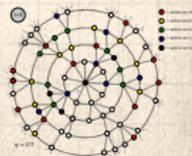
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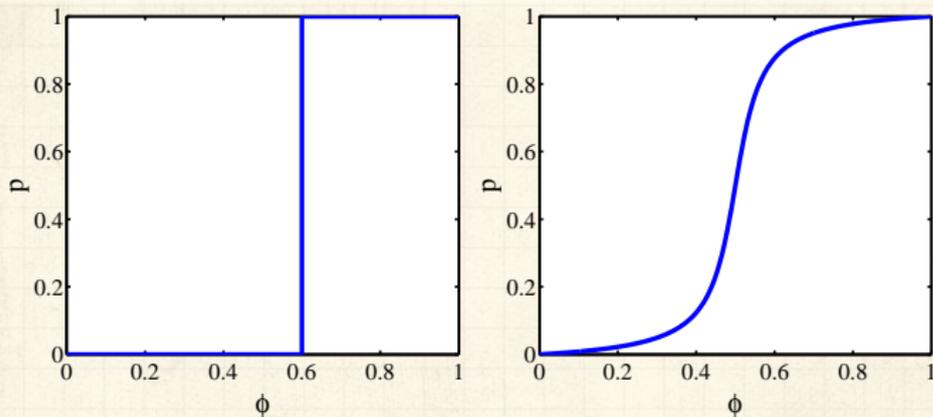


# Threshold models—response functions

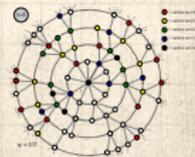
## Social Contagion Models

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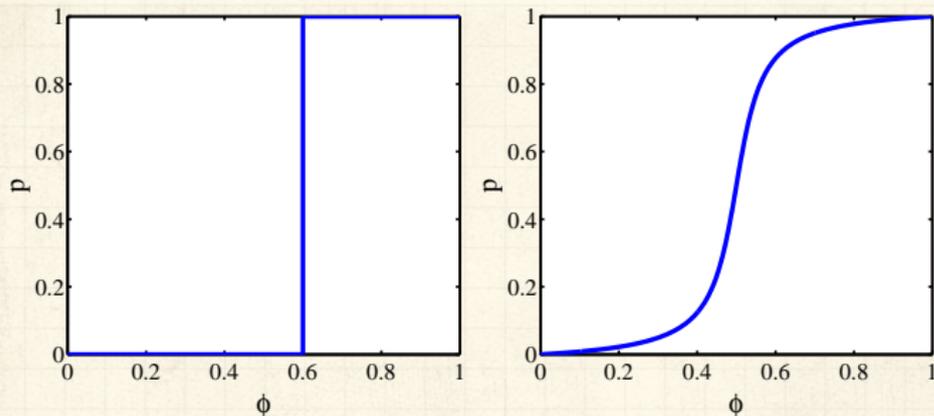
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 Example threshold influence response functions:  
**deterministic** and **stochastic**

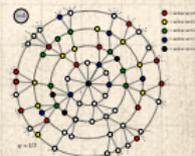


# Threshold models—response functions

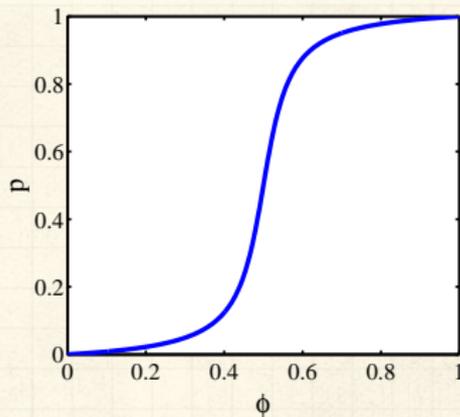
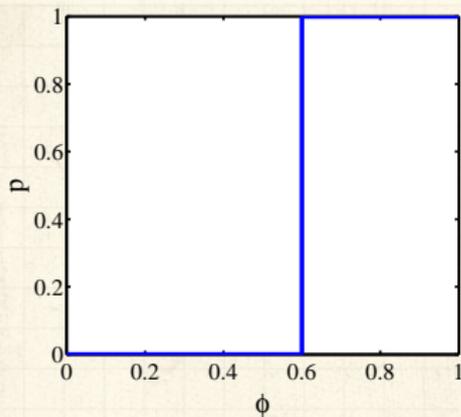


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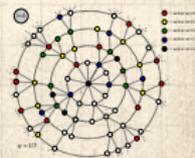
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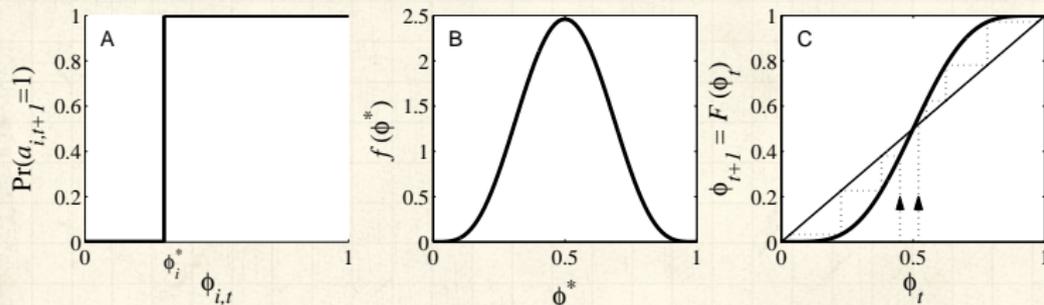
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 Two states: S and I.



# Threshold models

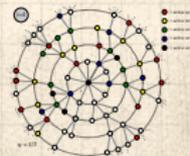
Action based on perceived behavior of others:



Two states: S and I.

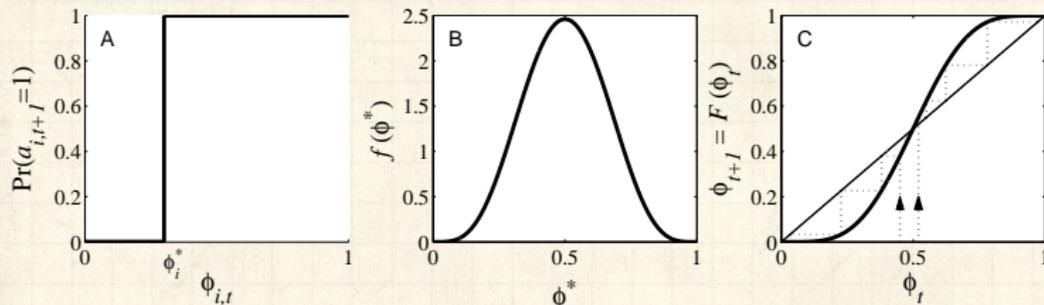


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# Threshold models

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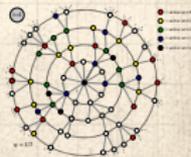
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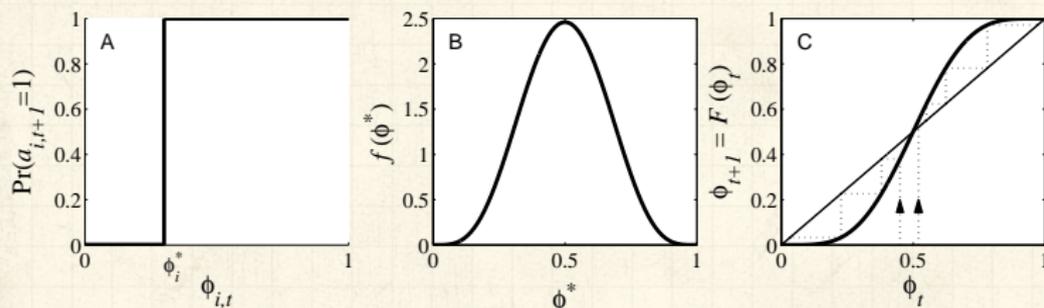


Discrete time update (strong assumption!)



# Threshold models

Action based on perceived behavior of others:



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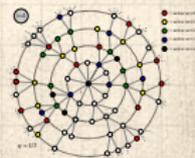
$\phi$  = fraction of contacts 'on' (e.g., rioting)



Discrete time update (strong assumption!)



This is a **Critical mass model**



# Threshold models

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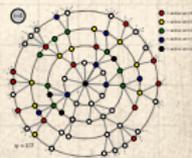
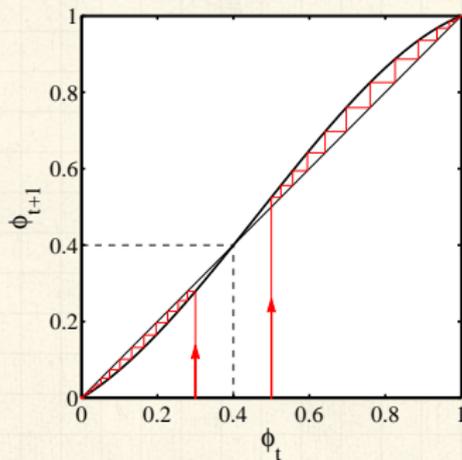
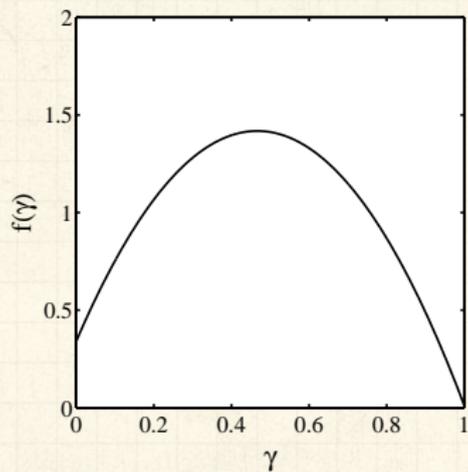
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Another example of critical mass model:



# Threshold models

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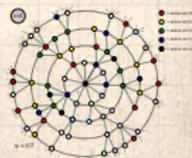
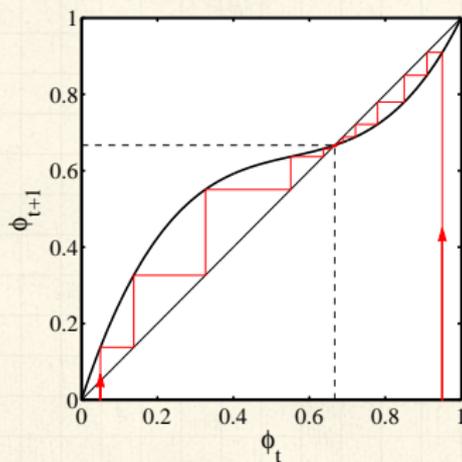
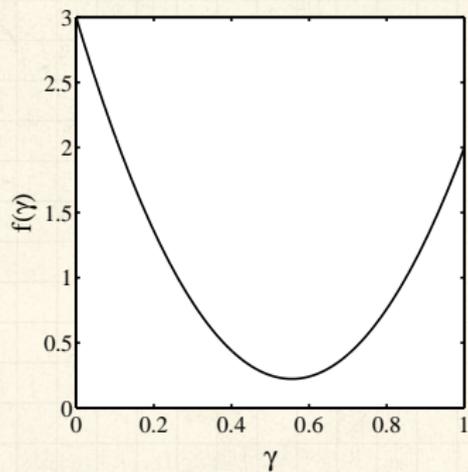
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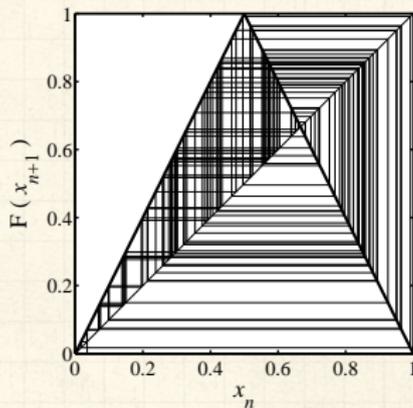
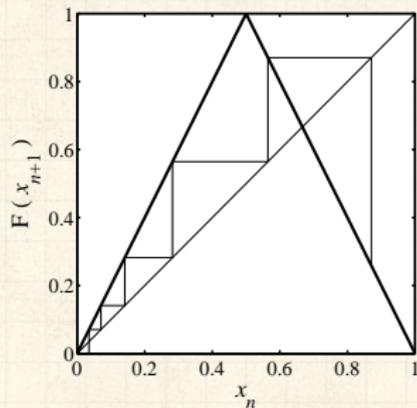
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Example of single stable state model:



## Chaotic behavior possible [17, 16, 9, 18]



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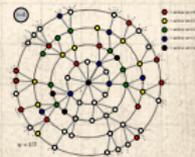
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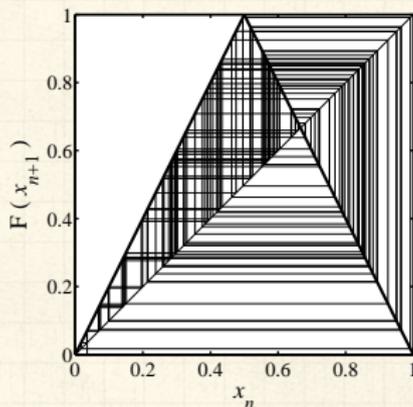
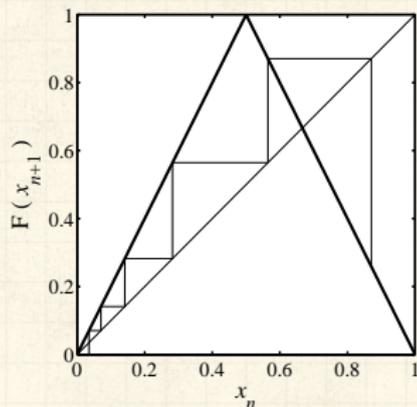
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Chaotic behavior possible [17, 16, 9, 18]



Period doubling arises as map amplitude  $r$  is increased.

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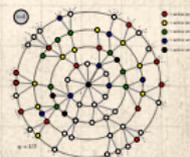
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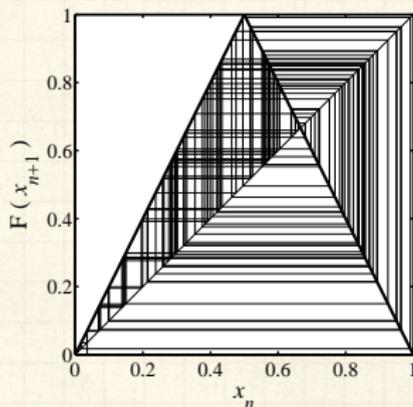
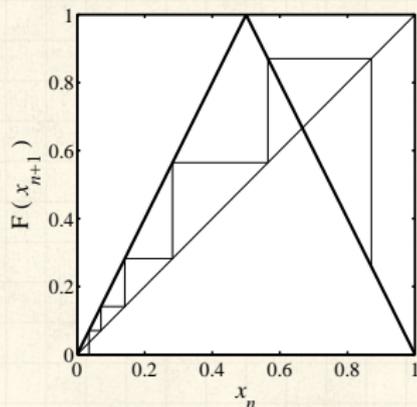
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## Chaotic behavior possible [17, 16, 9, 18]



 Period doubling arises as map amplitude  $r$  is increased.

 Synchronous update assumption is crucial

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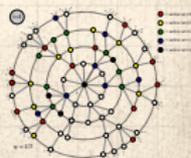
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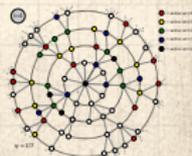
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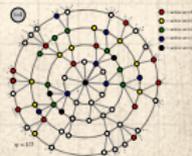
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Implications for collective action theory:



## Implications for collective action theory:

1. Collective uniformity  $\nRightarrow$  individual uniformity



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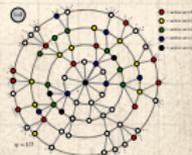
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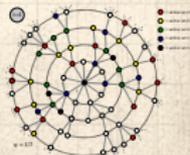
Implications for collective action theory:

1. Collective uniformity  $\nRightarrow$  individual uniformity
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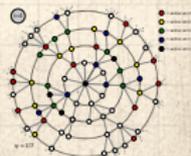
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4. System stories live in left null space of our stories—we can't even see them.



# Threshold models—Nutshell

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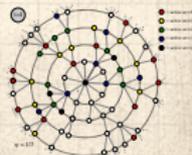
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4. System stories live in left null space of our stories—we can't even see them.
5. But we happily impose simplistic, individual-centric stories—we can't help ourselves ↗.



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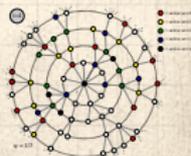
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"A simple model of global cascades on random networks"

D. J. Watts. Proc. Natl. Acad. Sci., 2002 [27]

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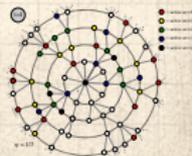
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Mean field model  $\rightarrow$  network model

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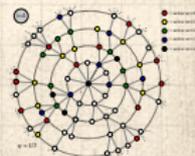
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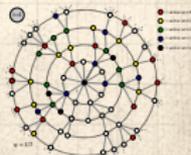
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Mean field model  $\rightarrow$  network model



Individuals now have a limited view of the world



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Mean field model → network model



Individuals now have a limited view of the world

## We'll also explore:



"Seed size strongly affects cascades on random networks" [14]

Gleeson and Cahalane, Phys. Rev. E, 2007.

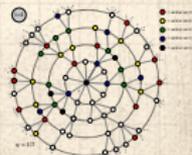


"Direct, physically motivated derivation of the contagion condition for spreading processes on generalized random networks" [10] Dodds, Harris, and Payne, Phys. Rev. E, 2011



"Influentials, Networks, and Public Opinion Formation" [28]

Watts and Dodds, J. Cons. Res., 2007.



# Threshold model on a network

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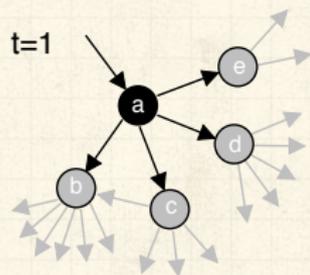
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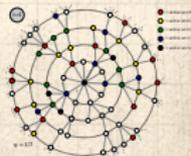
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 All nodes have threshold  $\phi = 0.2$ .



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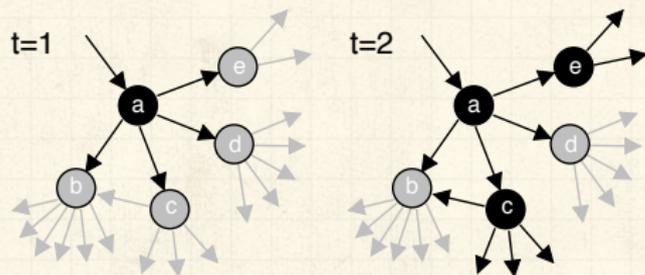
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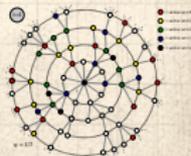
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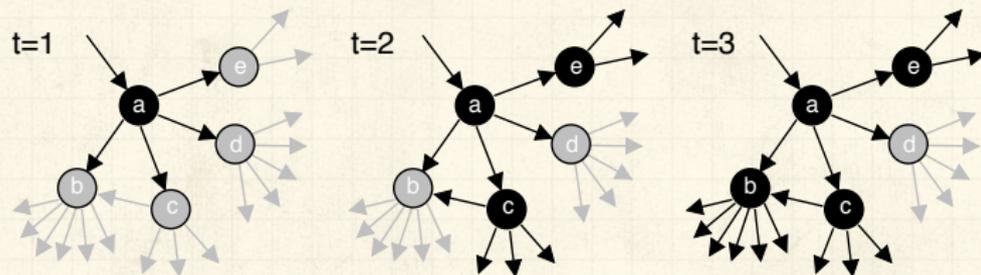
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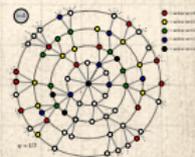
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# Threshold model on a network

 Interactions between individuals now represented by a network.

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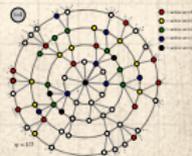
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# Threshold model on a network

 Interactions between individuals now represented by a network.

 Network is **sparse**.

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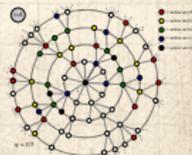
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# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.

## Social Contagion Models

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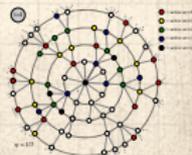
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# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.

## Social Contagion Models

Background

Granovetter's model

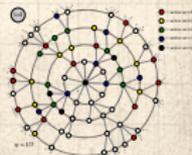
Network version

Final size

Spreading success

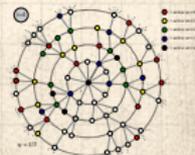
Groups

References



# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.
- Each individual  $i$  has a fixed threshold  $\phi_i$ .



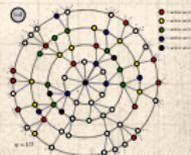
# Threshold model on a network

## Social Contagion Models

Background  
Granovetter's model  
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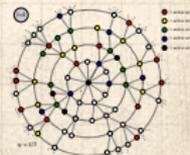
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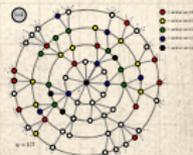
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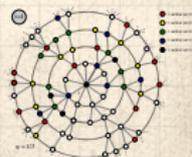
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- Individuals remain active when switched (no recovery = SI model).



# Snowballing

The PoCSverse  
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## Social Contagion Models

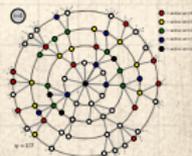
Background  
Granovetter's model

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First study random networks:



# Snowballing

## Social Contagion Models

Background  
Granovetter's model

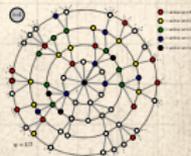
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First study random networks:

 Start with  $N$  nodes with a degree distribution  $P_k$



# Snowballing

## Social Contagion Models

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Granovetter's model

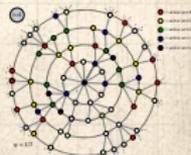
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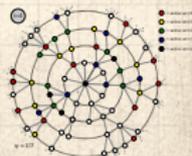
- Start with  $N$  nodes with a degree distribution  $P_k$
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# Snowballing

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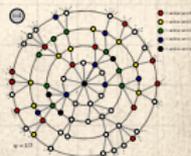
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- Aim: Figure out when activation will propagate



# Snowballing

## First study random networks:

- Start with  $N$  nodes with a degree distribution  $P_k$
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- Determine a **cascade condition**

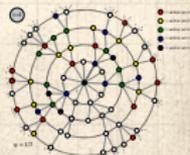


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- Start with  $N$  nodes with a degree distribution  $P_k$
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- Determine a **cascade condition**

## The Cascade Condition:

- If one individual is initially activated, what is the probability that an activation will spread over a network?



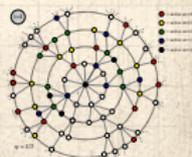
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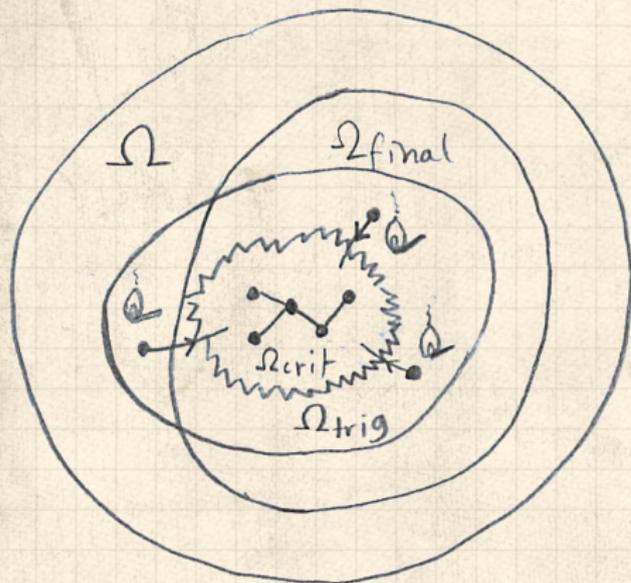
- Start with  $N$  nodes with a degree distribution  $P_k$
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- Aim: Figure out when activation will propagate
- Determine a **cascade condition**

## The Cascade Condition:

1. If one individual is initially activated, what is the probability that an activation will spread over a network?
2. What features of a network determine whether a cascade will occur or not?



# Example random network structure:



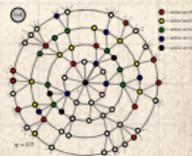
  $\Omega_{crit} = \Omega_{vuln} =$   
critical mass =  
global  
vulnerable  
component

  $\Omega_{trig} =$   
triggering  
component

  $\Omega_{final} =$   
potential  
extent of  
spread

  $\Omega =$  entire  
network

$$\Omega_{crit} \subset \Omega_{trig}; \Omega_{crit} \subset \Omega_{final}; \text{ and } \Omega_{trig}, \Omega_{final} \subset \Omega.$$



# Snowballing

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## Social Contagion Models

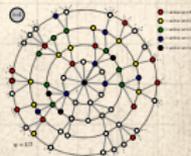
Background  
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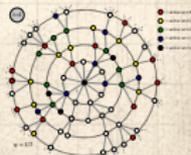
## References

Follow active links



## Follow active links

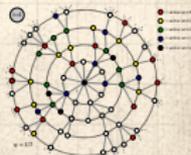
 An active link is a link connected to an activated node.



## Follow active links

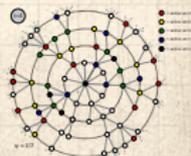
 An active link is a link connected to an activated node.

 If an infected link leads to **at least 1 more infected link**, then **activation spreads**.



## Follow active links

- ❏ An active link is a link connected to an activated node.
- ❏ If an infected link leads to **at least 1 more infected link**, then **activation spreads**.
- ❏ We need to understand which nodes can be activated when only one of their neighbors becomes active.



# The most gullible

Vulnerables:

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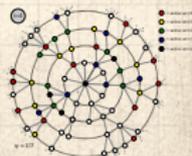
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# The most gullible

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## Vulnerables:

 We call individuals who can be activated by just one contact being active **vulnerables**

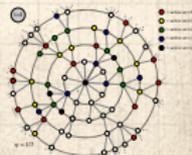
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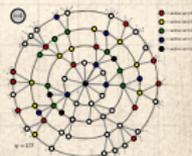
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 The vulnerability condition for node  $i$ :

$$1/k_i \geq \phi_i$$



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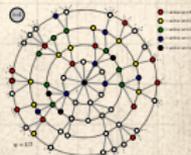
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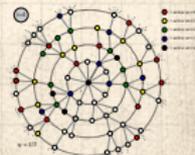
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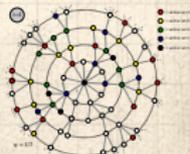
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 **Cluster of vulnerables = critical mass**



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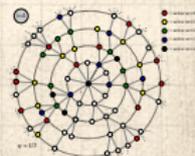
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 For global cascades on random networks, must have a *global cluster of vulnerables* <sup>[27]</sup>

 **Cluster of vulnerables = critical mass**

 Network story: 1 node  $\rightarrow$  critical mass  $\rightarrow$  everyone.



# Cascade condition

Back to following a link:

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Background

Granovetter's model

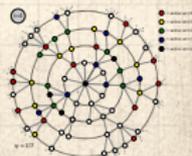
**Network version**

Final size

Spreading success

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References



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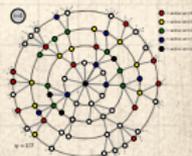
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## Social Contagion Models

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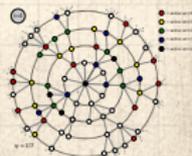
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$$\sum_{k=0}^{\infty} kP_k = \langle k \rangle$$

## Social Contagion Models

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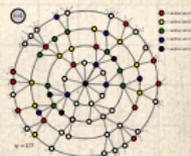
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 Normalization:

$$\sum_{k=0}^{\infty} kP_k = \langle k \rangle$$

 So

$$P(\text{linked node has degree } k) = \frac{kP_k}{\langle k \rangle}$$

## Social Contagion Models

Background

Granovetter's model

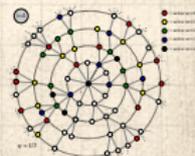
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# Cascade condition

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## Social Contagion Models

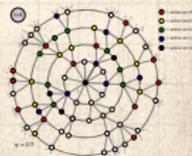
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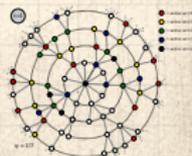
Next: Vulnerability of linked node



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 Linked node is **vulnerable** with probability

$$\beta_k = \int_{\phi'_*=0}^{1/k} f(\phi'_*) d\phi'_*$$



# Cascade condition

## Social Contagion Models

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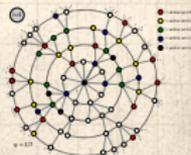
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 If linked node is **vulnerable**, it produces  $k - 1$  new outgoing active links



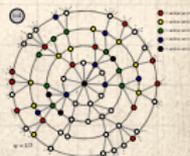
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 If linked node is **not vulnerable**, it produces **no** active links.



# Cascade condition

## Social Contagion Models

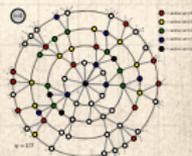
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Putting things together:

 Expected number of active edges produced by an active edge:



# Cascade condition

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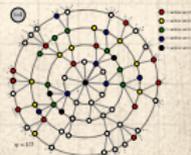
Spreading success  
Groups

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Putting things together:

 Expected number of active edges produced by an active edge:

$$R = \left[ \sum_{k=1}^{\infty} \underbrace{(k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle}}_{\text{success}} + \right]$$



# Cascade condition

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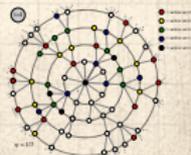
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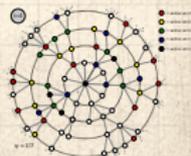


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$$= \sum_{k=1}^{\infty} (k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle}$$



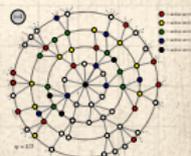
# Cascade condition

So... for random networks with fixed degree distributions, cascades take off when:

$$\sum_{k=1}^{\infty} (k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

  $\beta_k$  = probability a degree  $k$  node is vulnerable.

  $P_k$  = probability a node has degree  $k$ .



# Cascade condition

Two special cases:

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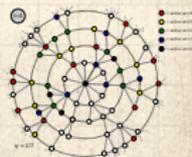
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# Cascade condition

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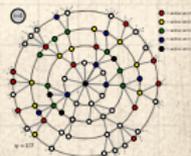
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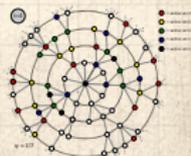
 (1) Simple disease-like spreading succeeds:  $\beta_k = \beta$



Two special cases:

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# Cascade condition

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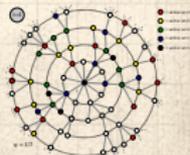
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Two special cases:

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$$\beta \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

 (2) Giant component exists:  $\beta = 1$



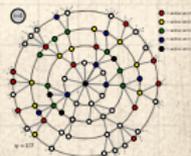
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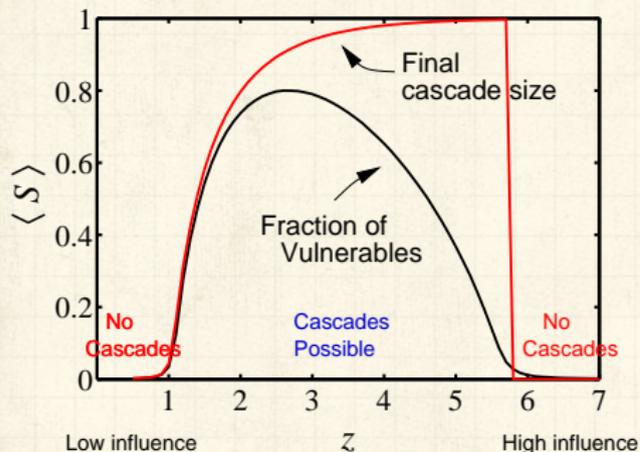
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🧱 (2) Giant component exists:  $\beta = 1$

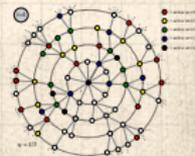
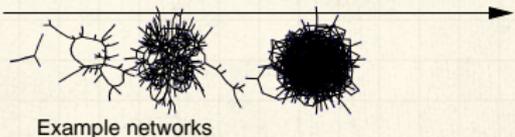
$$1 \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$



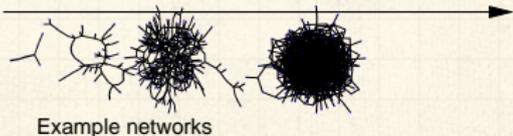
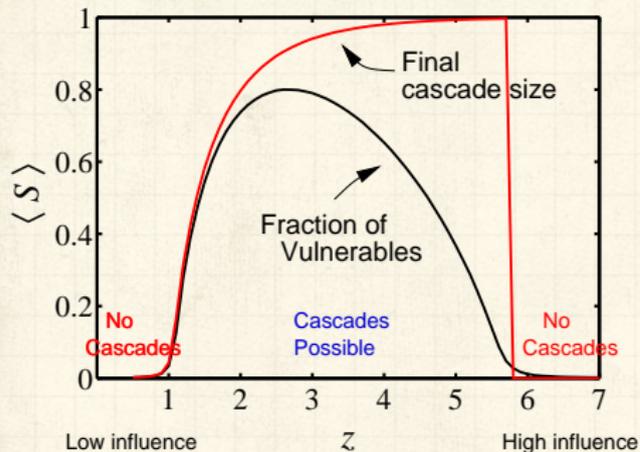
# Cascades on random networks



Cascades occur only if size of max vulnerable cluster  $> 0$ .



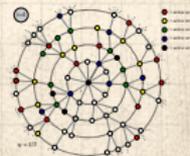
# Cascades on random networks



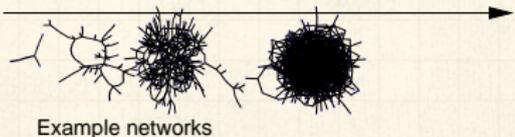
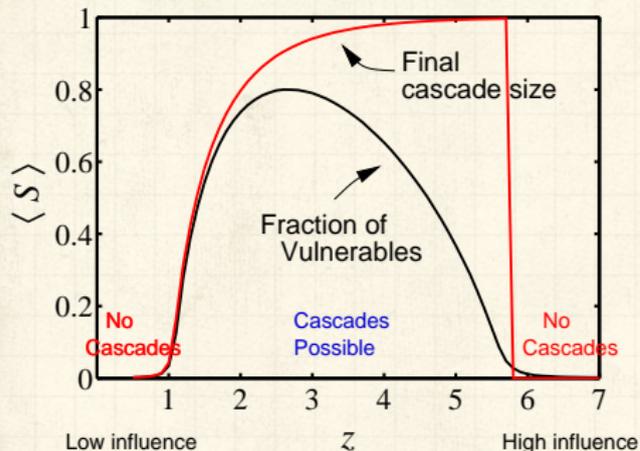
Cascades occur only if size of max vulnerable cluster  $> 0$ .



System may be 'robust-yet-fragile'.



# Cascades on random networks



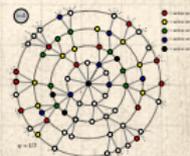
Cascades occur only if size of max vulnerable cluster  $> 0$ .



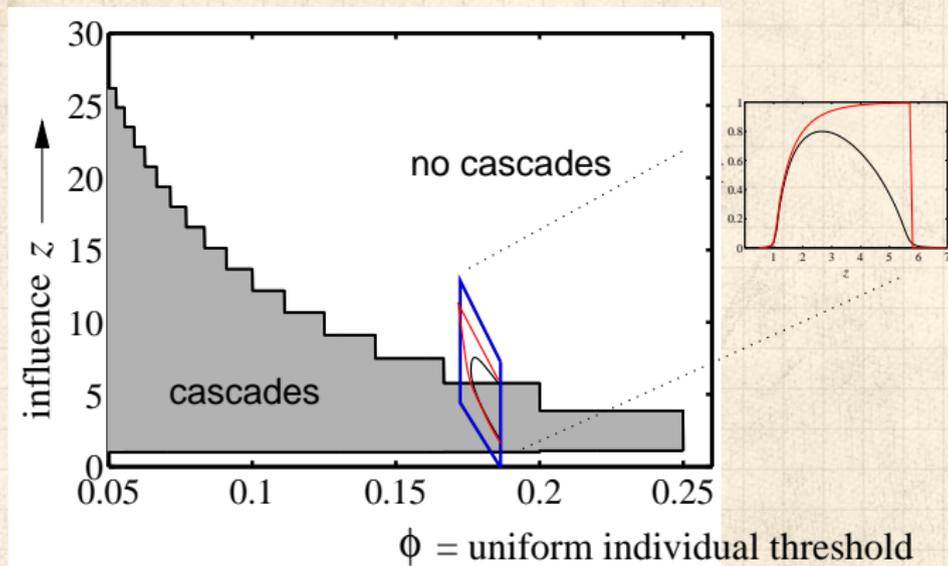
System may be 'robust-yet-fragile'.



'Ignorance' facilitates spreading.

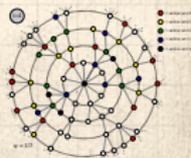


# Cascade window for random networks

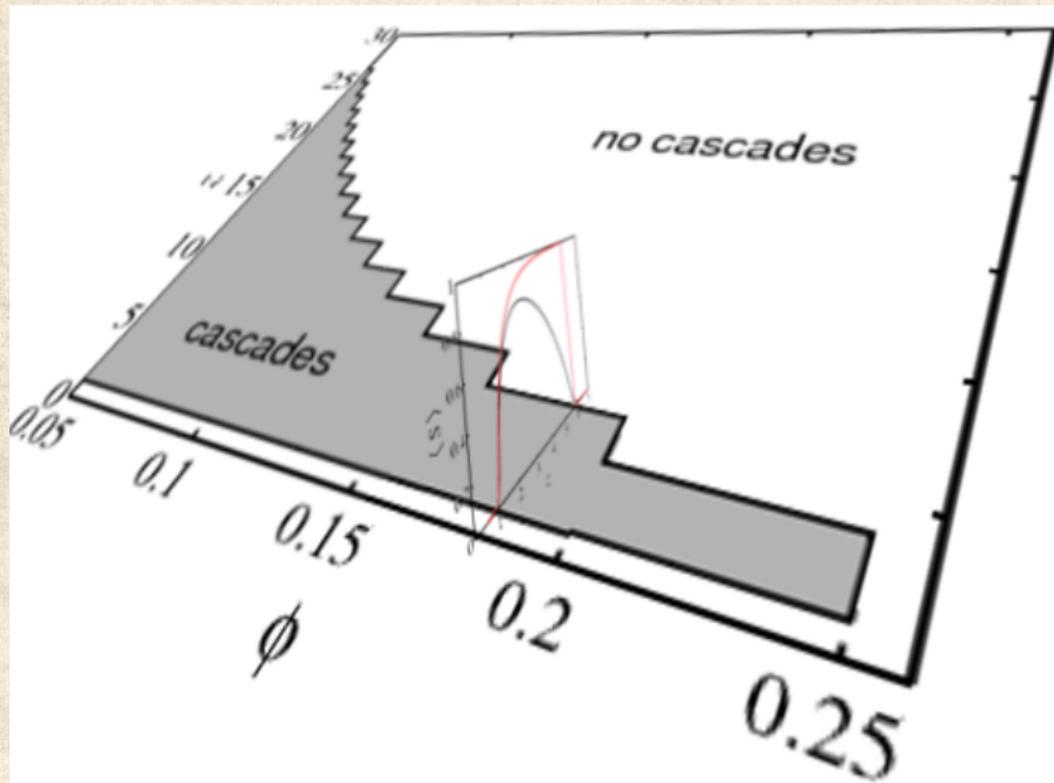


 'Cascade window' widens as threshold  $\phi$  decreases.

 Lower thresholds enable spreading.



# Cascade window for random networks



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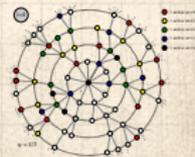
Social Contagion  
Models

Background  
Granovetter's model

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Spreading success  
Groups

References



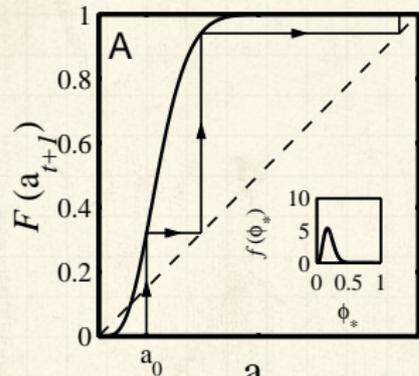
# All-to-all versus random networks

## Social Contagion Models

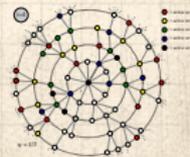
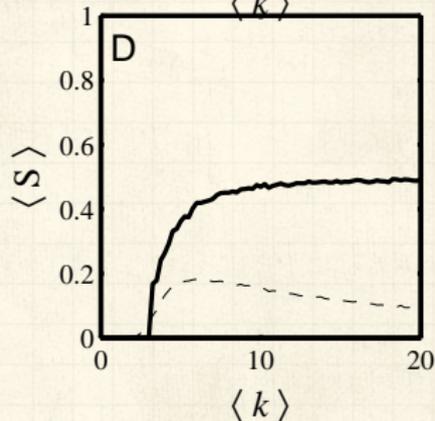
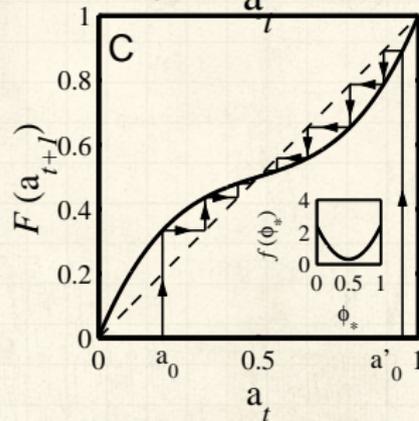
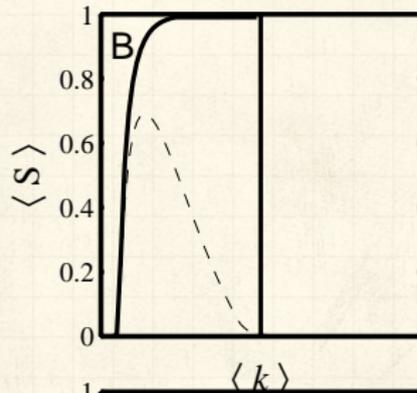
- Background
- Granovetter's model
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- Final size
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all-to-all networks



random networks



# Cascade window—summary

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Granovetter's model

**Network version**

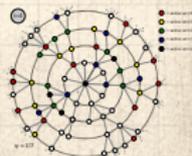
Final size

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## References

For our simple model of a uniform threshold:



# Cascade window—summary

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Background  
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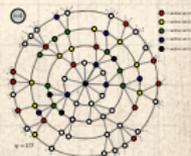
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For our simple model of a uniform threshold:

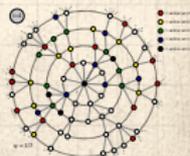
1. **Low  $\langle k \rangle$ :** No cascades in poorly connected networks.  
No global clusters of any kind.



# Cascade window—summary

For our simple model of a uniform threshold:

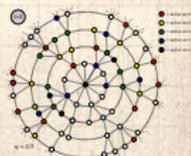
1. **Low  $\langle k \rangle$ :** No cascades in poorly connected networks.  
No global clusters of any kind.
2. **High  $\langle k \rangle$ :** Giant component exists but not enough vulnerables.



# Cascade window—summary

For our simple model of a uniform threshold:

1. **Low  $\langle k \rangle$ :** No cascades in poorly connected networks.  
No global clusters of any kind.
2. **High  $\langle k \rangle$ :** Giant component exists but not enough vulnerables.
3. **Intermediate  $\langle k \rangle$ :** Global cluster of vulnerables exists.  
Cascades are possible in **"Cascade window."**



# Outline

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## Social Contagion Models

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Granovetter's model

Network version

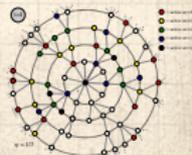
Final size

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## References



# Threshold contagion on random networks

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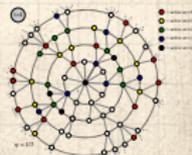
## Social Contagion Models

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**Next:** Find expected fractional size of spread.



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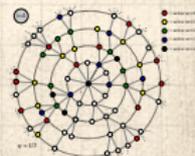
## References



**Next:** Find expected fractional size of spread.



Not obvious even for uniform threshold problem.



# Threshold contagion on random networks

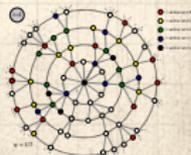
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-  **Next:** Find expected fractional size of spread.
-  Not obvious even for uniform threshold problem.
-  Difficulty is in figuring out if and when nodes that need  $\geq 2$  hits switch on.



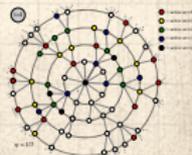
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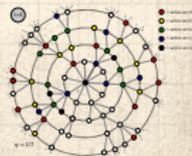
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- Next: Find expected fractional size of spread.
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- Problem **beautifully solved** for infinite seed case by Gleeson and Cahalane:  
"Seed size strongly affects cascades on random networks," Phys. Rev. E, 2007. <sup>[14]</sup>



# Threshold contagion on random networks

- Next: Find expected fractional size of spread.
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"Seed size strongly affects cascades on random networks," Phys. Rev. E, 2007. <sup>[14]</sup>
- Developed further by Gleeson in "Cascades on correlated and modular random networks," Phys. Rev. E, 2008. <sup>[13]</sup>



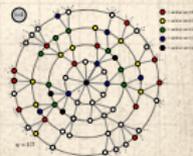
# Determining expected size of spread:

 Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$

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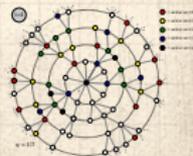
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# Determining expected size of spread:

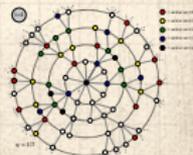
☰ Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$

☰ Capitalize on local branching network structure of random networks (again)



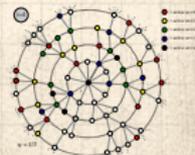
# Determining expected size of spread:

- ☰ Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- ☰ Capitalize on local branching network structure of random networks (again)
- ☰ Now think about what must happen for a specific node  $i$  to become active at time  $t$ :



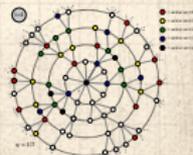
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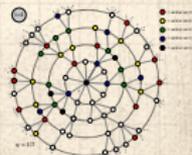
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  - $t = 1$ :  $i$  was not a seed but enough of  $i$ 's friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.



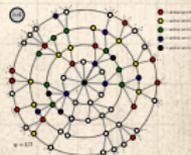
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  - $t = 2$ : enough of  $i$ 's friends and friends-of-friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.



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  - $t = 2$ : enough of  $i$ 's friends and friends-of-friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.
  - $t = n$ : enough nodes within  $n$  hops of  $i$  switched on at  $t = 0$  and their effects have propagated to reach  $i$ .

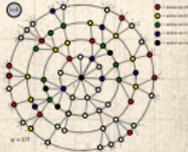
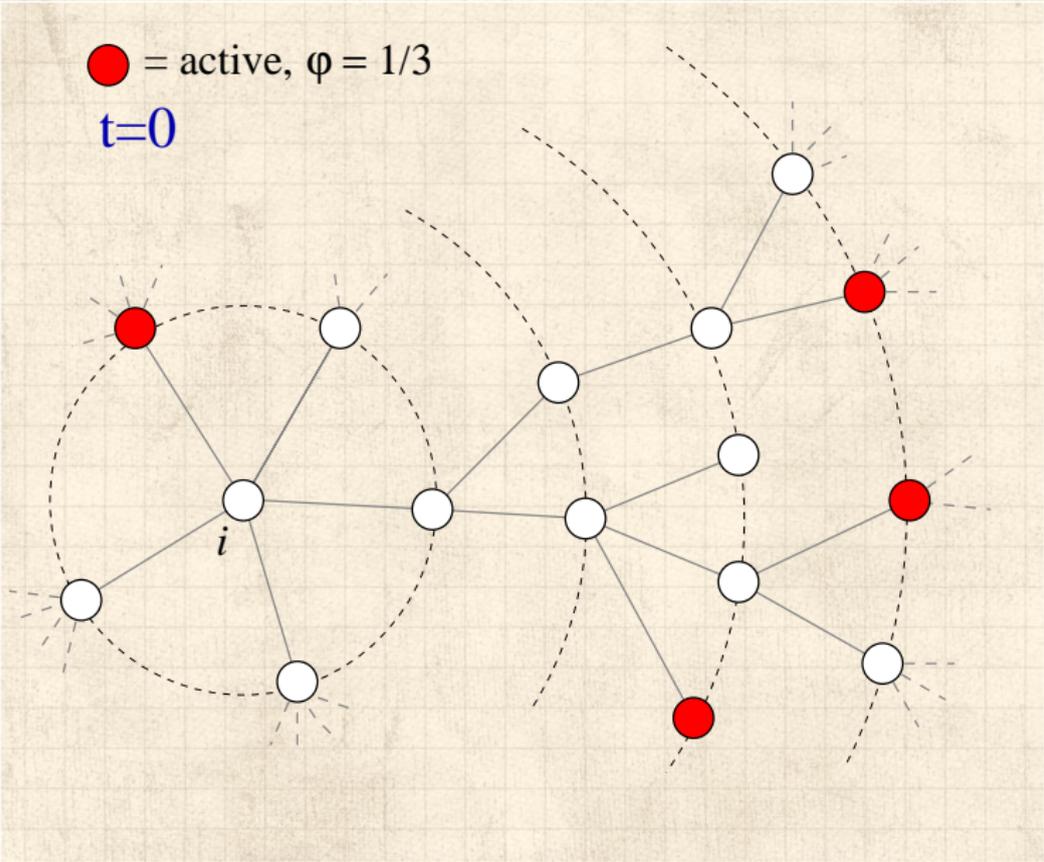


# Expected size of spread

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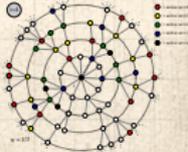
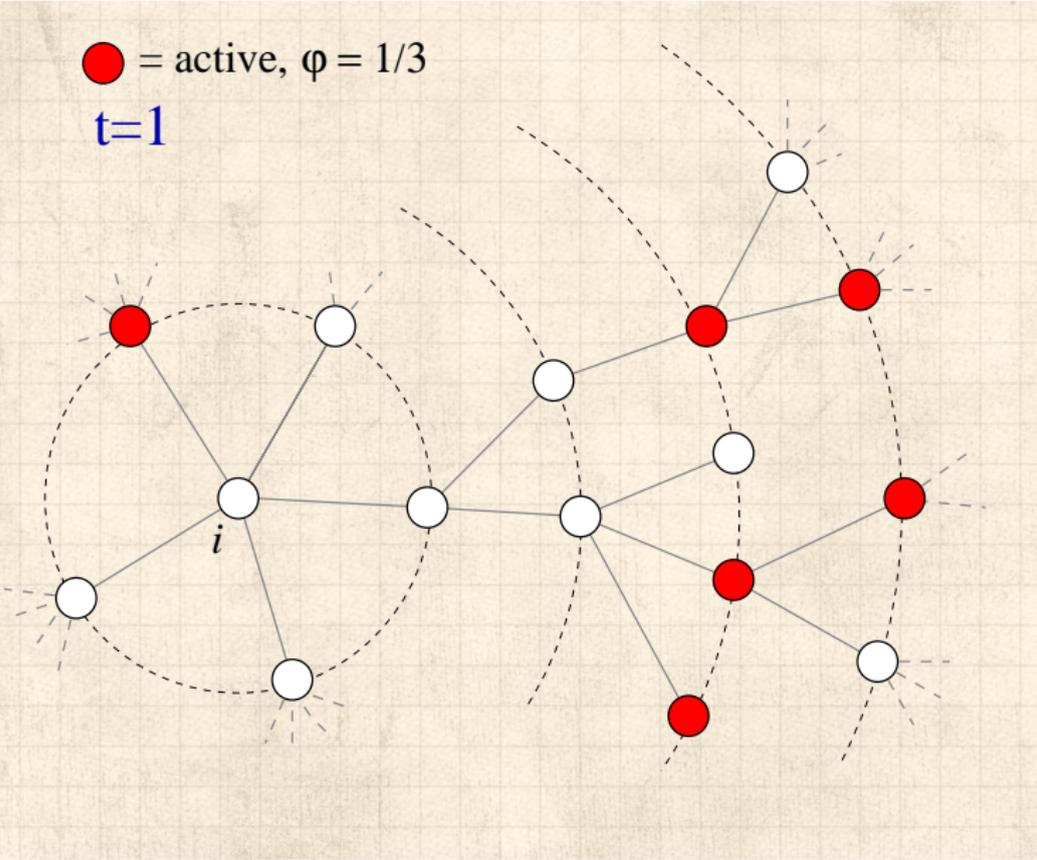
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● = active,  $\phi = 1/3$

$t=1$

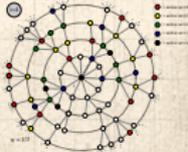
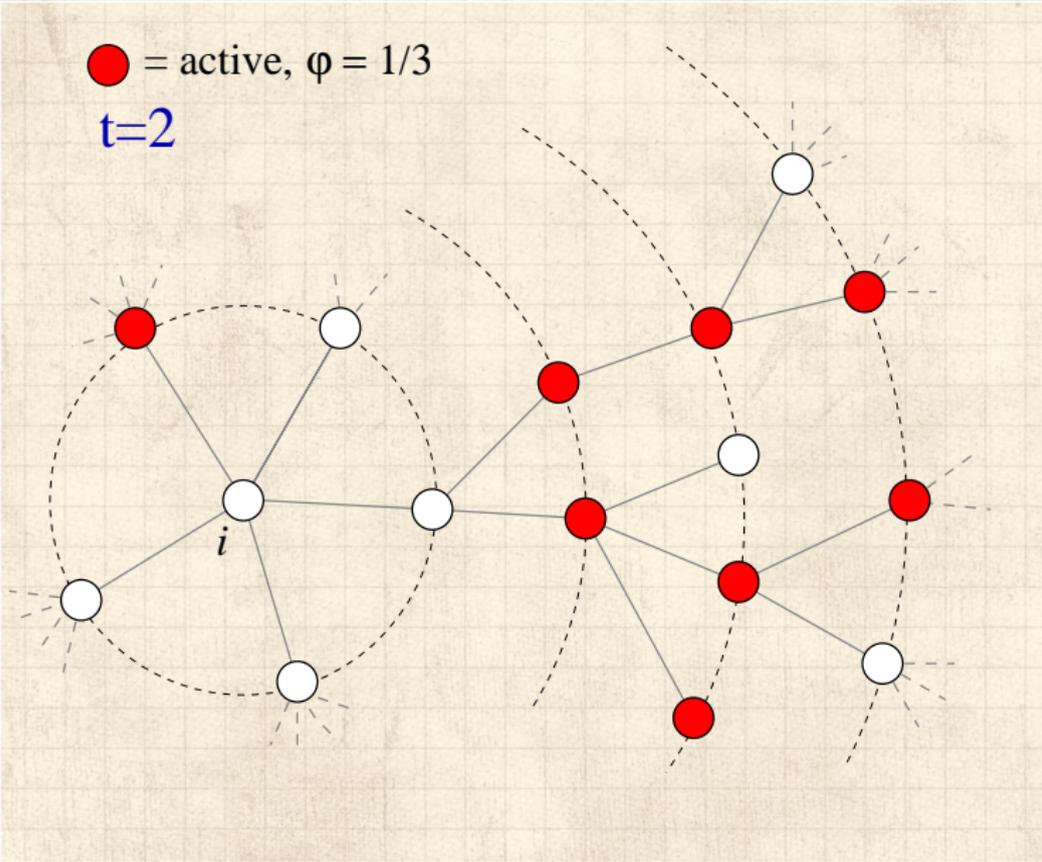


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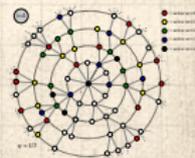
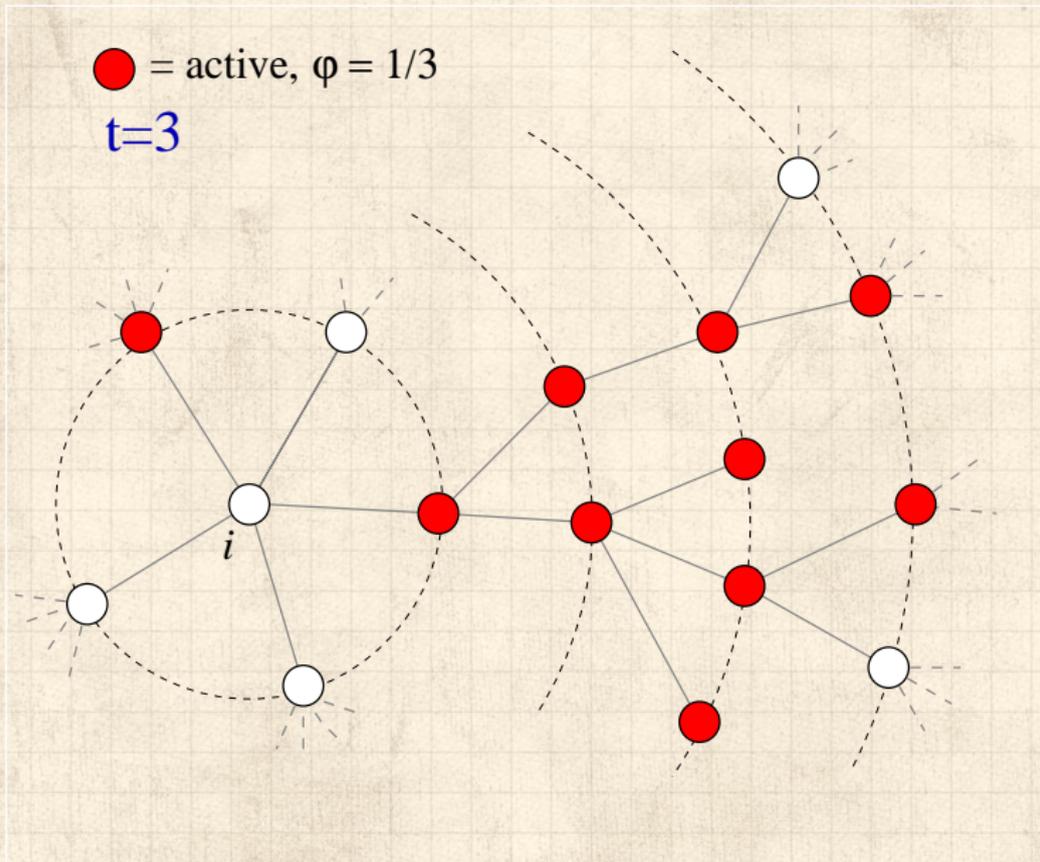


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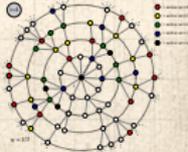
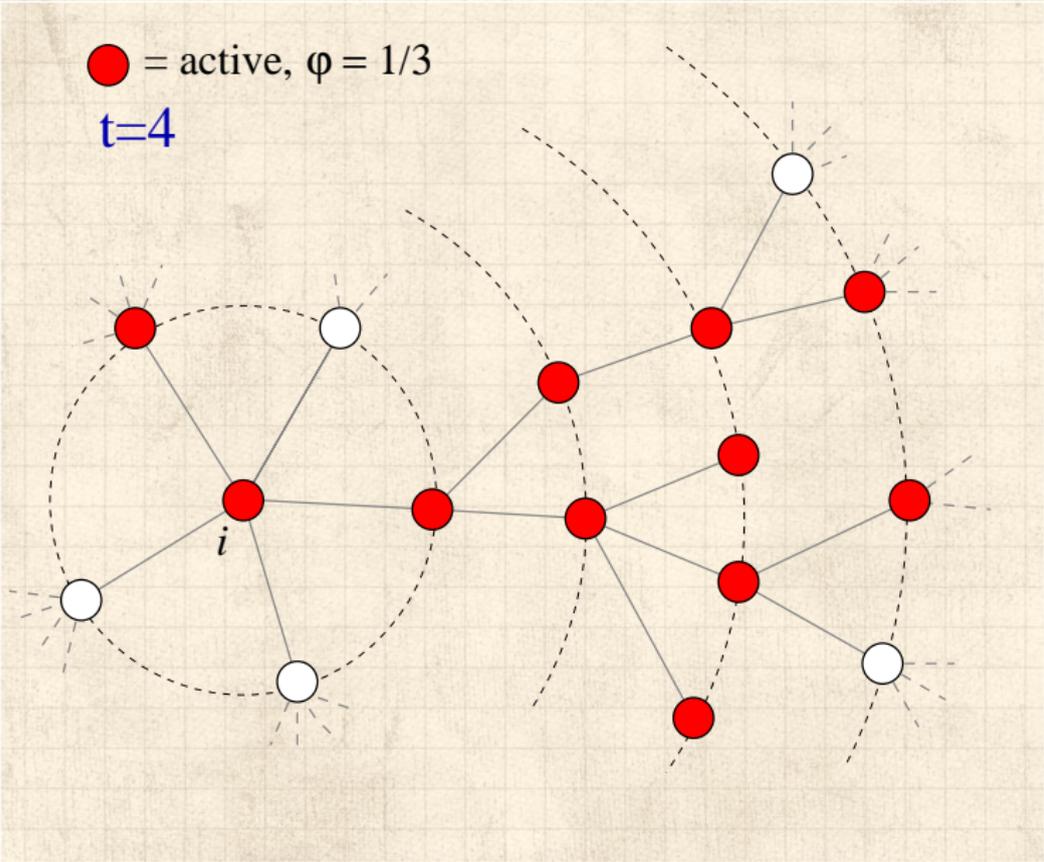


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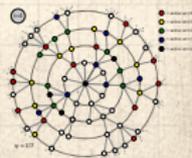
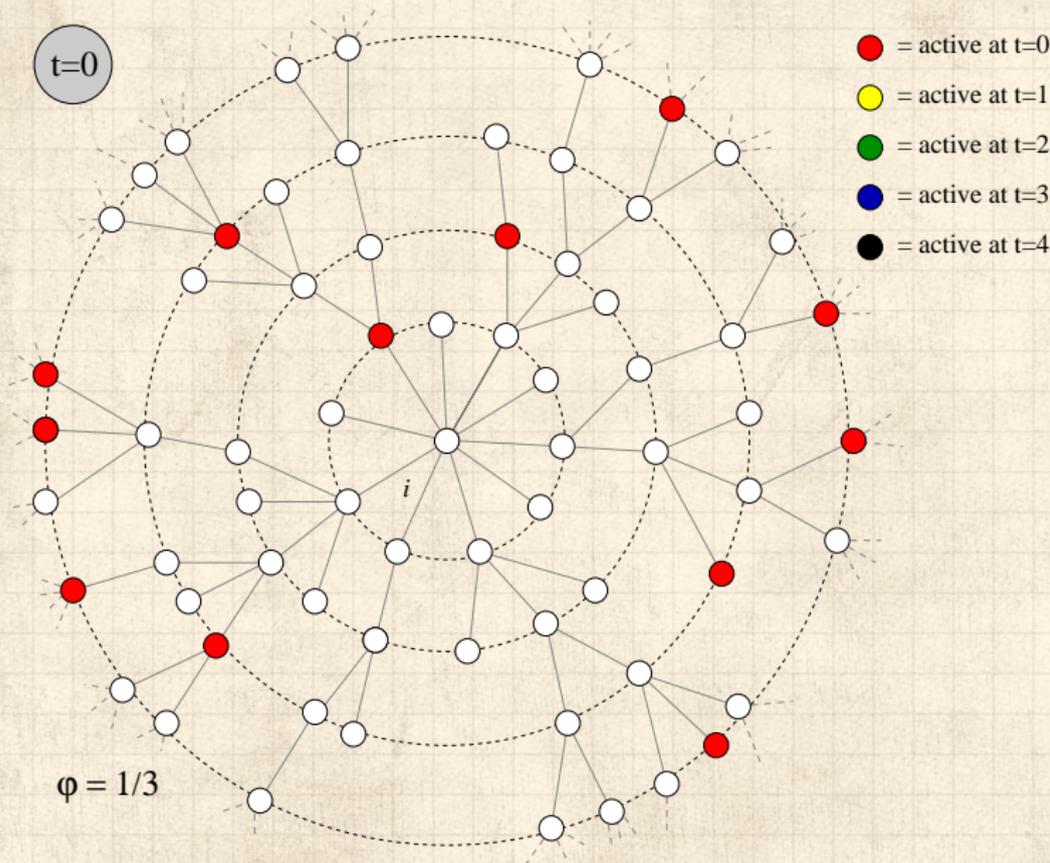


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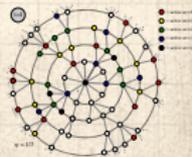
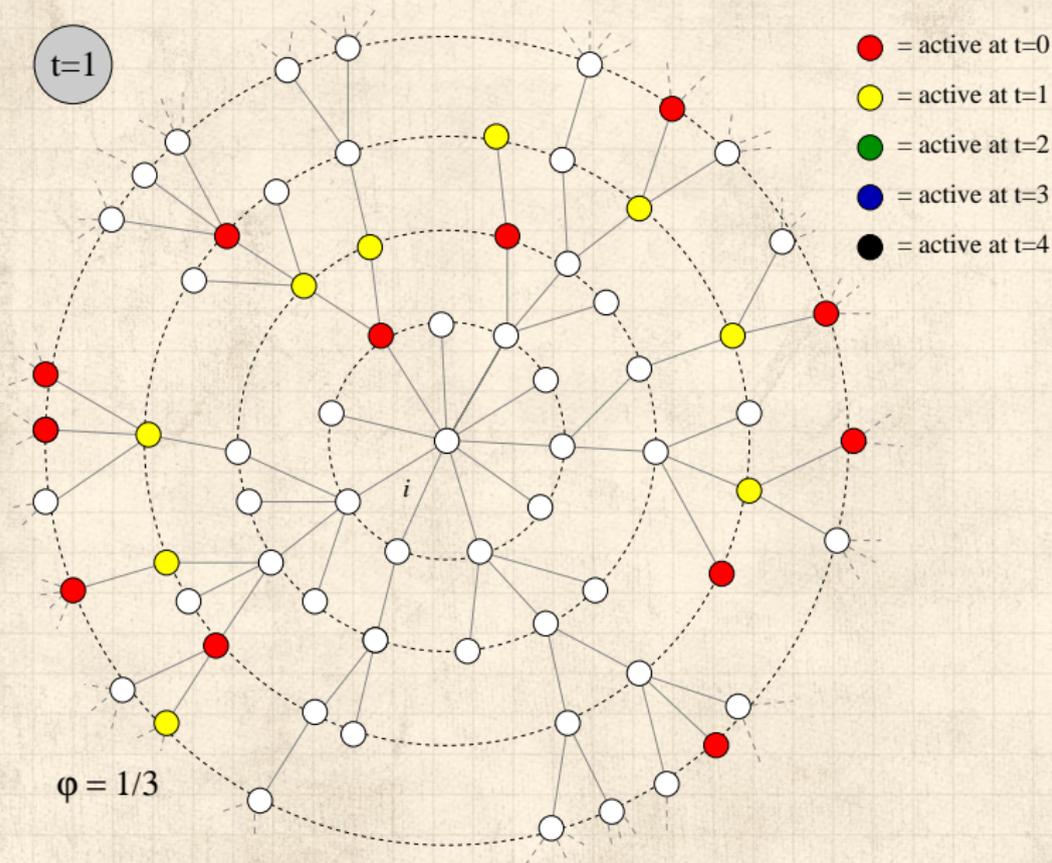


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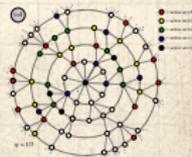
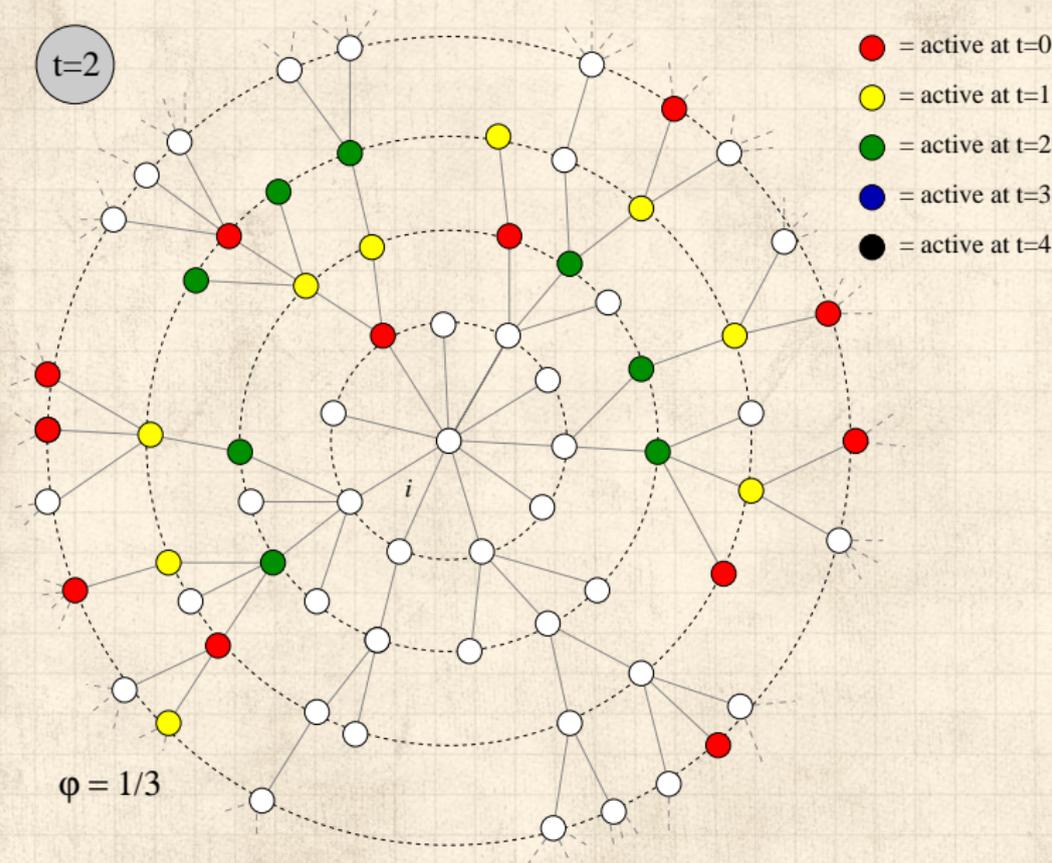


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Background  
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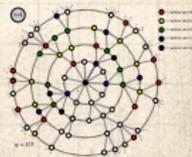
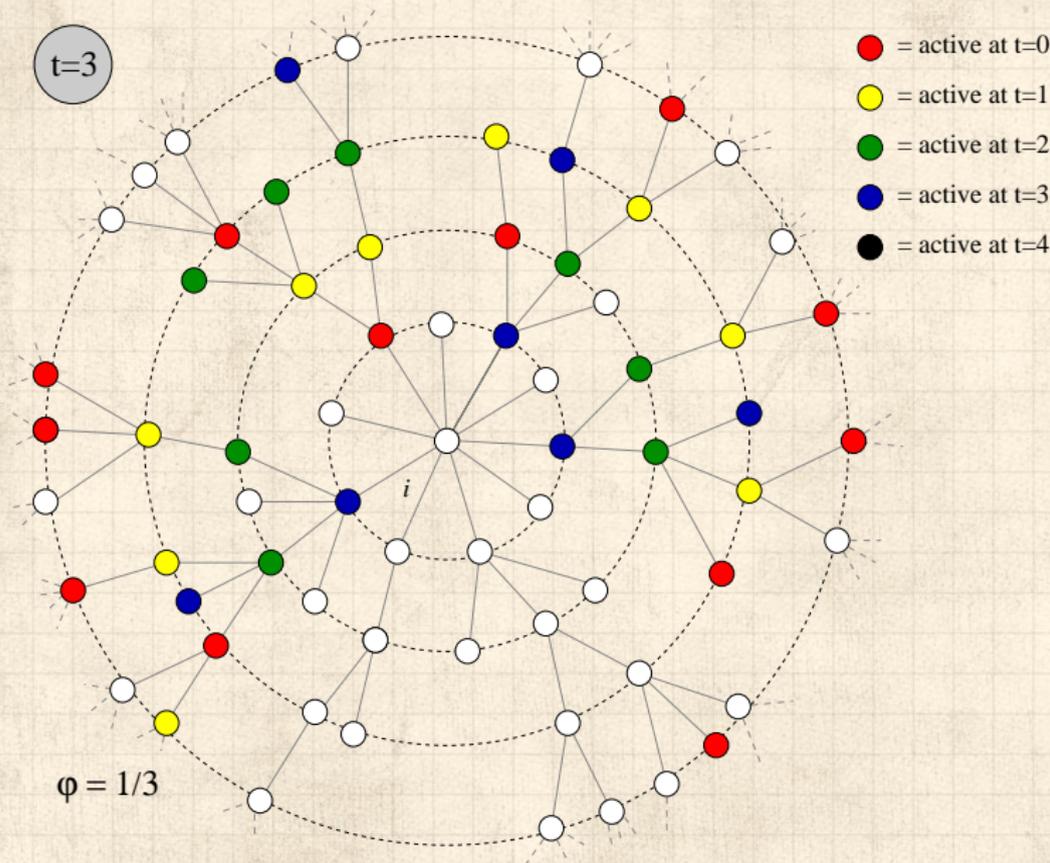


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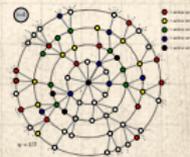
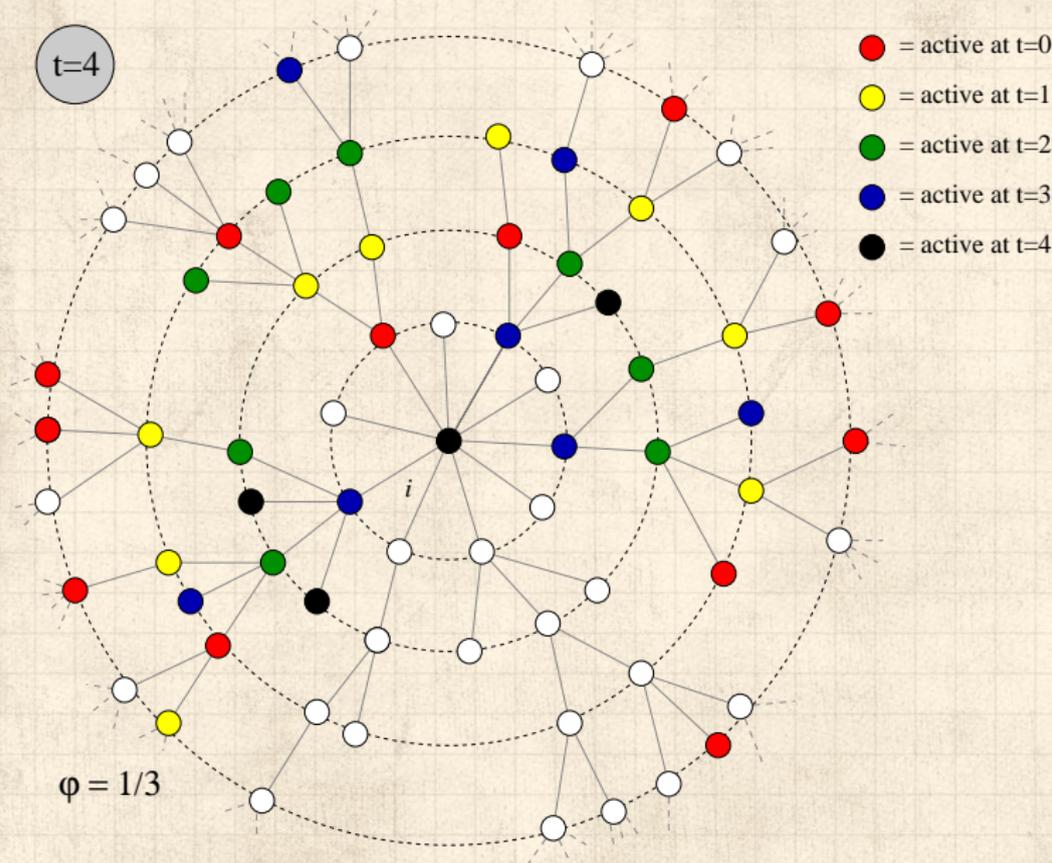


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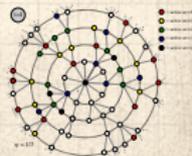
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### Notes:

- Calculations are possible if nodes do not become inactive (strong restriction).



# Expected size of spread

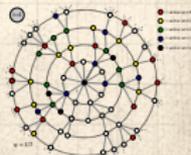
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- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.



# Expected size of spread

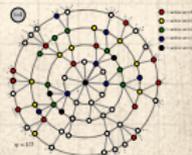
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### Notes:

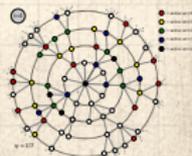
- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.
- We can analytically determine the entire time evolution, not just the final size.



# Expected size of spread

## Notes:

- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.
- We can analytically determine the entire time evolution, not just the final size.
- We can in fact determine  $\Pr(\text{node of degree } k \text{ switching on at time } t)$ .



# Expected size of spread

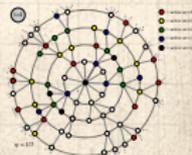
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### Notes:

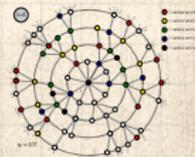
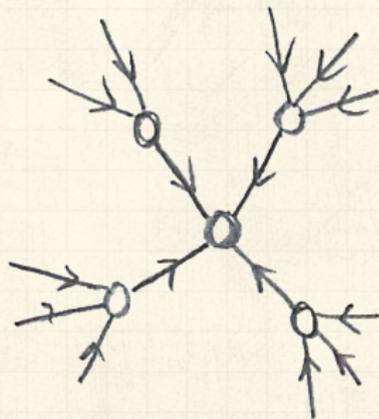
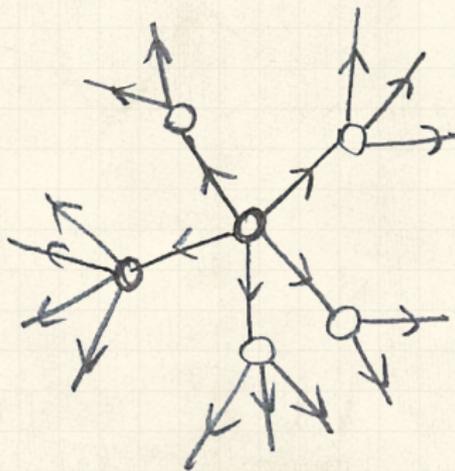
- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.
- We can analytically determine the entire time evolution, not just the final size.
- We can in fact determine  $\Pr(\text{node of degree } k \text{ switching on at time } t)$ .
- Asynchronous updating can be handled too.



# Expected size of spread

Pleasantness:

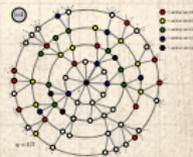
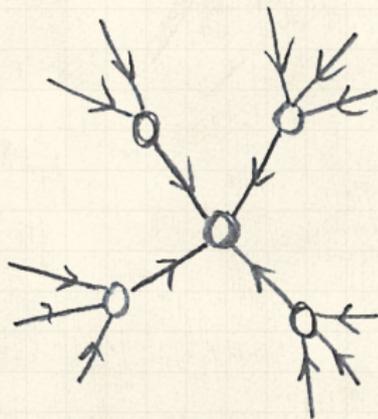
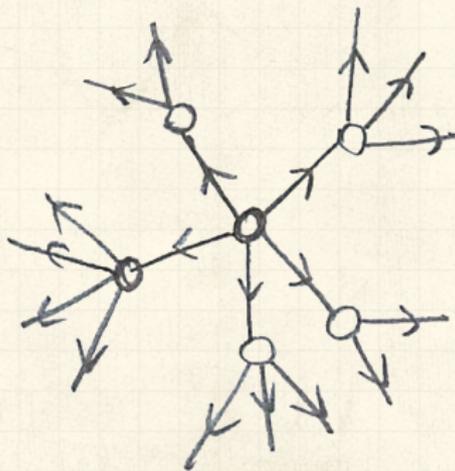
 Taking off from a single seed story is about **expansion** away from a node.



# Expected size of spread

## Pleasantness:

- ✉ Taking off from a single seed story is about **expansion** away from a node.
- ✉ Extent of spreading story is about **contraction** at a node.



# Expected size of spread



**Notation:**

$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).

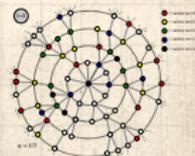
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# Expected size of spread



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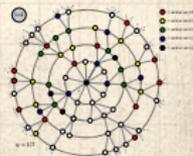


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# Expected size of spread



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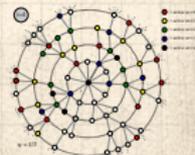
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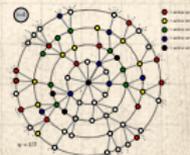


$\binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} = \mathbf{Pr}$  ( $j$  of a degree  $k$  node's neighbors were seeded at time  $t = 0$ ).

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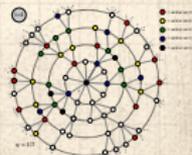


Probability a degree  $k$  node was a seed at  $t = 0$  is  $\phi_0$  (as above).

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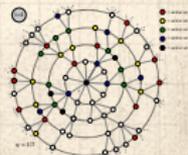


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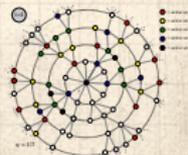
Combining everything, we have:

$$\phi_{k,1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^k \binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} B_{kj}.$$

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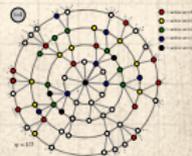


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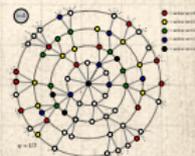
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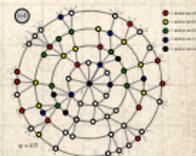
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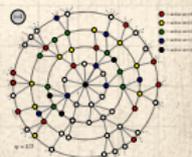
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Story analogous to  $t = 1$  case. For node  $i$ :

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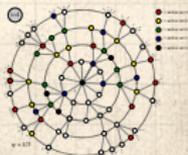
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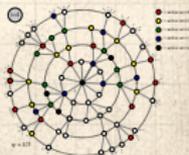
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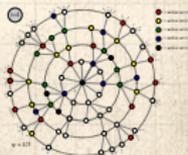
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So we need to compute  $\theta_t$ ... massive excitement...



# Expected size of spread

First connect  $\theta_0$  to  $\theta_1$ :

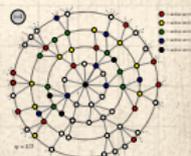
  $\theta_1 = \phi_0 +$

$$(1 - \phi_0) \sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_0^j (1 - \theta_0)^{k-1-j} B_{kj}$$

  $\frac{k P_k}{\langle k \rangle} = R_k = \mathbf{Pr}$  (edge connects to a degree  $k$  node).

  $\sum_{j=0}^{k-1}$  piece gives  $\mathbf{Pr}$ (degree node  $k$  activates) of its neighbors  $k - 1$  incoming neighbors are active.

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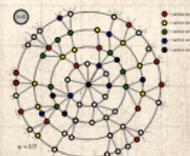
$$(1 - \phi_0) \sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_0^j (1 - \theta_0)^{k-1-j} B_{kj}$$

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 See this all generalizes to give  $\theta_{t+1}$  in terms of  $\theta_t \dots$



# Expected size of spread

Two pieces: edges first, and then nodes

$$1. \theta_{t+1} = \underbrace{\phi_0}_{\text{exogenous}}$$

$$+(1 - \phi_0) \underbrace{\sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_t^j (1 - \theta_t)^{k-1-j} B_{kj}}_{\text{social effects}}$$

with  $\theta_0 = \phi_0$ .

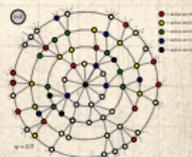
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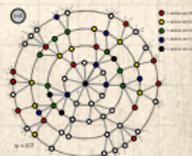
# Expected size of spread

Iterative map for  $\theta_t$  is key:

$$\theta_{t+1} = \underbrace{\phi_0}_{\text{exogenous}}$$

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$$= G(\theta_t; \phi_0)$$



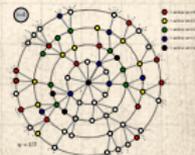
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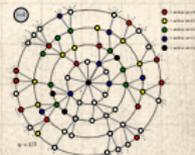
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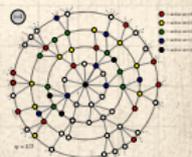


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$$G(0; \phi_0) = \sum_{k=1}^{\infty} \frac{kP_k}{\langle k \rangle} \bullet B_{k0} > 0.$$

meaning  $B_{k0} > 0$  for at least one value of  $k \geq 1$ .



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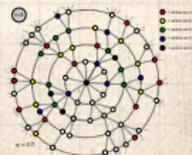
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- If  $\theta = 0$  is a fixed point of  $G$  (i.e.,  $G(0; \phi_0) = 0$ ) then spreading occurs if

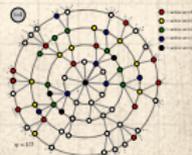
$$G'(0; \phi_0) = \sum_{k=0}^{\infty} \frac{kP_k}{\langle k \rangle} \bullet (k-1) \bullet B_{k1} > 1.$$



# Expected size of spread:

In words:

 If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.



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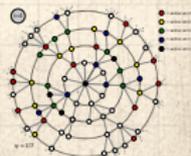
In words:

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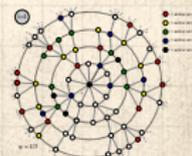
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- 🧱 Cascade condition is more complicated for  $\phi_0 > 0$ .



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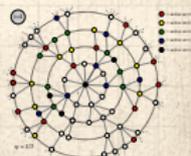
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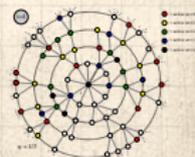
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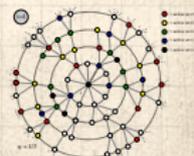
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- 🧱 A version of a critical mass model again.

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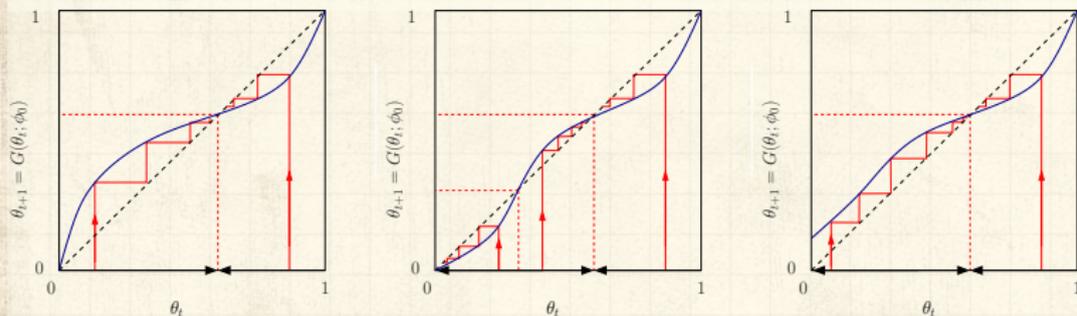


# General fixed point story:

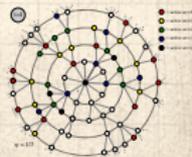
## Social Contagion Models

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## References



 Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.

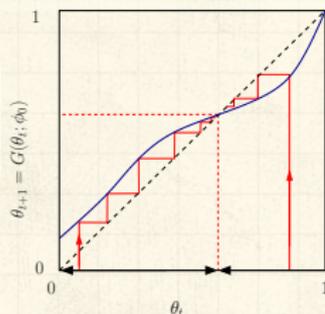
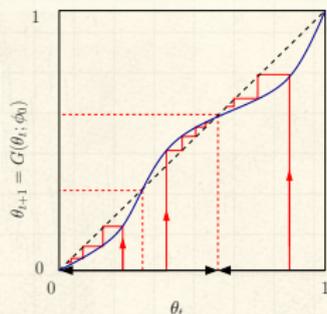
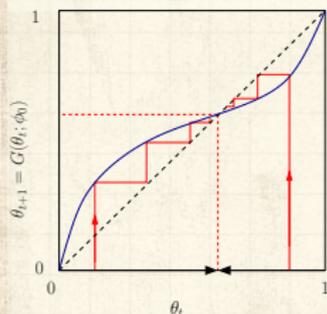


# General fixed point story:

## Social Contagion Models

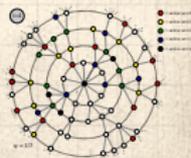
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 Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.

 n.b., adjacent fixed points must have opposite stability types.

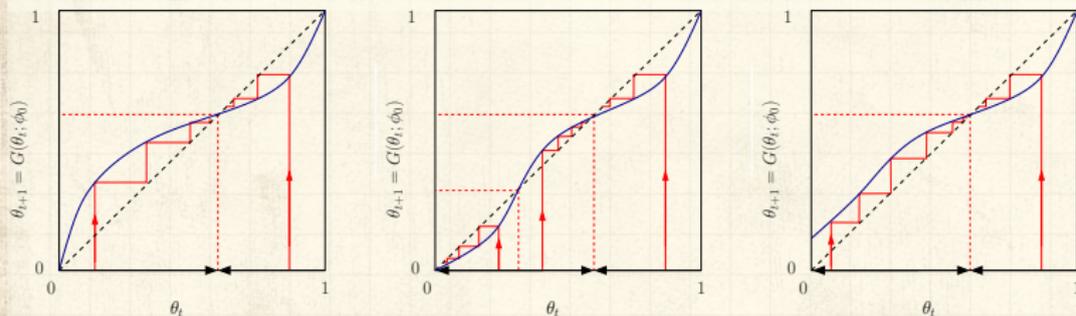


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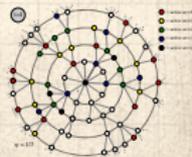
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-  Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.
-  n.b., adjacent fixed points must have opposite stability types.
-  **Important:** Actual form of  $G$  depends on  $\phi_0$ .

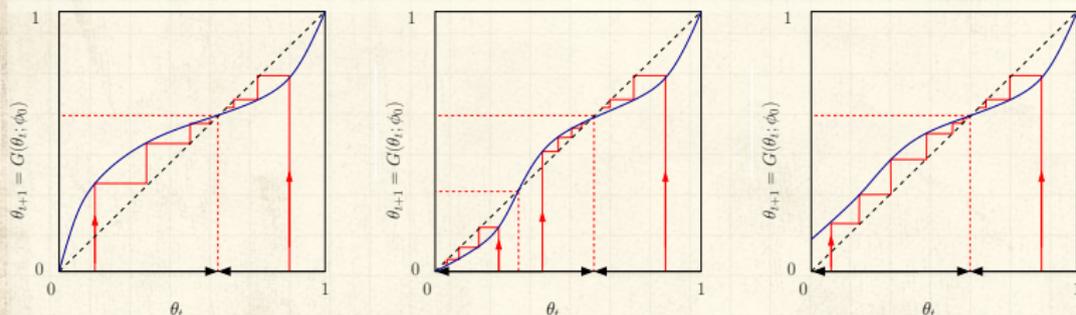


# General fixed point story:

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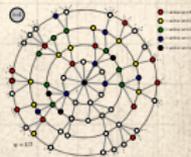


 Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.

 n.b., adjacent fixed points must have opposite stability types.

 **Important:** Actual form of  $G$  depends on  $\phi_0$ .

 So choice of  $\phi_0$  dictates both  $G$  and starting point—can't start anywhere for a given  $G$ .



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Network version

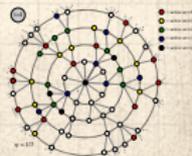
Final size

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# Early adopters—degree distributions

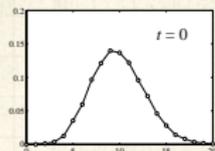
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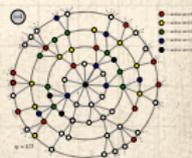
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$t = 0$



$P_{k,t}$  versus  $k$



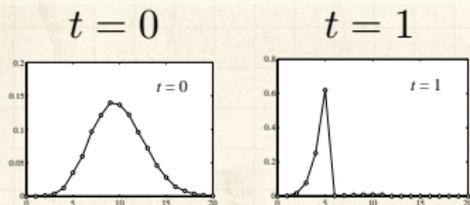
# Early adopters—degree distributions

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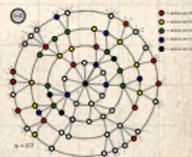
## Social Contagion Models

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$P_{k,t}$  versus  $k$



# Early adopters—degree distributions

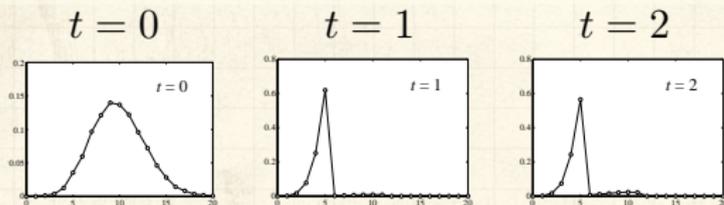
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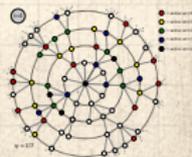
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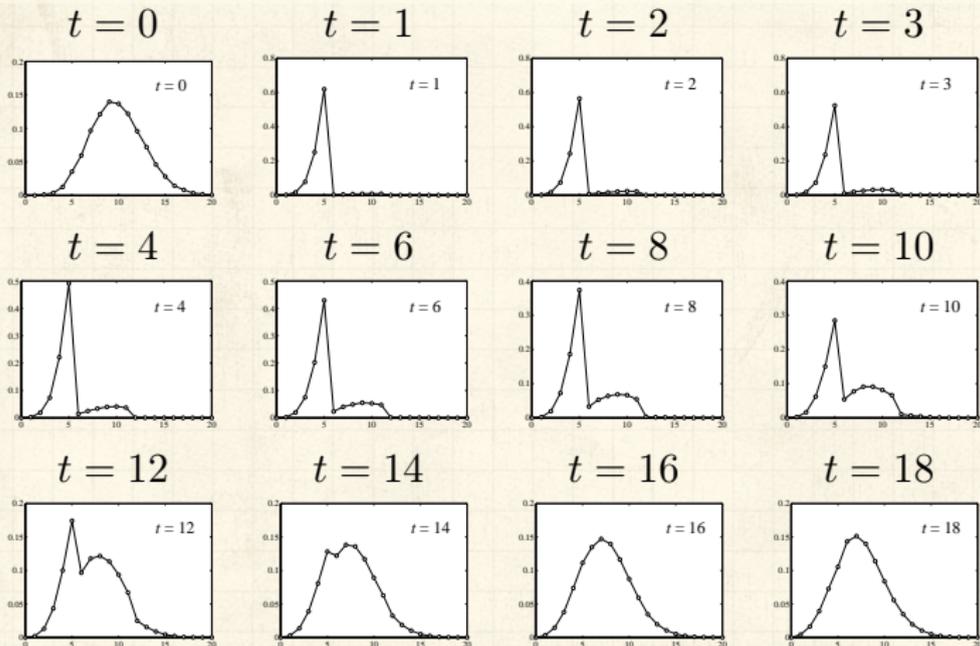


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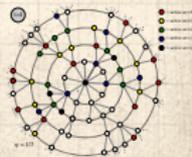
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$P_{k,t}$  versus  $k$

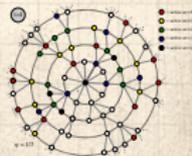




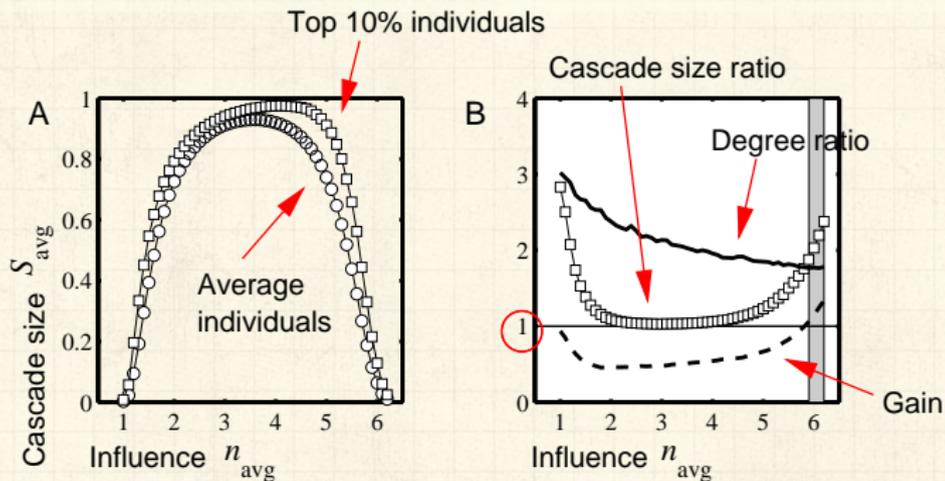
## "Influentials, Networks, and Public Opinion Formation"

Watts and Dodds,  
J. Consum. Res., **34**, 441–458, 2007. [28]

-  Exploration of threshold model of social contagion on various networks.
-  "Influentials" are limited in power.
-  Connected groups of weakly influential-vulnerable" individuals are key.
-  Average individuals can have more power than well connected ones.



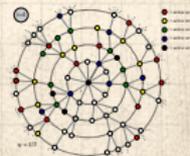
# The multiplier effect:



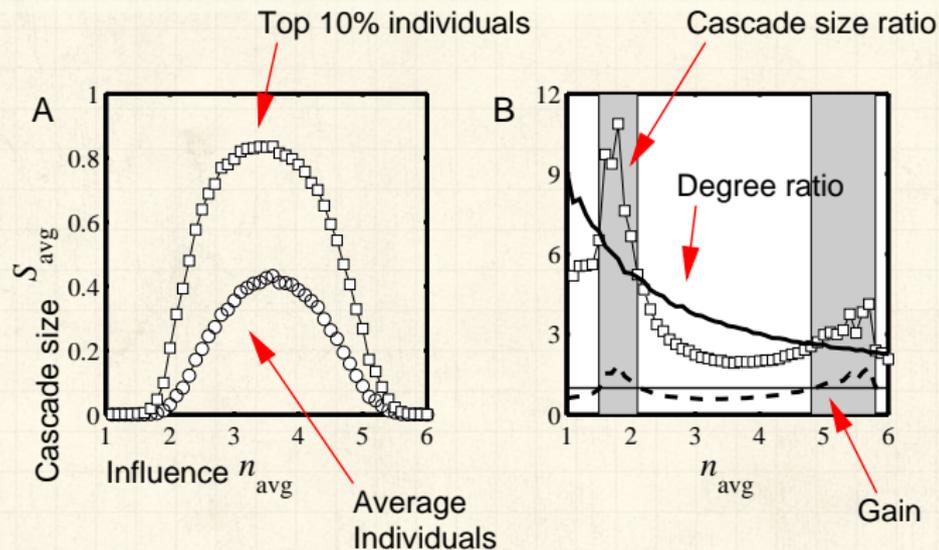
Fairly uniform levels of individual influence.



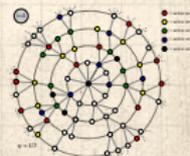
Multiplier effect is mostly below 1.



# The multiplier effect:



Skewed influence distribution example.

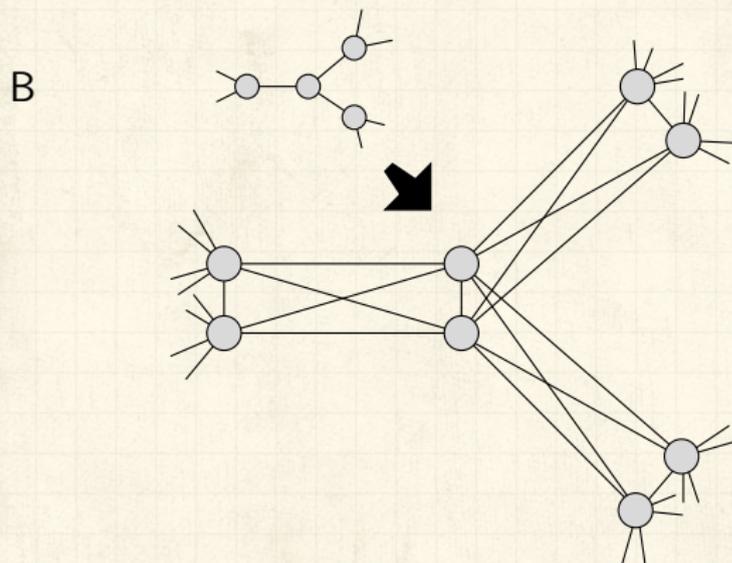
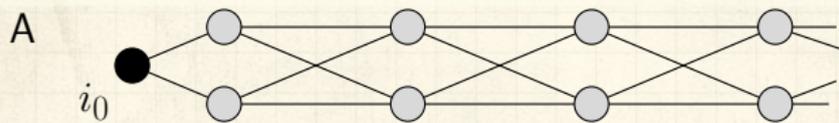


# Special subnetworks can act as triggers

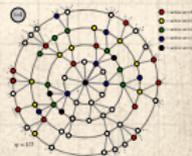
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  $\phi = 1/3$  for all nodes



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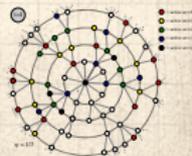
Final size

Spreading success

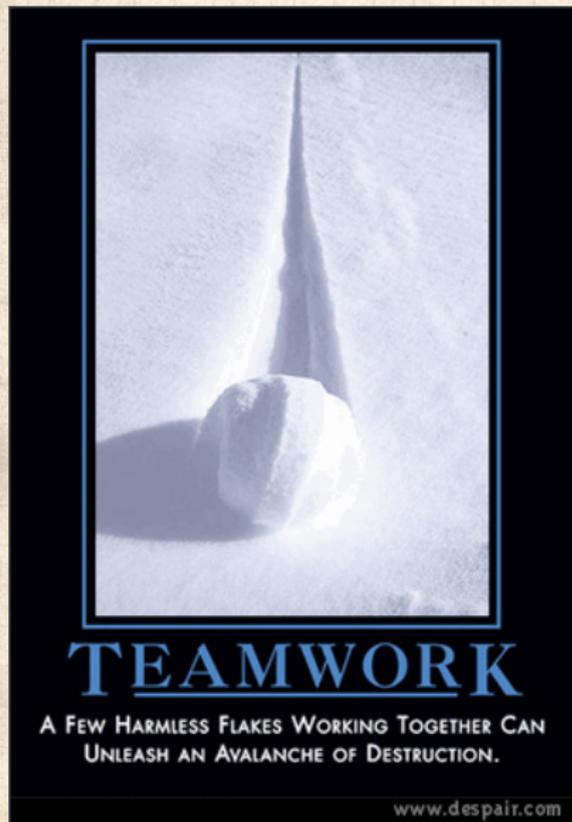
**Groups**

## References

## References



# The power of groups...



[despair.com](http://despair.com)

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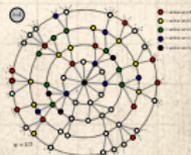
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"A few harmless flakes working together can unleash an avalanche of destruction."

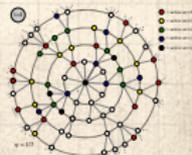




[“Threshold Models of Social Influence”](#)   
Watts and Dodds,  
The Oxford Handbook of Analytical  
Sociology, **34**, 475–497, 2009. <sup>[29]</sup>



Assumption of sparse interactions is good





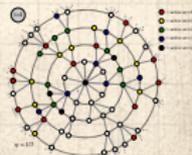
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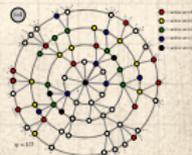
Degree distribution is (generally) key to a  
network's function





"Threshold Models of Social Influence"   
Watts and Dodds,  
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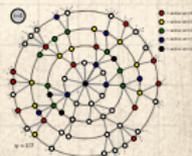
-  Assumption of sparse interactions is good
-  Degree distribution is (generally) key to a network's function
-  Still, random networks don't represent all networks





"Threshold Models of Social Influence"   
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-  Assumption of sparse interactions is good
-  Degree distribution is (generally) key to a network's function
-  Still, random networks don't represent all networks
-  Major element missing: **group structure**



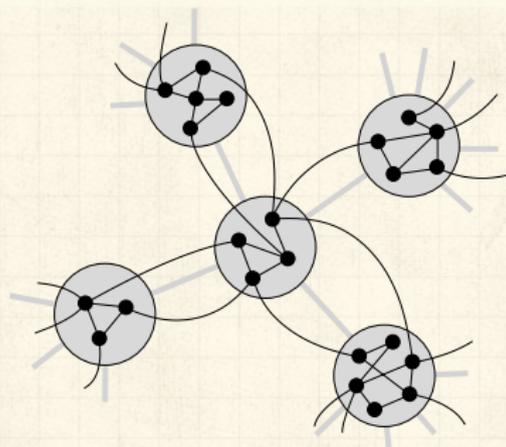
# Group structure—Ramified random networks

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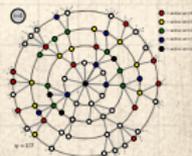
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$p$  = intergroup connection probability  
 $q$  = intragroup connection probability.

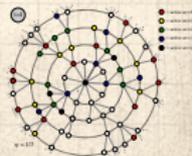
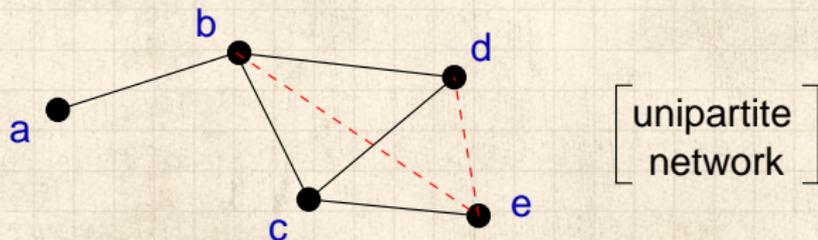
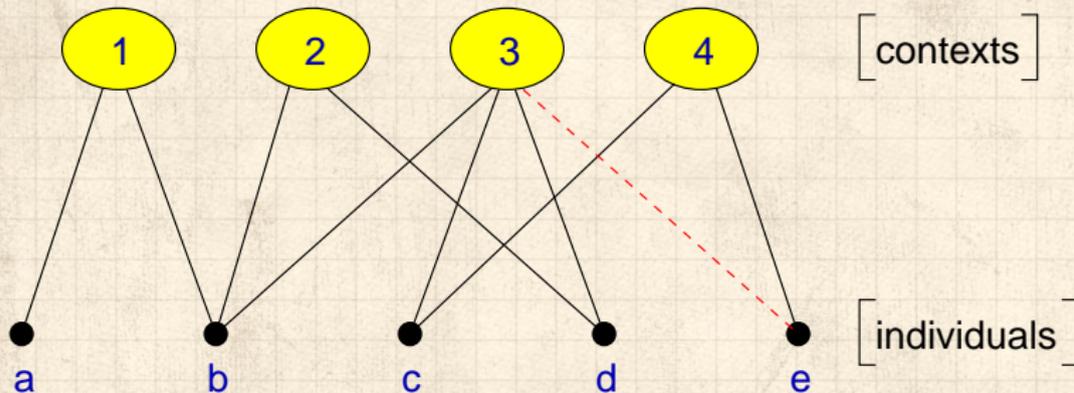


# Bipartite networks

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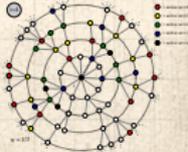
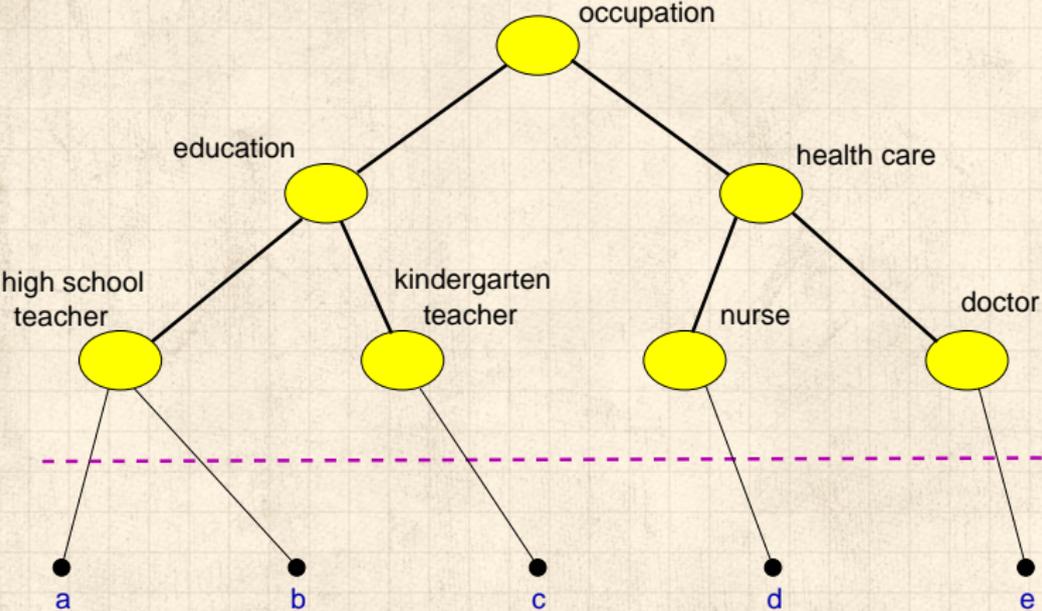


# Context distance

## Social Contagion Models

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## References

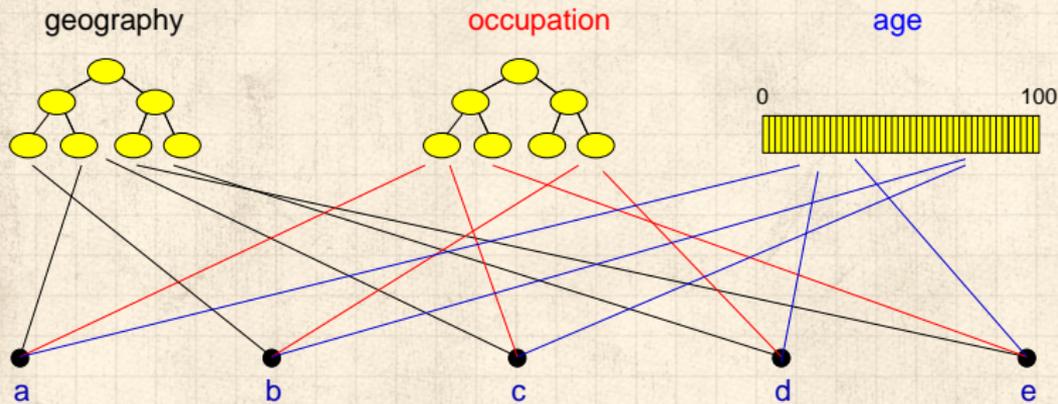


# Generalized affiliation model

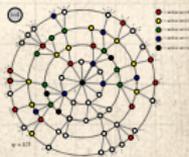
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(Blau & Schwartz, Simmel, Breiger)



# Generalized affiliation model networks with triadic closure



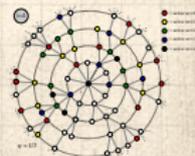
Connect nodes with probability  $\propto e^{-\alpha d}$

where

$\alpha$  = homophily parameter

and

$d$  = distance between nodes (height of lowest  
common ancestor)



# Generalized affiliation model networks with triadic closure



Connect nodes with probability  $\propto e^{-\alpha d}$

where

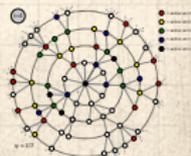
$\alpha$  = homophily parameter

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$\tau_1$  = intergroup probability of friend-of-friend connection



# Generalized affiliation model networks with triadic closure



Connect nodes with probability  $\propto e^{-\alpha d}$

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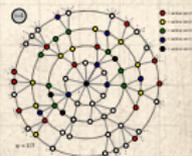
$d$  = distance between nodes (height of lowest common ancestor)



$\tau_1$  = intergroup probability of friend-of-friend connection



$\tau_2$  = intragroup probability of friend-of-friend connection



# Cascade windows for group-based networks

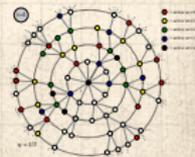
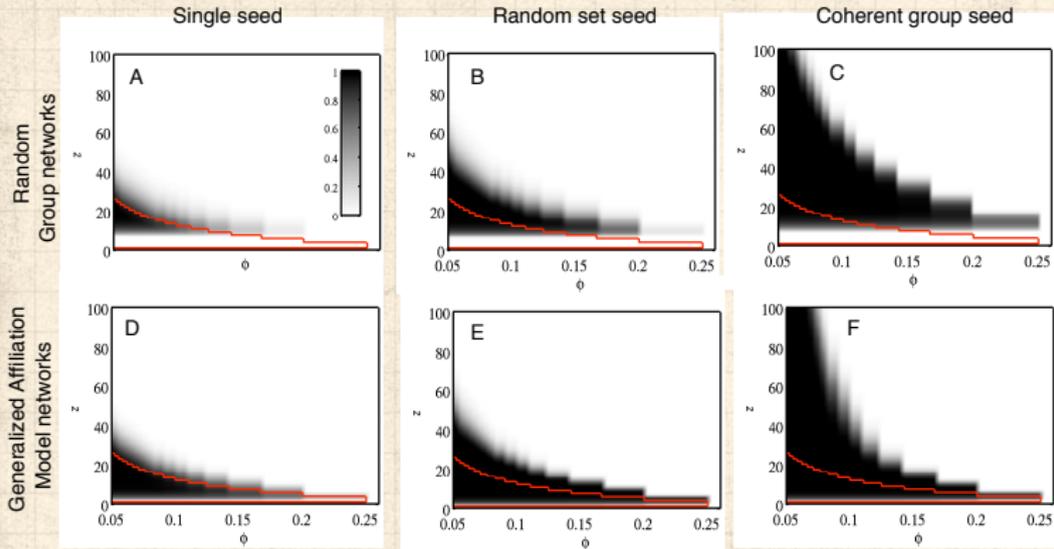
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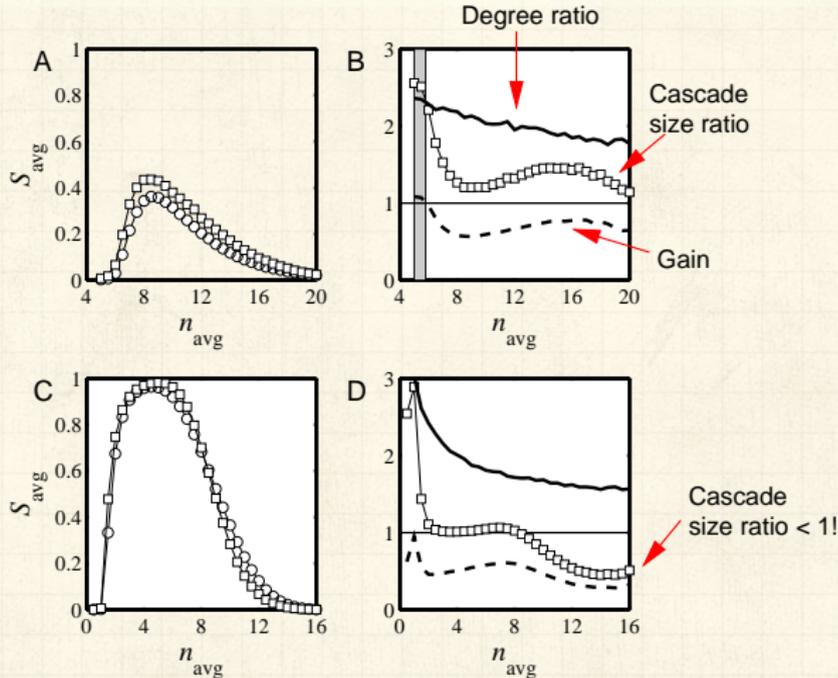


# Multiplier effect for group-based networks:

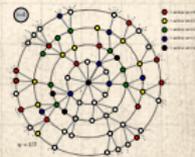
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Multiplier almost always below 1.

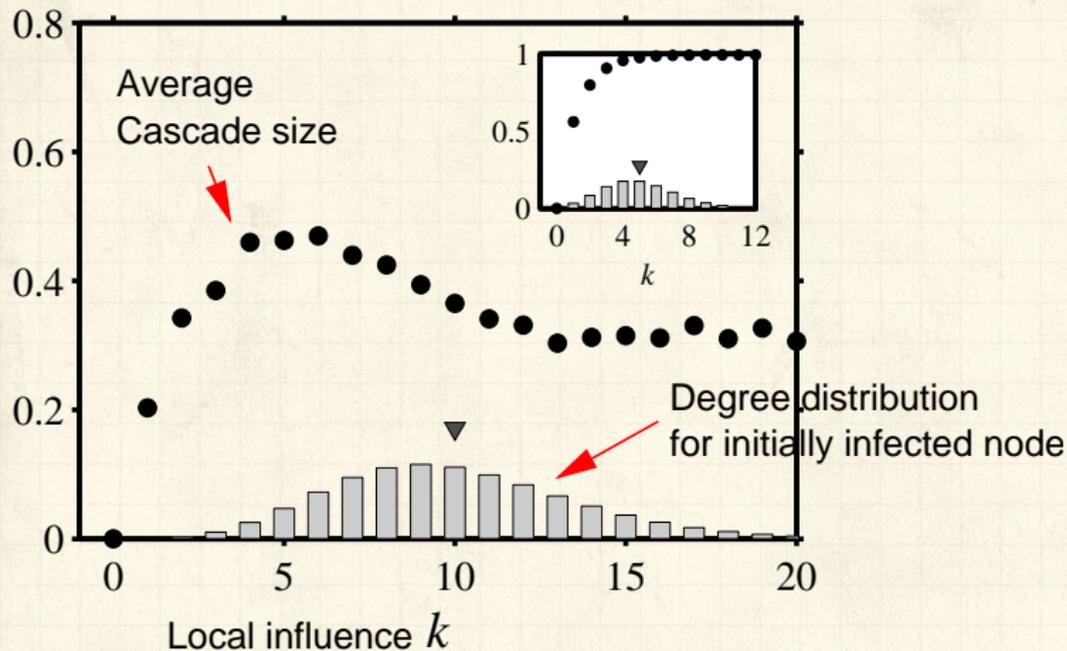


# Assortativity in group-based networks

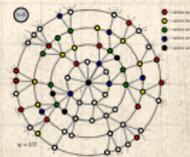
## Social Contagion Models

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 The most connected nodes aren't always the most 'influential.'

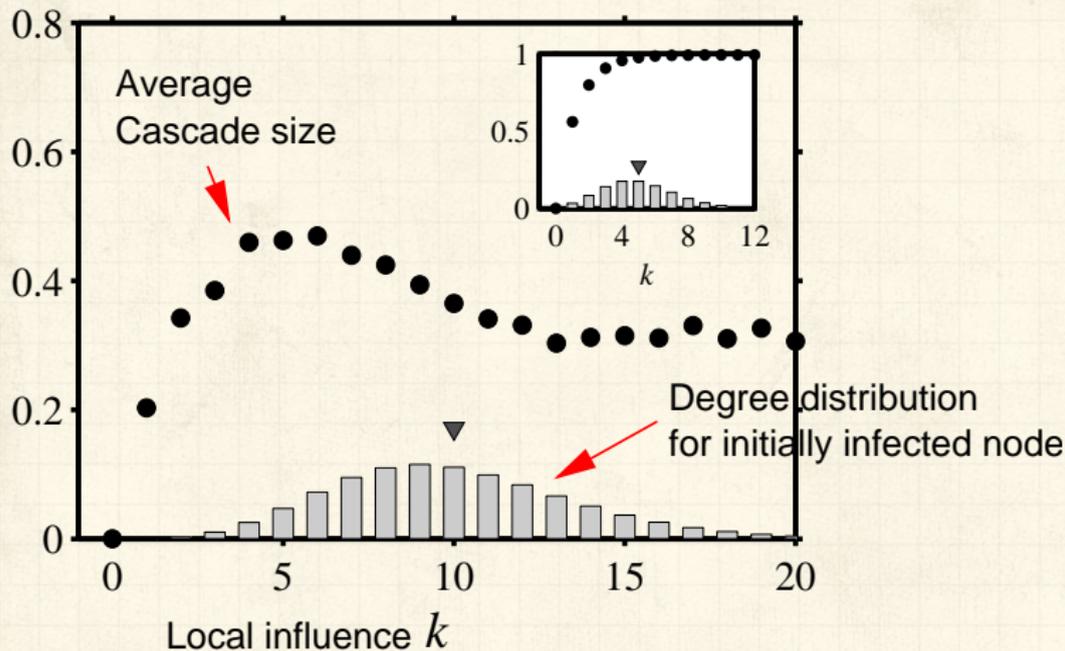


# Assortativity in group-based networks

## Social Contagion Models

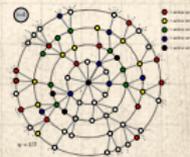
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 The most connected nodes aren't always the most 'influential.'

 **Degree assortativity** is the reason.



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“Without followers, evil cannot spread.” –Leonard Nimoy

## Summary

 **'Influential vulnerables'** are key to spread.

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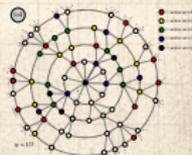
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# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

## Summary

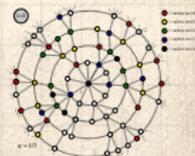
 **'Influential vulnerables'** are key to spread.

 Early adopters are mostly vulnerables.

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# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

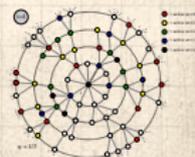
## Summary

- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.

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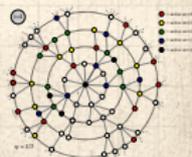
## Summary

- 📦 **'Influential vulnerables'** are key to spread.
- 📦 Early adopters are mostly vulnerables.
- 📦 Vulnerable nodes important but not necessary.
- 📦 Groups may greatly facilitate spread.

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“Without followers, evil cannot spread.” –Leonard Nimoy

## Summary

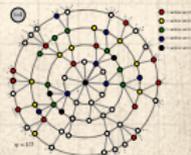
-  **'Influential vulnerables'** are key to spread.
-  Early adopters are mostly vulnerables.
-  Vulnerable nodes important but not necessary.
-  Groups may greatly facilitate spread.
-  Seems that cascade condition is a global one.

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# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

## Summary

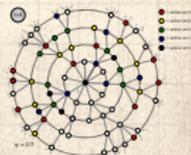
- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.
- 🧱 Groups may greatly facilitate spread.
- 🧱 Seems that cascade condition is a global one.
- 🧱 Most extreme/unexpected cascades occur in highly connected networks

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# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

## Summary

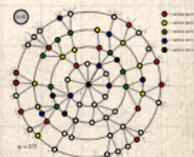
- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.
- 🧱 Groups may greatly facilitate spread.
- 🧱 Seems that cascade condition is a global one.
- 🧱 Most extreme/unexpected cascades occur in highly connected networks
- 🧱 'Influentials' are posterior constructs.

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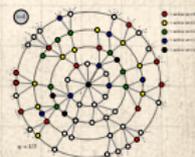
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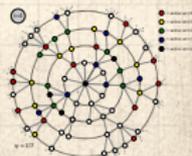
## Implications

 Focus on the influential vulnerables.

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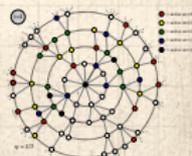
## Implications

- Focus on **the influential vulnerables**.
- Create entities that can be transmitted successfully through many individuals rather than broadcast from one 'influential.'

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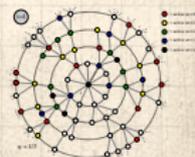
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(Idea of opinion leaders spreads well...)

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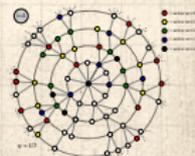
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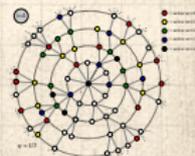
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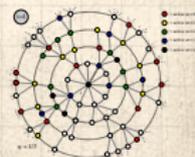
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- Displaying can be **passive** = free (fashion), or **active** = harder to achieve (political messages; even so: buttons and hats).
- Entities can be novel or designed to combine with others, e.g. block another one.

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# Spreading and unspreading: Empires

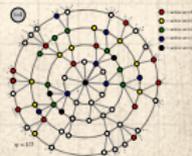
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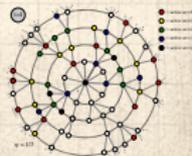
## References

<https://www.youtube.com/watch?v=FEaCflp9qR4?rel=0>

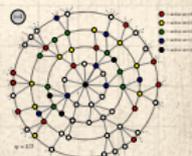


# References I

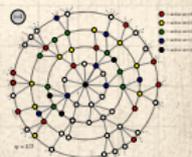
- [1] A. Bentley, M. Earls, and M. J. O'Brien.  
I'll Have What She's Having: Mapping Social Behavior.  
MIT Press, Cambridge, MA, 2011.
- [2] S. Bikhchandani, D. Hirshleifer, and I. Welch.  
A theory of fads, fashion, custom, and cultural change as informational cascades.  
J. Polit. Econ., 100:992–1026, 1992.
- [3] S. Bikhchandani, D. Hirshleifer, and I. Welch.  
Learning from the behavior of others:  
Conformity, fads, and informational cascades.  
J. Econ. Perspect., 12(3):151–170, 1998. pdf 



- [4] J. M. Carlson and J. Doyle.  
Highly optimized tolerance: A mechanism for  
power laws in designed systems.  
[Phys. Rev. E, 60\(2\):1412–1427, 1999. pdf](#)
- [5] J. M. Carlson and J. Doyle.  
Highly Optimized Tolerance: Robustness and  
design in complex systems.  
[Phys. Rev. Lett., 84\(11\):2529–2532, 2000. pdf](#)
- [6] N. A. Christakis and J. H. Fowler.  
The spread of obesity in a large social network  
over 32 years.  
[New England Journal of Medicine, 357:370–379,  
2007. pdf](#)



- [7] N. A. Christakis and J. H. Fowler.  
The collective dynamics of smoking in a large  
social network.  
[New England Journal of Medicine, 358:2249–2258,  
2008. pdf](#) 
- [8] R. B. Cialdini.  
[Influence: Science and Practice.](#)  
Allyn and Bacon, Boston, MA, 4th edition, 2000.
- [9] P. S. Dodds, K. D. Harris, and C. M. Danforth.  
Limited Imitation Contagion on random networks:  
Chaos, universality, and unpredictability.  
[Phys. Rev. Lett., 110:158701, 2013. pdf](#) 



- [10] P. S. Dodds, K. D. Harris, and J. L. Payne.  
Direct, physically motivated derivation of the  
contagion condition for spreading processes on  
generalized random networks.

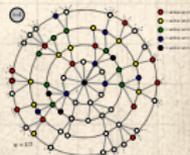
[Phys. Rev. E, 83:056122, 2011. pdf](#)

- [11] J. H. Fowler and N. A. Christakis.  
Dynamic spread of happiness in a large social  
network: longitudinal analysis over 20 years in  
the Framingham Heart Study.

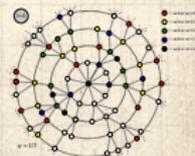
[BMJ, 337:article #2338, 2008. pdf](#)

- [12] M. Gladwell.  
The Tipping Point.

[Little, Brown and Company, New York, 2000.](#)



- [13] J. P. Gleeson.  
Cascades on correlated and modular random networks.  
[Phys. Rev. E, 77:046117, 2008. pdf](#) 
- [14] J. P. Gleeson and D. J. Cahalane.  
Seed size strongly affects cascades on random networks.  
[Phys. Rev. E, 75:056103, 2007. pdf](#) 
- [15] M. Granovetter.  
Threshold models of collective behavior.  
[Am. J. Sociol., 83\(6\):1420–1443, 1978. pdf](#) 



# References VI

- [16] M. Granovetter and R. Soong.  
Threshold models of diversity: Chinese  
restaurants, residential segregation, and the  
spiral of silence.

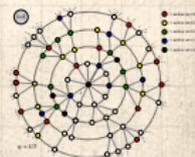
[Sociological Methodology, 18:69–104, 1988. pdf](#) 

- [17] M. S. Granovetter and R. Soong.  
Threshold models of interpersonal effects in  
consumer demand.

[J. Econ. Behav. Organ., 7:83–99, 1986. pdf](#) 

- [18] K. D. Harris, C. M. Danforth, and P. S. Dodds.  
Dynamical influence processes on networks:  
General theory and applications to social  
contagion.

[Phys. Rev. E, 88:022816, 2013. pdf](#) 



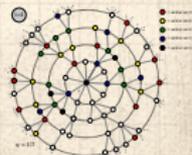
# References VII

- [19] E. Katz and P. F. Lazarsfeld.  
Personal Influence.  
The Free Press, New York, 1955.
- [20] T. Kuran.  
Now out of never: The element of surprise in the  
east european revolution of 1989.  
World Politics, 44:7-48, 1991. [pdf](#) 
- [21] T. Kuran.  
Private Truths, Public Lies: The Social  
Consequences of Preference Falsification.  
Harvard University Press, Cambridge, MA, Reprint  
edition, 1997.
- [22] T. Pratchett.  
The Truth.  
HarperCollins, 2000.

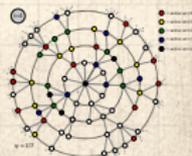
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- [23] T. C. Schelling.  
Dynamic models of segregation.  
[J. Math. Sociol.](#), 1:143–186, 1971. [pdf](#) 
- [24] T. C. Schelling.  
Hockey helmets, concealed weapons, and  
daylight saving: A study of binary choices with  
externalities.  
[J. Conflict Resolut.](#), 17:381–428, 1973. [pdf](#) 
- [25] T. C. Schelling.  
Micromotives and Macrobehavior.  
Norton, New York, 1978.
- [26] D. Sornette.  
Critical Phenomena in Natural Sciences.  
Springer-Verlag, Berlin, 1st edition, 2003.



# References IX

[27] D. J. Watts.

A simple model of global cascades on random networks.

[Proc. Natl. Acad. Sci., 99\(9\):5766–5771, 2002.](#)

[pdf](#) 

[28] D. J. Watts and P. S. Dodds.

Influentials, networks, and public opinion formation.

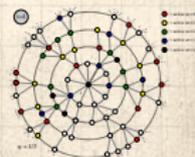
[Journal of Consumer Research, 34:441–458, 2007.](#)

[pdf](#) 

[29] D. J. Watts and P. S. Dodds.

Threshold models of social influence.

In P. Hedström and P. Bearman, editors, [The Oxford Handbook of Analytical Sociology](#), chapter 20, pages 475–497. Oxford University Press, Oxford, UK, 2009. [pdf](#) 



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