Data from our man Zipf

Last updated: 2022/08/27, 23:54:10 EDT

Principles of Complex Systems, Vols. 1, 2, & 3D CSYS/MATH 300, 303, & 394, 2022-2023 @pocsvox

Prof. Peter Sheridan Dodds | @peterdodds

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Outline

Zipf in brief

Zipfian empirics

Yet more Zipfian Empirics

References

George Kingsley Zipf:

In brief:

- 🖧 Zipf 🗹 (1902–1950) was a linguist at Harvard, specializing in Chinese languages.
- local passion for statistical analysis of texts.
- 🚯 Studied human behavior much more generally ...

Zipf's masterwork:

- 🚓 "Human Behavior and the Principle of Least Effort" Addison-Wesley, 1949 Cambridge, MA^[2]
- 🚳 Bonus field of study: Glottometrics. 🗹
- 🚳 Bonus 'word' word: Glossolalia. 🗹

Human Behavior/Principle of Least Effort: @pocsvox Data from our

From the Preface—

Nearly twenty-five years ago it occurred to me that we might gain considerable insight into the mainsprings of human behavior if we viewed it purely as a natural phenomenon like everything else in the universe, ...

And—

... the expressed purpose of this book is to establish The Principle of Least Effort as the primary principle that governs our entire individual and collective behavior ...

"... a person in solving his immediate problems will

view these against the background of his probable

"... he will strive ... to minimize the total work that he

must expend in solving both his immediate problems

"[he will strive to] minimize the probable average rate of

future problems as estimated by himself."

and his probable future problems."

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The Principle of Least Effort:

Zipf's framing (p. 1):



his work-expenditure..."

Within Human Behavior and the Principle of Least Effort:

- 🚳 City sizes
- - 🚳 # services (barber shops, beauty parlors, cleaning, ...)

 - 🚓 # one-way trips in cars
- 🚓 # people moving vs. distance 🚓 # marriages vs. distance
 - Observed general dependency of 'interactions' between cities A and B on $P_A P_B / D_{AB}$ where P_A and P_B are population size and D_{AB} is distance between A and B. \Rightarrow 'Gravity Law.'

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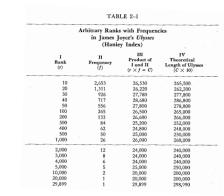
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Zipfian empirics

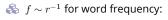
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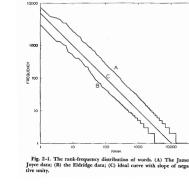
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\clubsuit vocabulary balance: $f \sim r^{-1} \rightarrow r \cdot f \sim \text{constant}$ (f = frequency, r = rank).



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- listener if all pieces of information correspond to different words (or morphemes).
- Analogy: a specialized tool for every task. Decoding is simple but encoding is hard
- Zipf thereby argues for a tension that should lead to an uneven distribution of word usage.
- No formal theory beyond this... (more later [1])

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Rampaging research

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 - # people in occupations
 - and trucks vs. distance

retail stores in cities line weight moved between

between cities

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- cities by rail # telephone messages

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Zipf's basic idea:

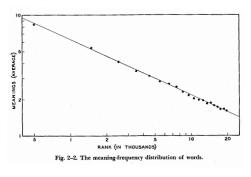
Forces of Unification and Diversification:

Easiest for the speaker to use just one word. Encoding is simple but decoding is hard

Zipf uses the analogy of tools: one tool for all tasks.

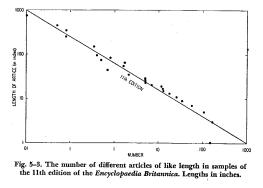


 \clubsuit Number of meanings $m_r \propto f_r^{1/2}$ where r is rank and f_r is frequency.



Zipfian empirics:

Article length in the Encyclopedia Britannica:

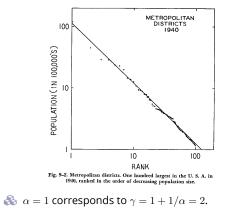


🗞 Not a rank-ordered plot; flipped frequency distribution.

(?) slope of -3/5 corresponds to $\gamma = 5/3$.

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Population size of districts:



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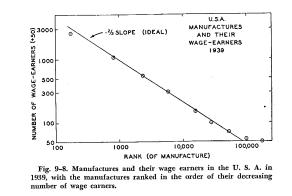
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Number of employees in organizations



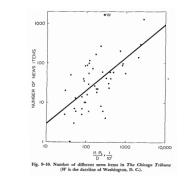
 $\alpha = 2/3$ corresponds to $\gamma = 1 + 1/\alpha = 5/2$. ୬ ବ ଦ 10 of 38

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 \Re # news items as a function of population P_2 of location in the Chicago Tribune

 $\bigotimes D$ = distance, P_1 = Chicago's population

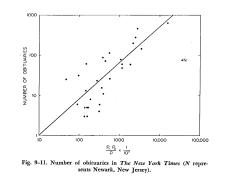
🚯 Solid line = +1 exponent.



Zipfian empirics:

obituaries in the New York Times for locations with population P_2 .

 $\gtrsim D$ = distance, P_1 = New York's population 🚳 Solid line = +1 exponent.



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corresponds to $\gamma = 2$.

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- A Movement of stuff between cities
- $\bigotimes D$ = distance, P_1 and P_2 = city populations.
- 🗞 Solid line = +1 exponent.

AP, 10 Fig. 9-14, Railway ailway express. The movement by weight (less carload lots) ween 13 arbitrary cities in the U. S. A., May 1939.

length of trip versus frequency of trip.

Not a rank-ordered plot; flipped frequency

distribution. Solid line = -1/2 exponent

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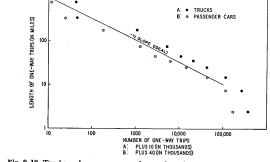
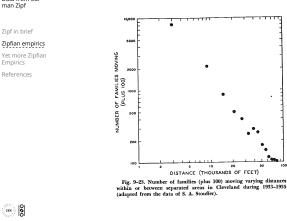


Fig. 9-19. Trucks and passenger cars: the number of one-way trips of like length.

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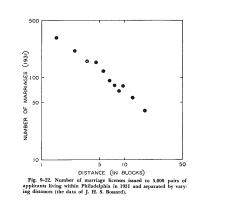
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Empirics References



The probability of marriage? $\gg \gamma = 1?$



Comment #60 in Math and the City 🕑 by Strogatz, NYT:

60. May 20, 2009 9:26 am

Link

George Kingsley Zipf was my teacher at Harvard...He had given a class project where we were to see if Chemical Companies when ranked by the number of different chemicles they produced, followed his Law of Least Effort. I missed turning in my assignment due to the accidental death of my father When I returned from the funeral I was given a message to call Dr. Zipf immediately. I did and when I explained why I was late turning in the data. He said, "Well, your father's gone and I (Zipf) have no pipeline to God. I expect the data will be on my desk tomorrow morning!".....My mother, sister and extended family spread huge books of trade magazines on the kitchen and dining room tables and furiously went to work We worked until late in the night and finished the project I drove to Harvard the next morning and angrily gave the hundreds of 'three by five cards' to Zipf. All he said was, "Thank you." Years later, I wondered whether his'meaness' had really been his way of helping me and my family to take our minds of our grief that day and concentrate on finishing my assignment. In my youth I thought not, but now as I approach 80, I like to think his seemingly hurtful attitude was really an act of kindness,,,,,

- Jim Terry

Zipfian empirics:



I Frequency (f)	Calculated N(f ² - 1/4)		
	II Ulyssea	III Plautus	
1	12,324	4,075	
2	15,410	4,490	
3	19,193	4,280	
4	20,239	4,750	
5	22,424	3,985	
6	22,773	4,504	
7	23,546	4,241	
8	23,651	4,399	
9	24,063	4,366	
10	22,145	4,289	
15	21,576	2,922	
20	27,844	5,996	
30	18,000	3,600	
40	25,600	4,800	
50	22,500	5,000	

Zipfian empirics:

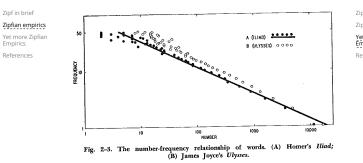
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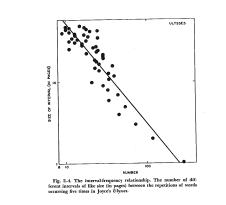
Zipf in brief

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Calculated values of negative slopes, errors, and Y-intercepts of the t ber, N, of intervalsites, I_{λ} between the repetition of words in 14 freque classes, f_{λ} as fitted to the equation $aX + Y = G$ where $X = \log R$ as $= \log I_{\lambda}$ and where I_{λ} has integral values from 1 through 21 inclusiv						
I No. of Analysis	II Frequency of Occur. (f)	III No. of Different Words of like f	IV Slope of Best Line of Y's (negative) (Y = log It)	V Error (root-mean- square)	VI Y-intercep (antilog thereof)	
1	5	906	1.21	.151	716	
2	6	637	1.20	.169	666	
3	10	222	1.27	.106	677	
4	12	155	1.24	.111	491	
5	15	96	1.15	.096	328	
6	16	86	.96	.124	153	
7	17	79	1.22	.174	422	
8	18	62	1.20	.120	264	
9	19	63	1.21	.148	350	
10	20	69	1.29	.124	944	
11	21	52	1.05	.138	212	
12	22	50	1.10	.117	264	
13	23	44	1.24	.113	352	
14F	24	34	1.01	.158	136	
15Z	24	34	1.05	.147	153	

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TABLE 2-4 The dispersion of single-page intervals between the f - 1 repetitions of all words that occur with ten arbitrarily selected frequencies of occurrence, f_r in Joyce's Ulysser (Hanley's Index).





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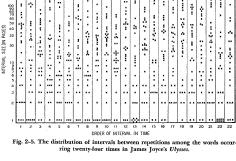
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TABLE 3-1 Zipf in brief The Frequencies and Average Lengths of Words (A) in terms of the number of phonemes, and (B) in terms of the num-ber of syllables in (A) American newspaper English and in (B) the Latin of Plautus. Zipfian empirics (B) LATIN OF PLAUTUS Yet more Zipfian Empirics Numbe of Occur-rences Average Number of Syllables Number of Occur-rences Average Number Number of of Words Syllables Average Number of Number of Words References 5429 1198 492 299 161 126 87 (3.23) (2.92) (2.05) (2.60) (2.53) (2.35) (2.35) (2.30) (2.30) (2.30) (2.30) (2.30) (2.30) (2.30) (2.07) (2.07) (2.40) (2.09) (2.09) (2.01) (2.05 (\$ 903) (1.70 (2,08)

62-514 33.094

8.43

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Numbe of Occur-

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Number of Words

(3.333) 12 666 (2,00)

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(A) AMERICAN NEWSPAPER ENGLISH

(According to R. C. Eldridge)

Numb of Occur

Number of Words

Average Number of

(6.656) (6.151) (6.015) (6.081) (5.768) (5.768) (5.333) (5.654) (5.377) (4.825) (5.459) (5.367) (4.825) (5.469) (5.500) (5.00) (5.500) (5.500) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.333) (5.564) (5.337) (5.564) (5.337) (5.564) (5.367) (5.

(3.455)

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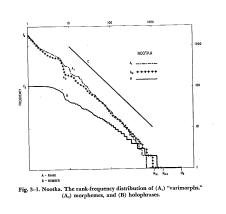
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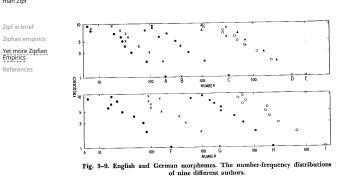


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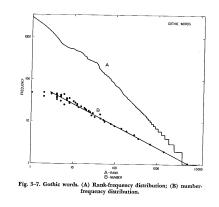
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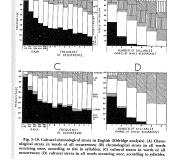






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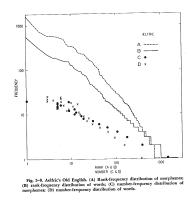
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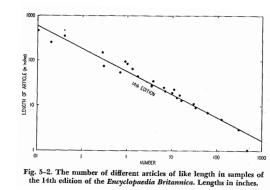
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Zipfian empirics (p. 176):

🗞 Article length in the Encylopedia Brittanica



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TABLE 6-1

The X Number of Different Genera of Like Y Number of Different Species of the Flora of Ceylon (After J. C. Willis)

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No. of Species No. of Genera X 573 1 176 2 85 3 49 4 5 36 6 20 etc.



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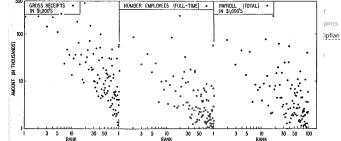


Fig. 9-9. Gross receipts, number of full-time employees, and total payroll of service establishments in the U.S.A. in 1939 when the service establishments are ranked in the order of their decreasing number of members as in Fig. 9-4 supra.

•• •••••

500 1000

50 100

Fig. 9-13. Charge accounts of Jordan Marsh Co., Boston, in 96 cities and towns in Masschusetts, New Hampshire, and Maine, with their percentages of total charge accounts plotted against the communities' values of P/D.

%

5000



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MBER OF CHARGE ACCOUNTS (PER CENT OF TOTAL)

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JORDAN MARSH CO. BOSTON

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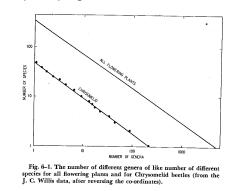


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🗞 # species per genera:





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 R. Ferrer-i-Cancho and R. V. Solé. Least effort and the origins of scaling in human language. 	Yet more Zipfian Empirics References
Proc. Natl. Acad. Sci, 100:788–791, 2003. pdf	
[2] G. K. Zipf. Human Behaviour and the Principle of Least-Effort.	
Addison-Wesley, Cambridge, MA, 1949.	

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