

# Allotaxonomy

Last updated: 2023/08/22, 11:48:25 EDT

Principles of Complex Systems, Vols. 1, 2, & 3D  
CSYS/MATH 6701, 6713, & a pretend number,  
2023–2024 | @pocsvox

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center  
Santa Fe Institute | University of Vermont



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A plenitude of  
distances

Rank-turbulence  
divergence

Probability-  
turbulence  
divergence

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Stories

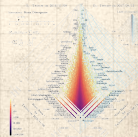
Mechanics of  
Fame

Superspreading

Lexical Ultrafame

Turbulent times

References



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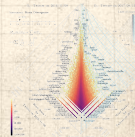
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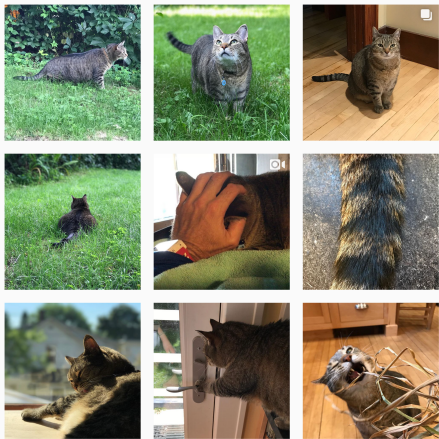
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## Special Guest Executive Producer



 On Instagram at [pratchett\\_the\\_cat](https://www.instagram.com/pratchett_the_cat) 

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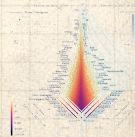
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# Outline

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Probability-turbulence divergence

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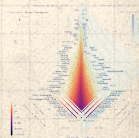
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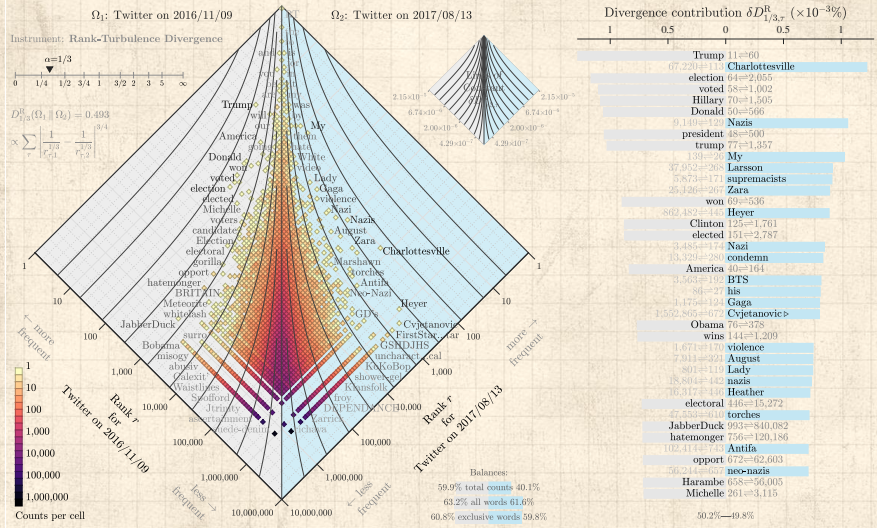
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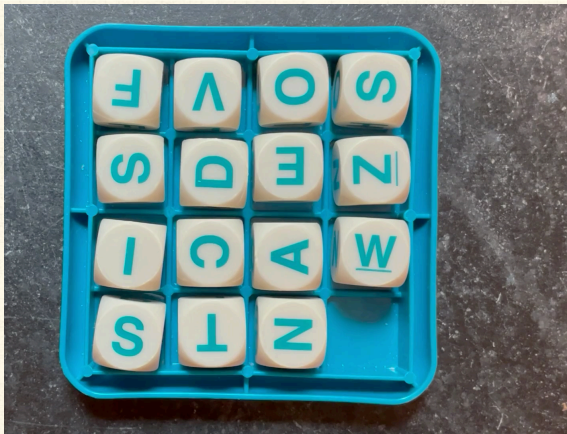
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# Goal—Understand this:



## The Boggoracle Speaks:



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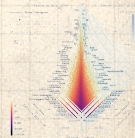
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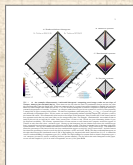
References



Site (papers, examples, code):

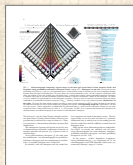
<http://compstorylab.org/allotaxonomy/>

Foundational papers:



"Allotaxonomy and rank-turbulence divergence: A universal instrument for comparing complex systems"

Dodds et al.,  
, 2020. <sup>[9]</sup>



"Probability-turbulence divergence: A tunable allotaxonomic instrument for comparing heavy-tailed categorical distributions"

Dodds et al.,  
, 2020. <sup>[11]</sup>

# Basic science = Describe + Explain:



Dashboards of single scale instruments helps us understand, monitor, and control systems.

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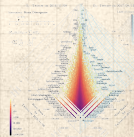
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# Basic science = Describe + Explain:

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- 🧱 Archetype: Cockpit dashboard for flying a plane

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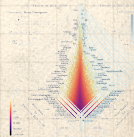
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- 🧱 Okay if comprehensible.

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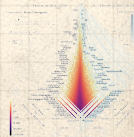
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 Complex systems present two problems for dashboards:

1. Scale with internal diversity of components: We need meters for every species, every company, every word.
2. Tracking change: We need to re-arrange meters on the fly.

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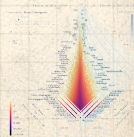
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 Goal—Create comprehensible, dynamically-adjusting, differential dashboards showing two pieces:<sup>1</sup>

1. 'Big picture' map-like overview,
2. A tunable ranking of components.

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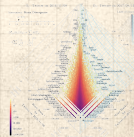
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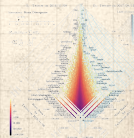
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<sup>1</sup>See the [lexicocalorimeter](#) 

# Baby names, much studied: [23]

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HOW TO: ABSURD SCIENTIFIC ADVICE FOR COMMON REAL-WORLD PROBLEMS

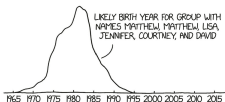
just a decade or so. If you were born in the United States around this year, these are names that are more likely to seem common and generic to you, but are distinctive generational markers.

1890 Will, Maudie, Minnie, May, Cora, Ida, Lela, Hattie, Annie, Ada  
1885 Gracey, Maudie, Will, Minnie, Lela, Edie, May, Cora, Lela, Nellie  
1880 Maudie, May, Minnie, Edie, Mabel, Bessie, Nettie, Hattie, Lela, Cora  
1865 Maudie, Mabel, Minnie, Bessie, Minnie, Myrtle, Hattie, Pearl, Ethel, Bertha  
1860 Mabel, Myrtle, Bessie, Minnie, Pearl, Blanche, Gertrude, Ethel, Minnie, Gladys  
1855 Gladys, Vada, Mabel, Myrtle, Gertrude, Pearl, Bessie, Blanche, Marnie, Ethel  
1910 Thelma, Gladys, Vada, Mildred, Beatrice, Lucille, Gertrude, Agnes, Hazel, Ethel  
1915 Mildred, Lucille, Thelma, Helen, Bernice, Pauline, Eleanor, Beatrice, Ruth, Dorothy  
1920 Marjorie, Dorothy, Mildred, Lucille, Warren, Thelma, Bernice, Virginia, Helen, Jane  
1925 Doris, Jane, Betty, Marjorie, Dorothy, Lorraine, Lisa, Susan, Virginia, Beverly  
1930 Dolores, Betty, Joan, Ethel, David, Norma, Lisa, Billy, Jane, Marilyn  
1935 Shirley, Marlene, Joan, Dolores, Marilyn, Bobby, Betty, Billy, Joyce, Beverly  
1940 Corde, Judith, Judy, Carol, Joyce, Barbara, Joan, Carolyn, Shirley, Jerry  
1945 Judy, Judith, Linda, Carol, Sharon, Sandra, Carolyn, Larry, Anita, Dennis  
1950 Linda, Deborah, Gill, Andy, Gary, Larry, Diane, Dennis, Brenda, Anita  
1955 Debra, Deborah, Cathy, Kathy, Pamela, Randy, Kim, Cynthia, Diane, Cheryl  
1960 Debbie, Kim, Tori, Cindy, Kathy, Cathy, Laverie, Lori, Debra, Ricky  
1965 Lisa, Tammy, Lori, Tiffani, Kim, Alexandra, Tracy, Tina, Dana, Michele  
1970 Tammy, Tanya, Tracy, Todd, Dana, Tina, Sherry, Stacy, Michele, Lisa  
1975 Chad, Jason, Tanya, Heather, Jennifer, Amy, Stacy, Shannon, Sherry, Tara  
1980 Brenda, Crystal, April, Susan, Jeremy, Kim, Tiffany, Jamie, Melissa, Jennifer  
1985 Crystal, Lindsay, Ashley, Lindsey, Doreen, Jessica, Amanda, Tiffany, Crystal, Amber  
1990 Britany, Chelsea, Kelsey, Cody, Ashley, Courtney, Ryan, Kyle, Megan, Jessica  
1995 Taylor, Kelley, Dakota, Austin, Haley, Cody, Tyler, Shelby, Brittany, Kayla  
2000 Destiny, Madison, Haley, Sydney, Alexis, Kaitlyn, Hunter, Brianna, Hannah, Alyssa  
2005 Aislin, Dkya, Guisli, Hailey, Ethan, Madison, Ava, Isabella, Jayden, Aiden  
2010 Jayden, Aislin, Noelle, Addison, Braxton, London, Peyton, Isabella, Ava, Liam  
2015 Arias, Harper, Scarlett, Jason, Grayson, Alexander, Hudson, Liam, Diego, Layla

If kids in your class were named Jeff, Lisa, Michael, Karan, and David, then you were probably born in the mid-1940s. If they were named Jayden, Isabella, Sophia, Ava, and Ethan, then you were probably born somewhere around 2010.

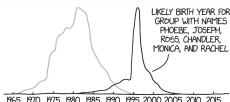
But names can reveal things about age in other ways.

The mid-1990s TV show *Friends* featured six roommates, played by actors named Matthew, Jennifer, Courtney, Lisa, David, and another Matthew. Each of those names has its own popularity curve. If we combine them all, we can guess what year the group of actors was likely born:



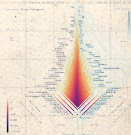
The actors were actually born in the late 1960s, on the very early edge of the popularity of their names. In other words, the actors all have names that were a little before their time. Courtney Cox and Jennifer Aniston had names that didn't really become popular until a decade later. (Maybe people with trendy parents are more likely to wind up in acting.) But the names are generally consistent with their era, if a little ahead of the curve.

We get something very different if we look at the names of their characters—Phoebe, Joseph, Ross, Chandler, Rachel, and Monica:




The show debuted in 1994. There's a clear spike in popularity of the names in 1995 and 1996, which can probably be attributed to the show putting the names in the minds of new parents. But it's not just the show—that name combination was clearly on the rise in the years before *Friends* premiered. It's possible that parents looking for good names for their children are influenced by some of the same cultural trends as TV writers looking for good names for their characters.

# How to build a dynamical dashboard that helps sort through a massive number of interconnected time series?

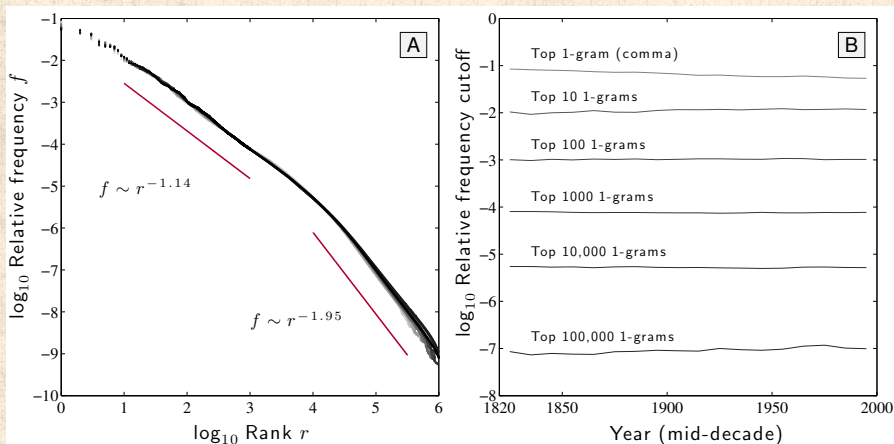




"Is language evolution grinding to a halt? The scaling of lexical turbulence in English fiction suggests it is not" 

Pechenick, Danforth, Dodds, Alshaabi, Adams, Dewhurst, Reagan, Danforth, Reagan, and Danforth.

Journal of Computational Science, **21**, 24–37, 2017. <sup>[25]</sup>



For language, Zipf's law has two scaling regimes: <sup>[34]</sup>

$$f \sim \begin{cases} r^{-\alpha} & \text{for } r \ll r_b, \\ r^{-\alpha'} & \text{for } r \gg r_b, \end{cases}$$

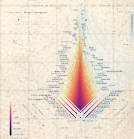
When comparing two texts, define Lexical turbulence as flux of words across a frequency threshold:

$$\phi \sim \begin{cases} f_{\text{thr}}^{-\mu} & \text{for } f_{\text{thr}} \ll f_b, \\ f_{\text{thr}}^{-\mu'} & \text{for } f_{\text{thr}} \gg f_b, \end{cases}$$

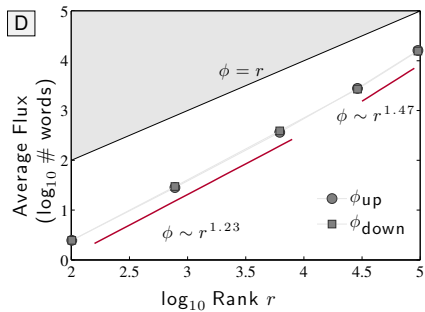
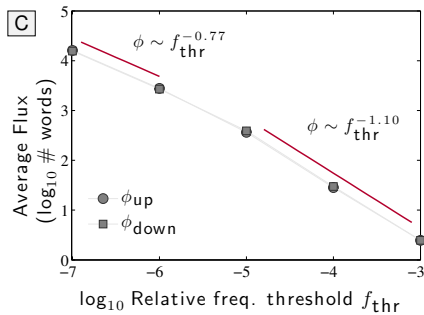
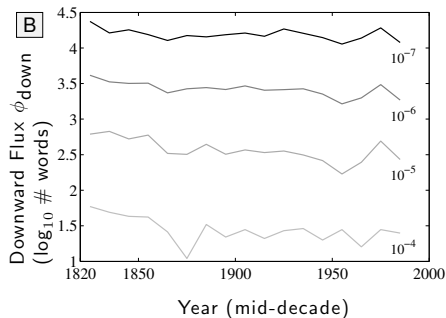
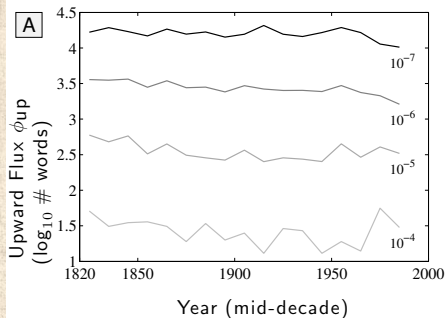
Estimates:  $\mu \simeq 0.77$  and  $\mu' \simeq 1.10$ , and  $f_b$  is the scaling break point.

$$\phi \sim \begin{cases} r^\nu = r^{\alpha\mu'} & \text{for } r \ll r_b, \\ r^{\nu'} = r^{\alpha'\mu} & \text{for } r \gg r_b. \end{cases}$$

Estimates: Lower and upper exponents  $\nu \simeq 1.23$  and  $\nu' \simeq 1.47$ .



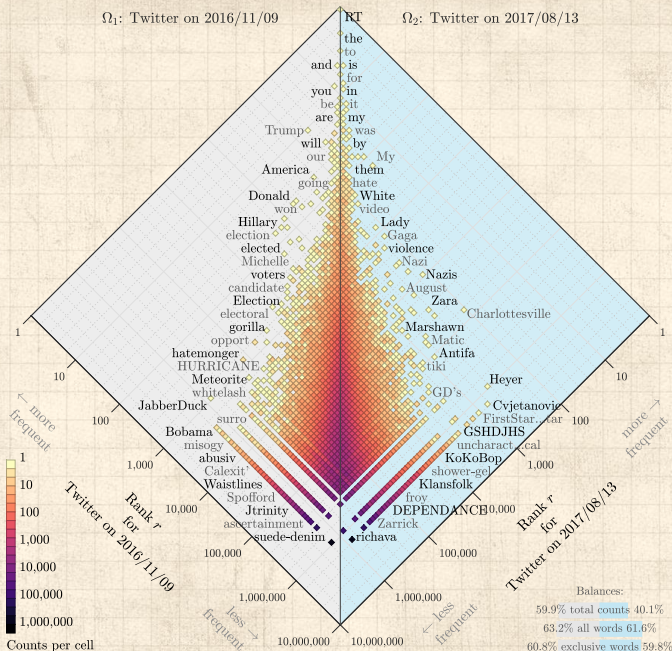




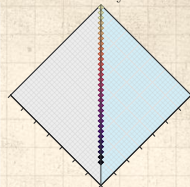
### A. Rank-turbulence histogram:

$\Omega_1$ : Twitter on 2016/11/09

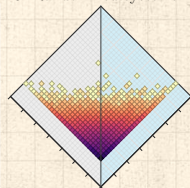
$\Omega_2$ : Twitter on 2017/08/13



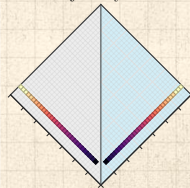
### B. Identical systems:



### C. Randomized systems:



### D. Disjoint systems:



Balances:

59.9% total counts 40.1%

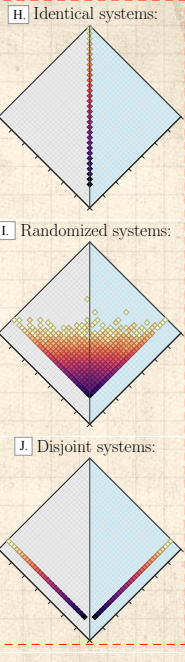
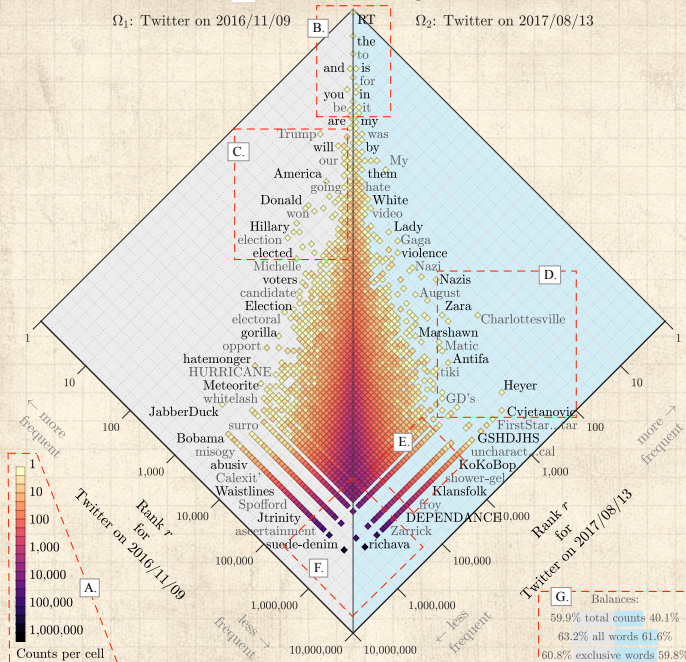
63.2% all words 61.6%

60.8% exclusive words 59.8%

# Rank-turbulence histogram:

$\Omega_1$ : Twitter on 2016/11/09

$\Omega_2$ : Twitter on 2017/08/13



**G.** Balances:  
59.9% total counts 40.1%  
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G.

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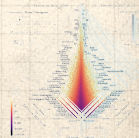
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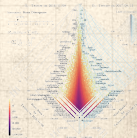
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## Exclusive types:

 We call types that are present in one system only 'exclusive types'.

 When warranted, we will use expressions of the form  $\Omega^{(1)}$ -exclusive and  $\Omega^{(2)}$ -exclusive to indicate to which system an exclusive type belongs.



# Probability-turbulence histogram:

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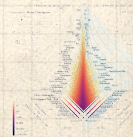
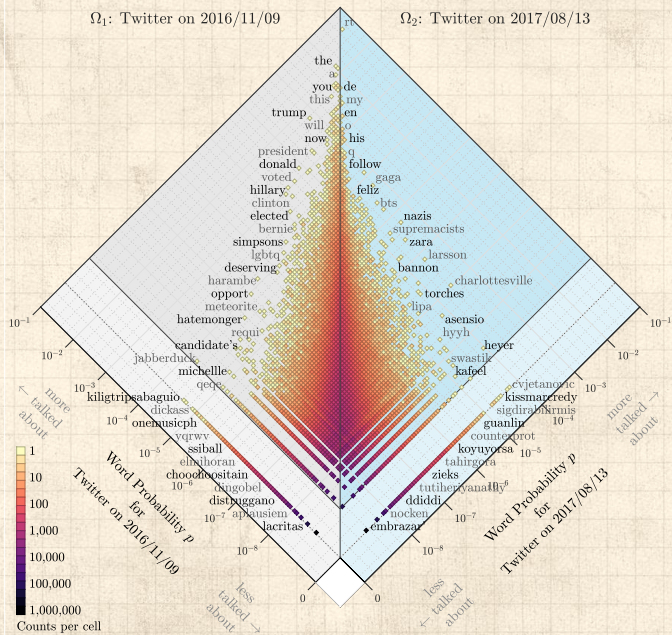
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So, so many ways to compare probability distributions:



"Families of Alpha- Beta- and Gamma-Divergences: Flexible and Robust Measures of Similarities" 

Cichocki and Amari,  
Entropy, **12**, 1532-1568, 2010. [6]

"Comprehensive survey on distance/similarity measures between probability density functions" 

Sung-Hyuk Cha,  
International Journal of Mathematical Models and Methods in Applied Sciences, **1**, 300-307, 2007. [3]



Comparisons are distances, divergences, similarities, inner products, fidelities ...



60ish kinds of comparisons grouped into 10 families



A worry: Subsampled distributions with very heavy tails

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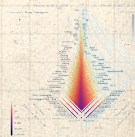
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# Quite the festival:

**Table 1. L<sub>p</sub> Minkowski family**

|                              |  |
|------------------------------|--|
| 1. Euclidean L <sub>2</sub>  | $d_{min} = \sqrt{\frac{P-Q}{P+Q}}$ (1)                     |
| 2. City block L <sub>1</sub> | $d_{min} = \frac{1}{2} \left  \frac{P-Q}{P+Q} \right $ (2) |
| 3. Minkowski L <sub>p</sub>  | $d_{min} = \sqrt[p]{\frac{P-Q}{P+Q}}$ (3)                  |
| 4. Chebyshev L <sub>∞</sub>  | $d_{min} = \max\{ P-Q \}$ (4)                              |

**Table 2. L<sub>p</sub> family**

|             |   |
|-------------|---|
| 5. Sorenson | $d_{min} = \frac{\sum (P-Q)}{\sum (P+Q)}$ (5) |
|-------------|---|

**6. Gower**

$$d_{min} = \frac{1}{2} \sqrt{\frac{P-Q}{P+Q}}$$
 (6)

$$+ \frac{1}{2} \sqrt{\sum (P-Q)}$$
 (7)

**7. Soregol**

$$d_{min} = \frac{\sum (P-Q)}{\sum \max(P,Q)}$$
 (8)

**8. Kulczyński d**

$$d_{min} = \frac{\sum (P-Q)}{\sum \min(P,Q)}$$
 (9)

**9. Canberra**

$$d_{min} = \sqrt{\frac{P-Q}{P+Q}}$$
 (10)

**10. Lovrentzian**

$$d_{min} = \sum \ln(1 + |P-Q|)$$
 (11)

\* L<sub>p</sub> family ⇒ Intersection (13), Wave Hodges (15), Czekanowski (16), Ruszka (21), Tanimoto (23), etc.

**Table 3. Intersection family**

|                  |   |
|------------------|---|
| 11. Intersection | $s_{in} = \sum \min(P,Q)$ (12)                              |
|                  | $d_{min} = 1 - s_{in} = \frac{1}{2} \sum (P-Q)$ (13)        |
| 12. Wave Hodges  | $d_{min} = \frac{\sum (\min(P,Q))}{\sum \max(P,Q)}$ (14)    |
|                  | $= \frac{\sum (P-Q)}{\sum \max(P,Q)}$ (15)                  |
| 13. Czekanowski  | $s_{in} = \frac{\sum \min(P,Q)}{\sum (P+Q)}$ (16)           |
|                  | $d_{min} = 1 - s_{in} = \frac{\sum (P-Q)}{\sum (P+Q)}$ (17) |

**Table 4. Inner Product family**

|                          |   |
|--------------------------|---|
| 18. Inner Product        | $s_{in} = P \cdot Q = \sum P_i Q_i$ (24)                                    |
| 19. Harmonic mean        | $s_{in} = \frac{\sum P_i Q_i}{\sum (P_i + Q_i)}$ (25)                       |
| 20. Cosine               | $s_{in} = \frac{\sum P_i Q_i}{\sqrt{\sum P_i^2} \sqrt{\sum Q_i^2}}$ (26)    |
| 21. Kumar-Hauschok (PCE) | $s_{in} = \frac{\sum P_i Q_i}{\sum P_i^2 + \sum Q_i^2 - \sum P_i Q_i}$ (27) |
| 22. Jaccard              | $s_{in} = \frac{\sum P_i Q_i}{\sum P_i^2 + \sum Q_i^2 - \sum P_i Q_i}$ (28) |
| 23. Dice                 | $s_{in} = \frac{\sum P_i Q_i}{\sum P_i^2 + \sum Q_i^2}$ (29)                |
|                          | $d_{min} = 1 - s_{in} = \frac{\sum (P-Q)^2}{\sum P_i^2 + \sum Q_i^2}$ (30)  |
| 24. Fidelity             | $s_{in} = \sum \sqrt{P_i Q_i}$ (32)   |
| 25. Bhattacharyya        | $d_{in} = -\ln \sum \sqrt{P_i Q_i}$ (33)                                    |
| 26. Hellinger            | $d_{in} = \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$ (34)                      |
|                          | $= \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$ (35)                             |

**Table 5. Fidelity family or Squared-chord family**

|                   |  |
|-------------------|--|
| 24. Fidelity      | $s_{in} = \sum \sqrt{P_i Q_i}$ (32)                    |
| 25. Bhattacharyya | $d_{in} = -\ln \sum \sqrt{P_i Q_i}$ (33)               |
| 26. Hellinger     | $d_{in} = \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$ (34) |
|                   | $= \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$ (35)        |

14. Moyalta  $d_{min} = \frac{\sum \max(P,Q)}{\sum (P+Q)}$  (18)

$d_{min} = 1 - s_{in} = \frac{\sum \max(P,Q)}{\sum (P+Q)}$  (19)

15. Kulczyński v  $s_{in} = \frac{1}{d_{min}} \frac{\sum \max(P,Q)}{\sum (P+Q)}$  (20)

16. Ruszka  $s_{in} = \frac{\sum \max(P,Q)}{\sum \min(P,Q)}$  (21)

17. Tanimoto  $d_{min} = \frac{\sum (P-Q) \cdot \sum \min(P,Q)}{\sum (P+Q) \cdot \sum \max(P,Q)}$  (22)

$d_{min} = \frac{\sum \max(P,Q) \cdot \sum \min(P,Q)}{\sum \max(P,Q)}$  (23)

**Table 6. Squared L<sub>p</sub> family or v<sup>2</sup> family**

|                                      |  |
|--------------------------------------|--|
| 29. Squared Euclidean                | $d_{min} = \sum (P_i - Q_i)^2$ (40)                                |
| 30. Pearson $\chi^2$                 | $d_{in}(P,Q) = \frac{\sum (P_i - Q_i)^2}{\sum Q_i}$ (41)           |
| 31. Neyman $\chi^2$                  | $d_{in}(P,Q) = \frac{\sum (P_i - Q_i)^2}{\beta}$ (42)              |
| 32. Squared $\chi^2$                 | $d_{min} = \frac{\sum (P_i - Q_i)^2}{P_i + Q_i}$ (43)              |
| 33. Probabilistic Symmetric $\chi^2$ | $d_{min} = \frac{\sum (P_i - Q_i)^2}{P_i + Q_i}$ (44)              |
| 34. Divergence                       | $d_{min} = 2 \sum \frac{(P_i - Q_i)^2}{(P_i + Q_i)}$ (45)          |
| 35. Clark                            | $d_{in} = \sqrt{\frac{ \sum (P_i - Q_i) }{\sum (P_i + Q_i)}}$ (46) |

36. Additive Symmetric  $\chi^2$   $d_{min} = \frac{\sum (P_i - Q_i)^2}{\sum \max(P_i + Q_i)}$  (47)

\* Squared L<sub>p</sub> family ⇒ Jaccard (29), Dice (31)

**Table 7. Shannon's entropy family**

|                       |   |
|-----------------------|---|
| 37. Kullback-Leibler  | $d_{in} = \sum P_i \ln \frac{P_i}{Q_i}$ (48)  |
| 38. Jeffreys          | $d_{in} = \sum (P_i - Q_i) \ln \frac{P_i}{Q_i}$ (49)  |
| 39. K. divergence     | $d_{in} = \sum P_i \ln \frac{2P_i}{P_i + Q_i}$ (50)   |
| 40. Topoc             | $d_{in} = \frac{1}{2} \sum P_i \ln \left( \frac{2P_i}{P_i + Q_i} \right) + Q_i \ln \left( \frac{2Q_i}{P_i + Q_i} \right)$ (51)  |
| 41. Jensen-Shannon    | $d_{in} = \frac{1}{2} \left[ \sum P_i \ln \left( \frac{2P_i}{P_i + Q_i} \right) + \sum Q_i \ln \left( \frac{2Q_i}{P_i + Q_i} \right) \right]$ (52)                      |
| 42. Jensen divergence | $d_{in} = \frac{1}{2} \left[ \sum P_i \ln \frac{P_i}{P_i + Q_i} + \sum Q_i \ln \frac{Q_i}{P_i + Q_i} \right] + \frac{1}{2} \ln \left( \frac{P_i + Q_i}{2} \right)$ (53) |

27. Matusita  $d_{in} = \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$  (36)

$= \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$  (37)

28. Squared-chord  $d_{in} = \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$  (38)

$s_{in} = 1 - d_{in}$   $s_{in} = \sum \sqrt{P_i Q_i} - 1$  (39)

**Table 8. Combinations**

|                               |   |
|-------------------------------|---|
| 43. Taneja                    | $d_{in} = \frac{\sum (P_i - Q_i)}{2} \ln \left  \frac{P_i + Q_i}{2 P_i Q_i} \right $ (54) |
| 44. Kumar-Johnson             | $d_{in} = \sum \left[ \frac{(P_i - Q_i)^2}{2 P_i Q_i} \right]^{1/2}$ (55)                 |
| 45. Avgul(L, L <sub>∞</sub> ) | $d_{min} = \frac{\sum (P_i - Q_i) \cdot \max\{P_i, Q_i\}}{2}$ (56)                        |

**Table 10. Vicissitude**

|                          |  |
|--------------------------|--|
| Vicis-Wave Hodges        | $d_{min} = \frac{\sum (P_i - Q_i)}{\sum \max(P_i, Q_i)}$ (60)  |
| Vicis-Symmetric $\chi^2$ | $d_{min} = \frac{\sum (P_i - Q_i)^2}{\sum \max(P_i, Q_i)}$ (61)                                      |
| Vicis-Symmetric $\chi^2$ | $d_{min} = \frac{\sum (P_i - Q_i)^2}{\sum \max(P_i, Q_i)}$ (62)                                      |
| Vicis-Symmetric $\chi^2$ | $d_{min} = \frac{\sum (P_i - Q_i)^2}{\sum \max(P_i, Q_i)}$ (63)                                      |
| max-Symmetric            | $d_{in} = \max \left( \frac{\sum (P_i - Q_i)^2}{\beta}, \frac{\sum (P_i - Q_i)^2}{Q_i} \right)$ (64) |
| min-Symmetric            | $d_{in} = \max \left( \frac{\sum (P_i - Q_i)^2}{\beta}, \frac{\sum (P_i - Q_i)^2}{P_i} \right)$ (65) |

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Probability-turbulence divergence

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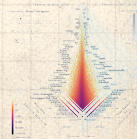
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## Shannon tried to slow things down in 1956:



"The bandwagon" 

Claude E Shannon,  
IRE Transactions on Information Theory, **2**,  
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 "Information theory has ... become something of a scientific bandwagon."

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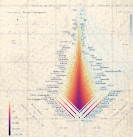
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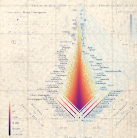
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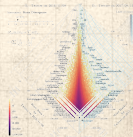


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-  "Information theory has ... become something of a scientific bandwagon."
-  "While ... information theory is indeed a valuable tool ... [it] is certainly no panacea for the communication engineer or ... for anyone else."
-  "A few first rate research papers are preferable to a large number that are poorly conceived or half-finished."





# We want two main things:

1. A measure of difference between systems
2. A way of sorting which types/species/words contribute to that difference

| Table 1. $L_p$ Minkowski family |   |     |
|---------------------------------|---|-----|
| 1. Euclidean $L_2$              | $d_{Euc} = \sqrt{\sum_{i=1}^d  P_i - Q_i ^2}$   | (1) |
| 2. City block $L_1$             | $d_{CB} = \sum_{i=1}^d  P_i - Q_i $             | (2) |
| 3. Minkowski $L_p$              | $d_{Mk} = \sqrt[p]{\sum_{i=1}^d  P_i - Q_i ^p}$ | (3) |
| 4. Chebyshev $L_\infty$         | $d_{Cheb} = \max_i  P_i - Q_i $                 | (4) |

| Table 2. $L_1$ family |   |     |
|-----------------------|---|-----|
| 5. Sørensen           | $d_{sor} = \frac{\sum_{i=1}^d  P_i - Q_i }{\sum_{i=1}^d (P_i + Q_i)}$ | (5) |

|          |  |     |
|----------|--|-----|
| 6. Gower | $d_{gow} = \frac{1}{d} \sum_{i=1}^d \frac{ P_i - Q_i }{R_i}$ | (6) |
|          | $= \frac{1}{d} \sum_{i=1}^d  P_i - Q_i $                     | (7) |

|            |   |     |
|------------|---|-----|
| 7. Soergel | $d_{sg} = \frac{\sum_{i=1}^d  P_i - Q_i }{\sum_{i=1}^d \max(P_i, Q_i)}$ | (8) |
|------------|---|-----|

|                   |  |     |
|-------------------|--|-----|
| 8. Kulczynski $d$ | $d_{kul} = \frac{\sum_{i=1}^d  P_i - Q_i }{\sum_{i=1}^d \min(P_i, Q_i)}$ | (9) |
|-------------------|--|-----|

|             |  |      |
|-------------|--|------|
| 9. Canberra | $d_{can} = \sum_{i=1}^d \frac{ P_i - Q_i }{P_i + Q_i}$ | (10) |
|-------------|--|------|

|                |   |      |
|----------------|---|------|
| 10. Lorentzian | $d_{lor} = \sum_{i=1}^d \ln(1 +  P_i - Q_i )$ | (11) |
|----------------|---|------|

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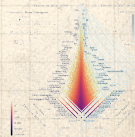
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|          |  |     |
|----------|--|-----|
| 6. Gower | $d_{gow} = \frac{1}{d} \sum_{i=1}^d \frac{ P_i - Q_i }{R_i}$ | (6) |
|          | $= \frac{1}{d} \sum_{i=1}^d  P_i - Q_i $                     | (7) |

|            |   |     |
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|------------|---|-----|

|                   |  |     |
|-------------------|--|-----|
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|-------------------|--|-----|

|             |  |      |
|-------------|--|------|
| 9. Canberra | $d_{can} = \sum_{i=1}^d \frac{ P_i - Q_i }{P_i + Q_i}$ | (10) |
|-------------|--|------|

|                |   |      |
|----------------|---|------|
| 10. Lorentzian | $d_{lor} = \sum_{i=1}^d \ln(1 +  P_i - Q_i )$ | (11) |
|----------------|---|------|

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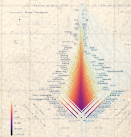
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We want two main things:

1. A measure of difference between systems
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For sorting, many comparisons give the same ordering.



A few basic building blocks:

- $|P_i - Q_i|$  (dominant)
- $\max(P_i, Q_i)$
- $\min(P_i, Q_i)$
- $P_i Q_i$
- $|P_i^{1/2} - Q_i^{1/2}|$  (Hellinger)

**Table 1.**  $L_p$  Minkowski family

|                    |   |     |
|--------------------|---|-----|
| 1. Euclidean $L_2$ | $d_{Euc} = \sqrt{\sum_{i=1}^d  P_i - Q_i ^2}$ | (1) |
|--------------------|---|-----|

|                     |                                     |     |
|---------------------|-------------------------------------|-----|
| 2. City block $L_1$ | $d_{CB} = \sum_{i=1}^d  P_i - Q_i $ | (2) |
|---------------------|-------------------------------------|-----|

|                    |   |     |
|--------------------|---|-----|
| 3. Minkowski $L_p$ | $d_{Mk} = \sqrt[p]{\sum_{i=1}^d  P_i - Q_i ^p}$ | (3) |
|--------------------|---|-----|

|                         |                                 |     |
|-------------------------|---------------------------------|-----|
| 4. Chebyshev $L_\infty$ | $d_{Cheb} = \max_i  P_i - Q_i $ | (4) |
|-------------------------|---------------------------------|-----|

**Table 2.**  $L_1$  family

|             |   |     |
|-------------|---|-----|
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|-------------|---|-----|

|          |  |     |
|----------|--|-----|
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|----------|--|-----|

|  |  |     |
|--|--|-----|
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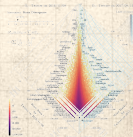
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sortings are more  
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|                           |   |     |
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**Table 2.**  $L_1$  family

|   |  |      |
|---|--|------|
| 5. Sørensen   | $d_{sor} = \frac{\sum_{i=1}^d  P_i - Q_i }{\sum_{i=1}^d (P_i + Q_i)}$    | (5)  |
| 6. Gower  | $d_{gow} = \frac{1}{d} \sum_{i=1}^d \frac{ P_i - Q_i }{R_i}$             | (6)  |
|   | $= \frac{1}{d} \sum_{i=1}^d  P_i - Q_i $                                 | (7)  |
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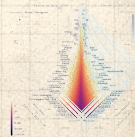
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$$5. \text{ Sørensen} \quad d_{\text{sov}} = \frac{\sum_{i=1}^d |P_i - Q_i|}{\sum_{i=1}^d (P_i + Q_i)} \quad (5)$$

$$6. \text{ Gower} \quad d_{\text{gow}} = \frac{1}{d} \sum_{i=1}^d \frac{|P_i - Q_i|}{R_i} \quad (6)$$

$$= \frac{1}{d} \sum_{i=1}^d |P_i - Q_i| \quad (7)$$

$$7. \text{ Soergel} \quad d_{\text{sg}} = \frac{\sum_{i=1}^d |P_i - Q_i|}{\sum_{i=1}^d \max(P_i, Q_i)} \quad (8)$$

$$8. \text{ Kulczynski } d \quad d_{\text{kul}} = \frac{\sum_{i=1}^d |P_i - Q_i|}{\sum_{i=1}^d \min(P_i, Q_i)} \quad (9)$$

$$9. \text{ Canberra} \quad d_{\text{can}} = \sum_{i=1}^d \frac{|P_i - Q_i|}{P_i + Q_i} \quad (10)$$

$$10. \text{ Lorentzian} \quad d_{\text{Lor}} = \sum_{i=1}^d \ln(1 + |P_i - Q_i|) \quad (11)$$

\*  $L_1$  family  $\supset$  {Intersectoin (13), Wave Hedges (15), Czekanowski (16), Ruzicka (21), Tanimoto (23), etc}.

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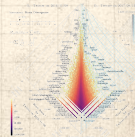
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## Shannon's Entropy:

$$H(P) = \langle \log_2 \frac{1}{p_\tau} \rangle = \sum_{\tau \in R_{1,2;\alpha}} p_\tau \log_2 \frac{1}{p_\tau} \quad (1)$$

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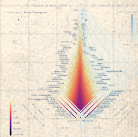
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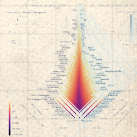
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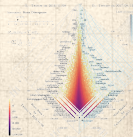
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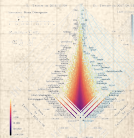
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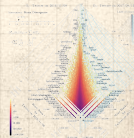
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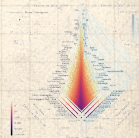
New problem: Re-read solution.



🌀 Jensen-Shannon divergence (JSD): [19, 13, 24, 3]

$$\begin{aligned} D^{\text{JS}}(P_1 \parallel P_2) &= \frac{1}{2} D^{\text{KL}}\left(P_1 \parallel \frac{1}{2}[P_1 + P_2]\right) + \frac{1}{2} D^{\text{KL}}\left(P_2 \parallel \frac{1}{2}[P_1 + P_2]\right) \\ &= \frac{1}{2} \sum_{\tau \in R_{1,2;\alpha}} \left( p_{1,\tau} \log_2 \frac{p_{1,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} + p_{2,\tau} \log_2 \frac{p_{2,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} \right). \end{aligned} \quad (3)$$

🌀 Involving a third intermediate averaged system means JSD is now finite:  $0 \leq D^{\text{JS}}(P_1 \parallel P_2) \leq 1$ .





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 &= \frac{1}{2} \sum_{\tau \in R_{1,2;\alpha}} \left( p_{1,\tau} \log_2 \frac{p_{1,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} + p_{2,\tau} \log_2 \frac{p_{2,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} \right).
 \end{aligned} \tag{3}$$

🌀 Involving a third intermediate averaged system means JSD is now finite:  $0 \leq D^{\text{JS}}(P_1 \parallel P_2) \leq 1$ .

🌀 Generalized entropy divergence: [6]

$$\begin{aligned}
 D_{\alpha}^{\text{AS2}}(P_1 \parallel P_2) &= \frac{1}{\alpha(\alpha-1)} \sum_{\tau \in R_{1,2;\alpha}} \left[ (p_{\tau,1}^{1-\alpha} + p_{\tau,2}^{1-\alpha}) \left( \frac{p_{\tau,1} + p_{\tau,2}}{2} \right)^{\alpha} - (p_{\tau,1} + p_{\tau,2}) \right].
 \end{aligned} \tag{4}$$

Produces JSD when  $\alpha \rightarrow 0$ .

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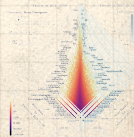
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$\Omega_1$ : Twitter on 2016/11/09

$\Omega_2$ : Twitter on 2017/08/13

Divergence contribution  $\delta D_{0,r}^H$  (%)

Instrument: Sym. Gen. Entropy Div.

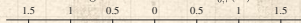
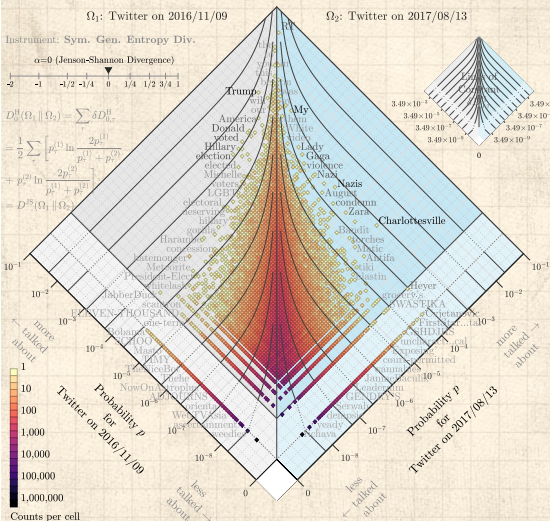
$\alpha=0$  (Jenson-Shannon Divergence)

$$D_{0,r}^H(\Omega_1 || \Omega_2) = \sum \delta D_{0,r}^H$$

$$= \frac{1}{2} \sum_r \left[ p_r^{(1)} \ln \frac{2p_r^{(1)}}{p_r^{(1)} + p_r^{(2)}} \right]$$

$$+ p_r^{(2)} \ln \frac{2p_r^{(2)}}{p_r^{(1)} + p_r^{(2)}}$$

$$= D^{JS}(\Omega_1 || \Omega_2)$$



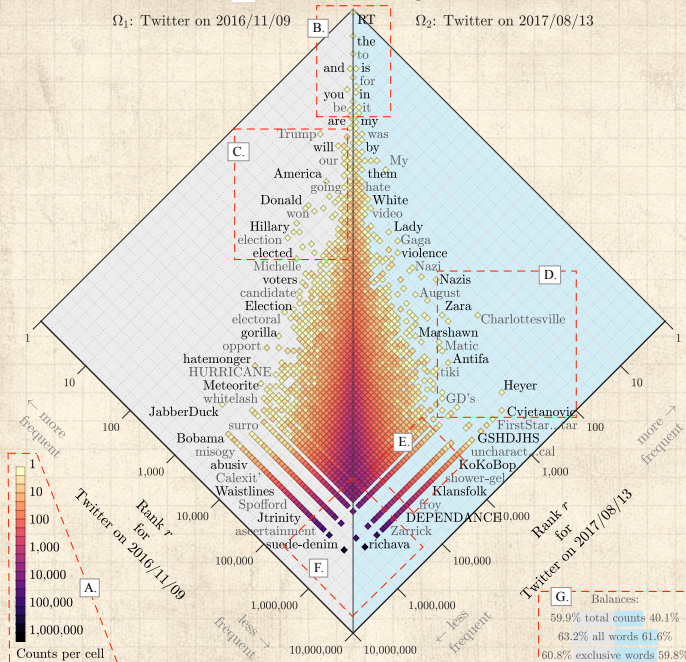
|            |                 |
|------------|-----------------|
| Trump      | 11=60           |
| voted      | 58=1,002        |
| Donald     | 50=566          |
| election   | 64=2,055        |
| president  | 48=500          |
| Hillary    | 70=1,505        |
| trump      | 77=1,357        |
| America    | 40=164          |
| won        | 69=536          |
| 67,220=113 | Charlottesville |
| 139=20     | My              |
| 9,149=129  | Nazis           |
| Clinton    | 125=1,761       |
| Obama      | 76=378          |
| elected    | 151=2,787       |
| wins       | 144=1,209       |
| will       | 23=51           |
| country    | 71=216          |
| 5,873=171  | supremacists    |
| 1,175=124  | Gaga            |
| 3,485=174  | Nazi            |
| 1=1        | RT              |
| 86=27      | his             |
| 801=119    | Lady            |
| votes      | 180=1,422       |
| 3,563=192  | BTS             |
| 37,952=268 | Larsson         |
| 25,126=267 | Zara            |
| 13,329=280 | condemn         |
| 1,671=170  | violence        |
| Michelle   | 261=3,115       |
| our        | 41=72           |
| 7,911=321  | August          |
| President  | 93=228          |
| voters     | 306=4,453       |
| 1,325=187  | supremacy       |
| people     | 27=45           |
| candidate  | 362=5,584       |
| 1,761=231  | police          |
| women      | 124=315         |

52.9%—47.1%

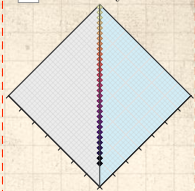
# Rank-turbulence histogram:

$\Omega_1$ : Twitter on 2016/11/09

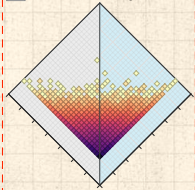
$\Omega_2$ : Twitter on 2017/08/13



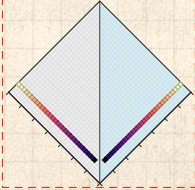
**H.** Identical systems:



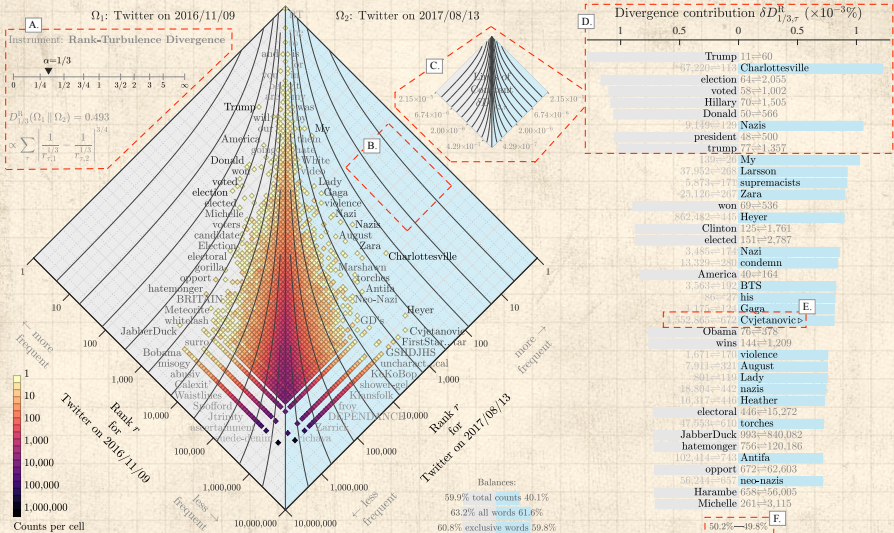
**I.** Randomized systems:



**J.** Disjoint systems:



**G.** Balances:  
59.9% total counts 40.1%  
63.2% all words 61.6%  
60.8% exclusive words 59.8%



# Desirable rank-turbulence divergence features:

## 1. Rank-based.

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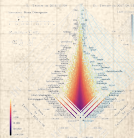
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## Desirable rank-turbulence divergence features:

1. Rank-based.
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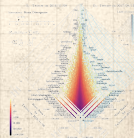
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## Desirable rank-turbulence divergence features:

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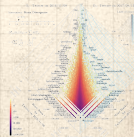
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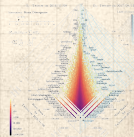
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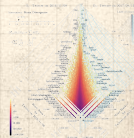
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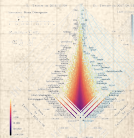
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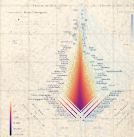
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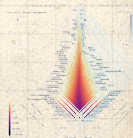
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8. Tunable.
9. Story-finding: Features 1–8 combine to show which component types are most 'important'

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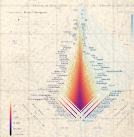
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# Some good things about ranks:

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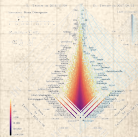
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# Some good things about ranks:

 Working with ranks is intuitive

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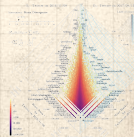
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## Some good things about ranks:



Working with ranks is intuitive



Affords some powerful statistics (e.g., Spearman's rank correlation coefficient)

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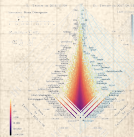
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## Some good things about ranks:

- Working with ranks is intuitive
- Affords some powerful statistics (e.g., Spearman's rank correlation coefficient)
- Can be used to generalize beyond systems with probabilities

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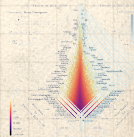
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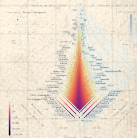
## Some good things about ranks:

- Working with ranks is intuitive
- Affords some powerful statistics (e.g., Spearman's rank correlation coefficient)
- Can be used to generalize beyond systems with probabilities

## A start:

$$\left| \frac{1}{r_{\tau,1}} - \frac{1}{r_{\tau,2}} \right|. \quad (5)$$

- Inverse of rank gives an increasing measure of 'importance'
- High rank means closer to rank 1
- We assign tied ranks for components of equal 'size'



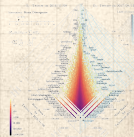
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- Issue: Biases toward high rank components



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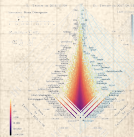
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We introduce a tuning parameter:

$$\left| \frac{1}{[r_{\tau,1}]^{\alpha}} - \frac{1}{[r_{\tau,2}]^{\alpha}} \right|^{1/\alpha} \quad (6)$$



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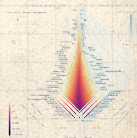
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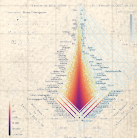
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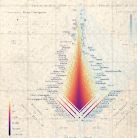
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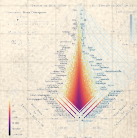
- As  $\alpha \rightarrow 0$ , high ranked components are increasingly dampened
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- As  $\alpha \rightarrow \infty$ , high rank components will dominate.



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- As  $\alpha \rightarrow 0$ , high ranked components are increasingly dampened
- For words in texts, for example, the weight of common words and rare words move increasingly closer together.
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- For texts, the contributions of rare words will vanish.





## Trouble:



The limit of  $\alpha \rightarrow 0$  does not behave well for

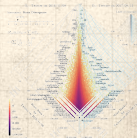
$$\left| \frac{1}{[r_{\tau,1}]^{\alpha}} - \frac{1}{[r_{\tau,2}]^{\alpha}} \right|^{1/\alpha}.$$



The leading order term is:

$$(1 - \delta_{r_{\tau,1} r_{\tau,2}}) \alpha^{1/\alpha} \left| \ln \frac{r_{\tau,1}}{r_{\tau,2}} \right|^{1/\alpha}, \quad (7)$$

which heads toward  $\infty$  as  $\alpha \rightarrow 0$ .



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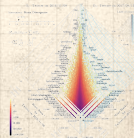
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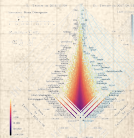
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🧱 But the insides look nutritious:

$$\left| \ln \frac{r_{\tau,1}}{r_{\tau,2}} \right|$$

is a nicely interpretable log-ratio of ranks.



## Some reworking:

$$\delta D_{\alpha, \tau}^R(R_1 \parallel R_2) \propto \frac{\alpha + 1}{\alpha} \left| \frac{1}{[r_{\tau, 1}]^\alpha} - \frac{1}{[r_{\tau, 2}]^\alpha} \right|^{1/(\alpha+1)} \quad (8)$$

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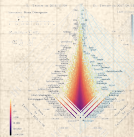
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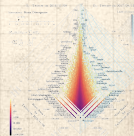
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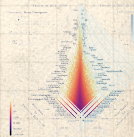
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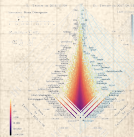
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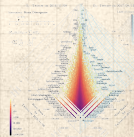
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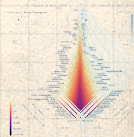




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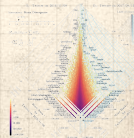
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## Rank-turbulence divergence:

$$D_{\alpha}^R(R_1 \parallel R_2) = \frac{1}{\mathcal{N}_{1,2;\alpha}} \sum_{\tau \in R_{1,2;\alpha}} \delta D_{\alpha, \tau}^R(R_1 \parallel R_2) \quad (9)$$



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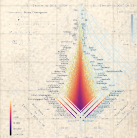
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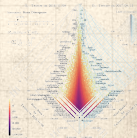
## Normalization:

 Take a data-driven rather than analytic approach  
to determining  $\mathcal{N}_{1,2;\alpha}$ .



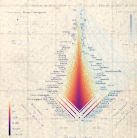
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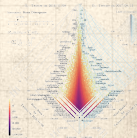
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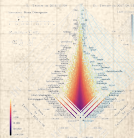
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- Ensures:  $0 \leq D_{\alpha}^R(R_1 \parallel R_2) \leq 1$
- Limits of 0 and 1 correspond to the two systems having identical and disjoint Zipf distributions.




## Rank-turbulence divergence:

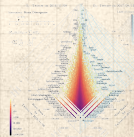
Summing over all types, dividing by a normalization prefactor  $\mathcal{N}_{1,2;\alpha}$  we have our prototype:

$$D_{\alpha}^R(R_1 || R_2) = \frac{1}{\mathcal{N}_{1,2;\alpha}} \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_{1,2;\alpha}} \left| \frac{1}{[r_{\tau,1}]^{\alpha}} - \frac{1}{[r_{\tau,2}]^{\alpha}} \right|^{1/(\alpha+1)} \quad (10)$$



## General normalization:

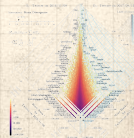
 If the Zipf distributions are disjoint, then in  $\Omega^{(1)}$ 's merged ranking, the rank of all  $\Omega^{(2)}$  types will be  $r = N_1 + \frac{1}{2}N_2$ , where  $N_1$  and  $N_2$  are the number of distinct types in each system.





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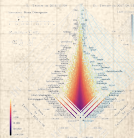
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- ☰ Similarly,  $\Omega^{(2)}$ 's merged ranking will have all of  $\Omega^{(1)}$ 's types in last place with rank  $r = N_2 + \frac{1}{2}N_1$ .



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- ☰ The normalization is then:

$$\begin{aligned} \mathcal{N}_{1,2;\alpha} = & \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_1} \left| \frac{1}{[r_{\tau,1}]^\alpha} - \frac{1}{[N_1 + \frac{1}{2}N_2]^\alpha} \right|^{1/(\alpha+1)} \\ & + \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_2} \left| \frac{1}{[N_2 + \frac{1}{2}N_1]^\alpha} - \frac{1}{[r_{\tau,2}]^\alpha} \right|^{1/(\alpha+1)} \end{aligned} \quad (11)$$



Limit of  $\alpha \rightarrow 0$ :

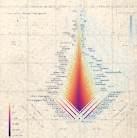
$$D_0^R(R_1 \parallel R_2) = \sum_{\tau \in R_{1,2;\alpha}} \delta D_{0,\tau}^R = \frac{1}{\mathcal{N}_{1,2;0}} \sum_{\tau \in R_{1,2;\alpha}} \left| \ln \frac{r_{\tau,1}}{r_{\tau,2}} \right|, \quad (12)$$

where

$$\mathcal{N}_{1,2;0} = \sum_{\tau \in R_1} \left| \ln \frac{r_{\tau,1}}{N_1 + \frac{1}{2}N_2} \right| + \sum_{\tau \in R_2} \left| \ln \frac{r_{\tau,2}}{\frac{1}{2}N_1 + N_2} \right|. \quad (13)$$



Largest rank ratios dominate.




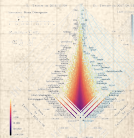
Limit of  $\alpha \rightarrow \infty$ :

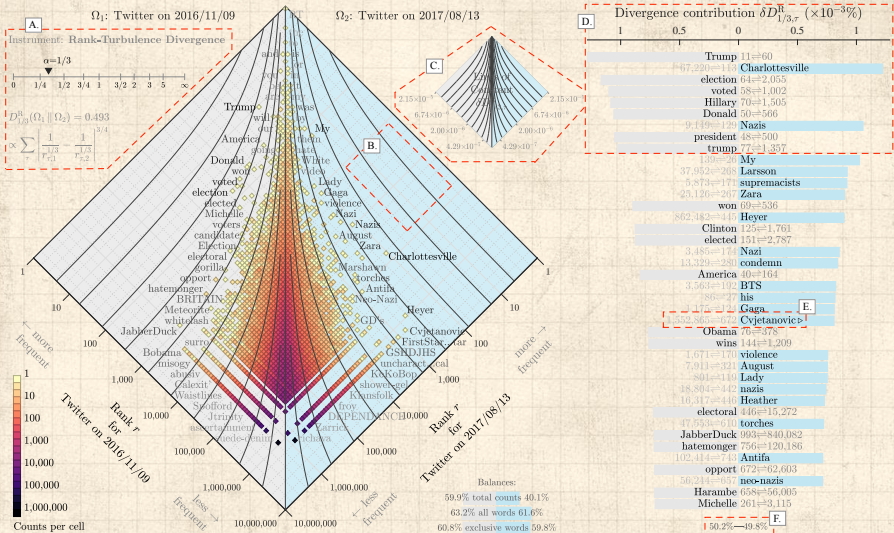
$$\begin{aligned} D_{\infty}^R(R_1 \| R_2) &= \sum_{\tau \in R_{1,2;\alpha}} \delta D_{\infty, \tau}^R \\ &= \frac{1}{N_{1,2;\infty}} \sum_{\tau \in R_{1,2;\alpha}} (1 - \delta_{r_{\tau,1} r_{\tau,2}}) \max_{\tau} \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}. \end{aligned} \quad (14)$$

where

$$N_{1,2;\infty} = \sum_{\tau \in R_1} \frac{1}{r_{\tau,1}} + \sum_{\tau \in R_2} \frac{1}{r_{\tau,2}}. \quad (15)$$


 Highest ranks dominate.






## Probability-turbulence divergence:

$$D_{\alpha}^{\text{P}}(P_1 \parallel P_2) = \frac{1}{\mathcal{N}_{1,2;\alpha}^{\text{P}}} \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_{1,2;\alpha}} \left| [p_{\tau,1}]^{\alpha} - [p_{\tau,2}]^{\alpha} \right|^{1/(\alpha+1)}. \quad (16)$$

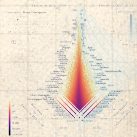
 For the unnormalized version ( $\mathcal{N}_{1,2;\alpha}^{\text{P}}=1$ ), some troubles return with 0 probabilities and  $\alpha \rightarrow 0$ .

 Weep not:  $\mathcal{N}_{1,2;\alpha}^{\text{P}}$  will save the day.

## Normalization:

With no matching types, the probability of a type present in one system is zero in the other, and the sum can be split between the two systems' types:

$$\mathcal{N}_{1,2;\alpha}^P = \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_1} [p_{\tau,1}]^{\alpha/(\alpha+1)} + \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_2} [p_{\tau,2}]^{\alpha/(\alpha+1)} \quad (17)$$

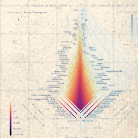


## Limit of $\alpha=0$ for probability-turbulence divergence

🧱 if both  $p_{\tau,1} > 0$  and  $p_{\tau,2} > 0$  then


$$\lim_{\alpha \rightarrow 0} \frac{\alpha + 1}{\alpha} \left| [p_{\tau,1}]^{\alpha} - [p_{\tau,2}]^{\alpha} \right|^{1/(\alpha+1)} = \left| \ln \frac{p_{\tau,2}}{p_{\tau,1}} \right|. \quad (18)$$

🧱 But if  $p_{\tau,1} = 0$  or  $p_{\tau,2} = 0$ , limit diverges as  $1/\alpha$ .




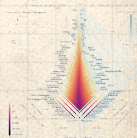


## Limit of $\alpha=0$ for probability-turbulence divergence

 Normalization:


$$\mathcal{N}_{1,2;\alpha}^P \rightarrow \frac{1}{\alpha} (N_1 + N_2). \quad (19)$$


 Because the normalization also diverges as  $1/\alpha$ , the divergence will be zero when there are no exclusive types and non-zero when there are exclusive types.

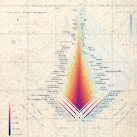


Combine these cases into a single expression:




$$D_0^P(P_1 \parallel P_2) = \frac{1}{(N_1 + N_2)} \sum_{\tau \in R_{1,2;0}} (\delta_{p_{\tau,1},0} + \delta_{0,p_{\tau,2}}). \quad (20)$$

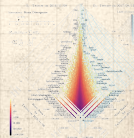
 The term  $(\delta_{p_{\tau,1},0} + \delta_{0,p_{\tau,2}})$  returns 1 if either  $p_{\tau,1} = 0$  or  $p_{\tau,2} = 0$ , and 0 otherwise when both  $p_{\tau,1} > 0$  and  $p_{\tau,2} > 0$ .

 Ratio of types that are exclusive to one system relative to the total possible such types,



## Type contribution ordering for the limit of $\alpha=0$

-  In terms of contribution to the divergence score, all exclusive types supply a weight of  $1/(N_1 + N_2)$ . We can order them by preserving their ordering as  $\alpha \rightarrow 0$ , which amounts to ordering by descending probability in the system in which they appear.
-  And while types that appear in both systems make no contribution to  $D_0^P(P_1 \parallel P_2)$ , we can still order them according to the log ratio of their probabilities.
-  The overall ordering of types by divergence contribution for  $\alpha=0$  is then: (1) exclusive types by descending probability and then (2) types appearing in both systems by descending log ratio.

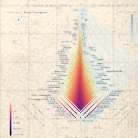


## Limit of $\alpha=\infty$ for probability-turbulence divergence





$$D_{\infty}^P(P_1 \| P_2) = \frac{1}{2} \sum_{\tau \in R_{1,2;\infty}} (1 - \delta_{p_{\tau,1}, p_{\tau,2}}) \max(p_{\tau,1}, p_{\tau,2}) \quad (21)$$

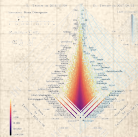
where

$$\mathcal{N}_{1,2;\infty}^P = \sum_{\tau \in R_{1,2;\infty}} (p_{\tau,1} + p_{\tau,2}) = 1 + 1 = 2. \quad (22)$$



## Connections for PTD:

-   $\alpha = 0$ : Similarity measure Sørensen-Dice coefficient <sup>[8, 31, 20]</sup>,  $F_1$  score of a test's accuracy <sup>[32, 29]</sup>.
-   $\alpha = 1/2$ : Hellinger distance <sup>[16]</sup> and Mautusita distance <sup>[21]</sup>.
-   $\alpha = 1$ : Many including all  $L^{(p)}$ -norm type constructions.
-   $\alpha = \infty$ : Motyka distance <sup>[7]</sup>.



$\Omega_1$ : Twitter on 2016/11/09

$\Omega_2$ : Twitter on 2017/08/13

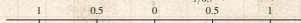
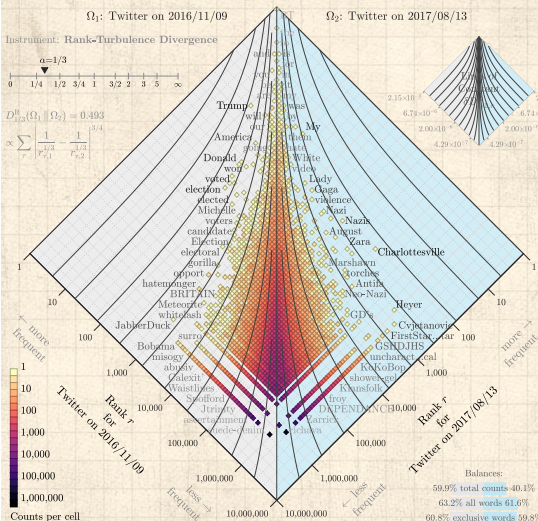
Divergence contribution  $\delta D_{1/3,7}^R$  ( $\times 10^{-3}\%$ )

Instrument: Rank-Turbulence Divergence

$\alpha=1/3$

$D_{1/3}^R(\Omega_1 || \Omega_2) = 0.493$

$$\infty \sum_r \left| \frac{1}{r_{-1/3}} - \frac{1}{r_{-2}} \right|^{3/4}$$



|               |                |
|---------------|----------------|
| Trump         | 11=60          |
| 17,220=113    | Charlotteville |
| election      | 64=2,055       |
| voted         | 58=1,002       |
| Hillary       | 70=1,505       |
| Donald        | 50=566         |
| 9,149=129     | Nazis          |
| president     | 48=500         |
| trump         | 77=1,357       |
| 139=20        | My             |
| 37,952=268    | Larsson        |
| 5,873=171     | supremacists   |
| 25,126=267    | Zara           |
| won           | 69=536         |
| 862,482=443   | Heyer          |
| Clinton       | 125=1,761      |
| elected       | 151=2,787      |
| 3,485=174     | Nazi           |
| 13,329=280    | condemn        |
| America       | 40=164         |
| 3,503=192     | BTS            |
| 86=27         | his            |
| 1,175=124     | gaga           |
| 1,562,865=673 | Cvjetanovic    |
| Obama         | 76=378         |
| wins          | 144=1,209      |
| 1,671=170     | violence       |
| 7,911=321     | August         |
| 801=110       | Lady           |
| 18,804=442    | nazis          |
| 16,317=140    | Heather        |
| electoral     | 446=15,272     |
| 47,558=610    | torches        |
| JabberDuck    | 993=840,082    |
| hatemonger    | 756=120,186    |
| 102,414=743   | Antifa         |
| opport        | 672=62,603     |
| 56,244=657    | neo-nazis      |
| Harambe       | 658=56,005     |
| Michelle      | 261=3,115      |
|               | 50.2%—49.8%    |

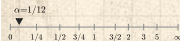
Balances:  
 59.9% total counts 40.1%  
 63.2% all words 61.6%  
 60.8% exclusive words 59.8%

$\Omega_1$ : Twitter on 2016/11/09

$\Omega_2$ : Twitter on 2017/08/13

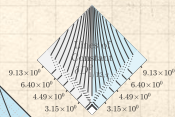
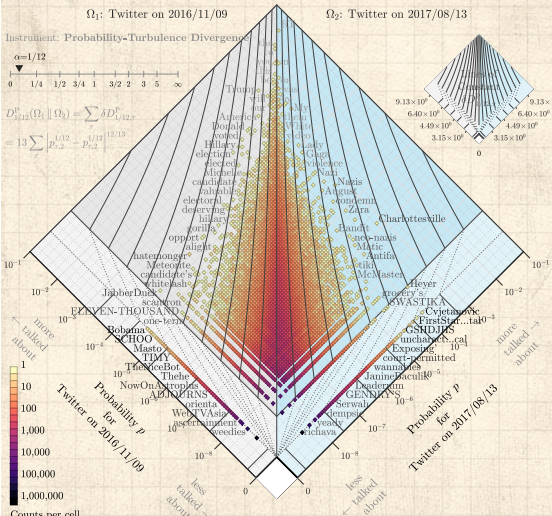
Divergence contribution  $\delta D_{1/12,r}^D (\times 10^{-4}\%)$

Instrument: Probability-Turbulence Divergence



$$D_{1/12}^D(\Omega_1 \parallel \Omega_2) = \sum \delta D_{1/12,r}^D$$

$$= 13 \sum_{P_{r,2}}^{1/12} \frac{1/12}{P_{r,2}} \frac{1/12}{P_{r,2}^{12/13}}$$

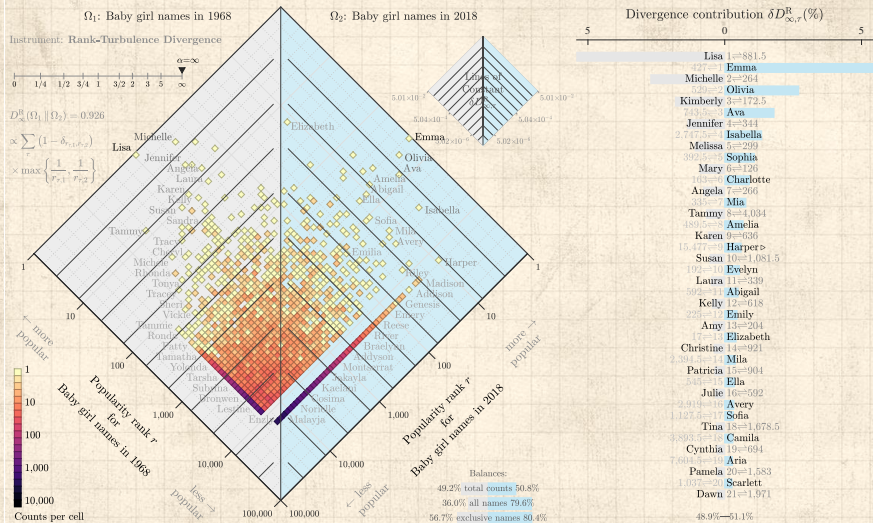


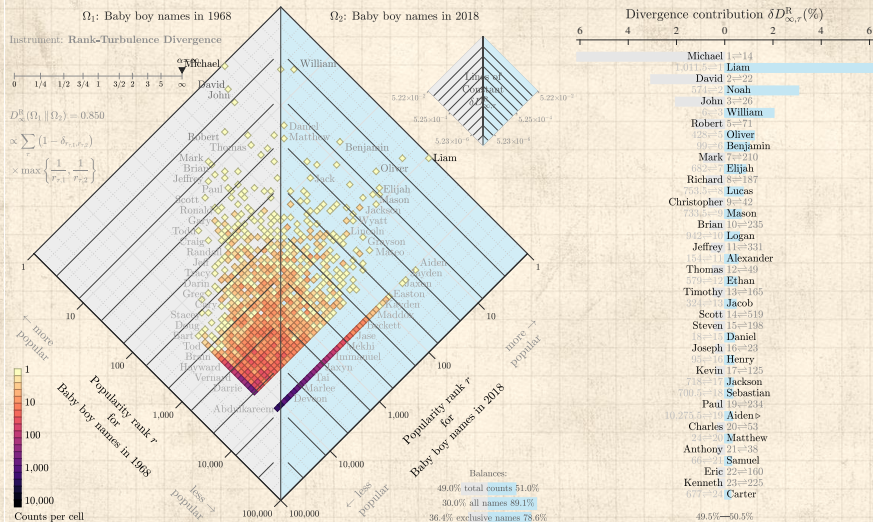
| 1                                   | 0 | 1                               |
|-------------------------------------|---|---------------------------------|
| 1.552,865=6.73                      |   | Cvjetanovic >                   |
| 1.552,865=1.116                     |   | FirstStarMagicAllStar >         |
| 1.552,865=1.47                      |   | KISSMARCHED >                   |
| 1.552,865=1.520                     |   | ForAllStarGames >               |
| 1.552,865=1.985                     |   | Kafeel >                        |
| 1.552,865=2.021                     |   | Starbz >                        |
|                                     |   | < Bobama 2,423=1,537,471        |
|                                     |   | < Oarack 2,425=1,537,471        |
|                                     |   | < Un-Leashed 2,703=1,537,471    |
| 1.552,865=3.088                     |   | GSHDJHS >                       |
| 1.552,865=3.099                     |   | Bodak >                         |
| < KiligTripSaBagnio 3,142=1,537,471 |   |                                 |
| < Somali-American 3,229=1,537,471   |   |                                 |
| < DICKASS 3,321=1,537,471           |   |                                 |
| < Michelle 3,412=1,537,471          |   |                                 |
| 1.552,865=3.673                     |   | Eastwatch >                     |
| < Un-leashed 3,645=1,537,471        |   |                                 |
| 1.552,865=3.983                     |   | Heyer's >                       |
| < SCHOO 3,921=1,537,471             |   |                                 |
| 1.552,865=4.382                     |   | uncharacteristical >            |
| 1.552,865=4.518                     |   | callejones >                    |
|                                     |   | < misogy 4,328=1,537,471        |
| 1.552,865=4.723                     |   | TLC >                           |
| 1.552,865=4.913                     |   | SORIBADA >                      |
| < tRyNna 4,660=1,537,471            |   |                                 |
| < aLmoSt 4,671=1,537,471            |   |                                 |
| 1.552,865=5.240                     |   | tcas >                          |
| < Ruline 5,097=1,537,471            |   |                                 |
| < Steinger 5,118=1,537,471          |   |                                 |
| 1.552,865=5.436                     |   | low-rise >                      |
| 1.552,865=5.662                     |   | climate-denying 5,191=1,537,471 |
| 1.552,865=5.682                     |   | CLITORIS >                      |
| 1.552,865=5.682                     |   | Adityanath >                    |
| < lambo's 5,383=1,537,471           |   |                                 |
| 1.552,865=5.755                     |   | DelHiHasret >                   |
| 1.552,865=5.755                     |   | FikBel >                        |
| 1.552,865=5.808                     |   | Walker-Peters >                 |
| < KBAT 5,617=1,537,471              |   |                                 |
| 1.552,865=6.040                     |   | UNIDAS >                        |
| < stammered 5,653=1,537,471         |   |                                 |

49.9%—50.1%









$\Omega_1$ : 1948 Google Books Fiction

$\Omega_2$ : 1987 Google Books Fiction

Instrument: Rank-Turbulence Divergence

$$D_{\infty}^R(\Omega_1, \Omega_2) = 0.522$$

$$\infty \sum_{\tau} (1 - \delta_{\tau,1} \delta_{\tau,2})$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$D_{\infty}^R(\Omega_1, \Omega_2) = 0.522$$

$$\infty \sum_{\tau} (1 - \delta_{\tau,1} \delta_{\tau,2})$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

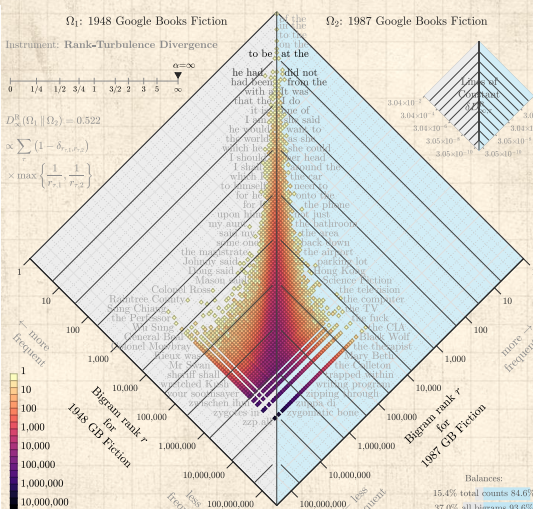
$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

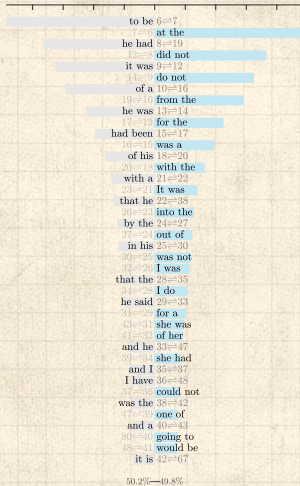
$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

$$\times \max \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}$$

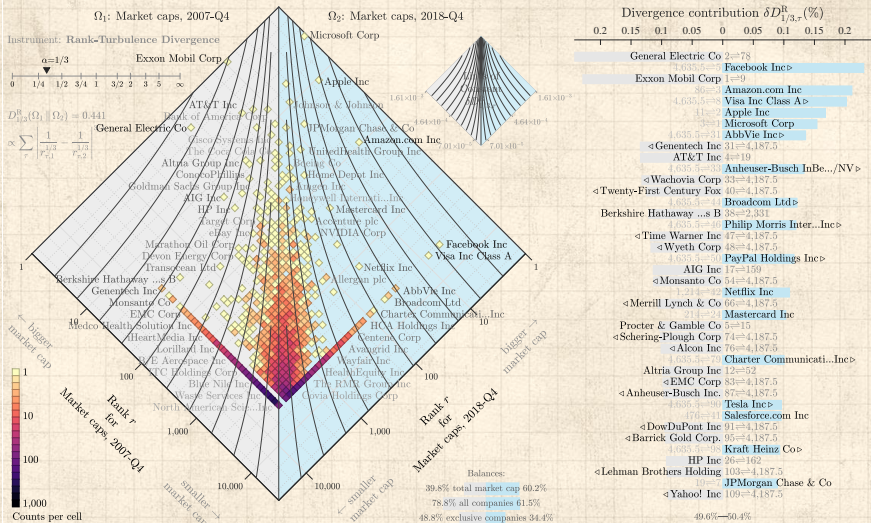


Divergence contribution  $\delta_{\infty,r}^R$  (%)

0.8 0.6 0.4 0.2 0 0.2 0.4 0.6 0.8

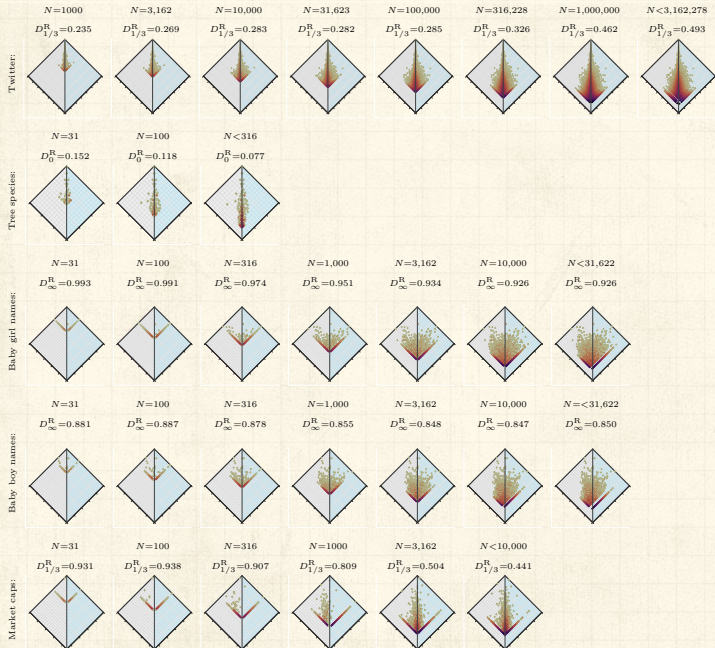


Balances:  
 15.4% total counts 84.6%  
 37.0% all bigrams 93.6%  
 17.2% exclusive bigrams 67.3%





# Effect of subsampling:



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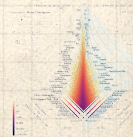
Mechanics of  
Fame

Superspreading

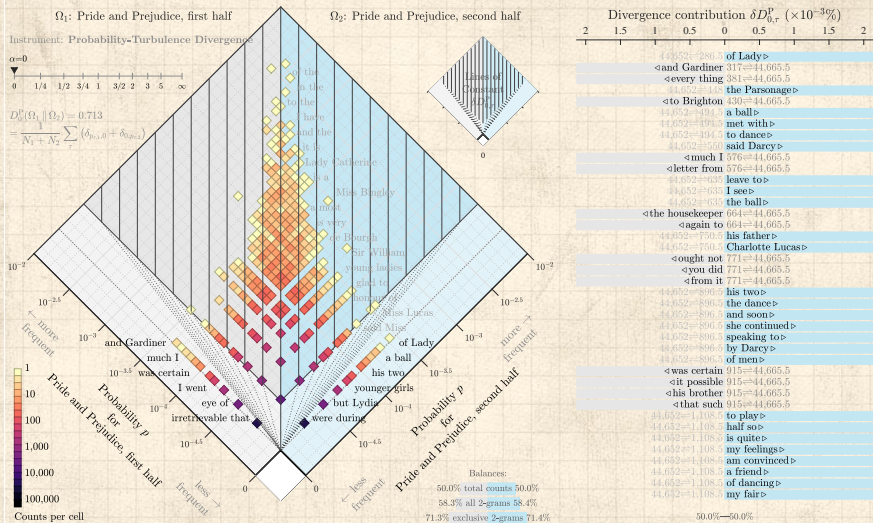
Lexical Ultrafame

Turbulent times

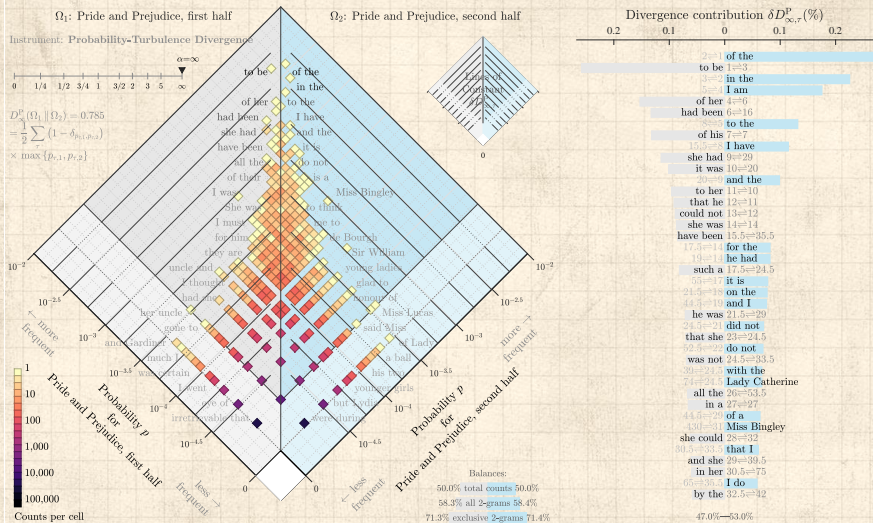
References







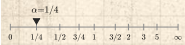




$\Omega_1$ : Twitter on 2020/03/12

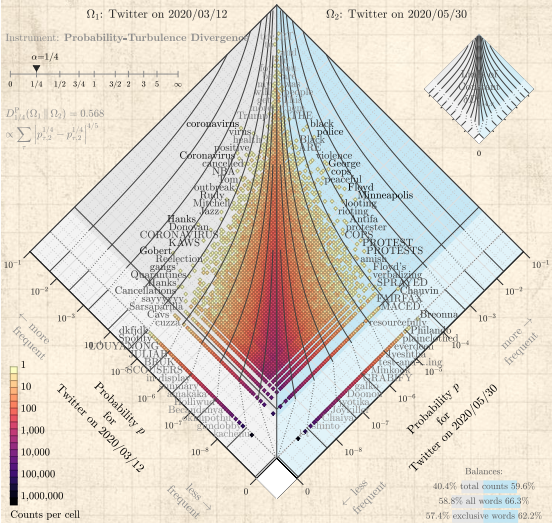
$\Omega_2$ : Twitter on 2020/05/30

Instrument: Probability-Turbulence Divergence

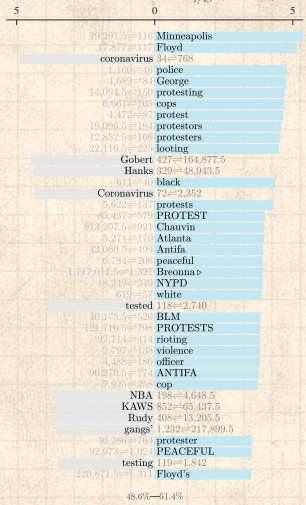


$$D_{1/4}^P(\Omega_1 || \Omega_2) = 0.568$$

$$\propto \sum_p |p_{\Omega_1}^{1/4} - p_{\Omega_2}^{1/4}|^{1/5}$$



Divergence contribution  $\delta D_{1/4,7}^P (\times 10^{-4}\%)$



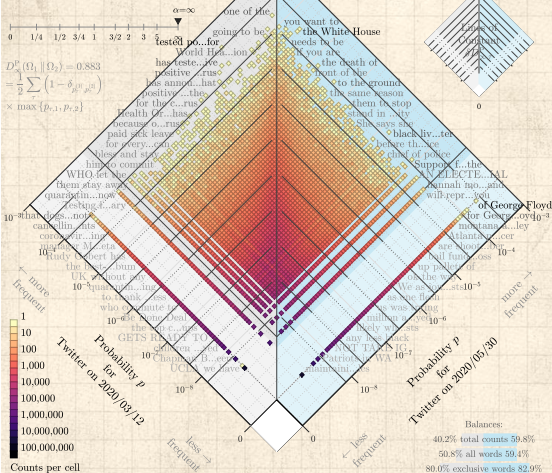
Balances:  
 40.4% total counts 59.6%  
 58.8% all words 66.3%  
 57.4% exclusive words 62.2%



$\Omega_1$ : Twitter on 2020/03/12

$\Omega_2$ : Twitter on 2020/05/30

Instrument: Probability-Turbulence Divergence

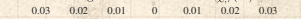


$$D_{\infty}^p(\Omega_1, \Omega_2) = 0.883$$

$$= \frac{1}{2} \sum (1 - \delta_{\Omega_1, \Omega_2}^p)$$

$$\times \max\{p_{r,1}, p_{r,2}\}$$

Divergence contribution  $\delta D_{\infty, r}^p$  (%)



- 1=4,975.5
  - 2=219.0
  - 3=11,879
  - 4=14,798
  - 5=7,264.5
  - 6=33
  - 7=108
  - 8=1,420
  - 9=78,795
  - 10=53,912
  - 11=603
  - 12=22,783.5
  - 13=45
  - 14=143.5
  - 15=30
  - 16=277,424.5
  - 17=631.5
  - 18=43,073,107
  - 19=22
  - 20=43,073,107
  - 21=172,568
  - 22=1,421
  - 23=43,073,107
  - 24=43,073,107
  - 25=17
- tested positive for  
 of George Floyd  
 the White House  
 in front of  
 one of the  
 has tested positive for  
 positive for coronavirus  
 the spread of  
 going to be  
 out of the  
 black lives matter  
 community in Minneapolis  
 is going to  
 to do with  
 part of the  
 you want to  
 World Health Organization  
 to the ground  
 for the coronavirus  
 the death of  
 for George Floyd  
 positive for  
 due to the  
 has announced that  
 needs to be  
 Support from the  
 be able to  
 the rest of  
 in the world  
 This is the  
 because of coronavirus  
 because of the  
 dogs cannot  
 the United States  
 announced that dogs  
 Health Organization has  
 the corona virus  
 dogs cannot contract  
 Organization has announced  
 white vs black

Balances:  
 40.2% total counts 59.8%  
 50.8% all words 59.4%  
 80.0% exclusive words 82.9%



50.4%—49.6%







# Flipbooks for RTD:



Twitter:

[instrument-flipbook-1-rank-div.pdf](#)  

[instrument-flipbook-2-probability-div.pdf](#)  

[instrument-flipbook-3-gen-entropy-div.pdf](#)  





Market caps:

[instrument-flipbook-4-marketcaps-6years-rank-div.pdf](#)  





Baby names:



[instrument-flipbook-5-babynames-girls-50years-rank-div.pdf](#)  

[instrument-flipbook-6-babynames-boys-50years-rank-div.pdf](#)  



Google books:

[instrument-flipbook-7-google-books-onograms-rank-div.pdf](#)  

[instrument-flipbook-8-google-books-bigrams-rank-div.pdf](#)  

[instrument-flipbook-9-google-books-trigrams-rank-div.pdf](#)  

# Flipbooks for PTD:



## Jane Austen:

[Pride and Prejudice, 1-grams](#)  



[Pride and Prejudice, 2-grams](#)  



[Pride and Prejudice, 3-grams](#)  



## Social media:

[Twitter, 1-grams](#)  

[Twitter, 2-grams](#)  

[Twitter, 3-grams](#)  



## Ecology:

[Barro Colorado Island](#)  

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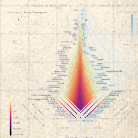
Lexical Ultrafame

Turbulent times

References

Code:

<https://gitlab.com/compstorylab/allotaxonometer>





# Claims, exaggerations, reminders:



Needed for comparing large-scale complex systems:

Comprehensible, dynamically-adjusting, differential dashboards

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Allotaxonomy  
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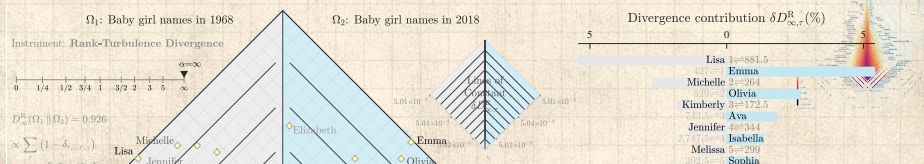
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# Claims, exaggerations, reminders:



Needed for comparing large-scale complex systems:

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Many measures seem poorly motivated and largely unexamined (e.g., JSD)

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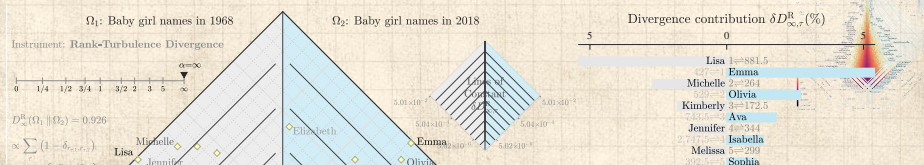
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# Claims, exaggerations, reminders:

-  Needed for comparing large-scale complex systems:
  - Comprehensible, dynamically-adjusting, differential dashboards
-  Many measures seem poorly motivated and largely unexamined (e.g., JSD)
-  Of value: Combining big-picture maps with ranked lists

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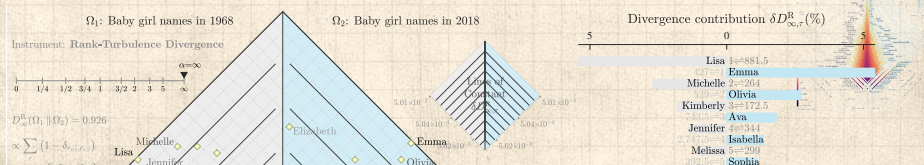
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# Claims, exaggerations, reminders:

- 
 Needed for comparing large-scale complex systems:
  - Comprehensible, dynamically-adjusting, differential dashboards
- 
 Many measures seem poorly motivated and largely unexamined (e.g., JSD)
- 
 Of value: Combining big-picture maps with ranked lists
- 
 Maybe one day: Online tunable version of rank-turbulence divergence (plus many other instruments)

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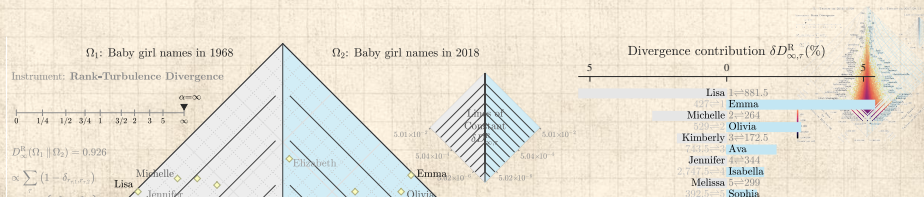
Mechanics of  
Fame

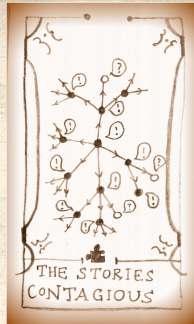
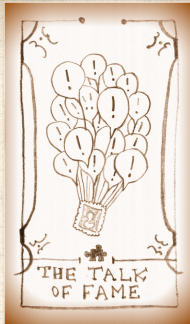
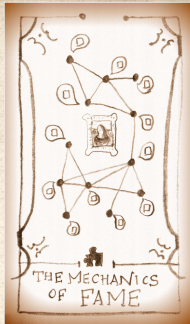
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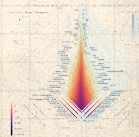
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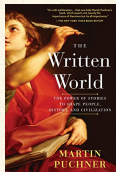
## The everywhere-ness of algorithms and stories:



“On the Origin of Stories: Evolution, Cognition, and Fiction” [a](#) [↗](#)  
by Brian Boyd (2010). <sup>[2]</sup>



“The Storytelling Animal: How Stories Make Us Human” [a](#) [↗](#)  
by Jonathan Gottschall (2013). <sup>[15]</sup>



“The Written World: How Literature Shaped Civilization” [a](#) [↗](#)  
by Martin Puchner (2017). <sup>[27]</sup>

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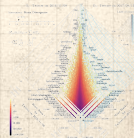
Mechanics of  
Fame

Superspreading

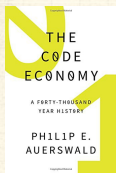
Lexical Ultrafame

Turbulent times

References

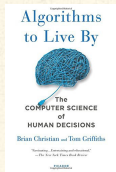


# Algorithms, recipes, stories, ...



“The Code Economy: A Forty-Thousand Year History” [a](#)

by Philip E Auerwald (2017). <sup>[1]</sup>



“Algorithms to Live By” [a](#)

by Christian and Griffiths (2016). <sup>[5]</sup>



“Once Upon an Algorithm” [a](#)

by Martin Erwig (2017). <sup>[14]</sup>

Also: Numerical Recipes in C <sup>[26]</sup> and How to Bake  $\pi$  <sup>[4]</sup>

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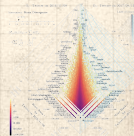
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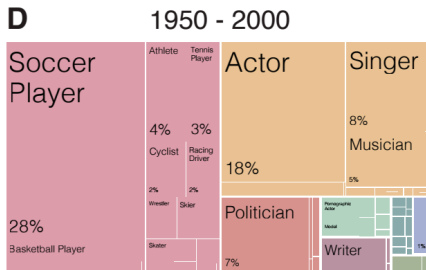
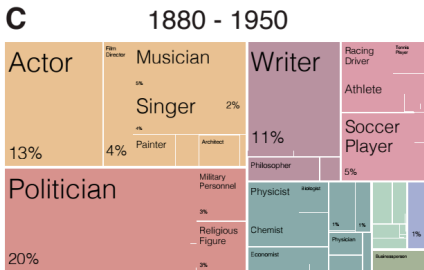
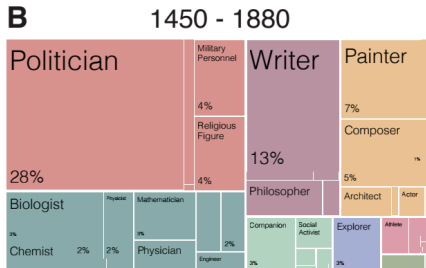
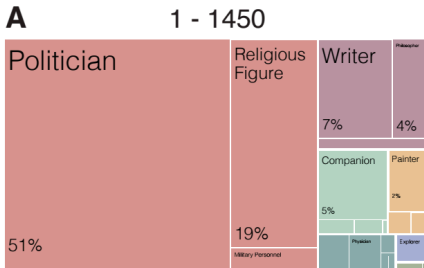
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References













## Super Survival of the Stories:



-  Study of Agta, Filipino hunter-gatherers.
-  Storytelling valued well above all other skills including hunting.
-  Stories encode prosocial norms such as cooperation.

The Desirability  
of  
Storytellers ,  
The Atlantic,  
Ed Yong,  
2017-12-05.

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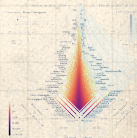
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## Super Survival of the Stories:



-  Study of Agta, Filipino hunter-gatherers.
-  Storytelling valued well above all other skills including hunting.
-  Stories encode prosocial norms such as cooperation.
-  Like the best stories, the best storytellers reproduce more successfully.

The Desirability  
of  
Storytellers ,  
The Atlantic,  
Ed Yong,  
2017-12-05.

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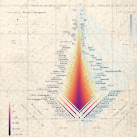
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# The most famous painting in the world:



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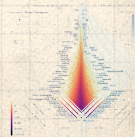
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# The dismal predictive powers of editors .....

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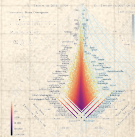
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Twelve ...

# The completely unpredicted fall of Eastern Europe:



Timur Kuran: <sup>[18]</sup> "Now Out of Never: The Element of Surprise in the East European Revolution of 1989"

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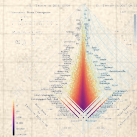
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# We understand bushfire stories:



1. Sparks start fires.

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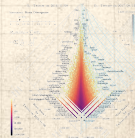
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# We understand bushfire stories:



1. Sparks start fires.
2. System properties control a fire's spread.

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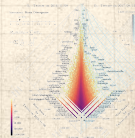
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# We understand bushfire stories:



1. Sparks start fires.
2. System properties control a fire's spread.
3. But for three reasons, we make two mistakes about **Social Fires** ...

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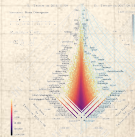
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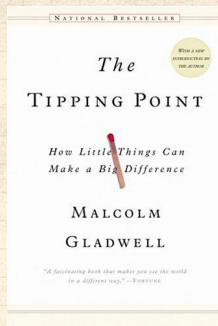
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# We understand bushfire stories:



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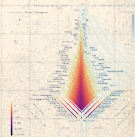
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# Reason 1—We are Homo Narrativus.

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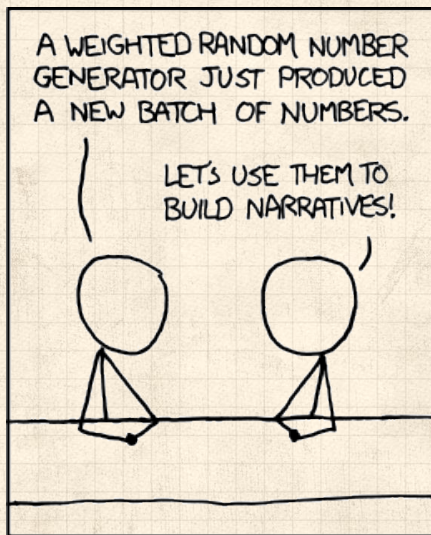
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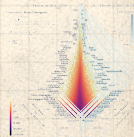
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ALL SPORTS COMMENTARY



## Reason 2—"We are all individuals."

Archival footage:

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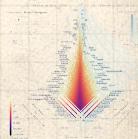
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Individual narratives are not enough to understand distributed, networked minds.



## Reason 3—We are spectacular imitators.

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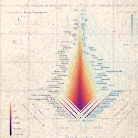
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BBC/David Attenborough.



# Mistake 1: Success is due to intrinsic properties



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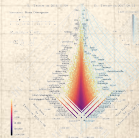
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See "Becoming Mona Lisa" by David Sassoon 

# Mistake 1: Success is due to intrinsic properties



it's just so disappointingly small

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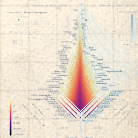
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See "Becoming Mona Lisa" by David Sassoon [↗](#)

# Mistake 1:

## Success is due to intrinsic properties



Stolen in 1913, recovered in 1915.

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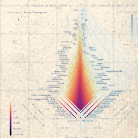
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See "Becoming Mona Lisa" by David Sassoon 



# Mistake 1: Success is due to intrinsic properties



Hidden during WWII.

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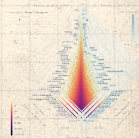
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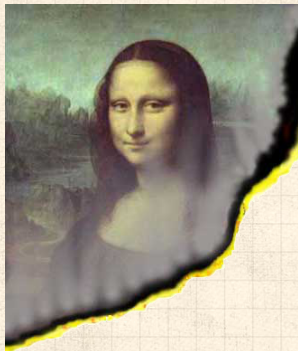
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References

See "Becoming Mona Lisa" by David Sassoon 



# Mistake 1: Success is due to intrinsic properties



[Repeatedly vandalised and attacked.](#)

[See "Becoming Mona Lisa" by David Sassoon](#)

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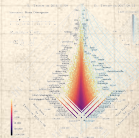
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48 songs  
30k participants

## Exp 1— weak social

| Rank | Title           | Likes | Rank |
|------|-----------------|-------|------|
| 1    | WANT TO BE      | 10    | 1    |
| 2    | DEEP END OF THE | 10    | 2    |
| 3    | THE WINDY CITY  | 10    | 3    |
| 4    | THE BIRDSONG    | 10    | 4    |
| 5    | THE BIRDSONG    | 10    | 5    |
| 6    | THE BIRDSONG    | 10    | 6    |
| 7    | THE BIRDSONG    | 10    | 7    |
| 8    | THE BIRDSONG    | 10    | 8    |
| 9    | THE BIRDSONG    | 10    | 9    |
| 10   | THE BIRDSONG    | 10    | 10   |
| 11   | THE BIRDSONG    | 10    | 11   |
| 12   | THE BIRDSONG    | 10    | 12   |
| 13   | THE BIRDSONG    | 10    | 13   |
| 14   | THE BIRDSONG    | 10    | 14   |
| 15   | THE BIRDSONG    | 10    | 15   |
| 16   | THE BIRDSONG    | 10    | 16   |
| 17   | THE BIRDSONG    | 10    | 17   |
| 18   | THE BIRDSONG    | 10    | 18   |
| 19   | THE BIRDSONG    | 10    | 19   |
| 20   | THE BIRDSONG    | 10    | 20   |
| 21   | THE BIRDSONG    | 10    | 21   |
| 22   | THE BIRDSONG    | 10    | 22   |
| 23   | THE BIRDSONG    | 10    | 23   |
| 24   | THE BIRDSONG    | 10    | 24   |
| 25   | THE BIRDSONG    | 10    | 25   |
| 26   | THE BIRDSONG    | 10    | 26   |
| 27   | THE BIRDSONG    | 10    | 27   |
| 28   | THE BIRDSONG    | 10    | 28   |
| 29   | THE BIRDSONG    | 10    | 29   |
| 30   | THE BIRDSONG    | 10    | 30   |
| 31   | THE BIRDSONG    | 10    | 31   |
| 32   | THE BIRDSONG    | 10    | 32   |
| 33   | THE BIRDSONG    | 10    | 33   |
| 34   | THE BIRDSONG    | 10    | 34   |
| 35   | THE BIRDSONG    | 10    | 35   |
| 36   | THE BIRDSONG    | 10    | 36   |
| 37   | THE BIRDSONG    | 10    | 37   |
| 38   | THE BIRDSONG    | 10    | 38   |
| 39   | THE BIRDSONG    | 10    | 39   |
| 40   | THE BIRDSONG    | 10    | 40   |
| 41   | THE BIRDSONG    | 10    | 41   |
| 42   | THE BIRDSONG    | 10    | 42   |
| 43   | THE BIRDSONG    | 10    | 43   |
| 44   | THE BIRDSONG    | 10    | 44   |
| 45   | THE BIRDSONG    | 10    | 45   |
| 46   | THE BIRDSONG    | 10    | 46   |
| 47   | THE BIRDSONG    | 10    | 47   |
| 48   | THE BIRDSONG    | 10    | 48   |

## Exp. 2—strong social

| Rank | Title           | Likes | Rank |
|------|-----------------|-------|------|
| 1    | WANT TO BE      | 10    | 1    |
| 2    | DEEP END OF THE | 10    | 2    |
| 3    | THE WINDY CITY  | 10    | 3    |
| 4    | THE BIRDSONG    | 10    | 4    |
| 5    | THE BIRDSONG    | 10    | 5    |
| 6    | THE BIRDSONG    | 10    | 6    |
| 7    | THE BIRDSONG    | 10    | 7    |
| 8    | THE BIRDSONG    | 10    | 8    |
| 9    | THE BIRDSONG    | 10    | 9    |
| 10   | THE BIRDSONG    | 10    | 10   |
| 11   | THE BIRDSONG    | 10    | 11   |
| 12   | THE BIRDSONG    | 10    | 12   |
| 13   | THE BIRDSONG    | 10    | 13   |
| 14   | THE BIRDSONG    | 10    | 14   |
| 15   | THE BIRDSONG    | 10    | 15   |
| 16   | THE BIRDSONG    | 10    | 16   |
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| 24   | THE BIRDSONG    | 10    | 24   |
| 25   | THE BIRDSONG    | 10    | 25   |
| 26   | THE BIRDSONG    | 10    | 26   |
| 27   | THE BIRDSONG    | 10    | 27   |
| 28   | THE BIRDSONG    | 10    | 28   |
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| 32   | THE BIRDSONG    | 10    | 32   |
| 33   | THE BIRDSONG    | 10    | 33   |
| 34   | THE BIRDSONG    | 10    | 34   |
| 35   | THE BIRDSONG    | 10    | 35   |
| 36   | THE BIRDSONG    | 10    | 36   |
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| 41   | THE BIRDSONG    | 10    | 41   |
| 42   | THE BIRDSONG    | 10    | 42   |
| 43   | THE BIRDSONG    | 10    | 43   |
| 44   | THE BIRDSONG    | 10    | 44   |
| 45   | THE BIRDSONG    | 10    | 45   |
| 46   | THE BIRDSONG    | 10    | 46   |
| 47   | THE BIRDSONG    | 10    | 47   |
| 48   | THE BIRDSONG    | 10    | 48   |

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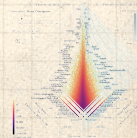
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References

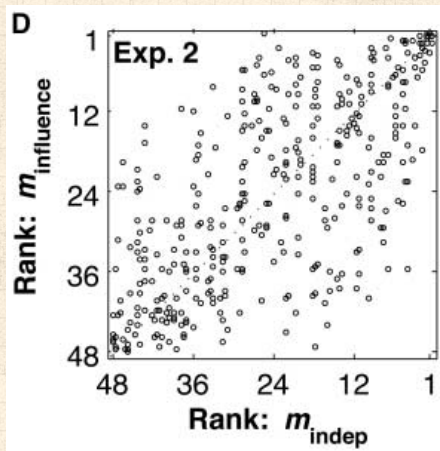


“An experimental study of inequality and unpredictability in an artificial cultural market” ↗

Salganik, Dodds, and Watts,  
Science, **311**, 854–856, 2006. [28]



# Resolving the paradox:



Increased social awareness leads to  
Stronger inequality + Less predictability.

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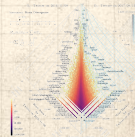
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# Payola/Deceptive advertising hurts us all:

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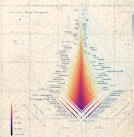
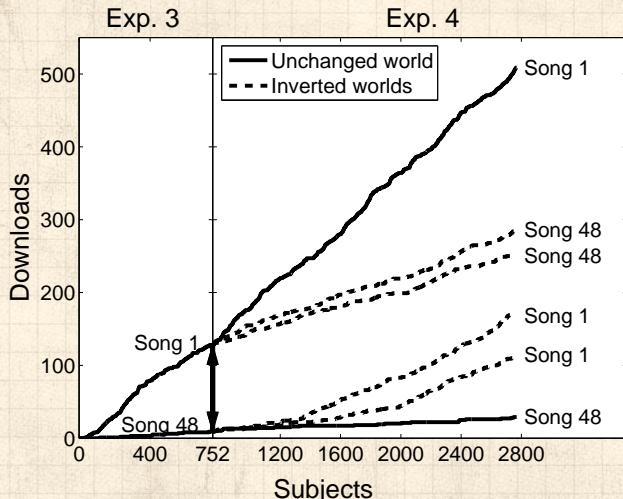
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## “Mistake” 2:

Seeing success is ‘due to social’ and  
wanting to say ‘all your interactions are  
belong to us’



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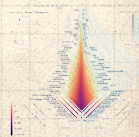
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# "This is truly the last time, believe me"

The Washington Post

Business Analysis



14 years of Mark Zuckerberg saying sorry, not sorry

By Geoffrey A. Fowler and Christal Etkin

Do you trust Mark Zuckerberg?

From the moment the Facebook founder entered the public eye in 2005 for creating a Harvard student hot-or-not rating site, he's been apologizing. So we collected this abbreviated history of his public mea culpas.

It reads like a record on repeat. Zuckerberg, who made "move fast and break things" his slogan, says sorry for being naive, and then promises solutions such as privacy "controls," "transparency" and better policy "enforcement." And then he promises it again the next time. You can track his [apologies to Congress](#) and [apologies to users](#) on the timeline below.

All the while, Facebook's access to our personal data increases and little changes about the way Zuckerberg handles it. So as Zuckerberg prepares to apologize for the first time in front of Congress, the question that lingers is: What will be different this time?

Robert Godwin Sr.

"Our **hearts go out** to the family and friends of Robert Godwin Sr., and we have a lot of work — and **we will keep doing all we can** to prevent tragedies like this from happening."



September 2017

While revealing a nine-step plan to stop nations from using Facebook to interfere in one another's elections, noting that the amount of "problematic content" found so far is "relatively small."

"I care deeply about the democratic process and protecting its integrity. ... It is a new challenge for internet communities to deal with



December 2007

After launching Beacon, which opted in everyone to sharing with advertisers what they were doing in outside websites and apps.

"We simply **did a bad job with this release, and I apologize for it.** ... People need to be able to explicitly choose what they share."

February 2009

After unveiling new terms of service that angered users.

"Over the past couple of days, we received a lot of questions and comments. ... Based on this feedback, we've **decided to return to our previous terms of use** while we resolve the issues."

"We won't prevent all mistakes or abuse, but **we currently make too many errors** enforcing our policies and preventing misuse of our tools. ... **This will be a serious year of self-improvement** and I'm looking forward to learning from working to fix our issues together."

March 2018

After details emerged about Cambridge Analytica taking user data.

"We have a responsibility to protect your data, and if we can't then we don't deserve to serve you. ... We will learn from this experience to secure our platform further and **make our community safer** for everyone going forward."

Commission for deceiving consumers about privacy.

"I'm the first to admit that **we've made a bunch of mistakes.** ... Facebook has always been committed to being transparent about the information you have stored with us — and we have led the internet in building tools to **give people the ability to see and control what they share.**"



July 2014

After an academic paper exposed that Facebook conducted psychological tests on nearly 700,000 users without their knowledge. (Apology by Facebook COO Sheryl Sandberg)

"It was my mistake, and I'm sorry. ... There's more we can do here to **limit the information developers can access and put more safeguards in place** to prevent abuse."

Related stories

Facebook: Most users may have had public data 'scraped'

Facebook COO Sheryl Sandberg on data leak: 'I am really sorry, we are late'

As Facebook confronts data misuse, foreign governments might force real change

What if we paid for Facebook — instead of letting it spy on us for free?

About this story

Photo/illustrations based on photos by Tony Avelar/Bloomberg News, Drew Angerer/Getty Images, Jeff Blomquist/WI, Jeff Watney/Getty Images, Craig Ruttle/WI, Paul Stewart/WI, Stephen Lamy/Reuters, Jon Green/Reuters, Richard Drew/AP

222 Comments

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The Facebook ads Russians showed to different groups

Facebook has said these ads were created by the Internet

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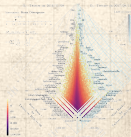
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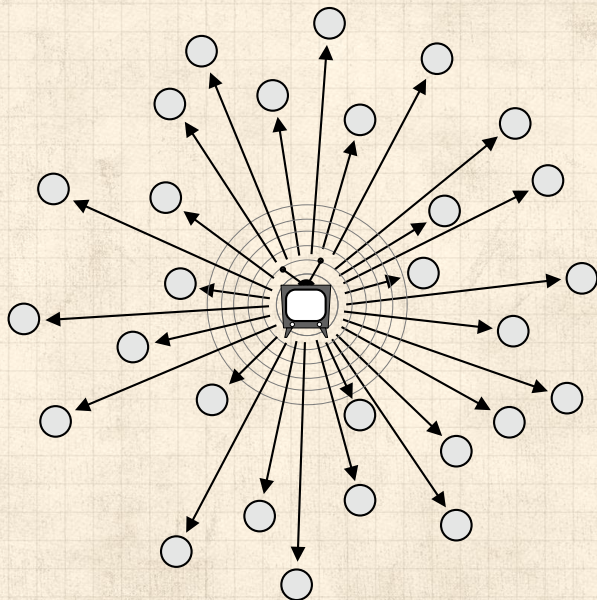
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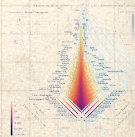
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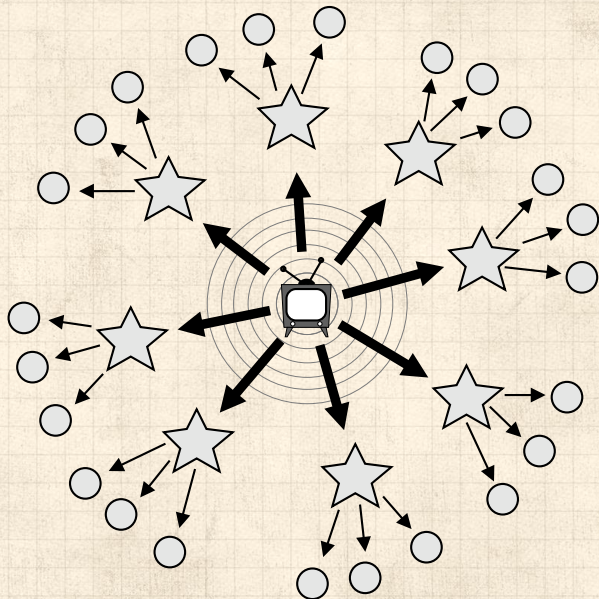
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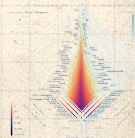
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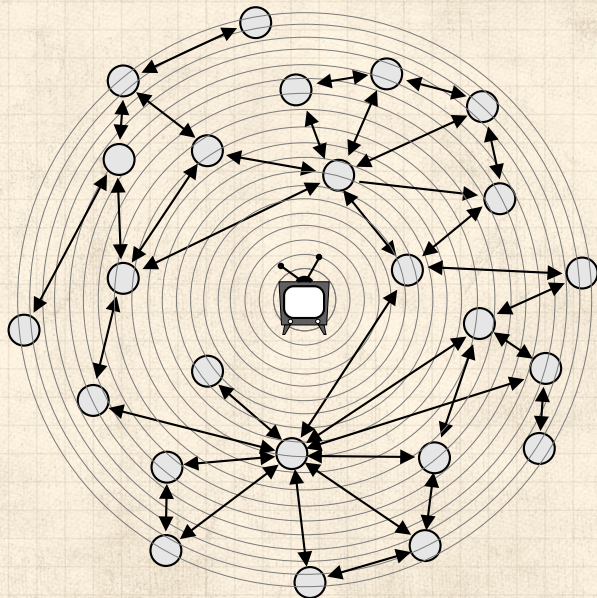
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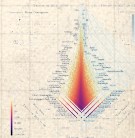
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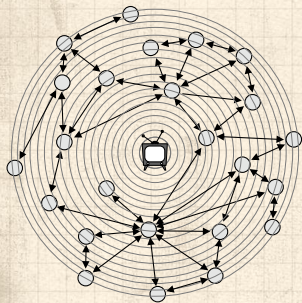
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## How superspreading works:

Many interconnected, average, trusting people must benefit from both **receiving** and **sharing** a message far from its source.



"Influentials, Networks, and Public Opinion Formation" 

Watts and Dodds,

J. Consum. Res., **34**, 441–458, 2007. <sup>[33]</sup>

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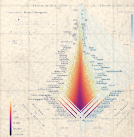
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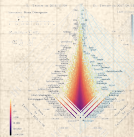
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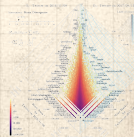
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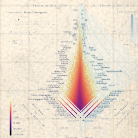
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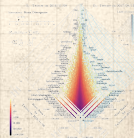
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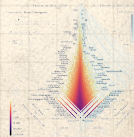
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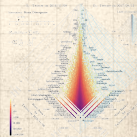
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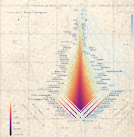
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
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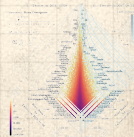
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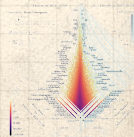
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# Oscar Wilde, The Picture of Dorian Gray: Raw Fame

THIS NUMBER CONTAINS

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By OSCAR WILDE.

COMPLETE.

JULY, 1890

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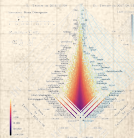
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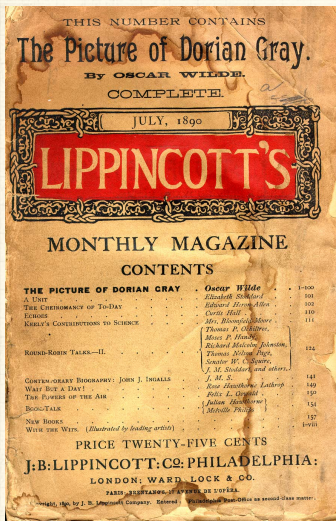
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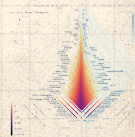
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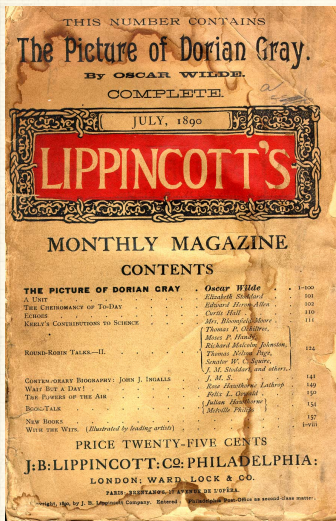
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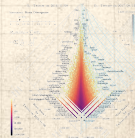
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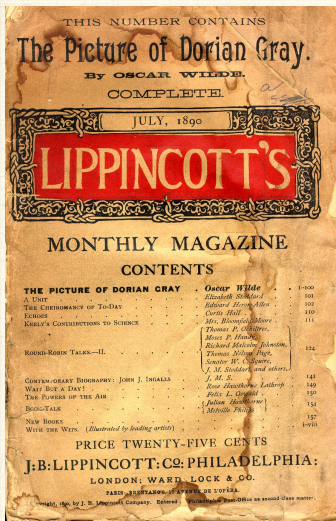
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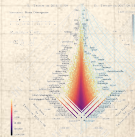
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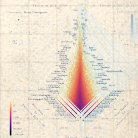
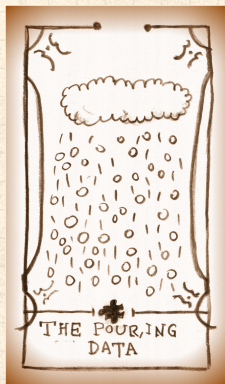
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“Computational timeline reconstruction of the stories surrounding Trump: Story turbulence, narrative control, and collective chronopathy”

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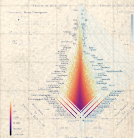
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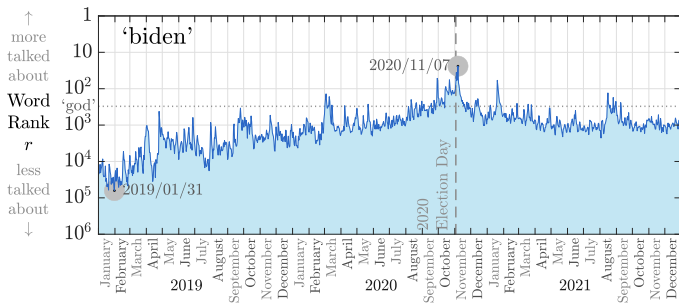
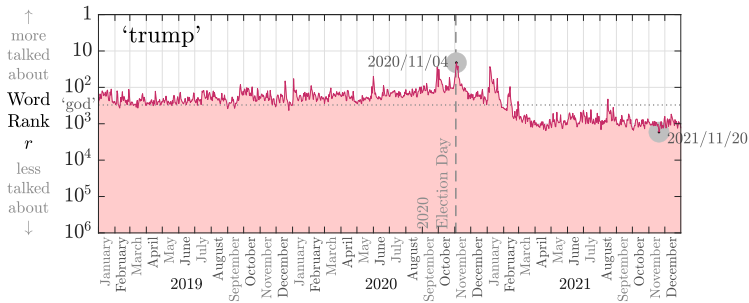
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```
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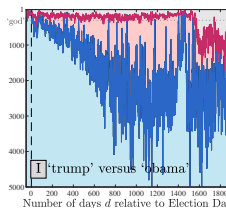
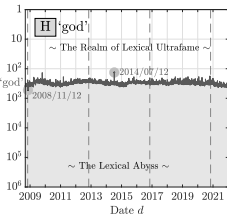
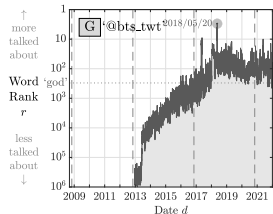
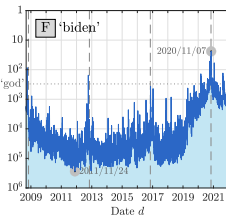
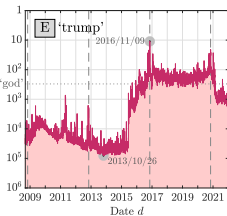
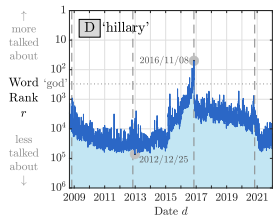
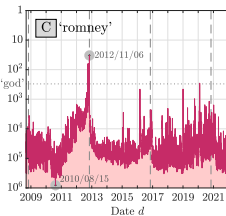
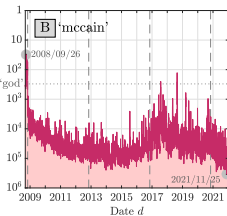
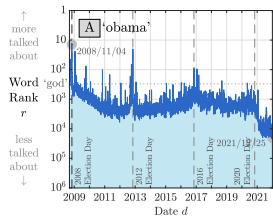
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zless 2018-01-06/1grams/en_*.tar.tsv
```

```
zless 2021-01-05/1grams/en_*.tar.tsv
```

```
zless 2021-01-06/1grams/en_*.tar.tsv
```

```
zless 2021-01-07/1grams/en_*.tar.tsv
```

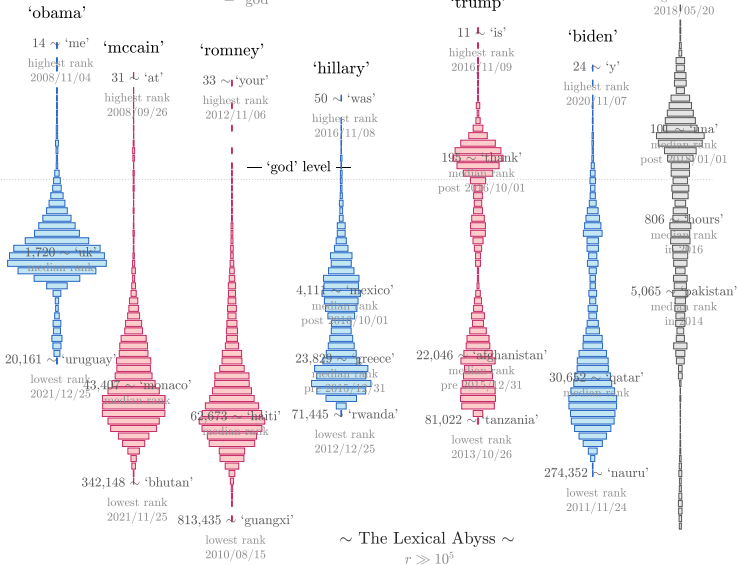






~ The Realm of Lexical Ultraframe ~

$r \leq r_{\text{god}} = 303$



~ The Lexical Abyss ~

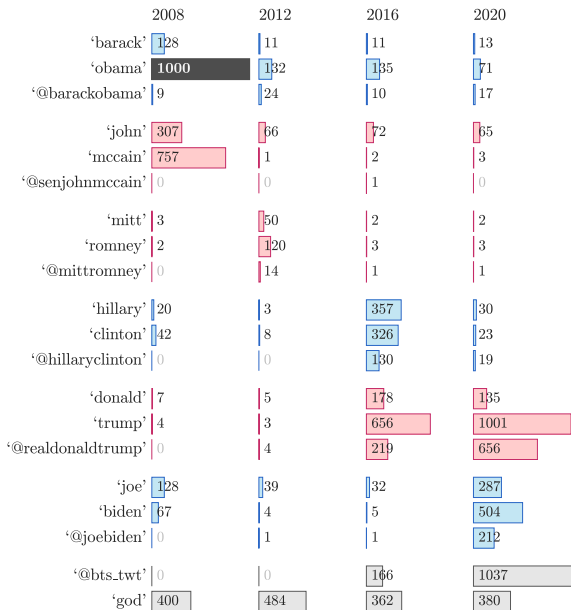
$r \gg 10^5$



## Ultrafame—Percentage of days per year ranked above 'god'

|                    | 2008  | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016  | 2017  | 2018   | 2019   | 2020   | 2021  |
|--------------------|-------|------|------|------|------|------|------|------|-------|-------|--------|--------|--------|-------|
| 'barack'           | 1.8%  | 0.3% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| 'obama'            | 54.4% | 6.9% | 0.5% | 0.5% | 2.2% | 0.3% | 0.0% | 0.3% | 2.2%  | 2.2%  | 0.5%   | 0.0%   | 0.3%   | 0.0%  |
| '@barackobama'     | 0.0%  | 0.0% | 0.0% | 0.0% | 0.5% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| 'john'             | 3.5%  | 0.6% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.3%  | 0.8%   | 0.3%   | 0.5%   | 0.0%  |
| 'mccain'           | 39.5% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.3%  | 1.1%   | 0.0%   | 0.0%   | 0.0%  |
| '@senjohnmccain'   | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| 'mitt'             | 0.0%  | 0.0% | 0.0% | 0.0% | 0.8% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| 'romney'           | 0.0%  | 0.0% | 0.0% | 0.0% | 1.6% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 0.3%   | 0.0%  |
| '@mittromney'      | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| 'hillary'          | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 10.4% | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| 'clinton'          | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 7.7%  | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| '@hillaryclinton'  | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 1.1%  | 0.0%  | 0.0%   | 0.0%   | 0.0%   | 0.0%  |
| 'donald'           | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 2.7%  | 0.5%  | 0.0%   | 0.0%   | 1.6%   | 0.6%  |
| 'trump'            | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.5% | 47.8% | 98.6% | 93.7%  | 92.3%  | 100.0% | 10.2% |
| '@realdonaldtrump' | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 2.7%  | 26.8% | 41.4%  | 62.7%  | 90.2%  | 2.2%  |
| 'joe'              | 3.5%  | 2.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 8.2%   | 0.6%  |
| 'biden'            | 1.8%  | 0.0% | 0.0% | 0.0% | 0.3% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 23.8%  | 6.1%  |
| '@joebiden'        | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0%  | 0.0%  | 0.0%   | 0.0%   | 4.1%   | 0.3%  |
| '@bts_twt'         | 0.0%  | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.0% | 0.5% | 8.5%  | 50.7% | 100.0% | 100.0% | 98.9%  | 93.1% |

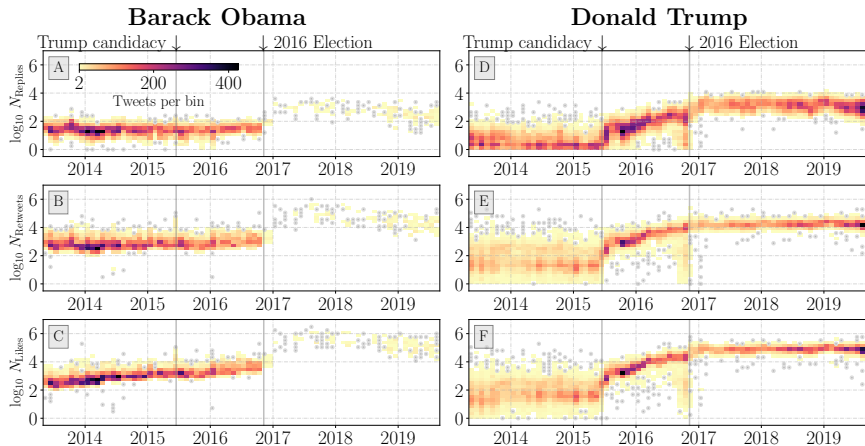
Relative median rates of ‘being talked about’  
in the 8 weeks (56 days) pre-election day:



Relative median rates of 'being talked about' per year:

|                    | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 | 2018 | 2019 | 2020 | 2021 |
|--------------------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 'barack'           | 50   | 38   | 17   | 9    | 10   | 7    | 8    | 11   | 14   | 15   | 14   | 14   | 19   | 3    |
| 'obama'            | 897  | 379  | 52   | 87   | 97   | 79   | 91   | 103  | 56   | 60   | 129  | 106  | 104  | 17   |
| '@barackobama'     | 10   | 8    | 11   | 10   | 17   | 15   | 16   | 13   | 13   | 17   | 17   | 13   | 24   | 5    |
| 'john'             | 405  | 274  | 88   | 26   | 117  | 104  | 113  | 121  | 118  | 29   | 28   | 114  | 108  | 82   |
| 'mccain'           | 579  | 11   | 4    | 2    | 2    | 2    | 1    | 1    | 3    | 15   | 7    | 5    | 3    | 2    |
| '@senjohnmccain'   | 0    | 2    | 1    | 0    | 0    | 1    | 1    | 1    | 1    | 9    | 2    | 0    | 0    | 0    |
| 'mitt'             | 5    | 8    | 5    | 6    | 25   | 6    | 5    | 4    | 4    | 2    | 2    | 3    | 3    | 2    |
| 'romney'           | 3    | 1    | 1    | 4    | 42   | 2    | 1    | 1    | 4    | 1    | 1    | 3    | 4    | 1    |
| '@mittromney'      | 0    | 0    | 0    | 0    | 5    | 0    | 0    | 0    | 1    | 0    | 0    | 1    | 1    | 0    |
| 'hillary'          | 28   | 10   | 5    | 3    | 3    | 4    | 6    | 30   | 69   | 72   | 61   | 43   | 33   | 6    |
| 'clinton'          | 62   | 25   | 16   | 10   | 8    | 6    | 8    | 27   | 40   | 65   | 62   | 45   | 32   | 8    |
| '@hillaryclinton'  | 0    | 0    | 0    | 0    | 0    | 0    | 1    | 11   | 71   | 22   | 19   | 21   | 23   | 3    |
| 'donald'           | 11   | 17   | 11   | 11   | 8    | 6    | 7    | 44   | 66   | 45   | 114  | 104  | 143  | 43   |
| 'trump'            | 7    | 20   | 10   | 7    | 4    | 3    | 3    | 77   | 583  | 1000 | 865  | 808  | 1134 | 229  |
| '@realdonaldtrump' | 0    | 0    | 0    | 1    | 2    | 3    | 2    | 32   | 219  | 468  | 555  | 652  | 888  | 1    |
| 'joe'              | 57   | 87   | 38   | 87   | 66   | 58   | 44   | 46   | 50   | 48   | 44   | 78   | 97   | 117  |
| 'biden'            | 72   | 7    | 3    | 1    | 2    | 2    | 2    | 3    | 5    | 3    | 4    | 52   | 284  | 221  |
| '@joebiden'        | 0    | 0    | 0    | 0    | 0    | 0    | 0    | 0    | 1    | 1    | 2    | 18   | 62   | 28   |
| '@bts_twt'         | 0    | 0    | 0    | 0    | 0    | 5    | 36   | 23   | 242  | 595  | 2487 | 1802 | 1440 | 1437 |
| 'god'              | 666  | 851  | 687  | 694  | 791  | 719  | 607  | 616  | 601  | 590  | 612  | 611  | 612  | 510  |

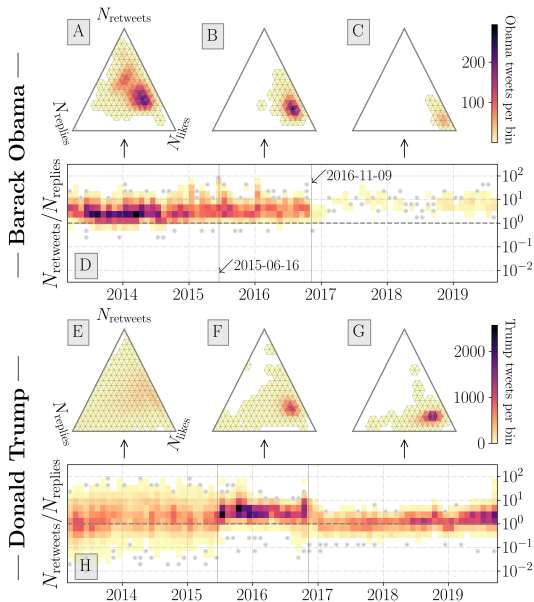
# Ratiometrics:



“Ratioming the President: An exploration of public engagement with Obama and Trump on Twitter,”

Minot et al., 2020 [22]

# Ratiometrics:



The PoCVerse  
Allotaxonomy  
102 of 124

A plenitude of  
distances

Rank-turbulence  
divergence

Probability-  
turbulence  
divergence

Explorations

Stories

Mechanics of  
Fame

Superspreading

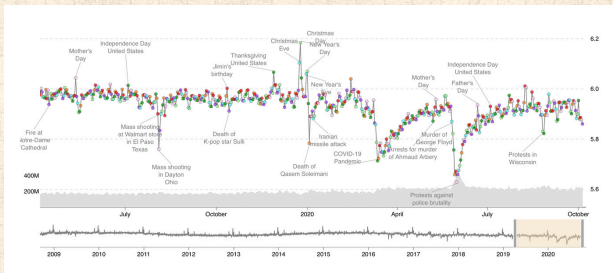
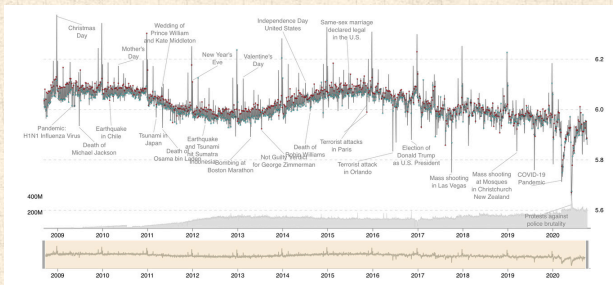
Lexical Ultrafame

Turbulent times

References



# Emotional turbulence:



The PoCverse  
Allotaxonomy  
103 of 124

A plenitude of  
distances

Rank-turbulence  
divergence

Probability-  
turbulence  
divergence

Explorations

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Mechanics of  
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Superspreading

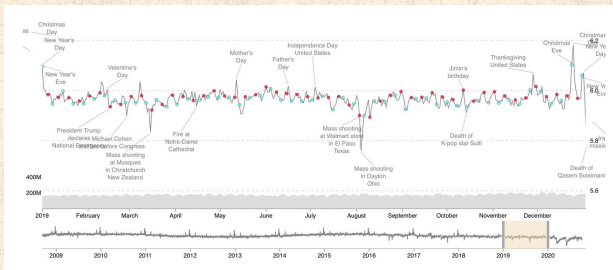
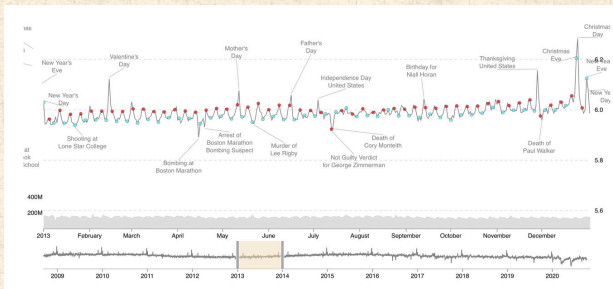
Lexical Ultrafame

Turbulent times

References



# Emotional turbulence:



The PoCverse  
Allotaxonomy  
104 of 124

A plenitude of  
distances

Rank-turbulence  
divergence

Probability-  
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Explorations

Stories

Mechanics of  
Fame

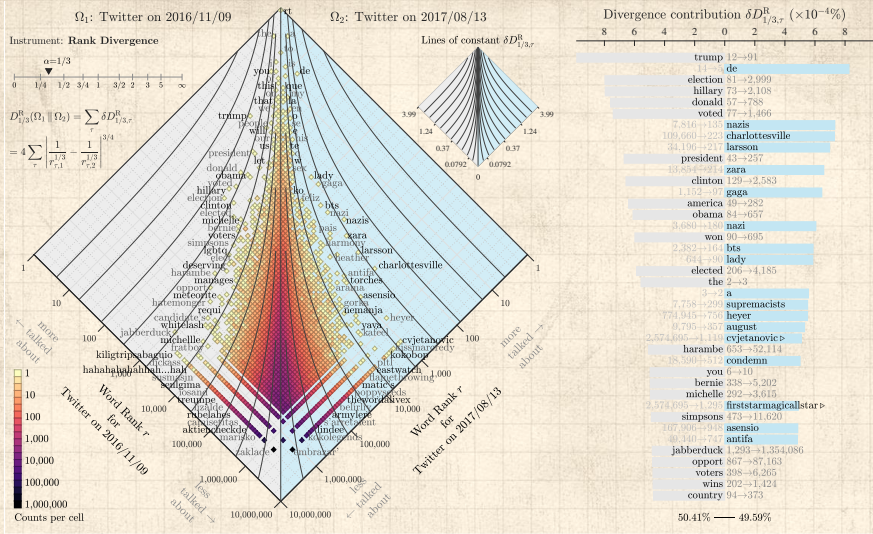
Superspreading

Lexical Ultrafame

Turbulent times

References





Allotaxonomy—  
the comparison of complex systems:

<http://compstoriolab.org/allotaxonomy/>



2016/01/01

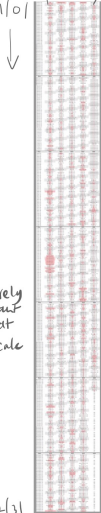


top 10 most narratively dominant words



01/01

2016 → 2020



most narratively dominant word at day-scale

most narratively dominant word at week-scale

narrative control

2020/10/05

12/31

| Week            | 2016              | 2017               | 2018          | 2019            | 2020             |
|-----------------|-------------------|--------------------|---------------|-----------------|------------------|
| 1. 01/01-01/07  | Hillary 34.7      | locking 28.6       | Bannon 2.2    | shutdown 0.0    | Iraq 9.6         |
| 2. 01/08-01/14  | Cruz 1.0          | Mercy 5.0          | Mueller 0.0   | shutdown 0.0    | Soleimani 5.9    |
| 3. 01/15-01/21  | Cruz 10.7         | inauguration 0.6   | DACA 6.7      | Pelosi 6.8      | Paras 0.0        |
| 4. 01/22-01/28  | Cruz 10.6         | inauguration 3.1   | Mueller 0.0   | Pelosi 2.6      | Ukraine 5.5      |
| 5. 01/29-02/04  | Cruz 11.2         | ban 2.1            | Mueller 0.0   | border 0.0      | impeachment 0.0  |
| 6. 02/05-02/11  | Cruz 5.1          | Bannon 0.0         | memo 2.3      | Whitaker 0.0    | Vindjanj 2.5     |
| 7. 02/12-02/18  | Cruz 6.9          | Flynn 0.0          | Mueller 0.0   | emergency 0.0   | Bar 2.2          |
| 8. 02/19-02/25  | Rubio 3.8         | Sweden 4.9         | Parkland 0.3  | Jussie 0.0      | Bloomberg 6.3    |
| 9. 02/26-03/04  | Rubio 9.2         | Russia 6.4         | Mueller 0.0   | Cohen 3.7       | coronavirus 0.0  |
| 10. 03/05-03/11 | Cruz 1.0          | Russia 4.8         | Mueller 0.0   | Nadler 13.7     | coronavirus 0.0  |
| 11. 03/12-03/18 | Cruz 5.7          | tax 1.8            | Mueller 2.2   | emergency 1.6   | coronavirus 0.0  |
| 12. 03/19-03/25 | Arizona 16.8      | Nunes 0.0          | Mueller 2.2   | Barr 0.0        | coronavirus 0.0  |
| 13. 03/26-04/01 | women 8.3         | Russia 9.9         | Stormy 0.0    | Schiff 5.2      | coronavirus 0.5  |
| 14. 04/02-04/08 | Cruz 1.5          | Russia 2.8         | Mueller 0.0   | returns 0.0     | coronavirus 0.0  |
| 15. 04/09-04/15 | Cruz 1.7          | Syria 0.4          | Mueller 2.0   | Bar 2.4         | coronavirus 0.0  |
| 16. 04/16-04/22 | Cruz 10.5         | Russia 0.5         | Mueller 0.1   | Bar 0.1         | coronavirus 0.0  |
| 17. 04/23-04/29 | Cruz 3.0          | days 0.1           | Kanye 8.0     | Biden 6.0       | coronavirus 0.0  |
| 18. 04/30-05/06 | Indiana 11.5      | Trumpcare 0.0      | Mueller 0.0   | Bar 0.0         | coronavirus 0.0  |
| 19. 05/07-05/13 | Ryan 2.5          | Comy 2.8           | Iraq 6.6      | Bar 0.0         | coronavirus 0.0  |
| 20. 05/14-05/20 | Berle 25.3        | Comy 1.0           | ZTE 4.5       | Bar 0.0         | coronavirus 0.0  |
| 21. 05/21-05/27 | Clinton 9.5       | budget 0.0         | Korea 18.2    | Bar 0.0         | pasdemie 0.0     |
| 22. 05/28-06/03 | Hillary 11.9      | Katly 4.4          | Roosevelt 4.0 | USS 3.0         | Minneapolis 32.1 |
| 23. 06/04-06/10 | Clinton 11.1      | Comy 0.8           | parson 0.0    | Memo 27.6       | police 4.2       |
| 24. 06/11-06/17 | Orlando 12.4      | Mueller 0.0        | Kin 4.1       | foreign 2.0     | Tuba 4.5         |
| 25. 06/18-06/24 | Hillary 23.9      | Trumpcare 0.0      | children 1.0  | Iraq 12.9       | Tuba 2.1         |
| 26. 06/25-07/01 | Clinton 13.0      | Russia 5.8         | Justice 8.3   | Moos 29.9       | bounties 0.0     |
| 27. 07/02-07/08 | Crooked 80.6      | CNN 0.0            | toeddlers 0.0 | parade 0.0      | Rushmore 2.3     |
| 28. 07/09-07/15 | Crooked 71.5      | Russian 1.2        | NATO 13.0     | Epstein 0.0     | coronavirus 0.0  |
| 29. 07/16-07/22 | Pence 2.9         | Mueller 0.0        | Helmski 3.1   | nazi 0.8        | coronavirus 0.0  |
| 30. 07/23-07/29 | DNC 6.1           | Scouts 0.0         | Cohen 0.0     | Baltimore 13.6  | Portland 11.8    |
| 31. 07/30-08/05 | Khan 6.5          | Mueller 0.0        | LeBron 0.7    | Baltimore 9.4   | pasdemie 0.0     |
| 32. 08/06-08/12 | Crooked 55.2      | Kore 5.8           | Omarosa 0.4   | Past 7.6        | USPS 0.0         |
| 33. 08/13-08/19 | Manafort 0.0      | Charlotteville 1.5 | Greenland 9.5 | Greenland 6.9   | USPS 0.0         |
| 34. 08/20-08/26 | Clinton 7.6       | Charlotteville 3.8 | Cohen 2.7     | Greenland 8.0   | Biden 6.6        |
| 35. 08/27-09/02 | Crooked 57.4      | Harvey 0.0         | Oh 14.0       | Dorian 12.2     | Kerzhals 9.5     |
| 36. 09/03-09/09 | Boudi 0.0         | DACA 2.4           | Kavanaugh 2.1 | Dustin 12.6     | Atlantic 4.8     |
| 37. 09/10-09/16 | deplorable 0.0    | ESPN 2.7           | Puerto 7.5    | flavored 0.0    | Woodward 2.6     |
| 38. 09/17-09/23 | Clinton 6.5       | Kin 4.9            | Kavanaugh 1.7 | Ukraine 4.5     | coronavirus 0.0  |
| 39. 09/24-09/30 | debate 4.9        | Puerto 4.7         | Kavanaugh 9.5 | Ukraine 6.8     | ballots 0.7      |
| 40. 10/01-10/07 | Pence 4.9         | Puerto 2.1         | Kavanaugh 6.8 | Ukraine 5.1     | Covid 0.0        |
| 41. 10/08-10/14 | sexual 0.3        | Puerto 1.8         | Kavanaugh 4.3 | Kurfs 8.2       |                  |
| 42. 10/15-10/21 | rigged 10.1       | Puerto 0.2         | Puerto 5.3    | Kurfs 3.7       |                  |
| 43. 10/22-10/28 | star 0.0          | Mueller 0.0        | Mueller 0.0   | caravan 0.0     | impeachment 0.0  |
| 44. 10/29-11/04 | FBI 5.9           | Mueller 0.0        | caravan 0.0   | impeachment 0.0 | impeachment 0.0  |
| 45. 11/05-11/11 | Clinton 0.9       | Gillespie 12.0     | Whitaker 6.2  | Ukraine 6.2     | Ukraine 5.2      |
| 46. 11/12-11/18 | Bannon 0.0        | sexual 1.7         | caravan 0.0   | Ukraine 5.2     | Ukraine 3.5      |
| 47. 11/19-11/25 | Hamtop 12.4       | LaVar 21.3         | Sund 1.6      | Moose 0.0       | impeachment 0.0  |
| 48. 11/26-12/02 | recount 0.0       | Moose 0.0          | Moose 0.0     | impeachment 0.0 | impeachment 0.0  |
| 49. 12/03-12/09 | Taxen 7.8         | Mueller 0.0        | Cohen 2.1     | impeachment 0.0 | impeachment 0.0  |
| 50. 12/10-12/16 | Russia 2.9        | Mueller 0.0        | Cohen 6.9     | impeachment 0.0 | impeachment 0.0  |
| 51. 12/17-12/23 | inauguration 11.8 | Mueller 0.0        | wall 9.8      | impeachment 1.4 | impeachment 1.4  |
| 52. 12/24-12/31 | inauguration 3.2  | Mueller 0.0        | wall 20.4     | impeachment 7.6 | impeachment 7.6  |

| Week            | 2016              | 2017                | 2018          | 2019            | 2020             | 2021               |
|-----------------|-------------------|---------------------|---------------|-----------------|------------------|--------------------|
| 1. 01/01-01/07  | Hillary 34.7      | hacking 28.6        | Bannon 2.2    | shutdown 0.0    | Iran 9.6         | Georgia 14.7       |
| 2. 01/08-01/14  | Cruz 1.0          | Meryl 5.0           | Mueller 0.0   | shutdown 0.0    | Soleimani 5.9    | Capitol 0.1        |
| 3. 01/15-01/21  | Cruz 10.7         | inauguration 3.6    | DACA 6.7      | Pelosi 6.8      | Parnas 0.0       | Capitol 0.0        |
| 4. 01/22-01/28  | Cruz 10.6         | inauguration 3.1    | Mueller 0.0   | Pelosi 2.6      | Ukraine 5.5      | insurrection 0.0   |
| 5. 01/29-02/04  | Cruz 11.2         | ban 2.1             | Mueller 0.0   | border 0.0      | impeachment 0.0  | Greene 0.0         |
| 6. 02/05-02/11  | Cruz 5.1          | Bannon 0.0          | memo 2.3      | Whitaker 0.0    | Vindman 2.5      | insurrection 0.0   |
| 7. 02/12-02/18  | Cruz 6.9          | Flynn 0.0           | Mueller 0.0   | emergency 0.0   | Barr 2.2         | Capitol 0.0        |
| 8. 02/19-02/25  | Rubio 3.8         | Sweden 4.9          | Parkland 0.3  | Jussie 0.0      | Bloomberg 6.3    | Capitol 0.0        |
| 9. 02/26-03/04  | Rubio 9.2         | Russia 6.4          | Mueller 0.0   | Cohen 3.7       | coronavirus 0.0  | Capitol 0.0        |
| 10. 03/05-03/11 | Cruz 1.0          | Russian 4.8         | Mueller 0.0   | Nadler 13.7     | coronavirus 0.0  | insurrection 0.0   |
| 11. 03/12-03/18 | Cruz 5.7          | tax 1.8             | Mueller 2.2   | emergency 1.6   | coronavirus 0.0  | Biden 0.0          |
| 12. 03/19-03/25 | Arizona 16.8      | Nunes 0.0           | Mueller 2.2   | Barr 0.0        | coronavirus 0.0  | Biden 0.0          |
| 13. 03/26-04/01 | women 8.3         | Russia 9.9          | Stormy 0.0    | Schiff 5.2      | coronavirus 0.5  | Capitol 0.0        |
| 14. 04/02-04/08 | Cruz 1.5          | Russia 2.8          | Mueller 0.0   | returns 0.0     | coronavirus 0.0  | Matt 0.0           |
| 15. 04/09-04/15 | Cruz 1.7          | Syria 4.0           | Mueller 2.0   | Barf 2.4        | coronavirus 0.0  | Capitol 0.0        |
| 16. 04/16-04/22 | Cruz 10.5         | Russia 0.5          | Mueller 0.1   | Barr 0.1        | coronavirus 0.0  | Capitol 0.0        |
| 17. 04/23-04/29 | Cruz 3.0          | days 0.1            | Kanye 8.0     | Biden 6.0       | coronavirus 0.0  | audit 0.0          |
| 18. 04/30-05/06 | Indiana 11.5      | Trumpcare 0.0       | Mueller 0.0   | Barr 0.0        | coronavirus 0.0  | Cheeny 0.0         |
| 19. 05/07-05/13 | Ryan 2.5          | Comey 2.8           | Iran 6.6      | Barr 0.0        | coronavirus 0.0  | Cheeny 0.0         |
| 20. 05/14-05/20 | Bernie 25.3       | Comey 1.0           | ZTE 4.5       | Barr 0.0        | coronavirus 0.0  | Cheeny 0.0         |
| 21. 05/21-05/27 | Clinton 9.5       | budget 0.0          | Korea 18.2    | Barr 0.0        | pandemic 0.0     | Weisselberg 0.0    |
| 22. 05/28-06/03 | Hillary 11.9      | Kathy 4.4           | Roseanne 4.0  | USS 3.0         | Minneapolis 32.1 | reinstated 0.0     |
| 23. 06/04-06/10 | Clinton 11.1      | Comey 0.8           | pardon 0.0    | Mexico 27.6     | police 4.2       | McGahn 0.0         |
| 24. 06/11-06/17 | Orlando 12.4      | Mueller 0.0         | Kim 4.1       | foreign 2.0     | Tulsa 4.5        | DOJ 0.0            |
| 25. 06/18-06/24 | Hillary 23.9      | Trumpcare 0.0       | children 1.0  | Iran 12.9       | Tulsa 2.1        | Capitol 0.0        |
| 26. 06/25-07/01 | Clinton 13.0      | Russia 5.8          | Justice 8.3   | Moon 29.9       | bounties 0.0     | Organization 0.0   |
| 27. 07/02-07/08 | Crooked 80.6      | CNN 0.7             | toddlers 0.0  | parade 0.0      | Rushmore 2.3     | Weisselberg 0.0    |
| 28. 07/09-07/15 | Crooked 71.5      | Russian 1.2         | NATO 13.0     | Epstein 0.0     | coronavirus 0.0  | CPAC 0.0           |
| 29. 07/16-07/22 | Pence 2.9         | Mueller 0.0         | Helsinki 3.1  | racist 0.8      | coronavirus 0.0  | vaccinated 0.0     |
| 30. 07/23-07/29 | DNC 6.1           | Scouts 0.0          | Cohen 0.0     | Baltimore 13.6  | Portland 11.8    | Jan 0.0            |
| 31. 07/30-08/05 | Khan 6.5          | Mueller 0.0         | LeBron 0.7    | Baltimore 9.4   | pandemic 0.0     | Capitol 0.0        |
| 32. 08/06-08/12 | Crooked 55.2      | Korea 5.8           | Omarosa 4.4   | Paso 7.6        | USPS 0.0         | Rosen 0.0          |
| 33. 08/13-08/19 | Manafort 0.7      | Charlottesville 1.5 | Omarosa 9.5   | Greenland 6.9   | USPS 0.0         | Taliban 0.0        |
| 34. 08/20-08/26 | Clinton 7.6       | Charlottesville 3.8 | Cohen 2.7     | Greenland 8.0   | Biden 6.6        | Taliban 0.0        |
| 35. 08/27-09/02 | Crooked 57.4      | Harvey 0.0          | Ohr 14.0      | Dorian 12.2     | Kenosha 9.5      | Taliban 0.0        |
| 36. 09/03-09/09 | Bondi 0.0         | DACA 2.4            | Kavanaugh 2.1 | Dorian 12.6     | Atlantic 4.8     | Afghanistan 0.0    |
| 37. 09/10-09/16 | deplorable 0.0    | ESPN 2.7            | Puerto 7.5    | flavored 0.0    | Woodward 2.6     | Millie 0.0         |
| 38. 09/17-09/23 | Clinton 6.5       | Kim 4.9             | Kavanaugh 1.7 | Ukraine 4.5     | coronavirus 0.0  | Eastman 0.0        |
| 39. 09/24-09/30 | debate 4.9        | Puerto 4.7          | Kavanaugh 9.5 | Ukraine 6.8     | ballots 0.7      | audit 0.0          |
| 40. 10/01-10/07 | Pence 4.9         | Puerto 2.1          | Kavanaugh 9.8 | Ukraine 5.1     | Covid 1.4        | Bannon 0.0         |
| 41. 10/08-10/14 | sexual 0.3        | Puerto 1.8          | Kavanaugh 4.3 | Kurds 8.2       | COVID 1.4        | Jan 0.0            |
| 42. 10/15-10/21 | rigged 10.1       | Puerto 0.2          | Saudi 5.3     | Kurds 3.7       | Biden 8.2        | Powell 0.0         |
| 43. 10/22-10/28 | star 0.0          | Mueller 0.0         | caravan 0.0   | impeachment 0.0 | Biden 9.2        | Jan 0.0            |
| 44. 10/29-11/04 | FBI 5.9           | Mueller 0.0         | caravan 0.0   | impeachment 0.0 | Biden 10.0       | Youngkin 0.0       |
| 45. 11/05-11/11 | Clinton 0.9       | Gillespie 12.0      | Whitaker 6.2  | Ukraine 6.2     | votes 3.4        | infrastructure 0.0 |
| 46. 11/12-11/18 | Bannon 0.0        | sexual 1.7          | caravan 0.0   | Ukraine 5.2     | Dominion 23.2    | Christie 0.0       |
| 47. 11/19-11/25 | Hamilton 12.4     | LaVar 21.3          | Saudi 1.6     | Ukraine 3.5     | Sidney 0.1       | Rittenhouse 0.0    |
| 48. 11/26-12/02 | recount 0.0       | Moore 0.0           | Moscov 0.1    | impeachment 3.1 | votes 24.1       | Waukesha 0.0       |
| 49. 12/03-12/09 | Taiwan 7.8        | Mueller 0.0         | Cohen 2.1     | impeachment 0.0 | Georgia 20.2     | Meadows 0.0        |
| 50. 12/10-12/16 | Russia 2.9        | Mueller 0.0         | Cohen 6.9     | impeachment 0.0 | vaccine 11.1     | Meadows 0.0        |
| 51. 12/17-12/23 | inauguration 11.8 | Mueller 0.0         | wall 9.8      | impeachment 1.4 | vaccine 15.4     | Manchin 0.0        |
| 52. 12/24-12/31 | inauguration 3.2  | Mueller 0.0         | wall 20.4     | impeachment 7.6 | Election 60.2    | Brandon 0.0        |

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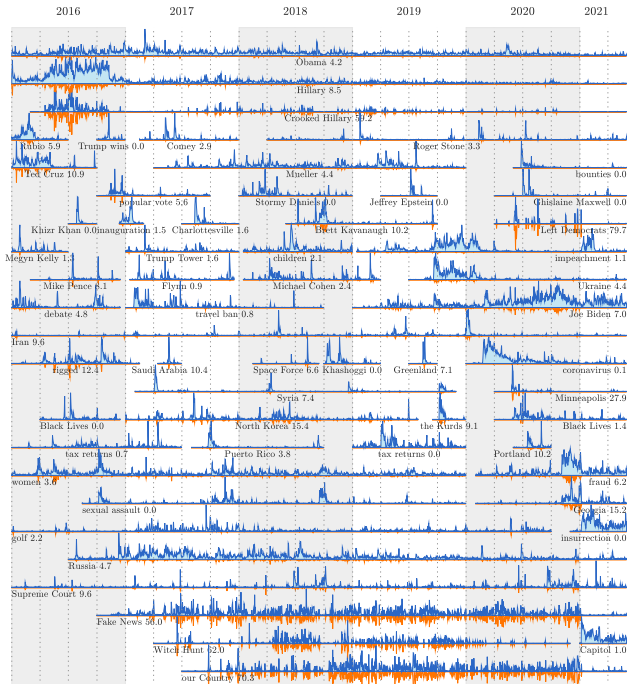
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| Week            | 2016                  | 2017                     | 2018                       | 2019                    | 2020                  | 2021                    |
|-----------------|-----------------------|--------------------------|----------------------------|-------------------------|-----------------------|-------------------------|
| 1. 01/01-01/07  | Hillary Clinton 32.7  | plant in 85.1            | Steve Bannon 5.7           | the government 0.0      | a war 6.6             | in Georgia 20.2         |
| 2. 01/08-01/14  | Trump rally 0.0       | Meryl Streep 6.6         | shithole countries 0.0     | the border 1.0          | impeachment trial 0.0 | the Capitol 0.0         |
| 3. 01/15-01/21  | Ted Cruz 26.0         | Trump's inauguration 0.0 | the government 1.4         | Cohen to 0.0            | impeachment trial 0.0 | the Capitol 0.0         |
| 4. 01/22-01/28  | Megyn Kelly 4.9       | executive order 0.0      | the FBI 5.6                | the government 0.0      | impeachment trial 0.0 | the Capitol 0.0         |
| 5. 01/29-02/04  | Ted Cruz 19.7         | travel ban 1.6           | the FBI 9.4                | Ralph Northam 26.0      | impeachment trial 0.0 | the Capitol 0.0         |
| 6. 02/05-02/11  | New Hampshire 19.5    | travel ban 1.1           | military parade 0.0        | El Paso 4.7             | Alexander Vindman 7.0 | the Capitol 0.0         |
| 7. 02/12-02/18  | Ted Cruz 15.7         | Michael Flynn 0.0        | school shooting 3.1        | national emergency 0.0  | Roger Stone 4.0       | the Capitol 0.0         |
| 8. 02/19-02/25  | Ted Cruz 30.1         | Trump administration 0.0 | the NRA 0.0                | Jussie Smollett 0.0     | Bernie Sanders 13.6   | the Capitol 0.0         |
| 9. 02/26-03/04  |                       | to Russia 22.0           | Hope Hicks 0.0             | Michael Cohen 5.3       | the coronavirus 0.0   | the Capitol 0.0         |
| 10. 03/05-03/11 |                       | travel ban 0.0           | Stormy Daniels 0.0         | Tim Apple 0.0           | the coronavirus 0.0   | voted for 0.0           |
| 11. 03/12-03/18 |                       | Meals on 0.1             | Stormy Daniels 0.0         | New Zealand 17.9        | the coronavirus 0.0   | Lara Trump 0.0          |
| 12. 03/19-03/25 | Lyin' Ted 66.2        | health care 0.0          | Cambridge Analytics 0.0    | Mueller report 0.0      | the coronavirus 0.0   | the border 0.0          |
| 13. 03/26-04/01 | Trump is 0.0          | Freedom Caucus 20.8      | Stormy Daniels 0.0         | Mueller report 0.0      | the coronavirus 0.0   | Matt Gaetz 0.0          |
| 14. 04/02-04/08 | Ted Cruz 3.9          | Susan Rice 0.3           | National Guard 0.0         | tax returns 0.0         | the coronavirus 0.0   | Matt Gaetz 0.0          |
| 15. 04/09-04/15 | New York 19.3         | in Syria 0.2             | Michael Cohen 0.0          | sanctuary cities 5.3    | the coronavirus 0.0   | Matt Gaetz 0.0          |
| 16. 04/16-04/22 | Ted Cruz 28.1         | turnout for 0.0          | Michael Cohen 2.4          | Mueller report 0.0      | the coronavirus 0.0   | Maxine Waters 0.0       |
| 17. 04/23-04/29 | Trump rally 0.0       | tax plan 0.0             | the Korean 0.0             | Mueller report 0.0      | the coronavirus 0.0   | Liz Cheney 0.0          |
| 18. 04/30-05/06 | Ted Cruz 5.5          | health care 0.0          | Stormy Daniels 0.0         | Mueller report 0.0      | treated worse 0.0     | Liz Cheney 0.0          |
| 19. 05/07-05/13 | Paul Ryan 2.0         | James Comey 6.7          | the Iran 9.0               | tax returns 0.0         | tested positive 0.0   | Liz Cheney 0.0          |
| 20. 05/14-05/20 | Hillary Clinton 26.5  | Saudi Arabia 12.5        | are animals 0.0            | Lindsay Graham 0.0      | the pandemic 0.0      | Kevin McCarthy 0.0      |
| 21. 05/21-05/27 | Hillary Clinton 24.8  | Saudi Arabia 8.2         | the FBI 23.3               | Nancy Pelosi 12.5       | a mask 6.3            | the January 0.0         |
| 22. 05/28-06/03 | Trump University 3.4  | Kathy Griffin 5.7        | Samantha Bee 4.4           | John McCain 0.0         | photo op 0.0          | Memorial Day 0.0        |
| 23. 06/04-06/10 | Hillary Clinton 18.6  | James Comey 0.2          | Justin Trudeau 8.5         | with Mexico 39.2        | Left Democrats 75.1   | Jean Carroll 0.0        |
| 24. 06/11-06/17 | Trump is 0.0          | obstruction of 12.6      | their parents 0.0          | the FBI 8.5             | in Tulsa 7.4          | Trump DOJ 0.0           |
| 25. 06/18-06/24 | Hillary Clinton 20.6  | Karen Handel 16.6        | their parents 3.4          | need soap 0.0           | in Tulsa 2.2          | the Capitol 0.0         |
| 26. 06/25-07/01 | Hillary Clinton 20.5  | Fake News 37.6           | Supreme Court 3.7          | Jean Carroll 0.0        | American soldiers 0.0 | Trump Organization 0.0  |
| 27. 07/02-07/08 | Crooked Hillary 82.8  | North Korea 28.6         | Trump administration 0.0   | Jeffrey Epstein 0.0     | Mount Rushmore 3.9    | Ashli Babbitt 0.0       |
| 28. 07/09-07/15 | Crooked Hillary 73.3  | Trump Jr 0.0             | Supreme Court 7.9          | Jeffrey Epstein 0.0     | Roger Stone 0.0       | the Capitol 0.0         |
| 29. 07/16-07/22 | Mike Pence 6.8        | Secret Service 0.0       | in Helsinki 1.7            | a racist 0.0            | in Portland 0.0       | Tom Barrack 0.0         |
| 30. 07/23-07/29 | Crooked Hillary 79.6  | Boy Scouts 0.0           | Walk of 0.0                | Elijah Cummings 27.2    | in Portland 8.9       | the Capitol 0.0         |
| 31. 07/30-08/05 | Khizr Khan 0.0        | Maxine Waters 0.0        | enemy of 22.2              | El Paso 11.1            | the election 3.4      | the Capitol 0.0         |
| 32. 08/06-08/12 | Hillary Clinton 10.5  | North Korea 5.7          | Space Force 11.1           | El Paso 7.7             | Social Security 0.0   | ouvertun 0.0            |
| 33. 08/13-08/19 | Trump campaign 0.0    | white supremacists 0.0   | security clearance 0.0     | New Hampshire 26.5      | the USPS 0.0          | the Taliban 0.0         |
| 34. 08/20-08/26 | Hillary Clinton 19.1  | Joe Arpaio 3.5           | Michael Cohen 4.3          | Prime Minister 28.7     | Joe Biden 5.9         | the Taliban 0.0         |
| 35. 08/27-09/02 | Crooked Hillary 61.8  | Hurricane Harvey 0.1     | John McCain 0.2            | Hurricane Dorian 9.6    | Joe Biden 2.7         | the Taliban 0.0         |
| 36. 09/03-09/09 | in Detroit 0.0        | to end 0.0               | Brett Kavanaugh 7.6        | the Taliban 3.0         | Joe Biden 3.4         | Robert E 0.0            |
| 37. 09/10-09/16 | tax returns 0.0       | white supremacist 0.0    | Puerto Rico 8.4            | Dan Bishop 37.7         | Joe Biden 13.3        | the Taliban 0.0         |
| 38. 09/17-09/23 | Trump Jr 0.0          | North Korea 12.8         | Blasey Ford 0.0            | a foreign 6.4           | Supreme Court 7.3     | to overturn 0.0         |
| 39. 09/24-09/30 | Hillary Clinton 7.5   | Puerto Rico 5.2          | Brett Kavanaugh 15.2       | impeachment inquiry 0.0 | Supreme Court 5.7     | debt ceiling 0.0        |
| 40. 10/01-10/07 | Mike Pence 8.9        | Puerto Rico 2.6          | Supreme Court 6.9          | Adam Schiff 13.3        | Walter Reed 5.7       | the debt 0.0            |
| 41. 10/08-10/14 | sexual assault 0.0    | Puerto Rico 2.2          | Kanye West 0.0             | the Kurds 11.3          | Biden is 26.5         | the January 0.0         |
| 42. 10/15-10/21 | Hillary Clinton 19.9  | families of 0.0          | Saudi Arabia 6.6           | the Kurds 3.8           | Joe Biden 12.1        | the January 0.0         |
| 43. 10/22-10/28 | Hillary Clinton 11.7  | Myshia Johnson 0.0       | the bombs 0.0              | World Series 0.0        | Joe Biden 10.1        | Alec Baldwin 0.0        |
| 44. 10/29-11/04 | Hillary Clinton 6.5   | Twitter employee 0.0     | birthright citizenship 0.0 | the impeachment 0.0     | Joe Biden 12.6        | in Virginia 0.0         |
| 45. 11/05-11/11 | Trump wins 0.0        | mental health 0.0        | Jim Acosta 0.0             | pro quo 8.1             | the election 2.2      | infrastructure bill 0.0 |
| 46. 11/12-11/18 | Steve Bannon 0.0      | ban on 0.0               | president who 0.0          | impeachment inquiry 0.0 | the election 7.5      | Chris Christie 0.0      |
| 47. 11/19-11/25 | Mike Pence 24.3       | Roy Moore 0.0            | Saudi Arabia 2.5           | quid pro 1.3            | the election 6.7      | Kyle Rittenhouse 0.0    |
| 48. 11/26-12/02 | popular vote 17.4     | Native American 0.1      | Trump Tower 2.5            | Hong Kong 0.0           | voter fraud 32.2      | Donald Trump 0.0        |
| 49. 12/03-12/09 | Air Force 18.2        | Roy Moore 3.5            | campaign finance 0.0       | to impeach 7.7          | in Georgia 12.9       | Donald Trump 0.0        |
| 50. 12/10-12/16 | of State 7.6          | of sexual 0.0            | Michael Cohen 7.8          | articles of 0.0         | the election 9.0      | Mark Meadows 0.0        |
| 51. 12/17-12/23 | Electoral College 5.8 | tax bill 0.0             | the wall 13.7              | Christianity Today 8.1  | election fraud 13.9   | the Capitol 0.0         |



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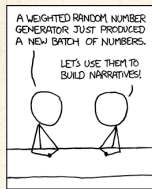
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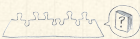




# Understanding the Sociotechnocene—Stories:



[xkcd.com/904/](http://xkcd.com/904/)



Toward a Science of Stories.



Claim: Homo narrativus—we run on stories.



“What’s the John Dory?”



“They’ve lost the plot/thread”



Narrative hierarchies and scalability of stories.



Research: Real-time and offline extraction of metaphors, frames, plots, narratives, conspiracy theories, and stories from large-scale text.



Research: The taxonomy of human stories.



To be built:  
Storyscopes—improvable, online, interactive instruments.

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