

# Social Contagion

Last updated: 2022/08/28, 08:34:20 EDT

Principles of Complex Systems, Vols. 1, 2, & 3D  
CSYS/MATH 300, 303, & 394, 2022-2023 | @pocsvox

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center  
Santa Fe Institute | University of Vermont

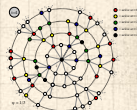


The PoCVerse  
Social Contagion  
1 of 112

Social Contagion  
Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References



Licensed under the *Creative Commons Attribution-NonCommercial-ShareAlike 3.0 License*.

These slides are brought to you by:

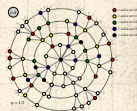
The PoCSverse  
Social Contagion  
2 of 112

Sealie & Lambie  
Productions

Social Contagion  
Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References



# These slides are also brought to you by:

## Special Guest Executive Producer



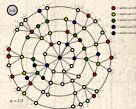
 On Instagram at [pratchett\\_the\\_cat](https://www.instagram.com/pratchett_the_cat) 

The PoCSverse  
Social Contagion  
3 of 112

Social Contagion  
Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References



# Outline

The PoCSverse  
Social Contagion  
4 of 112

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References

## Social Contagion Models

Background

Granovetter's model

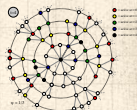
Network version

Final size

Spreading success

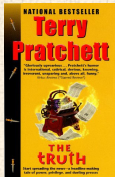
Groups

## References

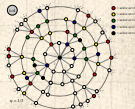




'The rumor spread through the city like wildfire



"The Truth"    
by Terry Pratchett (2000). [22]

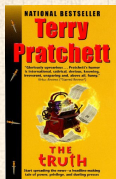


Social Contagion  
Models

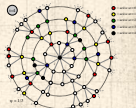
- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References

'The rumor spread through the city like wildfire which had quite often spread through Ankh-Morpork



"The Truth"    
by Terry Pratchett (2000). [22]

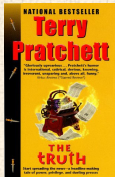


Social Contagion  
Models

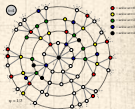
- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References

'The rumor spread through the city like wildfire which had quite often spread through Ankh-Morpork since its citizens had learned the words



"The Truth"    
by Terry Pratchett (2000). [22]



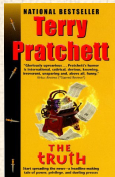


Social Contagion  
Models

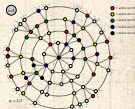
- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References

'The rumor spread through the city like wildfire which had quite often spread through Ankh-Morpork since its citizens had learned the words "fire insurance").'



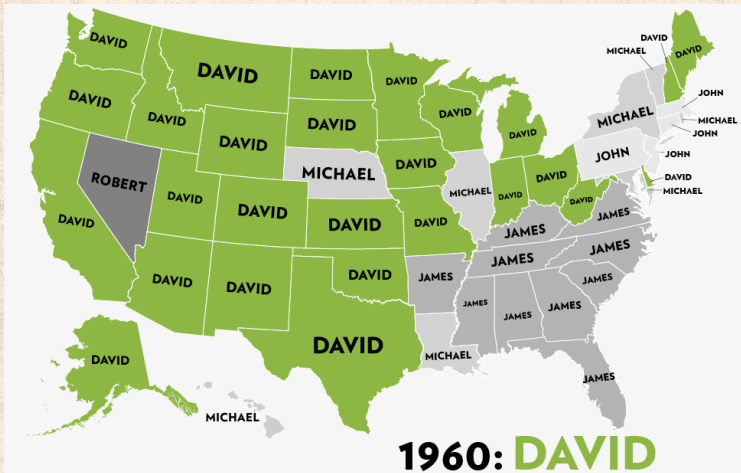
"The Truth"    
by Terry Pratchett (2000). [22]



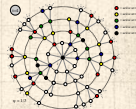
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



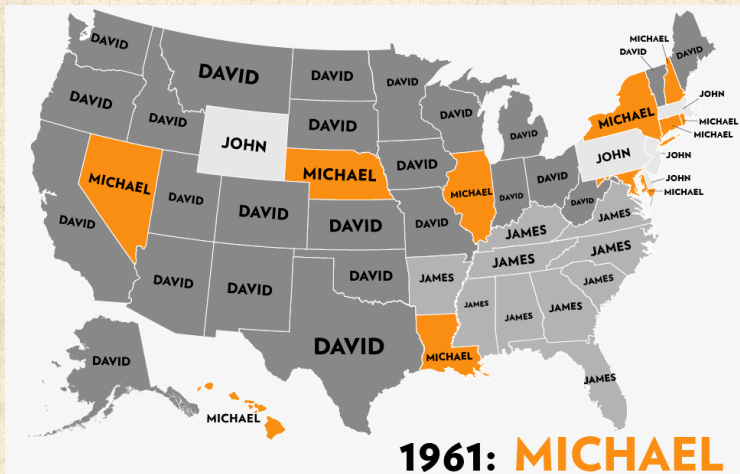
From the Atlantic ↗



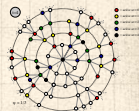
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



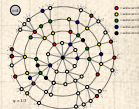
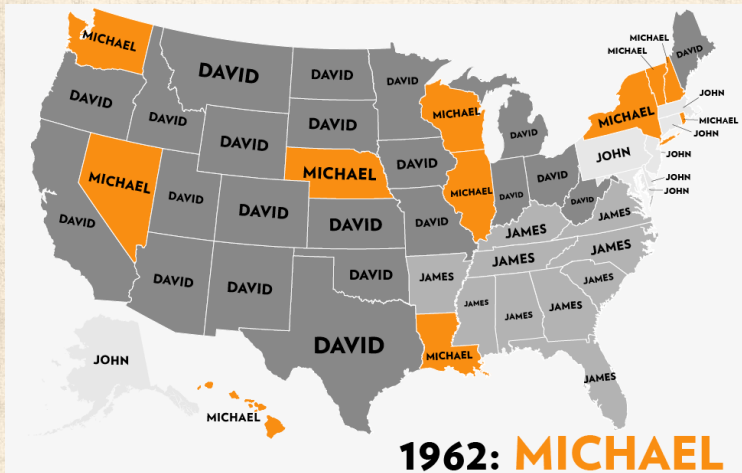
From the Atlantic 



## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References

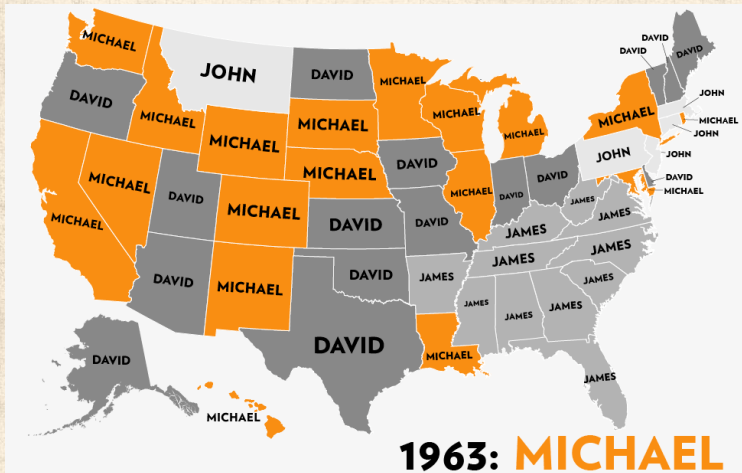


From the Atlantic 

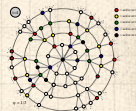
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



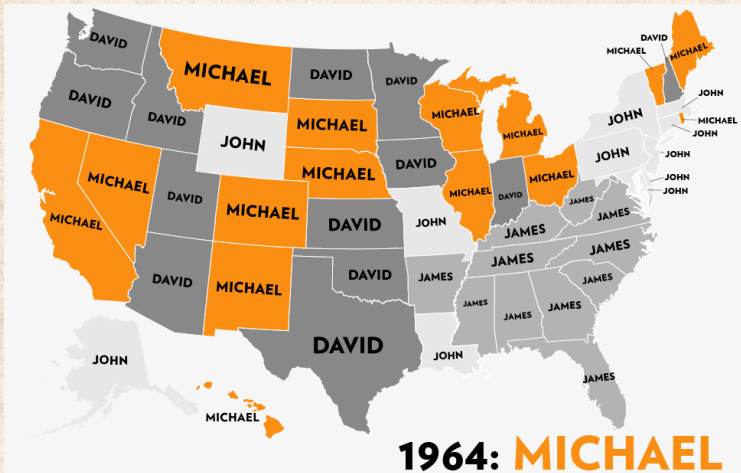
From the Atlantic 



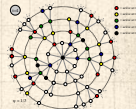
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



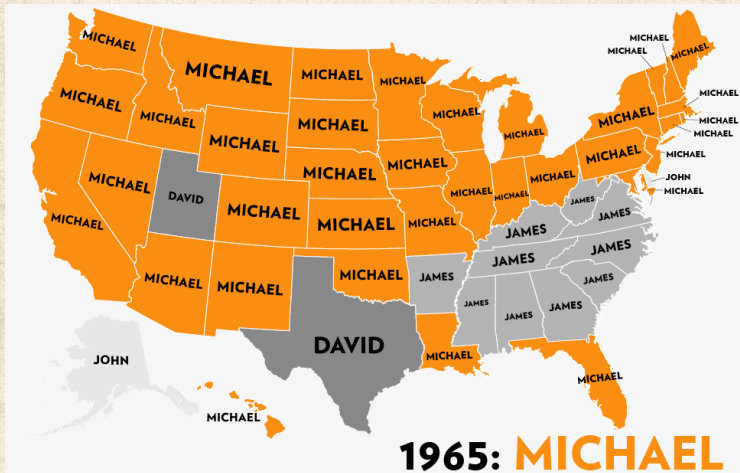
From the Atlantic ↗



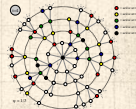
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



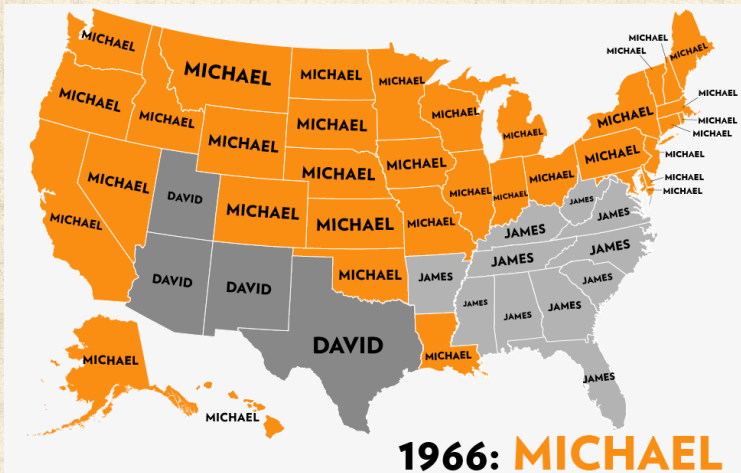
From the Atlantic ↗



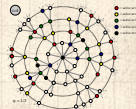
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic ↗

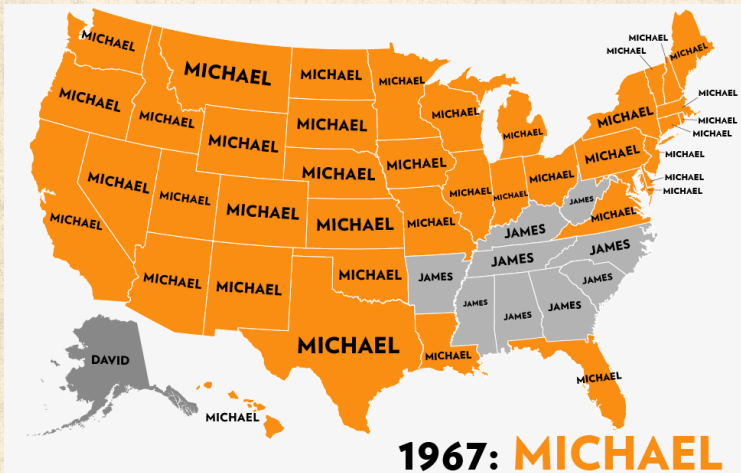




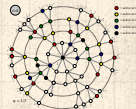
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



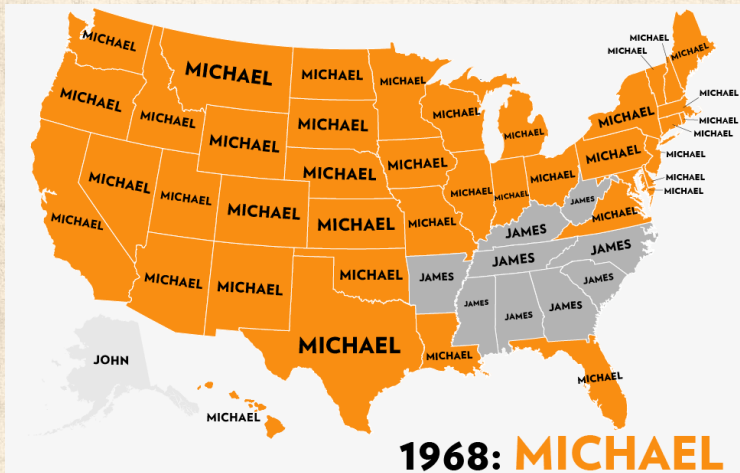
From the Atlantic ↗



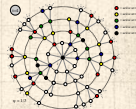
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



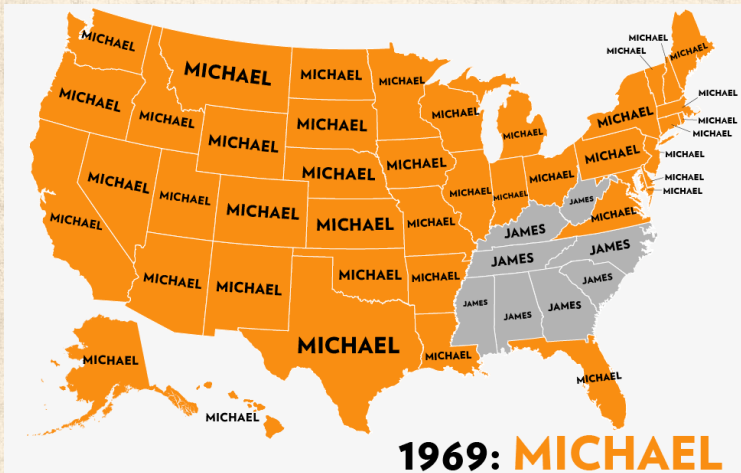
From the Atlantic ↗



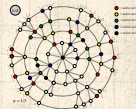
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



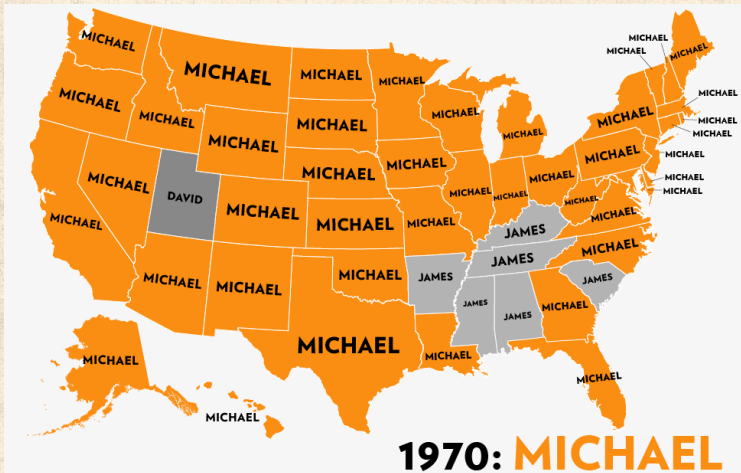
From the Atlantic ↗



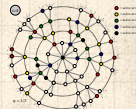
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



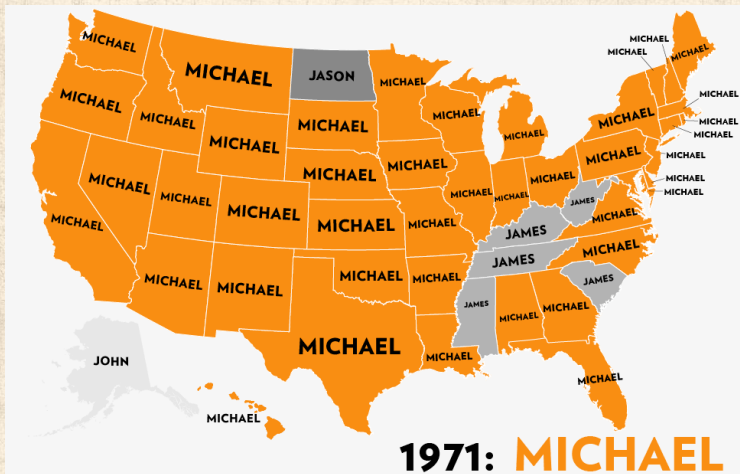
From the Atlantic ↗



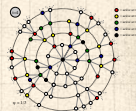
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



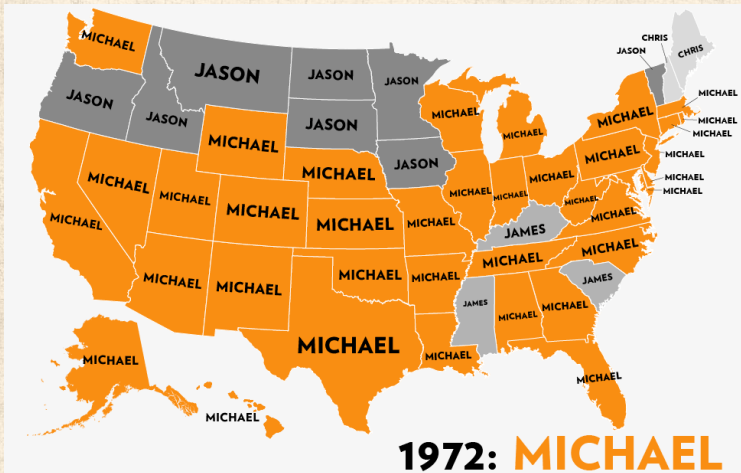
From the Atlantic ↗



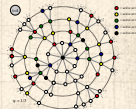
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



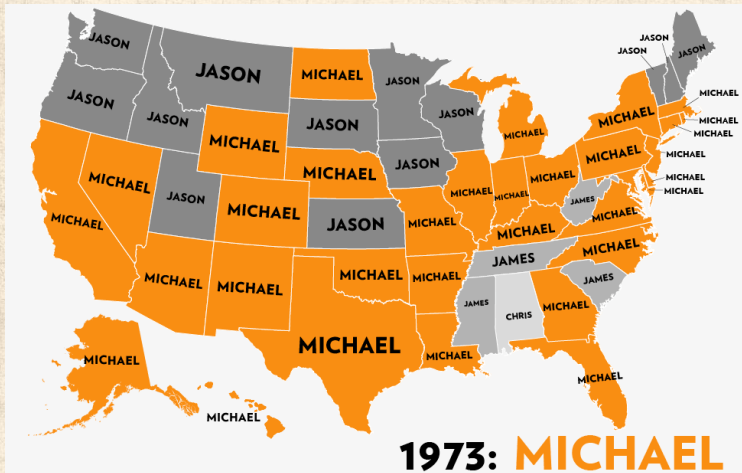
From the Atlantic ↗



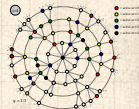
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



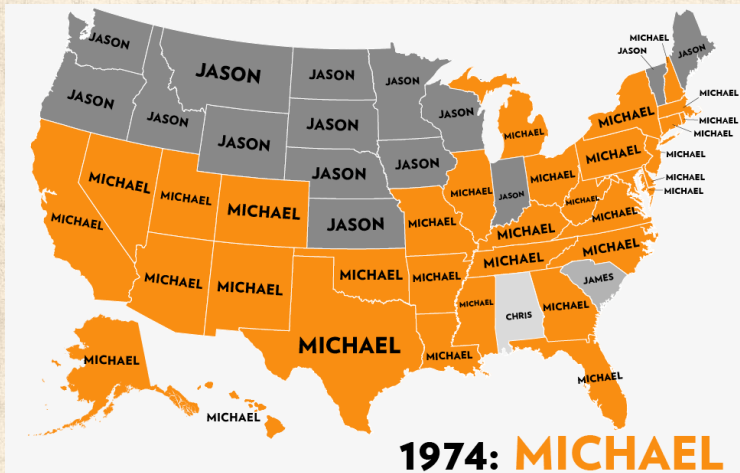
From the Atlantic 



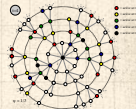
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic 

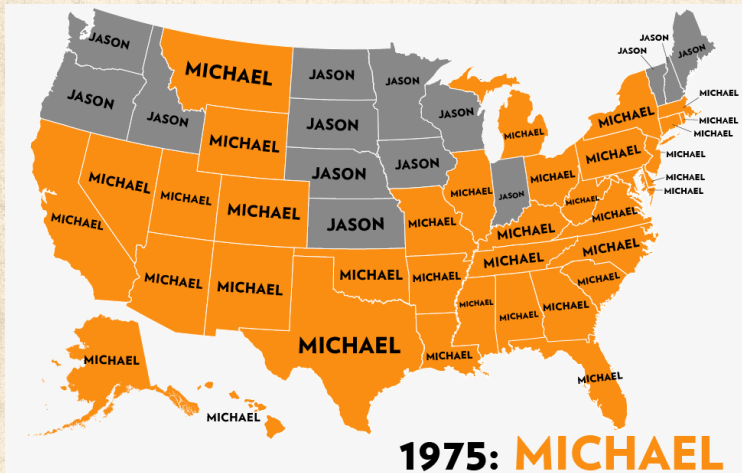




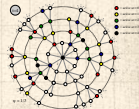
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



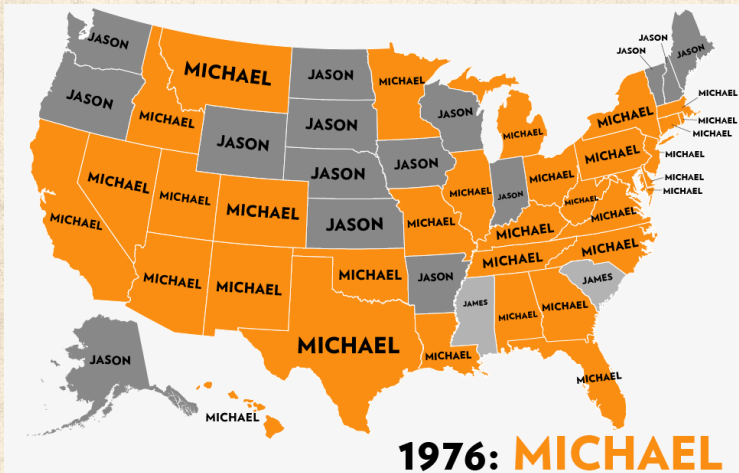
From the Atlantic 



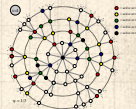
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



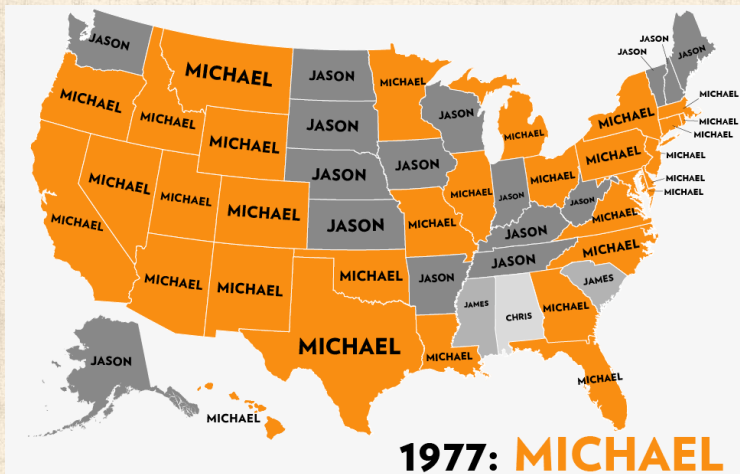
From the Atlantic ↗



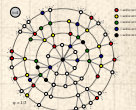
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



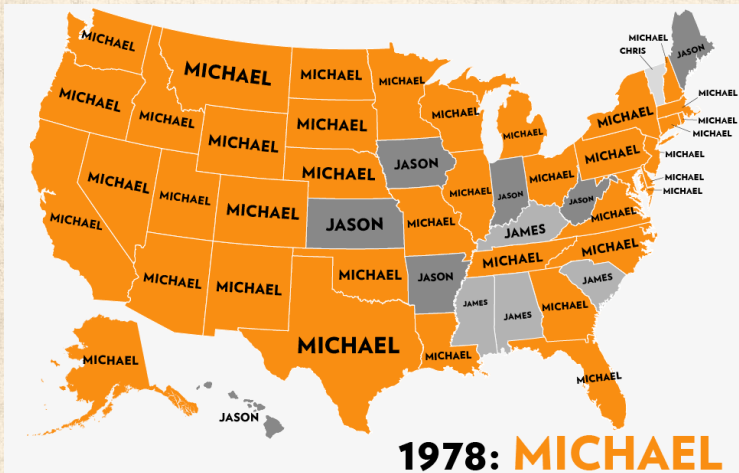
From the Atlantic ↗



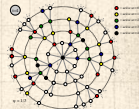
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



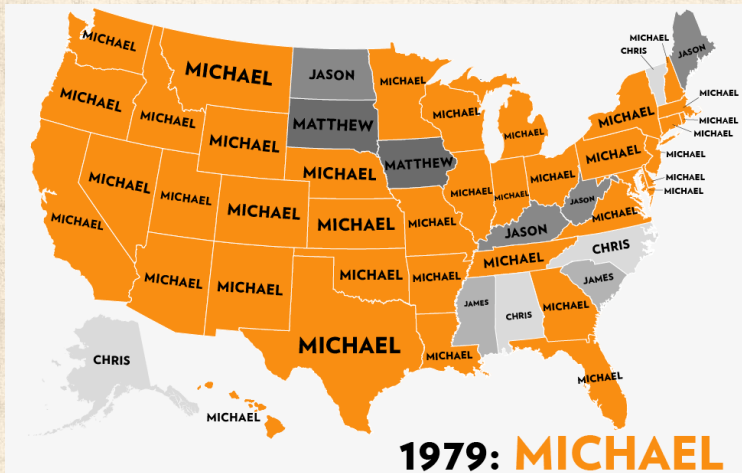
From the Atlantic 



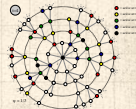
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



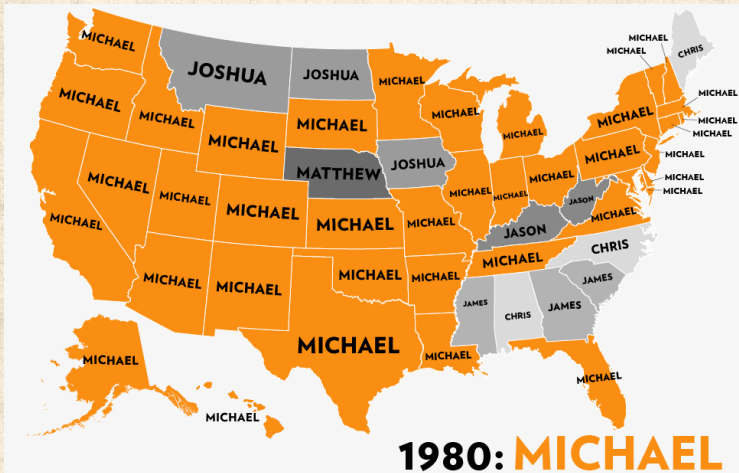
From the Atlantic ↗



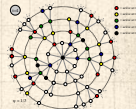
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



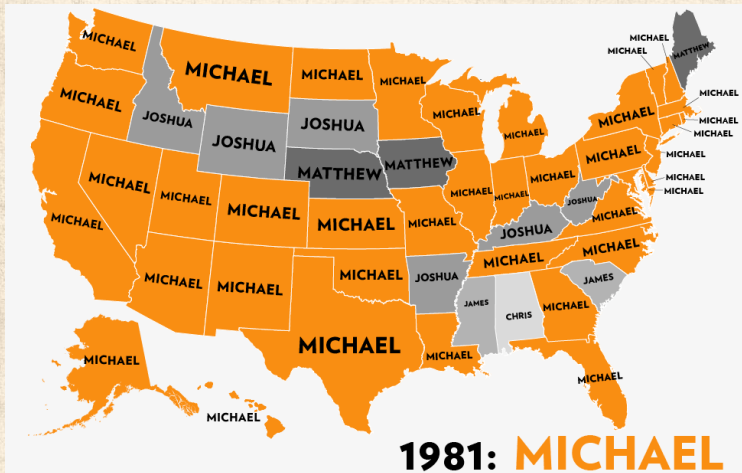
From the Atlantic ↗



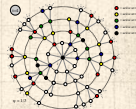
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



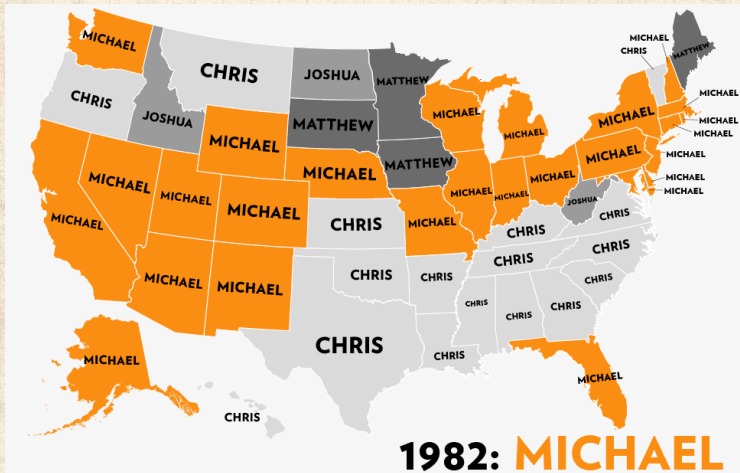
From the Atlantic ↗



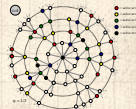
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic ↗





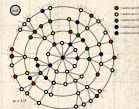
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



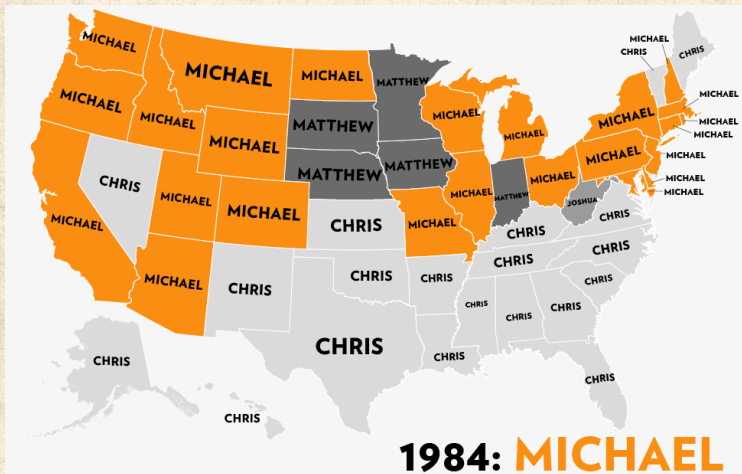
From the Atlantic 



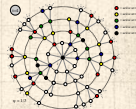
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



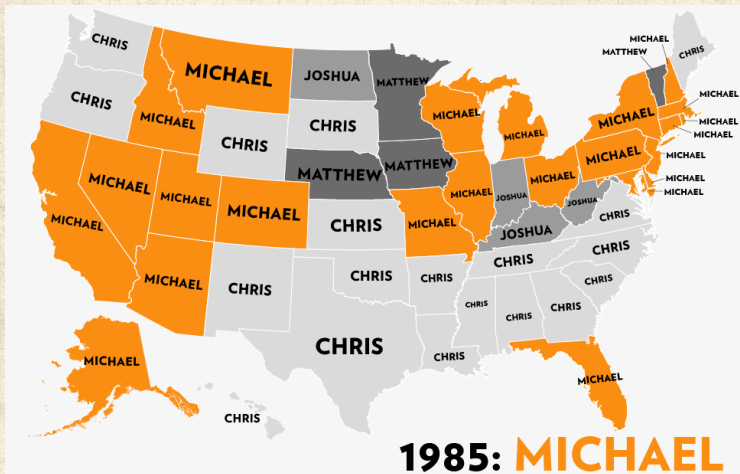
From the Atlantic 



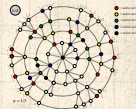
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



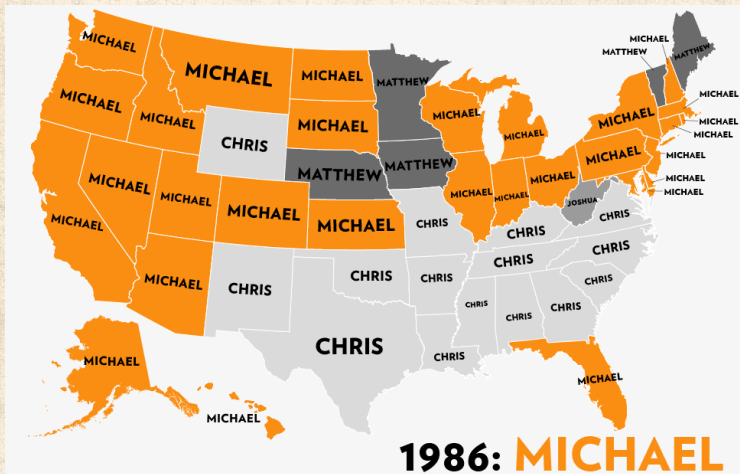
From the Atlantic ↗



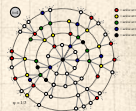
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



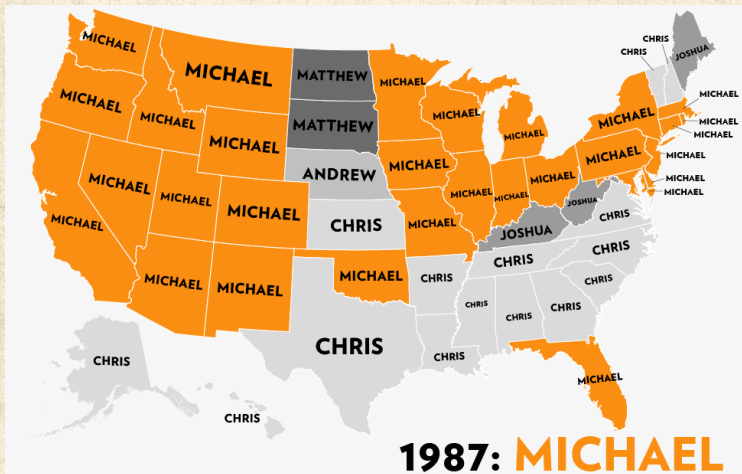
From the Atlantic 



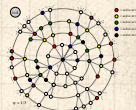
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



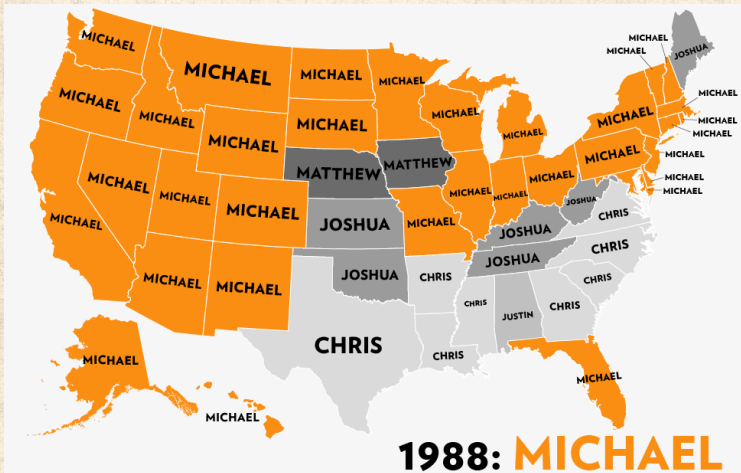
From the Atlantic ↗



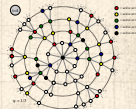
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



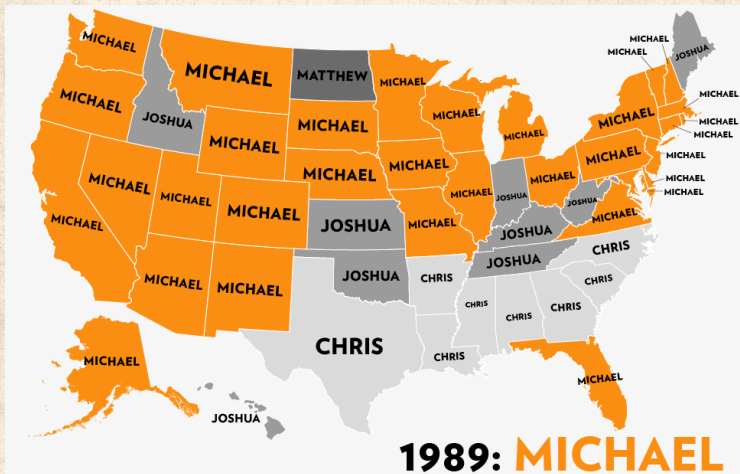
From the Atlantic ↗



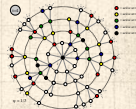
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



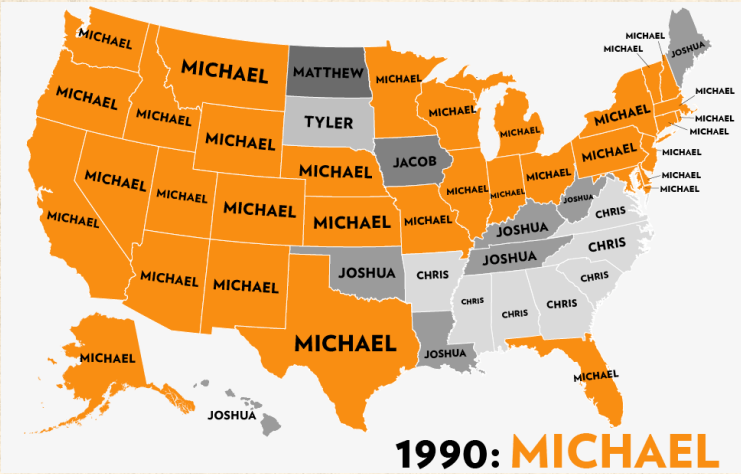
From the Atlantic ↗



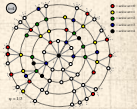
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



From the Atlantic ↗

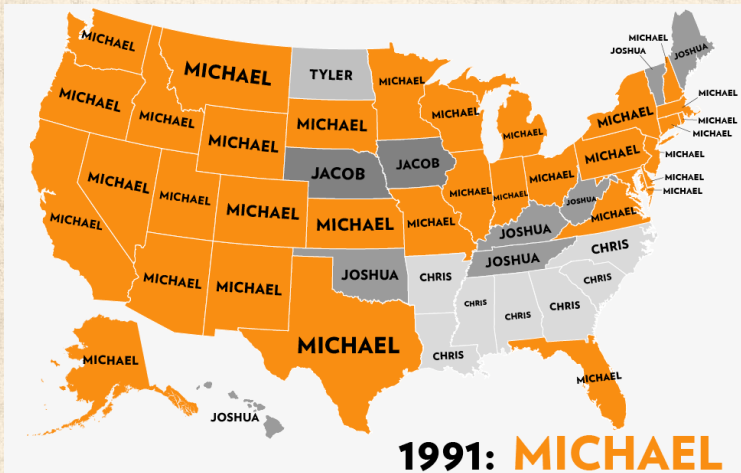




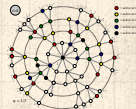
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



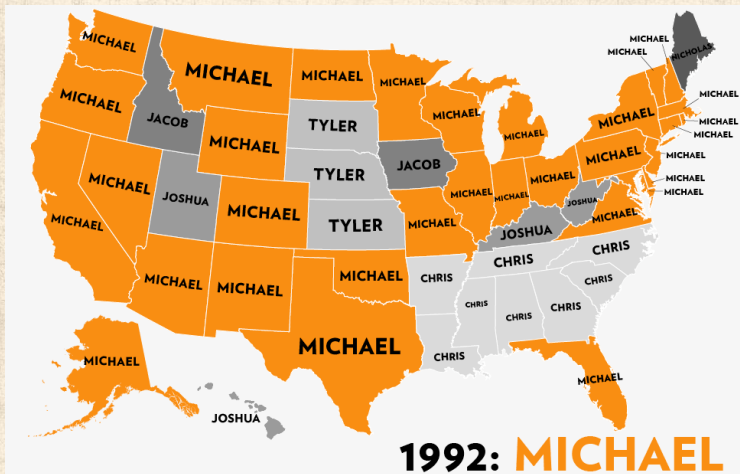
From the Atlantic ↗



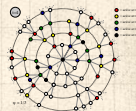
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



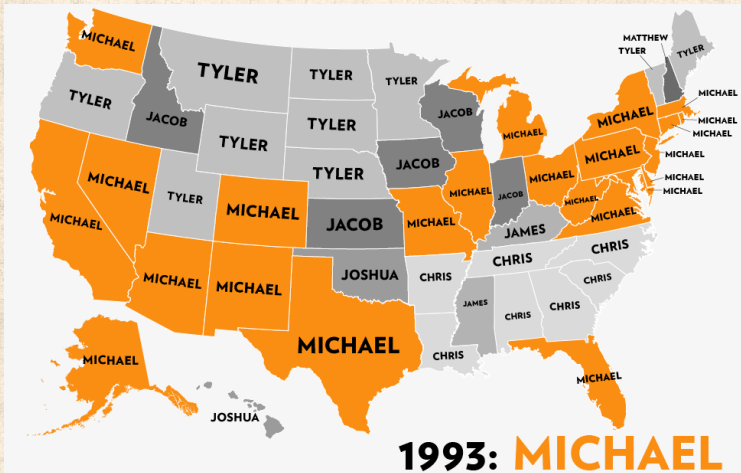
From the Atlantic ↗



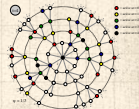
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



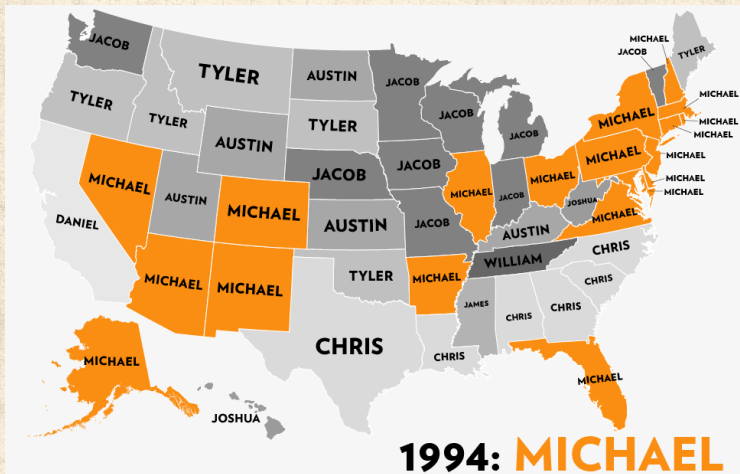
From the Atlantic 



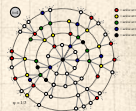
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



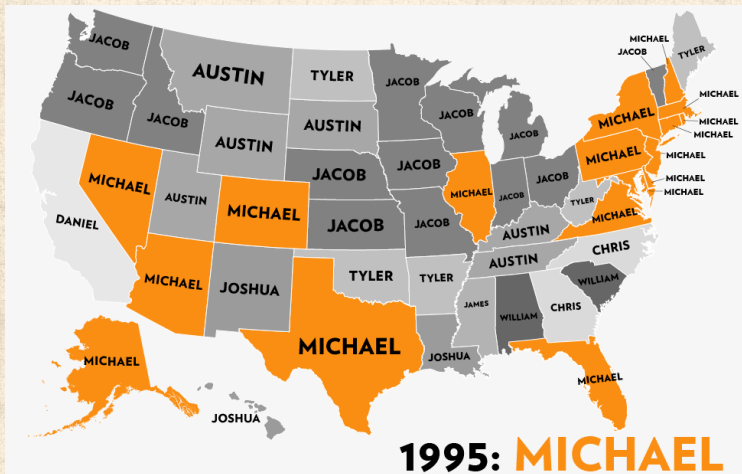
From the Atlantic 



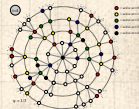
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



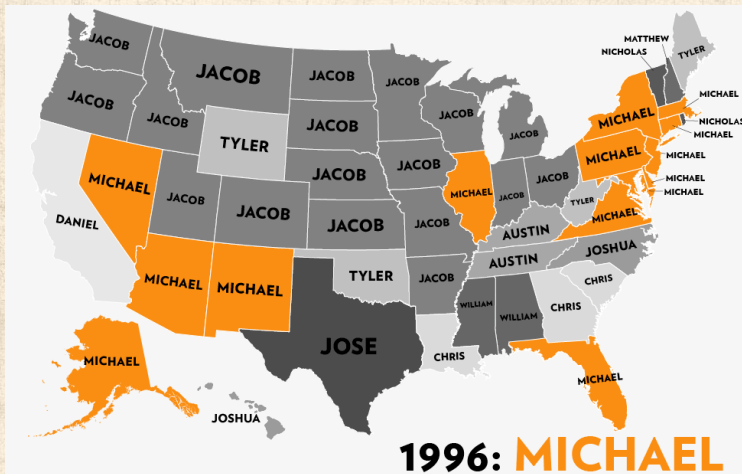
From the Atlantic 



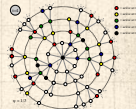
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



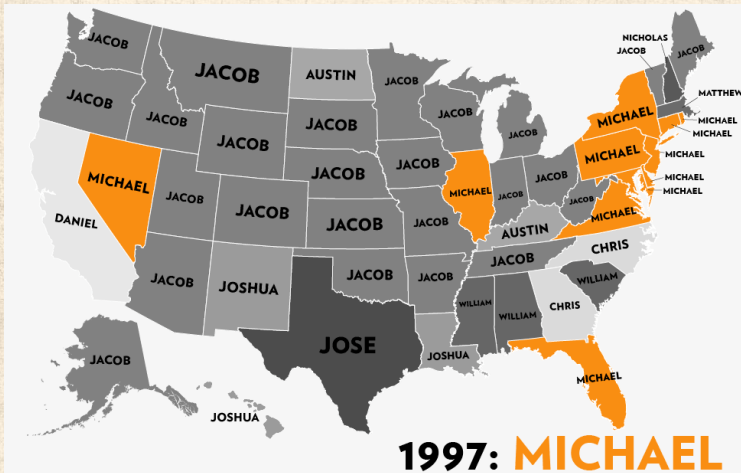
From the Atlantic 



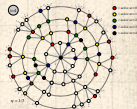
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



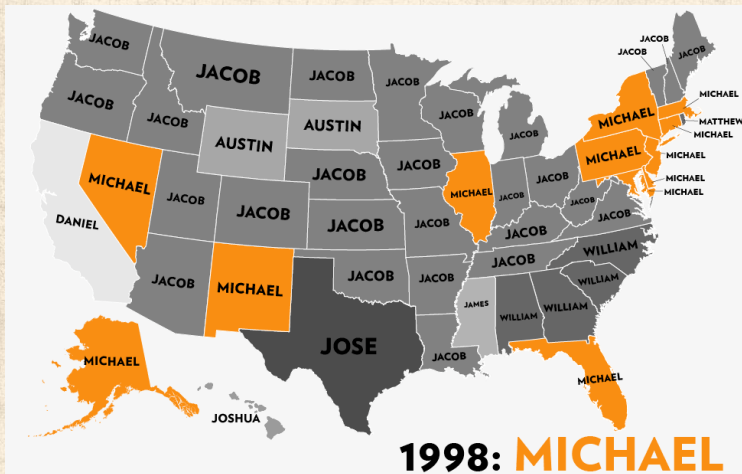
From the Atlantic ↗



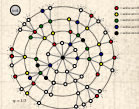
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic 

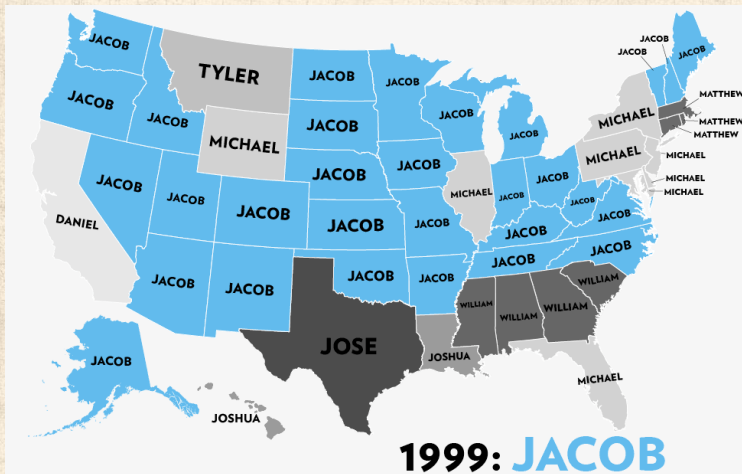




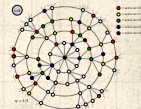
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



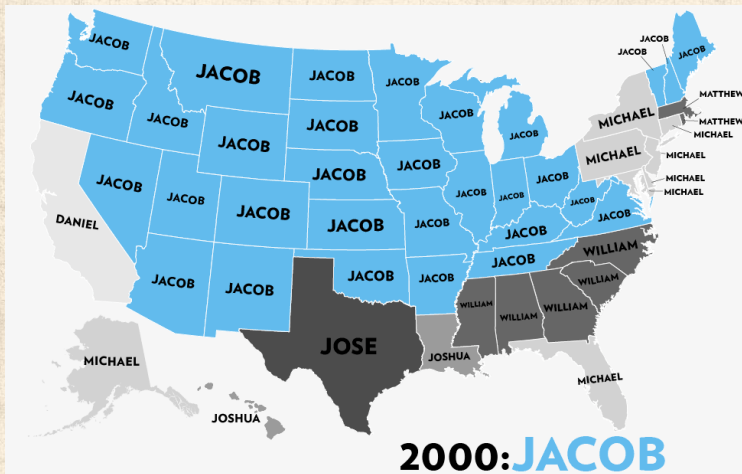
From the Atlantic 



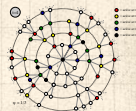
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



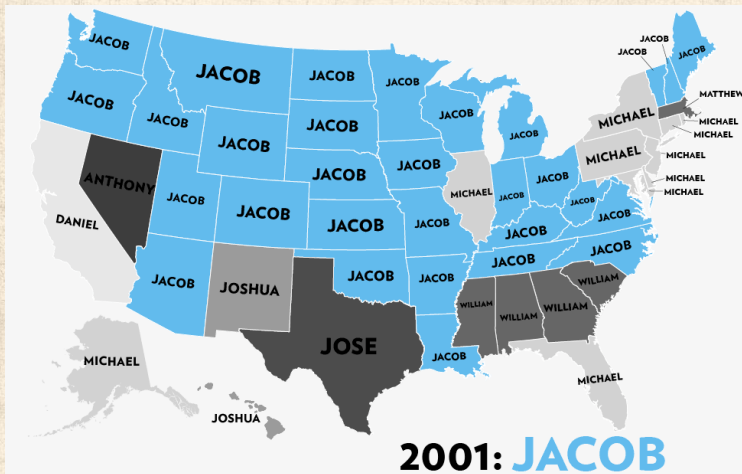
From the Atlantic ↗



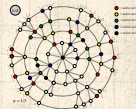
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



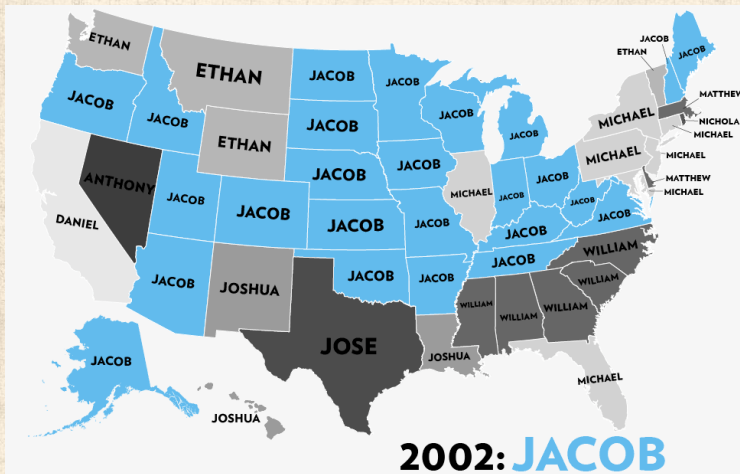
From the Atlantic 



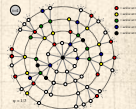
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



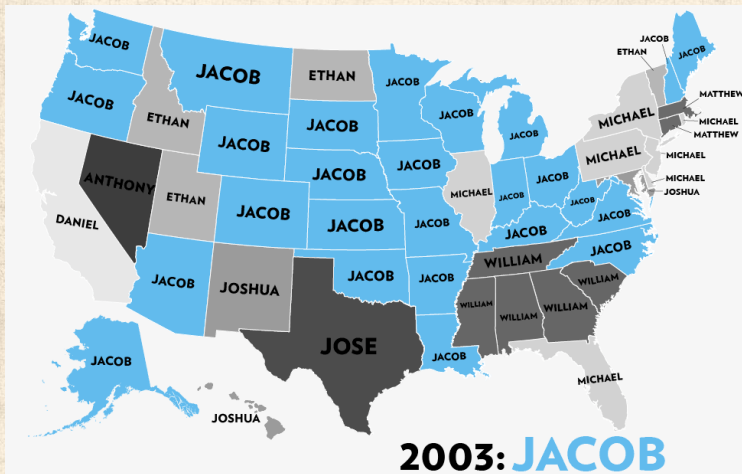
From the Atlantic 



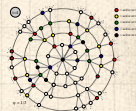
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



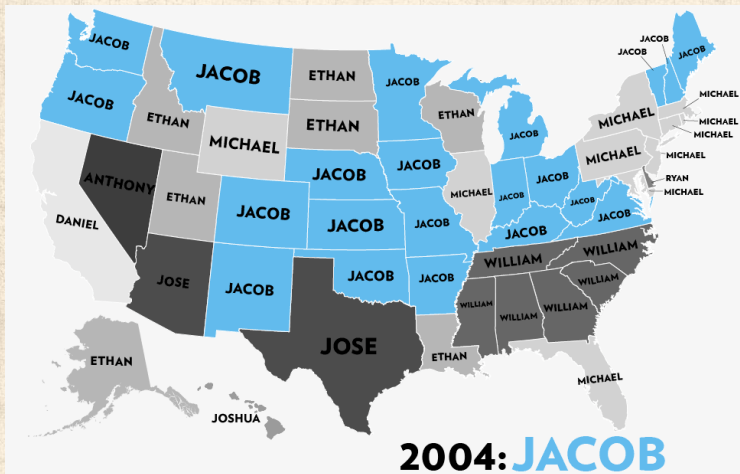
From the Atlantic 



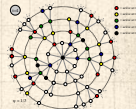
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



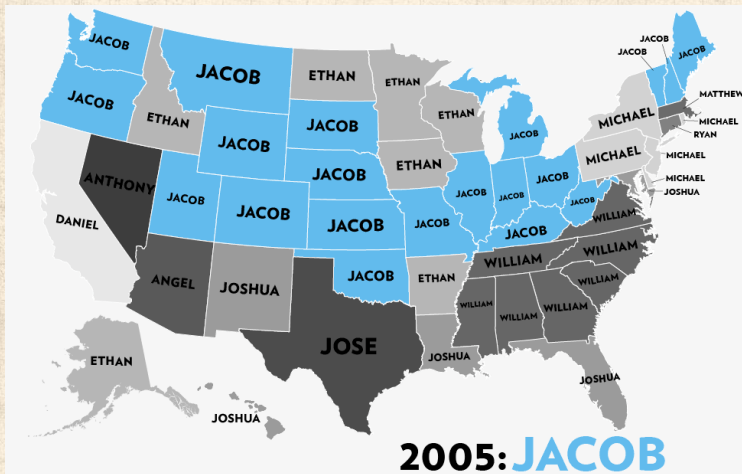
From the Atlantic 



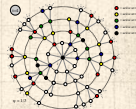
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



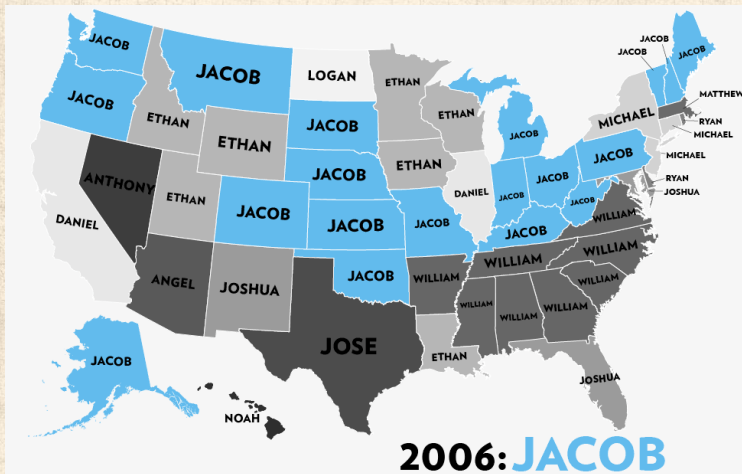
From the Atlantic 



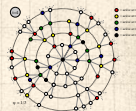
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic 

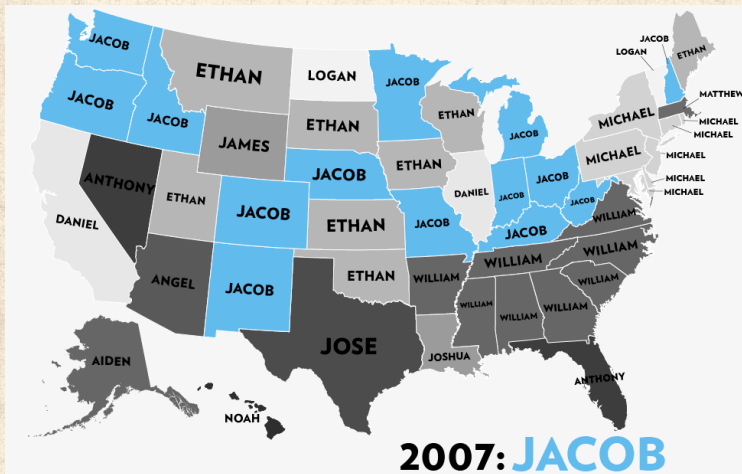




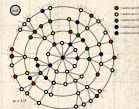
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



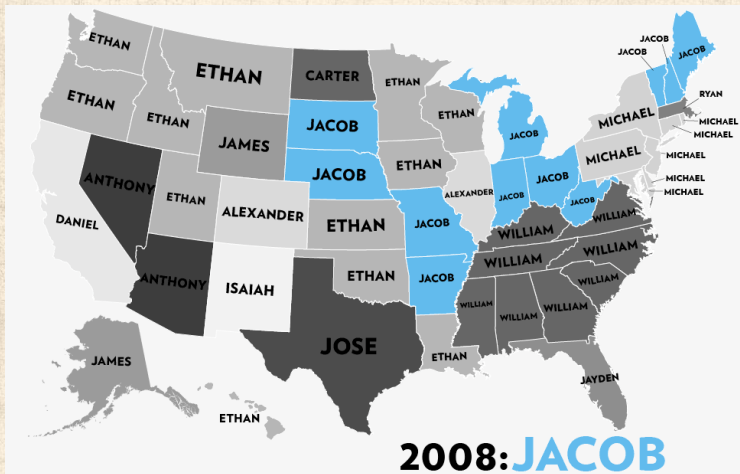
From the Atlantic 



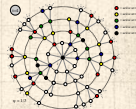
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



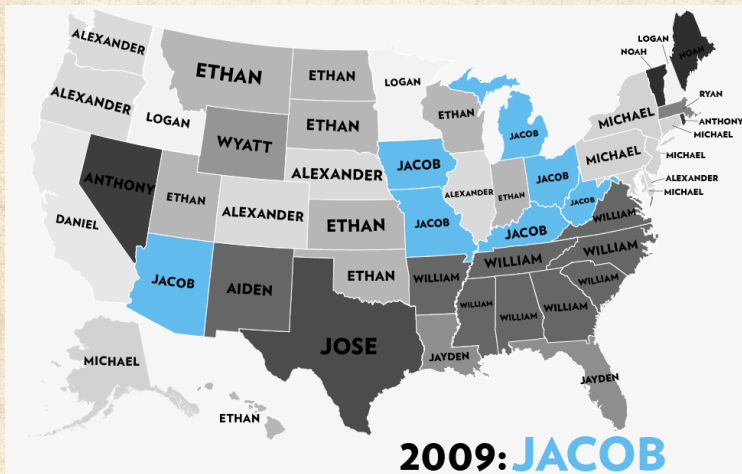
From the Atlantic 



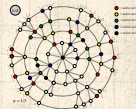
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



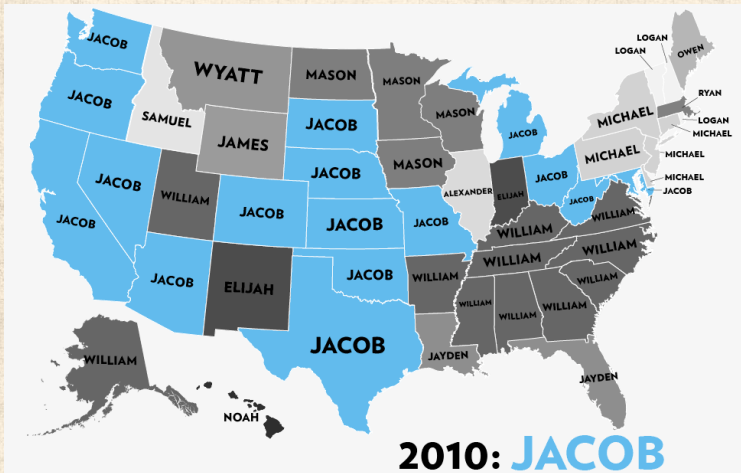
From the Atlantic 



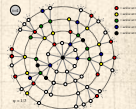
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



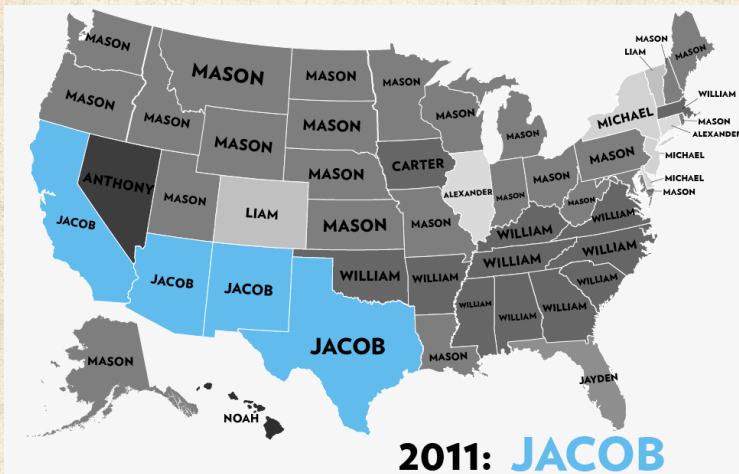
From the Atlantic 



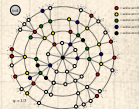
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



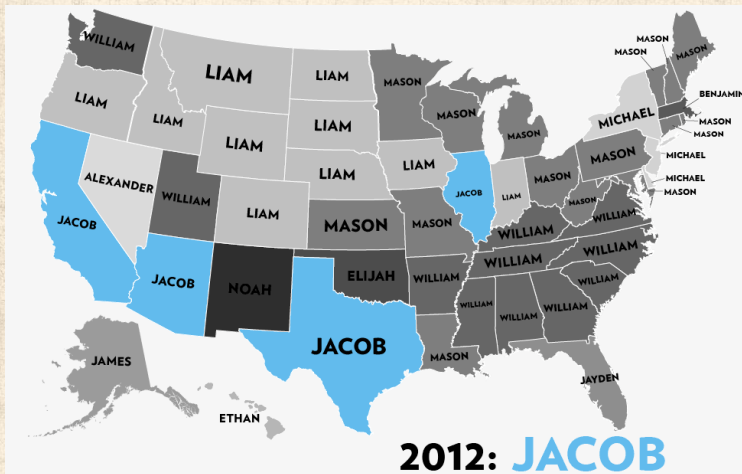
From the Atlantic 



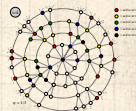
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



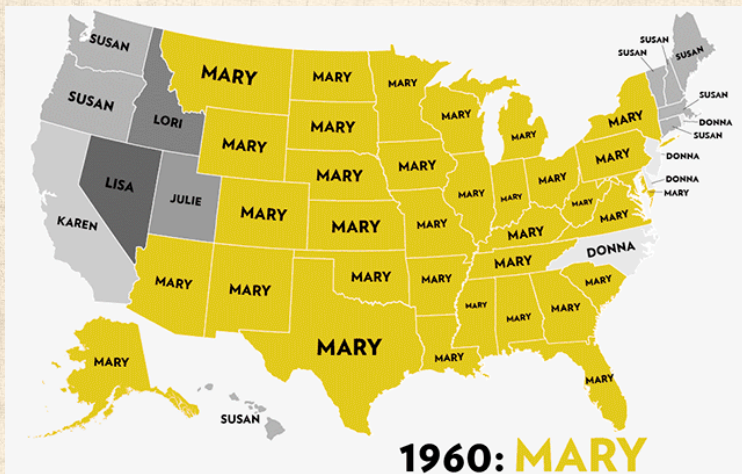
From the Atlantic 



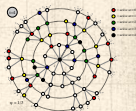
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



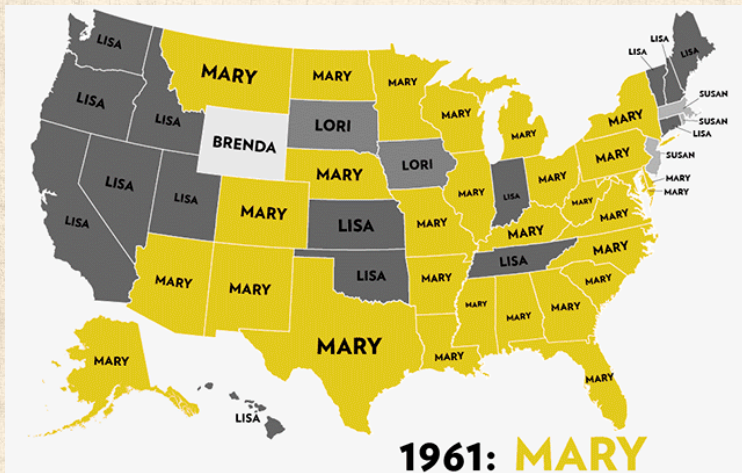
From the Atlantic 



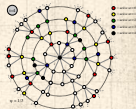
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic 

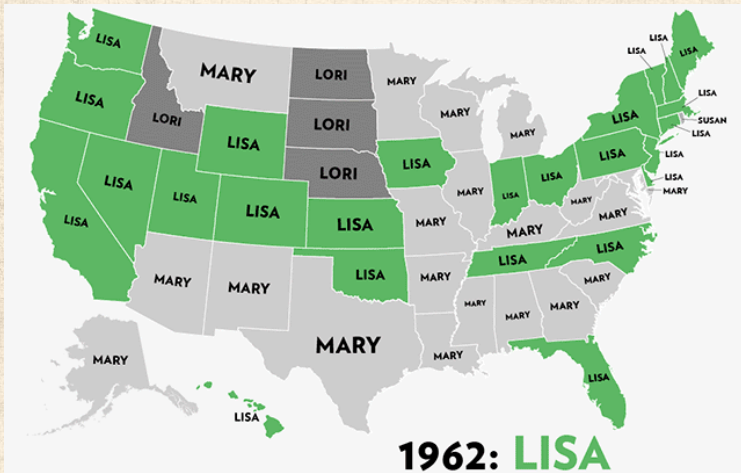




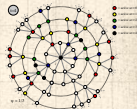
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



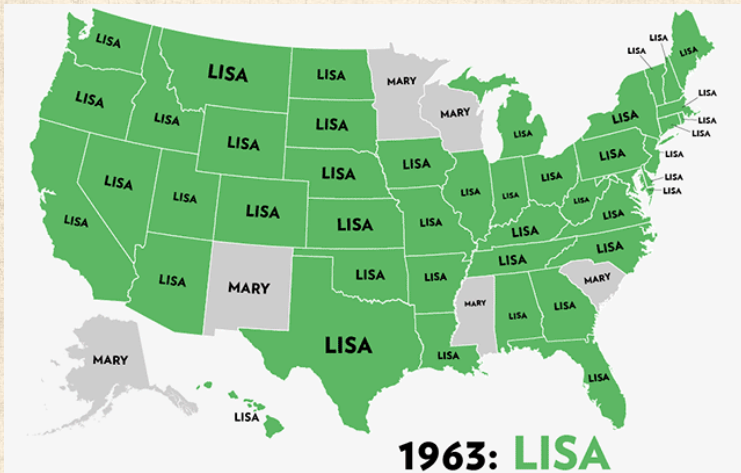
From the Atlantic 



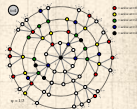
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



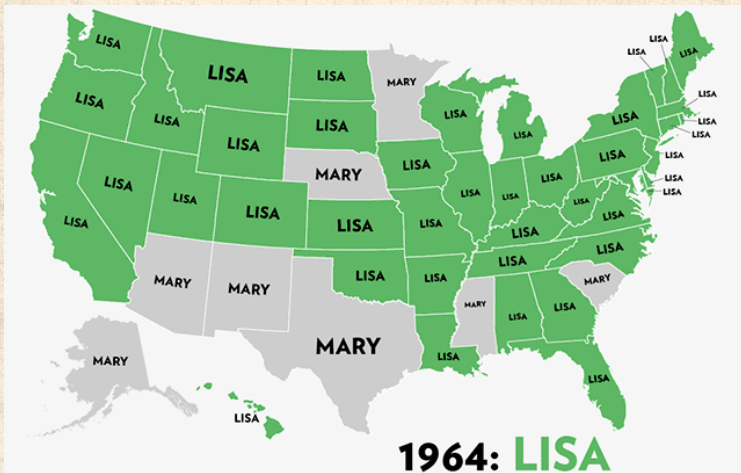
From the Atlantic 



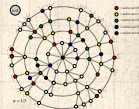
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



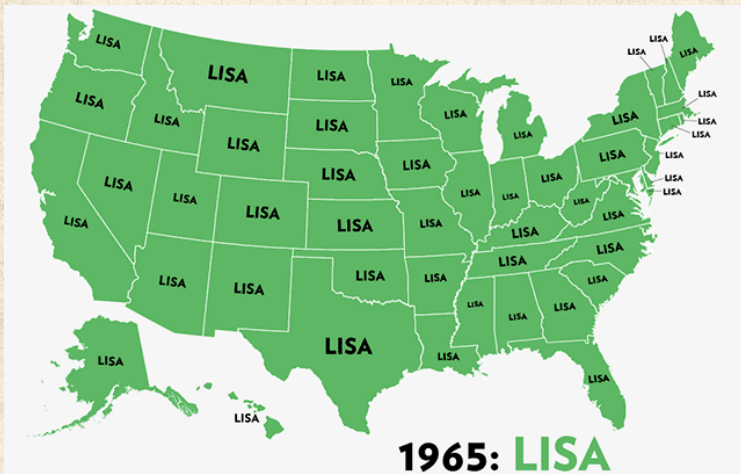
From the Atlantic 



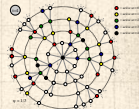
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



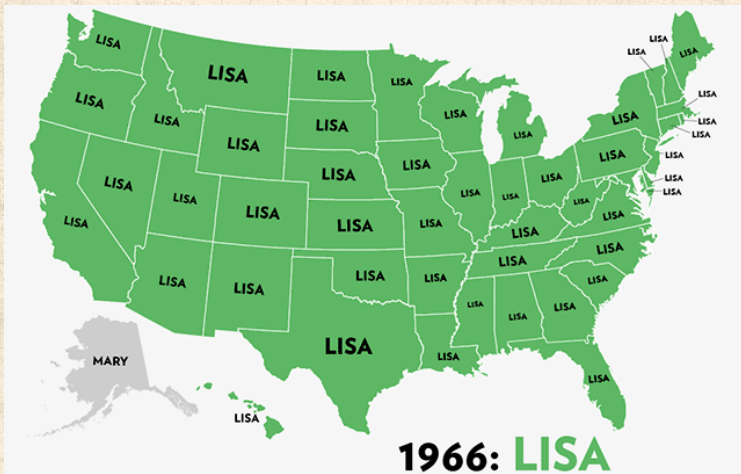
From the Atlantic 



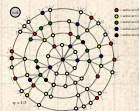
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



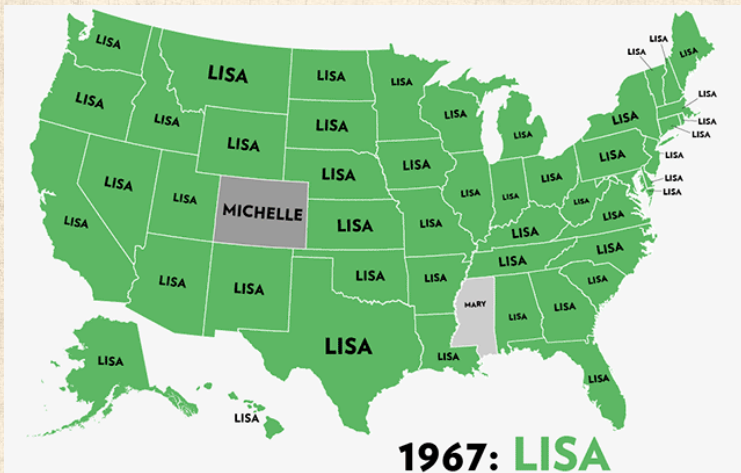
From the Atlantic 



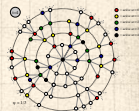
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



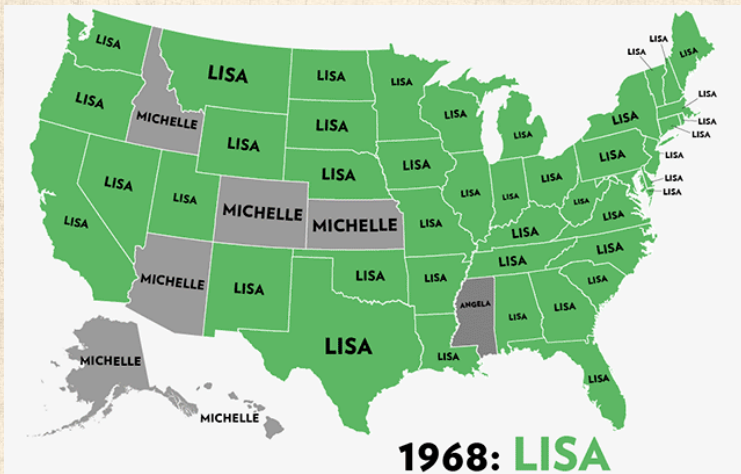
From the Atlantic 



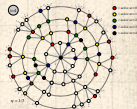
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



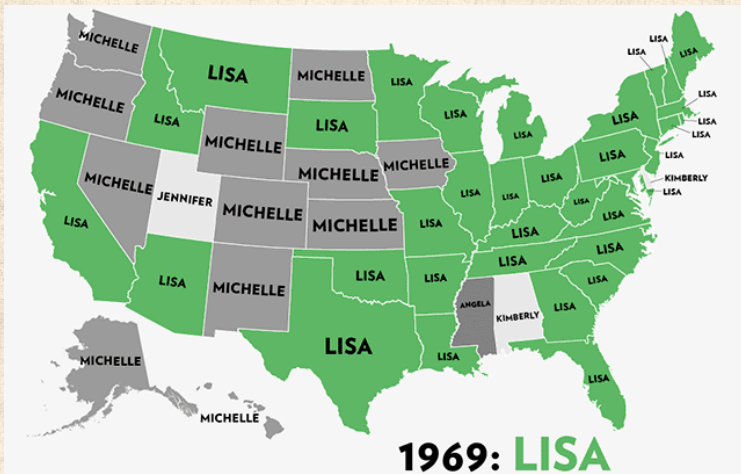
From the Atlantic ↗



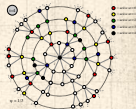
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic ↗

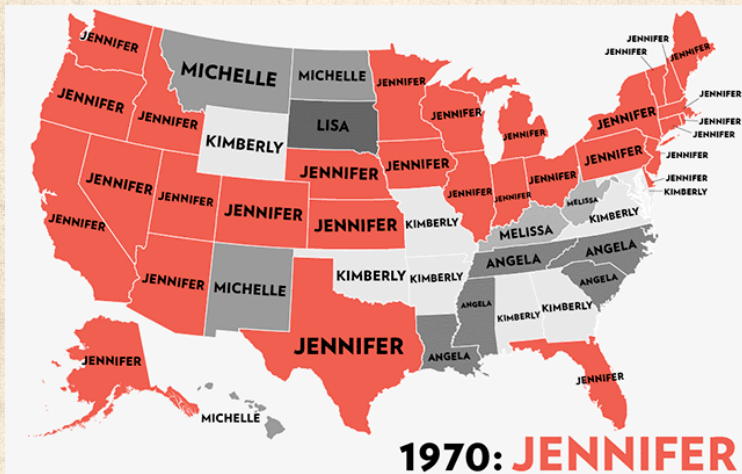




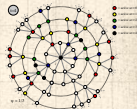
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



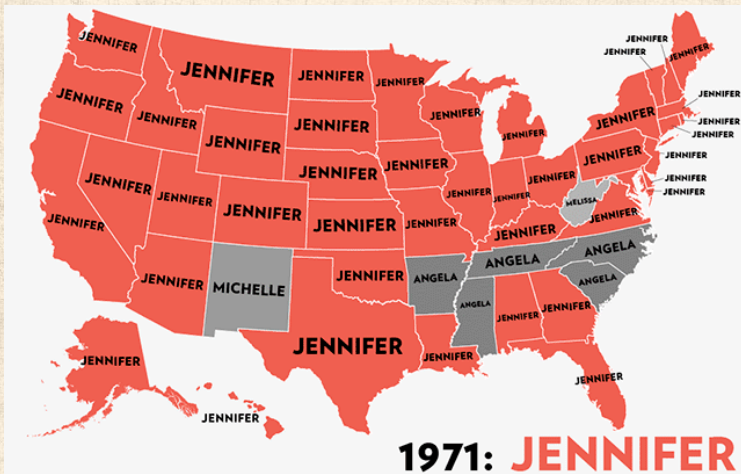
From the Atlantic ↗



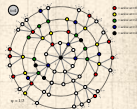
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



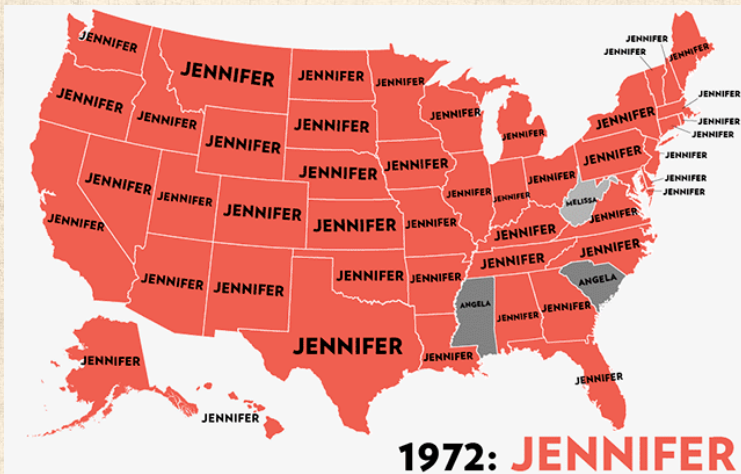
From the Atlantic ↗



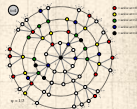
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



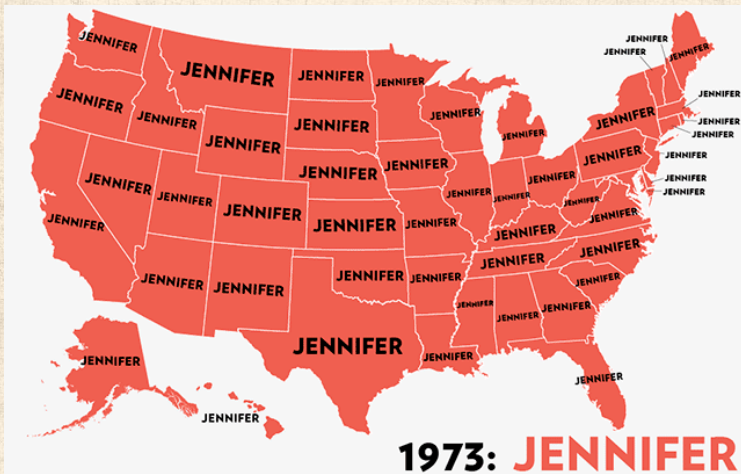
From the Atlantic ↗



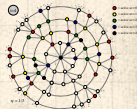
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



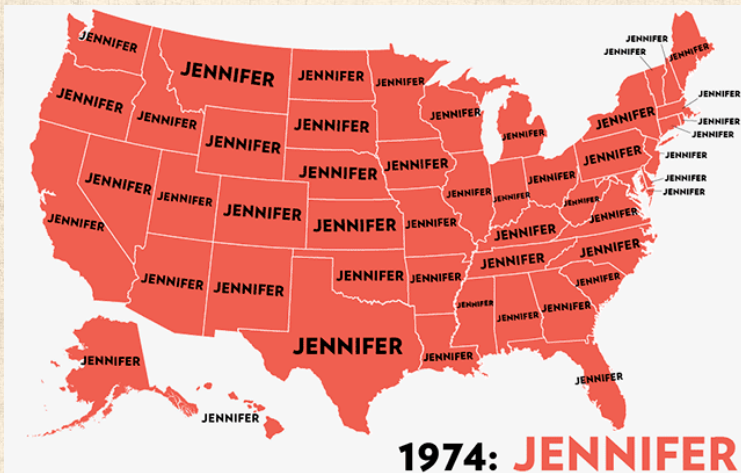
From the Atlantic 



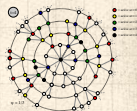
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



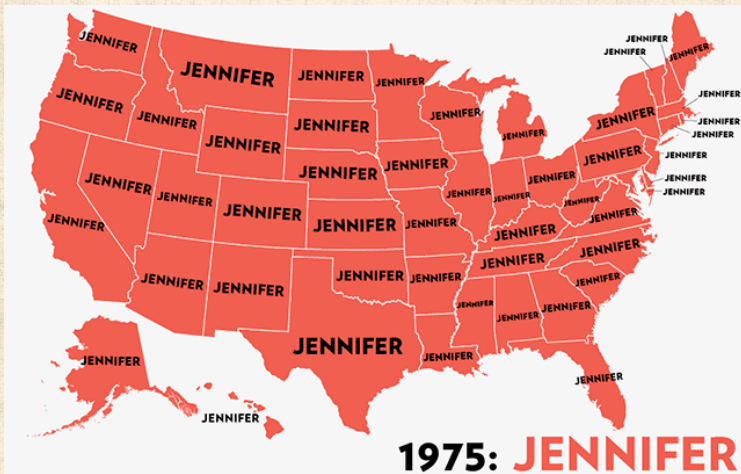
From the Atlantic ↗



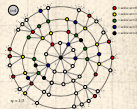
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



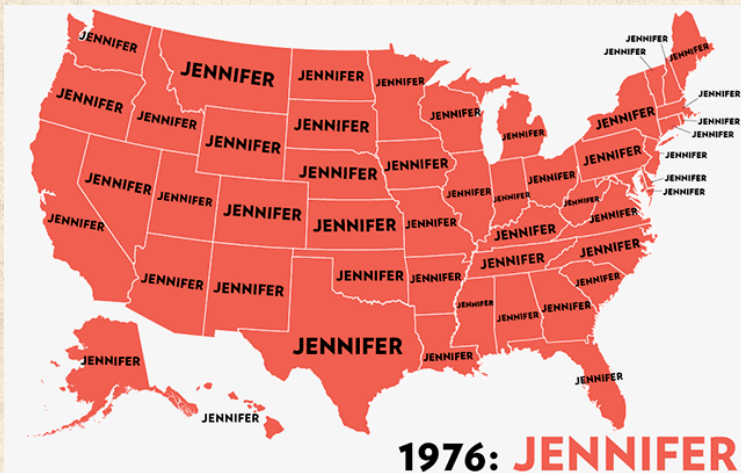
From the Atlantic 



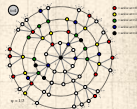
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



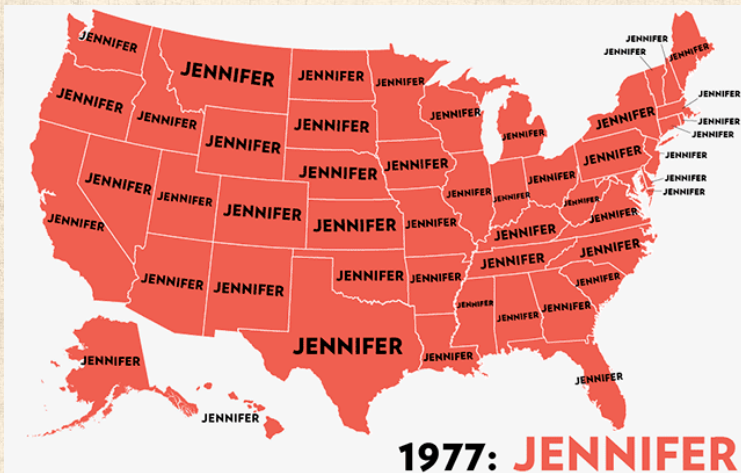
From the Atlantic 



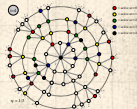
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic ↗

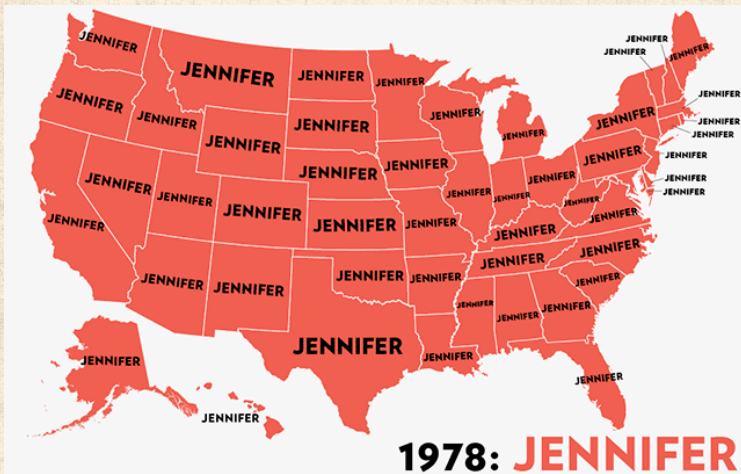




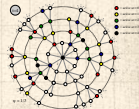
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



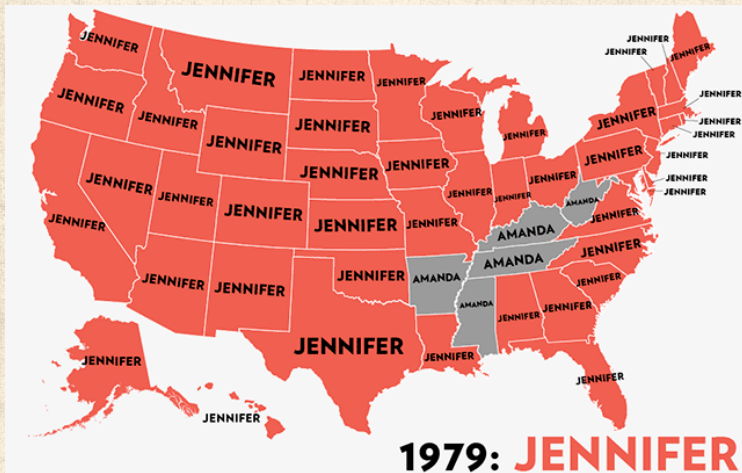
From the Atlantic ↗



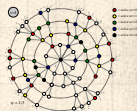
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



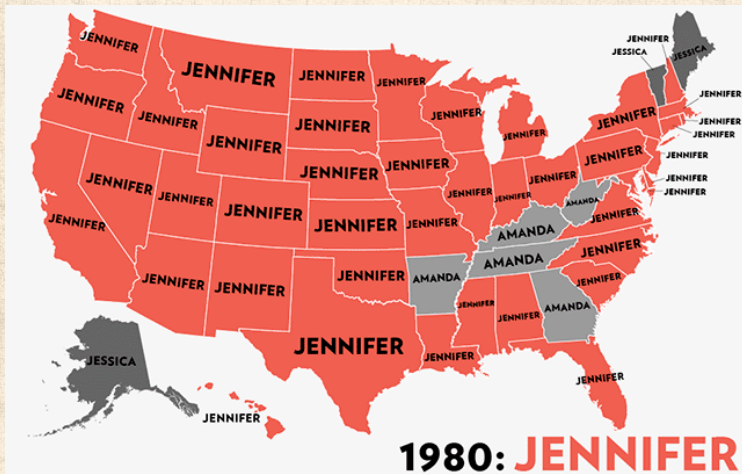
From the Atlantic 



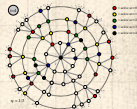
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



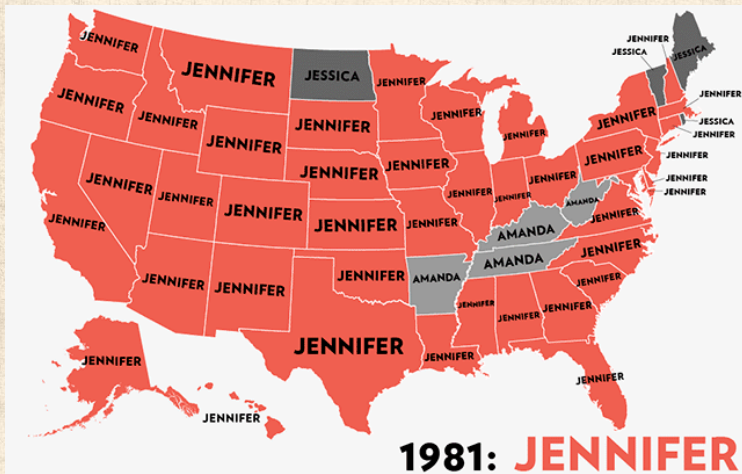
From the Atlantic ↗



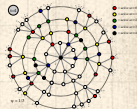
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



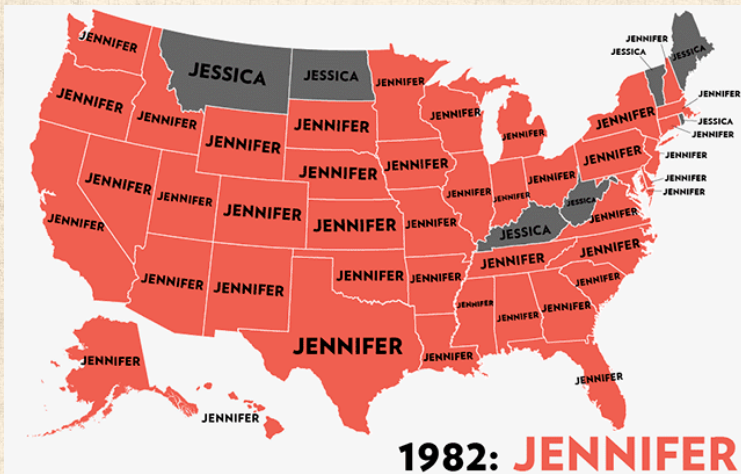
From the Atlantic 



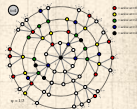
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



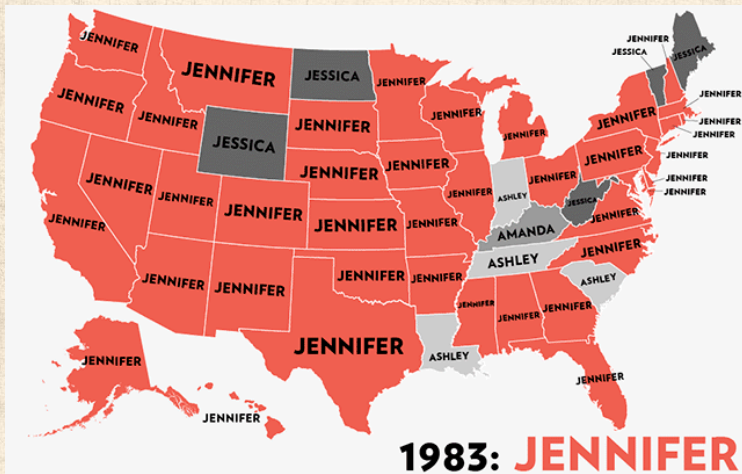
From the Atlantic ↗



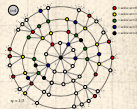
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



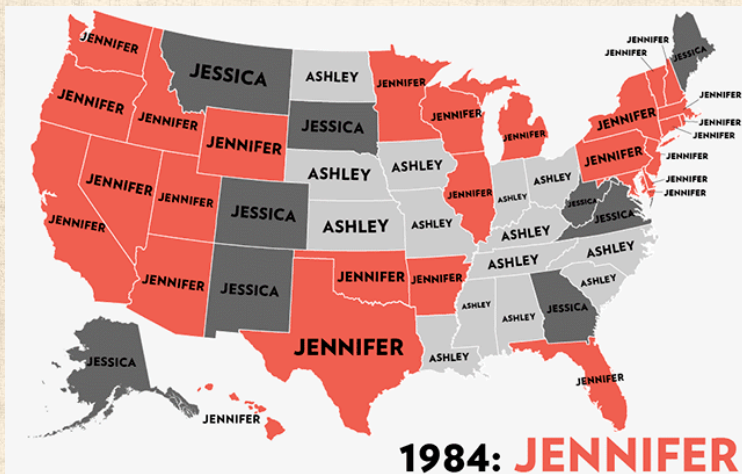
From the Atlantic ↗



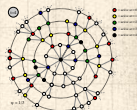
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



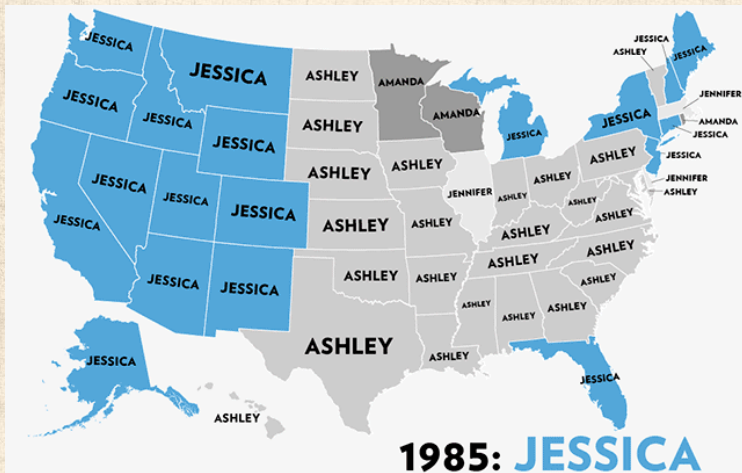
From the Atlantic 



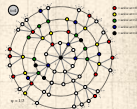
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic ↗

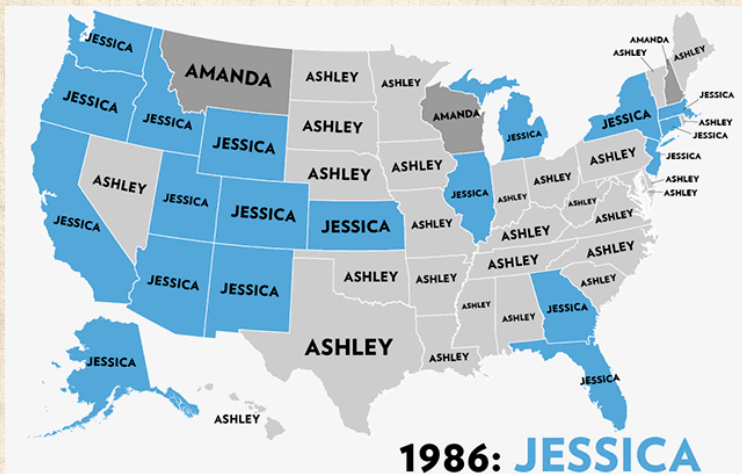




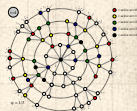
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



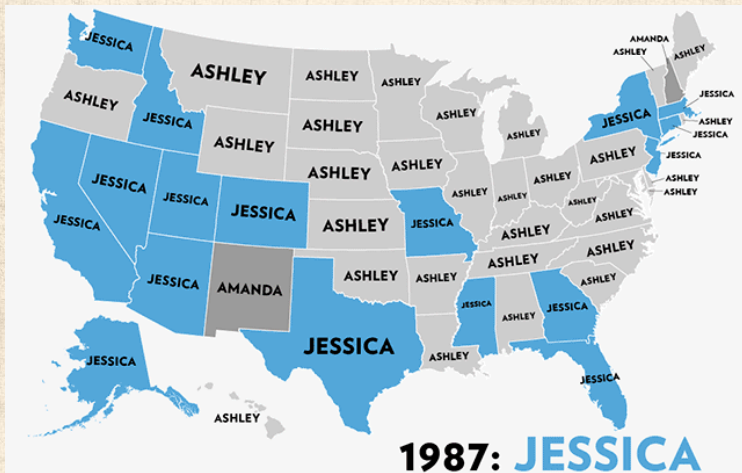
From the Atlantic ↗



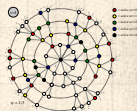
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



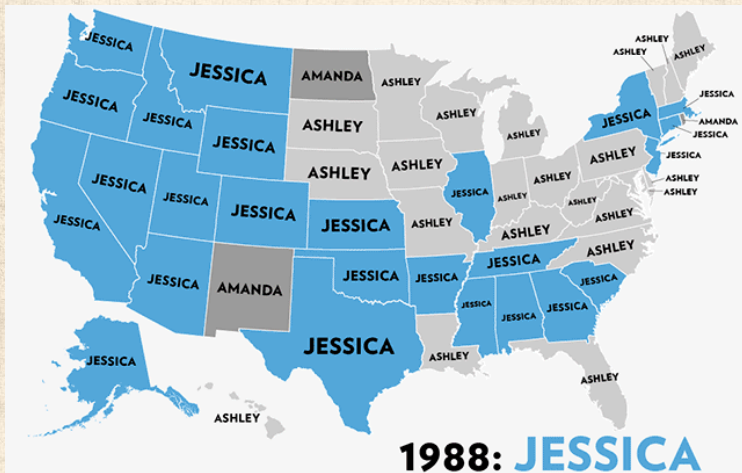
From the Atlantic ↗



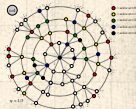
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



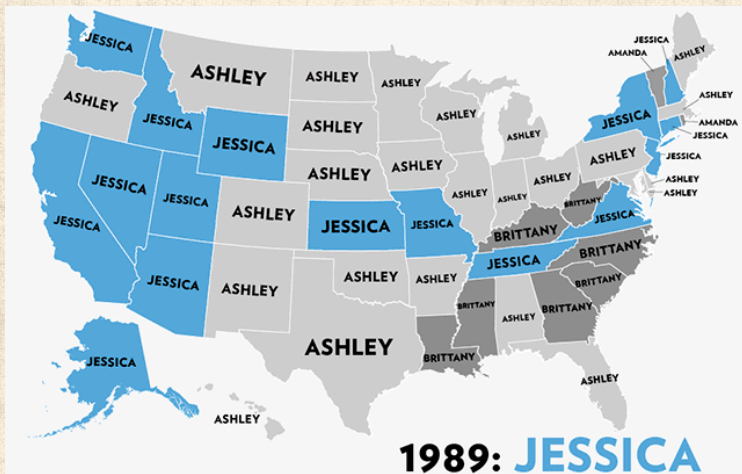
From the Atlantic 



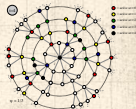
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



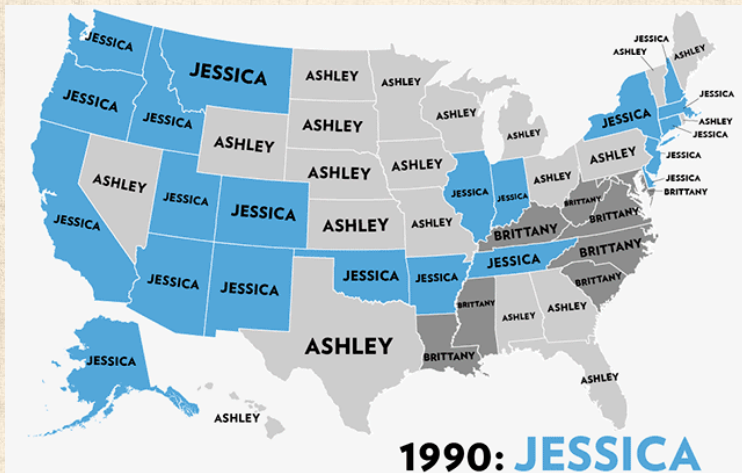
From the Atlantic ↗



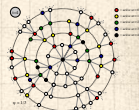
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



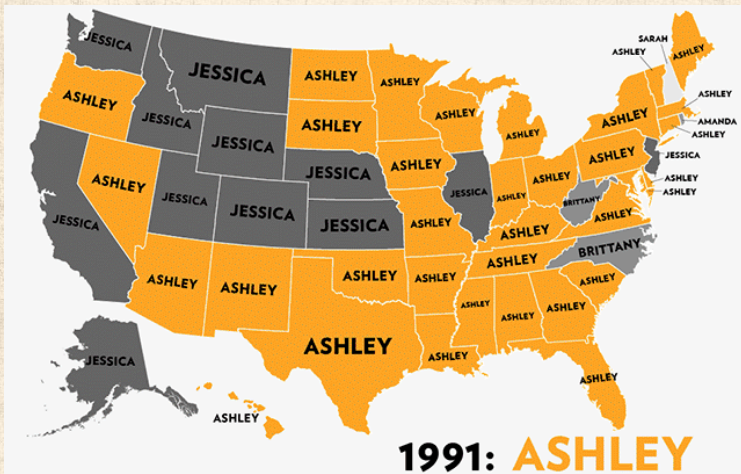
From the Atlantic 



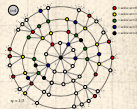
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



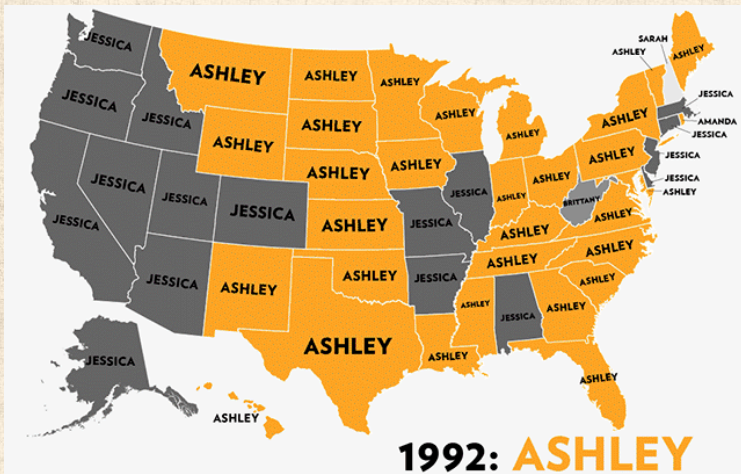
From the Atlantic 



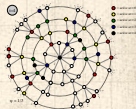
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



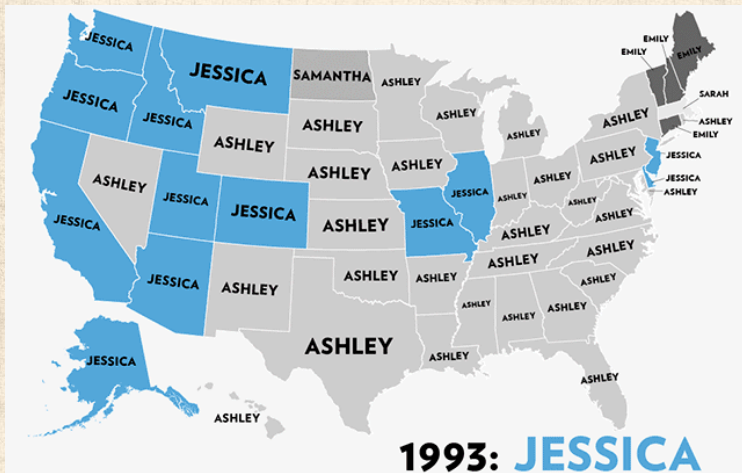
From the Atlantic ↗



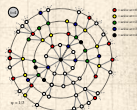
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic 

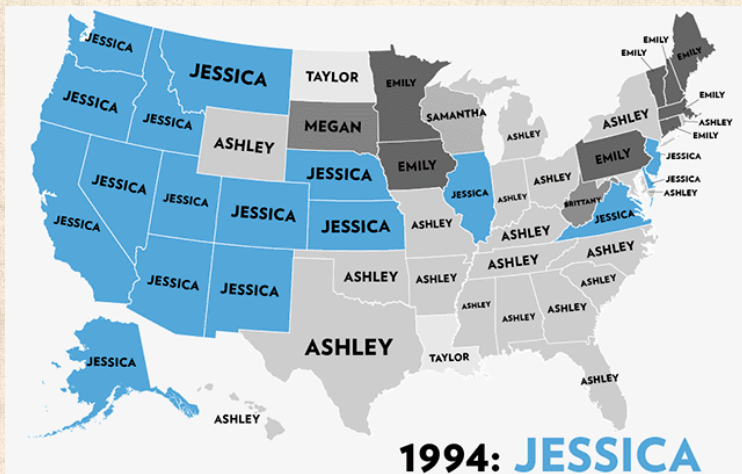




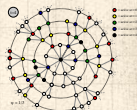
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



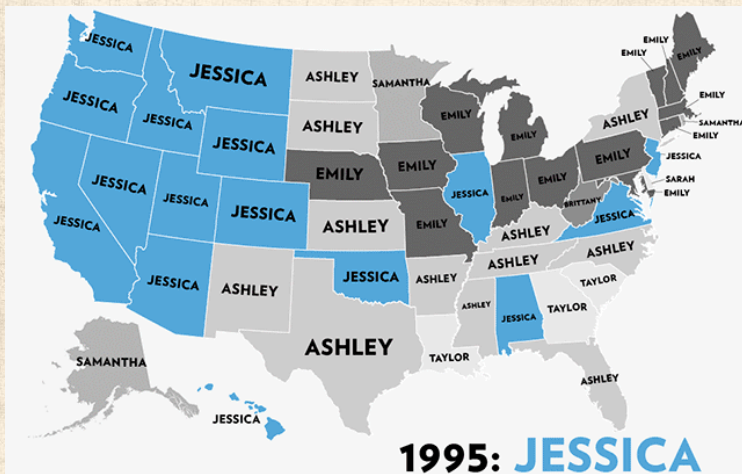
From the Atlantic 



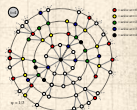
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



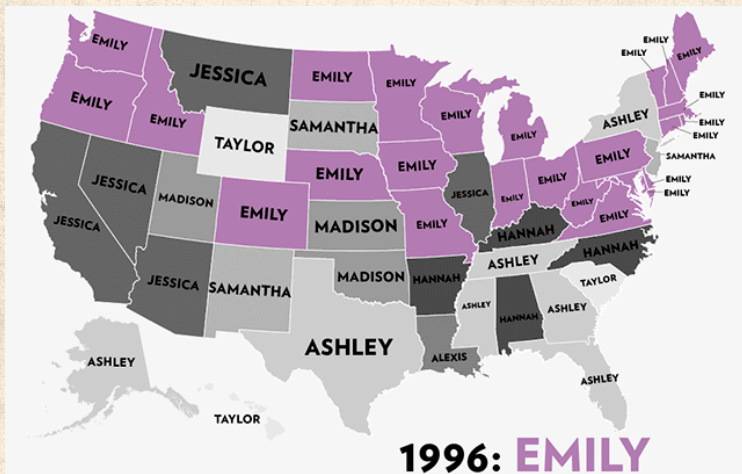
From the Atlantic ↗



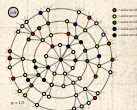
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



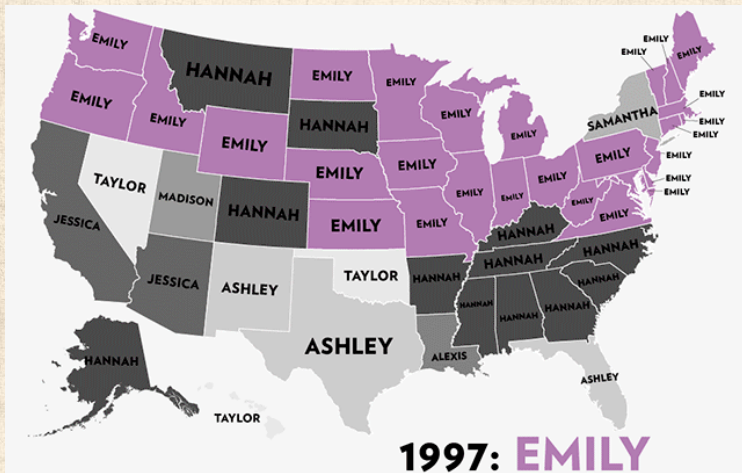
From the Atlantic 



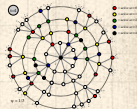
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



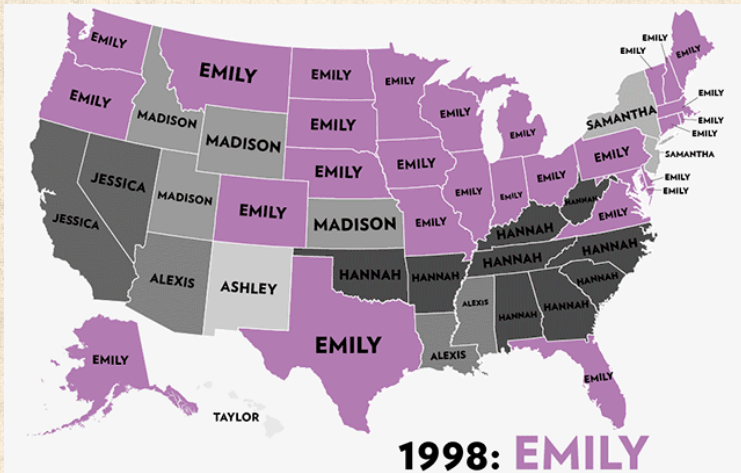
From the Atlantic ↗



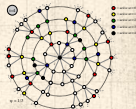
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



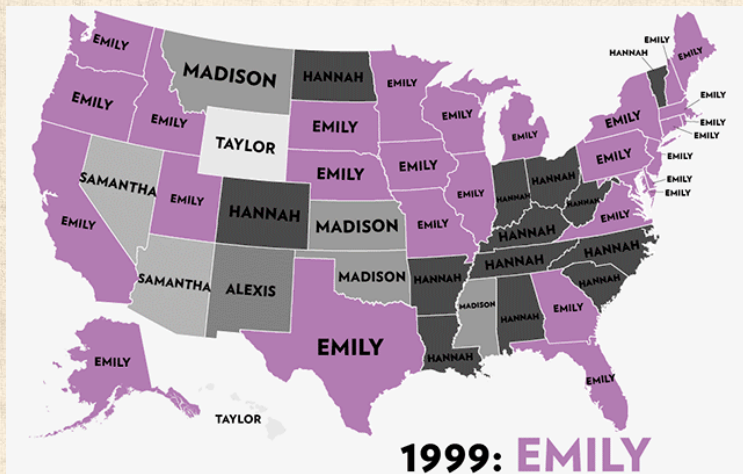
From the Atlantic 



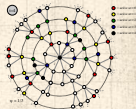
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



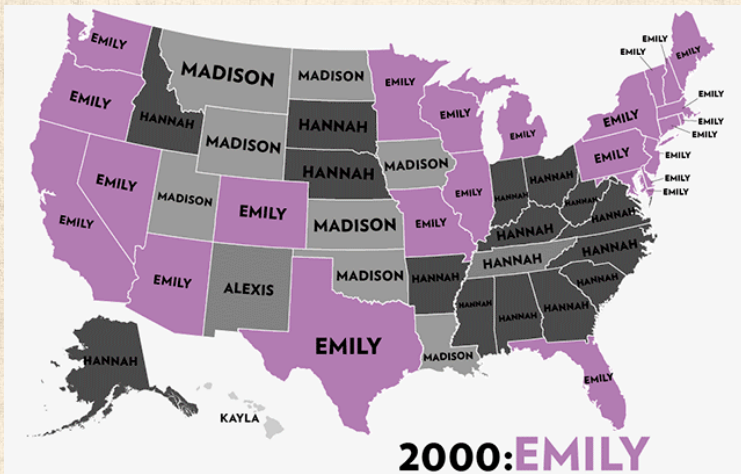
From the Atlantic 



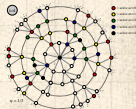
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



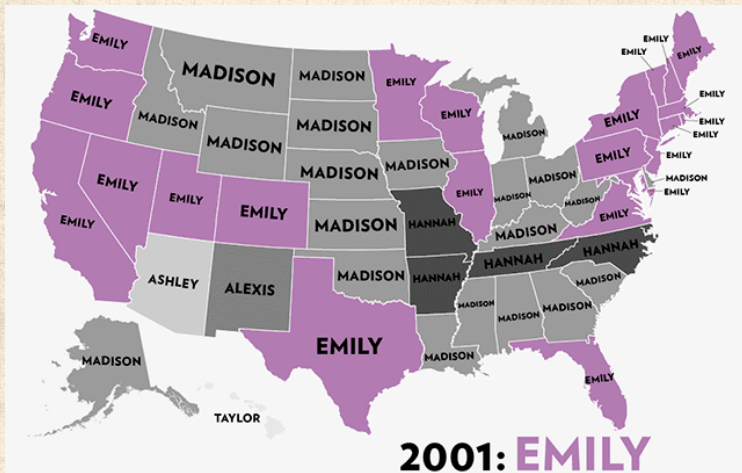
From the Atlantic ↗



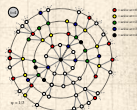
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



From the Atlantic ↗

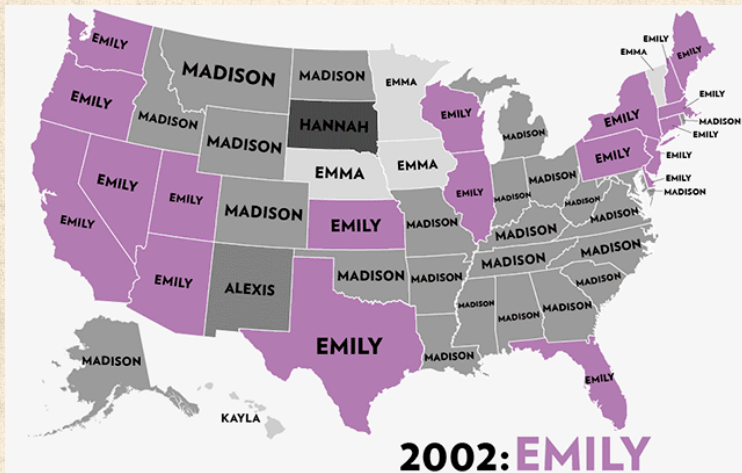




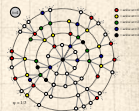
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



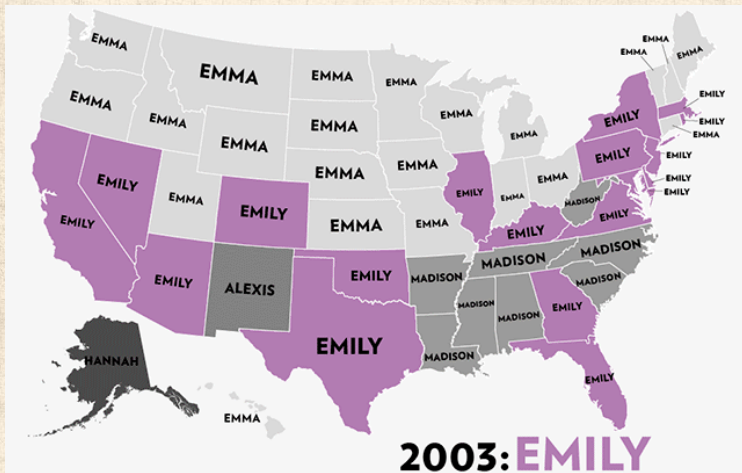
From the Atlantic 



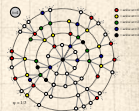
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



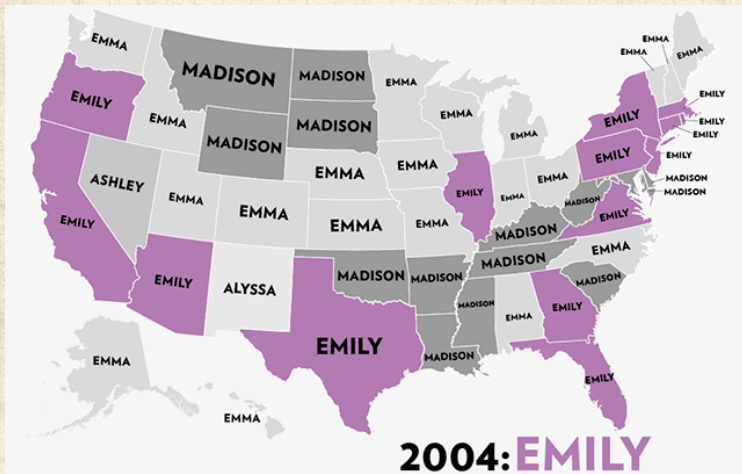
From the Atlantic 



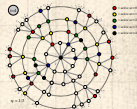
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



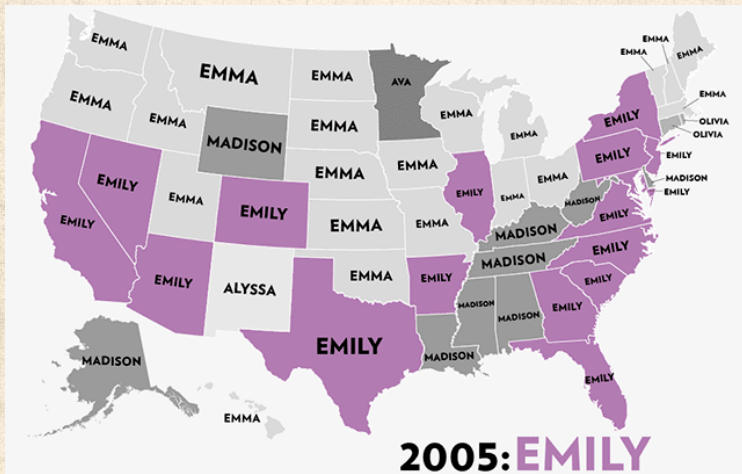
From the Atlantic 



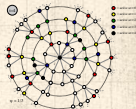
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



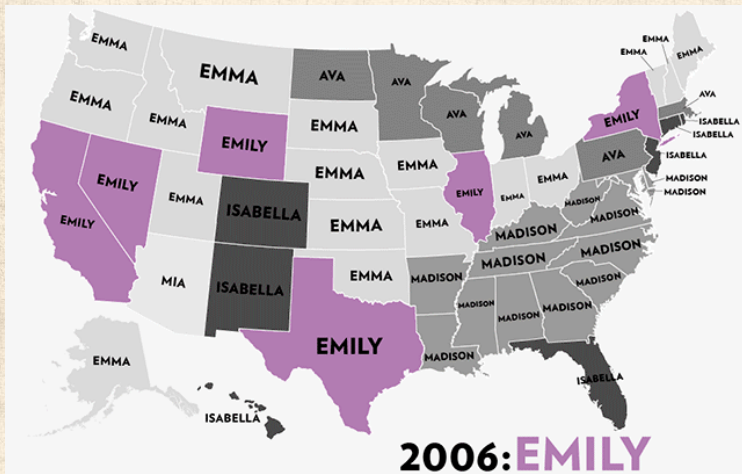
From the Atlantic 



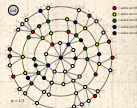
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



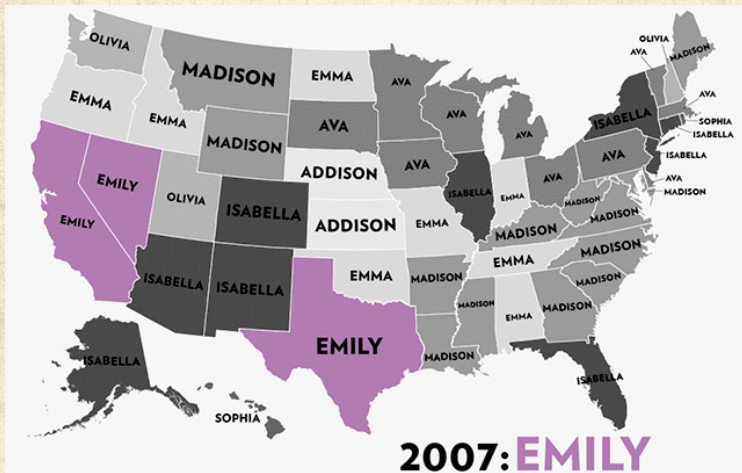
From the Atlantic ↗



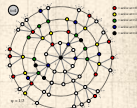
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



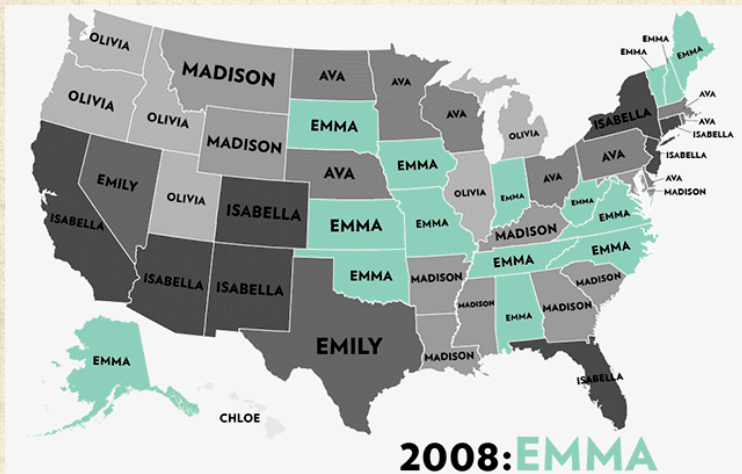
From the Atlantic 



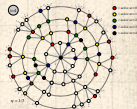
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



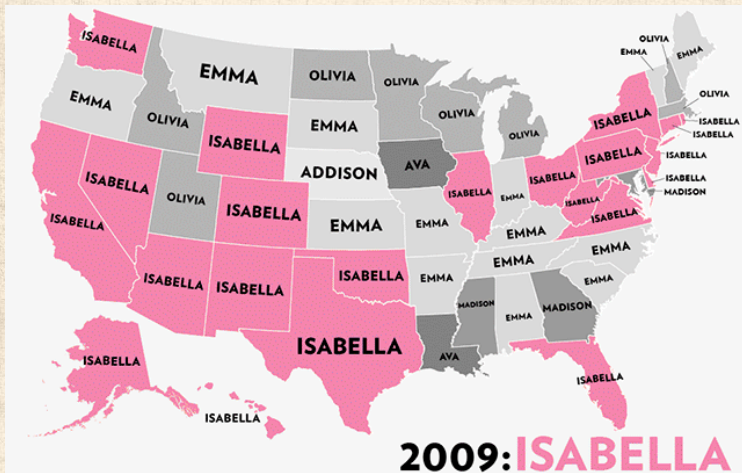
From the Atlantic 



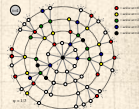
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



From the Atlantic 

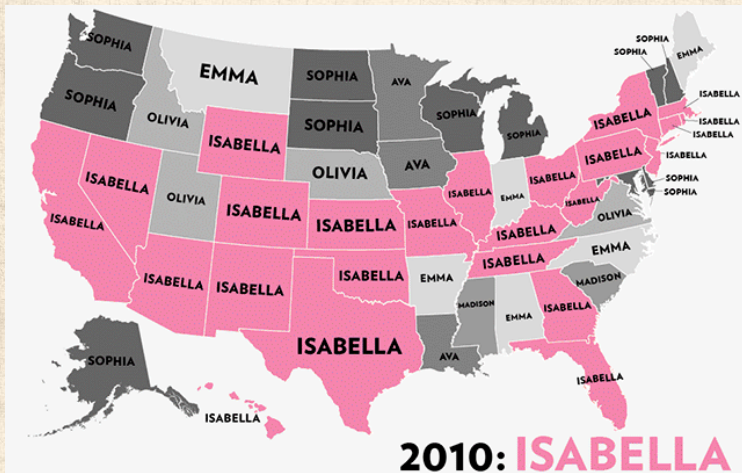




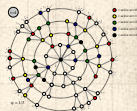
### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References



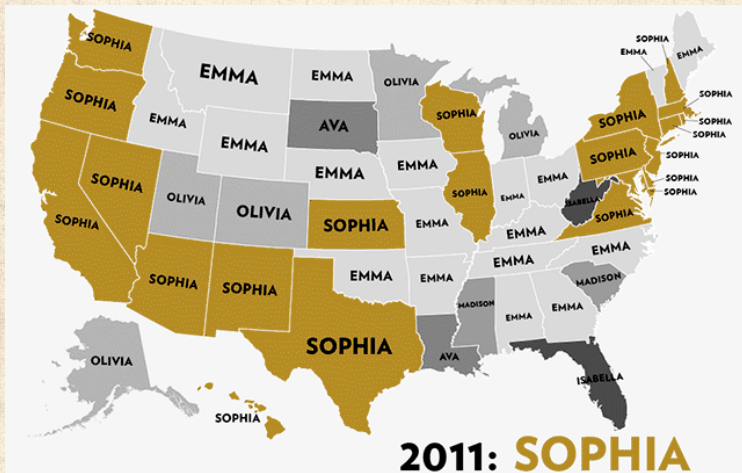
From the Atlantic ↗



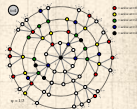
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



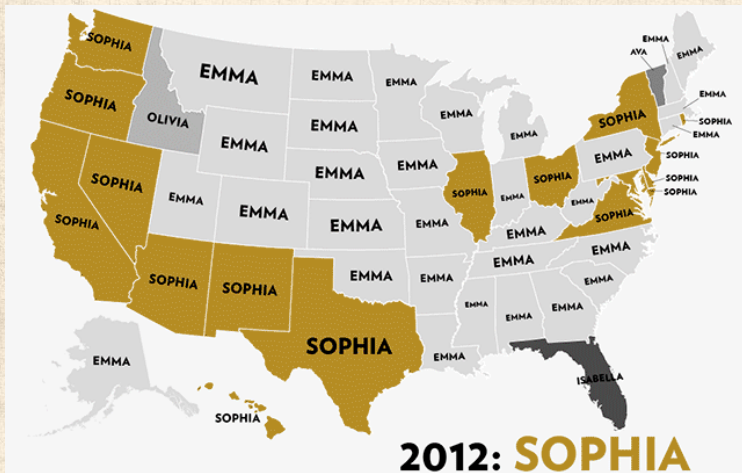
From the Atlantic ↗



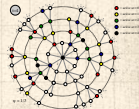
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From the Atlantic ↗

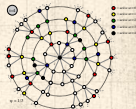


## Richard Feynmann on the Social Sciences:

### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

### References

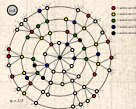


## Sheldon Cooper on the Social Sciences:

### Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups



### References



# Things that spread well:

[buzzfeed.com](http://buzzfeed.com) 



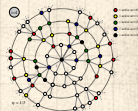
 Dangerously self aware: [11 Elements that make a perfect viral video.](#) 

The PoCSverse  
Social Contagion  
11 of 112


Social Contagion  
Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups



References



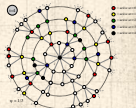
# Things that spread well:

[buzzfeed.com](http://buzzfeed.com) 



 Dangerously self aware: [11 Elements that make a perfect viral video.](#) 

+ News ...



LOL + cute + fail + wtf:

The PoCSverse  
Social Contagion  
12 of 112

Social Contagion  
Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

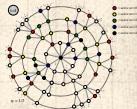
References

# Oopsie!



**BUZZFEED FELL DOWN AND WENT BOOM.**

Please try reloading this page. If the problem persists [let us know](#).





# The whole lolcats thing:

The PoCverse  
Social Contagion  
13 of 112

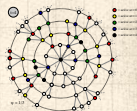
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



:~p



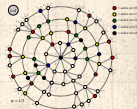
# Some things really stick:

The PoCSverse  
Social Contagion  
14 of 112

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



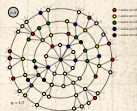
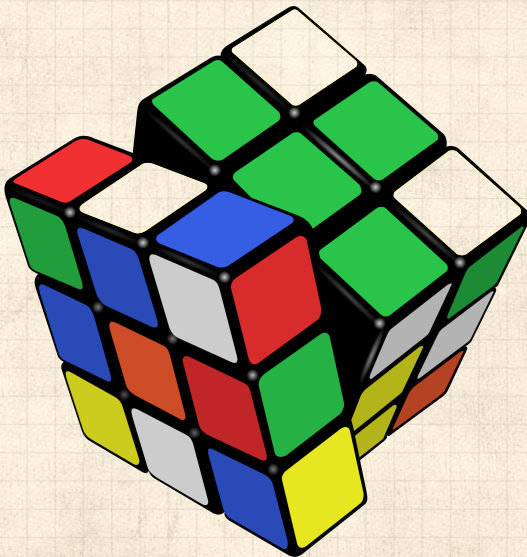
wtf + geeky + omg:

The PoCSverse  
Social Contagion  
15 of 112

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



# Outline

The PoCSverse  
Social Contagion  
16 of 112

## Social Contagion Models

### Background

Granovetter's model

Network version

Final size

Spreading success

Groups

## Social Contagion Models

### Background

Granovetter's model

Network version

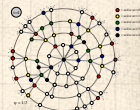
Final size

Spreading success

Groups

## References

## References



# Why social contagion works so well:

The PoCSverse  
Social Contagion  
17 of 112

Social Contagion  
Models

Background

Granovetter's model

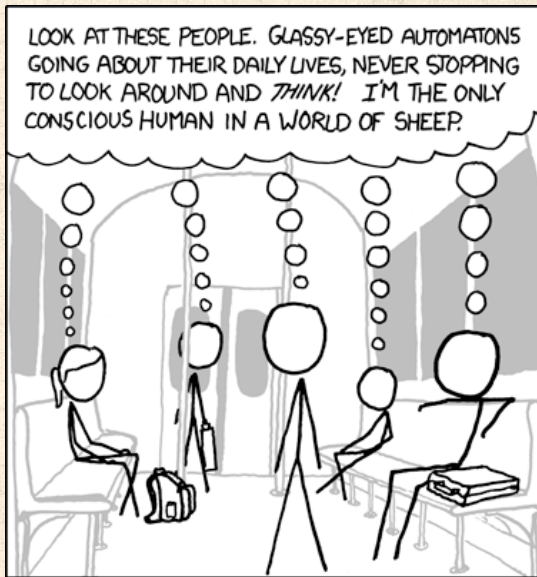
Network version

Final size

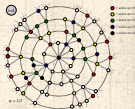
Spreading success

Groups

References



<http://xkcd.com/610/>



# Social Contagion

The PoCSverse  
Social Contagion  
18 of 112

## Social Contagion Models

### Background

Granovetter's model

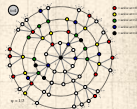
Network version

Final size

Spreading success

















Groups

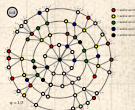
## References



# Social Contagion



















Examples are claimed to abound:

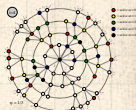
-  Fashion
-  Striking
-  smoking  [7]
-  Residential segregation [23]
-  iPhones and iThings
-  obesity  [6]
-  Stupidity
-  Harry Potter
-  voting
-  gossip
-  Rubik's cube 
-  religious beliefs
-  school shootings



# Social Contagion

Examples are claimed to abound:

-  Fashion
-  Striking
-  smoking  [7]
-  Residential segregation [23]
-  iPhones and iThings
-  obesity  [6]
-  Stupidity
-  Harry Potter
-  voting
-  gossip
-  Rubik's cube 
-  religious beliefs
-  school shootings
-  yawning 

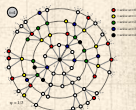




# Social Contagion



















Examples are claimed to abound:

-  Fashion
-  Striking
-  smoking  [7]
-  Residential segregation [23]
-  iPhones and iThings
-  obesity  [6]
-  Stupidity
-  Harry Potter
-  voting
-  gossip
-  Rubik's cube 
-  religious beliefs
-  school shootings
-  yawning 
-  **leaving lectures**




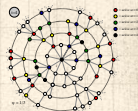
# Social Contagion

Examples are claimed to abound:

-  Fashion
-  Striking
-  smoking  [7]
-  Residential segregation [23]
-  iPhones and iThings
-  obesity  [6]
-  Stupidity
-  Harry Potter
-  voting
-  gossip
-  Rubik's cube 
-  religious beliefs
-  school shootings
-  yawning 
-  **leaving lectures**









SIR and SIRS type contagion possible

 Classes of behavior versus specific behavior




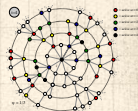
# Social Contagion

Examples are claimed to abound:

-  Fashion
-  Striking
-  smoking  [7]
-  Residential segregation [23]
-  iPhones and iThings
-  obesity  [6]
-  Stupidity
-  Harry Potter
-  voting
-  gossip
-  Rubik's cube 
-  religious beliefs
-  school shootings
-  yawning 
-  **leaving lectures**

SIR and SIRS type contagion possible

-  Classes of behavior versus specific behavior :  
**dieting, horror movies, getting married, invading countries, ...**



# Mixed messages: Please copy, but also, don't copy ...

The PoCSverse  
Social Contagion  
20 of 112

## Social Contagion Models

### Background

Granovetter's model

Network version

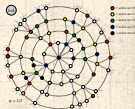
Final size

Spreading success

Groups

## References

<http://www.youtube.com/watch?v=TgDxWNV4wWY?rel=0>



# Mixed messages: Please copy, but also, don't copy ...

The PoCSverse  
Social Contagion  
20 of 112

Social Contagion  
Models

## Background

Granovetter's model

Network version

Final size

Spreading success

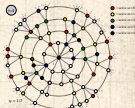
Groups

References

<http://www.youtube.com/watch?v=TgDxWNV4wWY?rel=0>



Cindy Harrell appeared in the (terrifying) music video for Ray Parker Jr.'s Ghostbusters.



# Mixed messages: Please copy, but also, don't copy ...

The PoCSverse  
Social Contagion  
20 of 112

Social Contagion  
Models

## Background

Granovetter's model

Network version


Final size


Spreading success

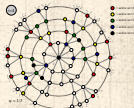
Groups

References

<http://www.youtube.com/watch?v=TgDxWNV4wWY?rel=0>

 [Cindy Harrell appeared](#) in the (terrifying) music video for Ray Parker Jr.'s [Ghostbusters](#).

 [In Stranger Things 2](#), Steve Harrington [reveals his Fabergé secret](#).



# Market much?

The PoCSverse  
Social Contagion  
21 of 112

## Social Contagion Models

### Background

Granovetter's model

Network version

Final size


Spreading success

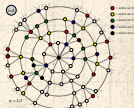
Groups

## References

<http://www.youtube.com/watch?v=FEaCflp9qR4?rel=0>







Advertisement enjoyed during "Herstory of  
Dance" , Community S4E08, April 2013.



# Framingham heart study:

## Evolving network stories (Christakis and Fowler):

 The spread of quitting smoking  [7]

 The spread of spreading  [6]

The PoCSverse  
Social Contagion  
22 of 112

Social Contagion  
Models

Background

Granovetter's model

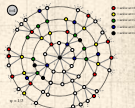
Network version

Final size

Spreading success

Groups

References









# Framingham heart study:

The PoCSverse  
Social Contagion  
22 of 112

## Evolving network stories (Christakis and Fowler):

 The spread of quitting smoking  <sup>[7]</sup>

 The spread of spreading  <sup>[6]</sup>

 Also: happiness  <sup>[11]</sup>, loneliness, ...

Social Contagion  
Models

### Background

Granovetter's model

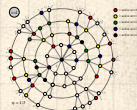
Network version

Final size

Spreading success









Groups

References



# Framingham heart study:

## Evolving network stories (Christakis and Fowler):

-  The spread of quitting smoking  <sup>[7]</sup>
-  The spread of spreading  <sup>[6]</sup>
-  Also: happiness  <sup>[11]</sup>, loneliness, ...
-  The book: Connected: The Surprising Power of Our Social Networks and How They Shape Our Lives 

## Social Contagion Models

### Background

Granovetter's model

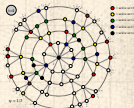
Network version

Final size

Spreading success









Groups

## References



# Framingham heart study:

## Evolving network stories (Christakis and Fowler):

-  The spread of quitting smoking  <sup>[7]</sup>
-  The spread of spreading  <sup>[6]</sup>
-  Also: happiness  <sup>[11]</sup>, loneliness, ...
-  The book: Connected: The Surprising Power of Our Social Networks and How They Shape Our Lives 

## Social Contagion Models

### Background

Granovetter's model

Network version



Final size

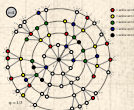
Spreading success

Groups

## References









## Controversy:

-  Are your friends making you fat?  (Clive Thomson, NY Times, September 10, 2009).



# Framingham heart study:

## Evolving network stories (Christakis and Fowler):

-  The spread of quitting smoking  <sup>[7]</sup>
-  The spread of spreading  <sup>[6]</sup>
-  Also: happiness  <sup>[11]</sup>, loneliness, ...
-  The book: Connected: The Surprising Power of Our Social Networks and How They Shape Our Lives 

## Social Contagion Models

### Background

Granovetter's model

Network version





Final size

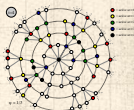
Spreading success

Groups

## References

## Controversy:

-  Are your friends making you fat?  (Clive Thomson, NY Times, September 10, 2009).
-  Everything is contagious  —Doubts about the social plague stir in the human superorganism (Dave Johns, Slate, April 8, 2010).



# Social Contagion

Two focuses for us

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

Background

Granovetter's model

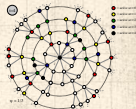
Network version

Final size

Spreading success

Groups


References



# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Two focuses for us

 Widespread media influence

Social Contagion  
Models

Background

Granovetter's model

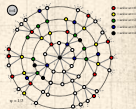
Network version

Final size

Spreading success

Groups


References




# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Two focuses for us

 Widespread media influence

 Word-of-mouth influence

Social Contagion  
Models

## Background

Granovetter's model

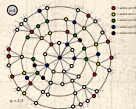
Network version

Final size

Spreading success

Groups

References



# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

## Background

Granovetter's model

Network version


Final size


Spreading success

Groups

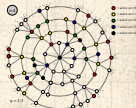
References

Two focuses for us

 Widespread media influence

 Word-of-mouth influence

We need to understand influence





# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

## Background

Granovetter's model

Network version


Final size


Spreading success

Groups


References

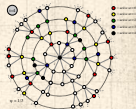
## Two focuses for us

 Widespread media influence

 Word-of-mouth influence

## We need to understand influence

 Who influences whom?



# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

## Background

Granovetter's model

Network version


Final size


Spreading success

Groups


References

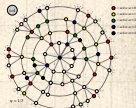
## Two focuses for us

 Widespread media influence

 Word-of-mouth influence

## We need to understand influence

 Who influences whom? Very hard to measure...



# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version


Final size


Spreading success

Groups


References


## Two focuses for us

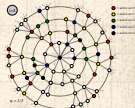
 Widespread media influence

 Word-of-mouth influence

## We need to understand influence

 Who influences whom? Very hard to measure...

 What kinds of influence response functions are there?



# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

Spreading success

Groups

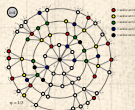
References

## Two focuses for us

- Widespread media influence
- Word-of-mouth influence

## We need to understand influence

- Who influences whom? Very hard to measure...
- What kinds of influence response functions are there?
- Are some individuals super influencers?



# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

Spreading success

Groups

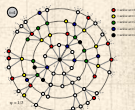
References

## Two focuses for us

- Widespread media influence
- Word-of-mouth influence

## We need to understand influence

- Who influences whom? Very hard to measure...
- What kinds of influence response functions are there?
- Are some individuals super influencers?  
Highly popularized by Gladwell<sup>[12]</sup> as 'connectors'



# Social Contagion

The PoCSverse  
Social Contagion  
23 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

Spreading success

Groups

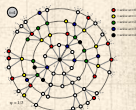
References

## Two focuses for us

- Widespread media influence
- Word-of-mouth influence

## We need to understand influence

- Who influences whom? Very hard to measure...
- What kinds of influence response functions are there?
- Are some individuals super influencers?  
Highly popularized by Gladwell<sup>[12]</sup> as 'connectors'
- The infectious idea of opinion leaders (Katz and Lazarsfeld)<sup>[19]</sup>



# The hypodermic model of influence

The PoCSverse  
Social Contagion  
24 of 112

## Social Contagion Models

### Background

Granovetter's model

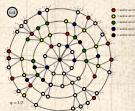
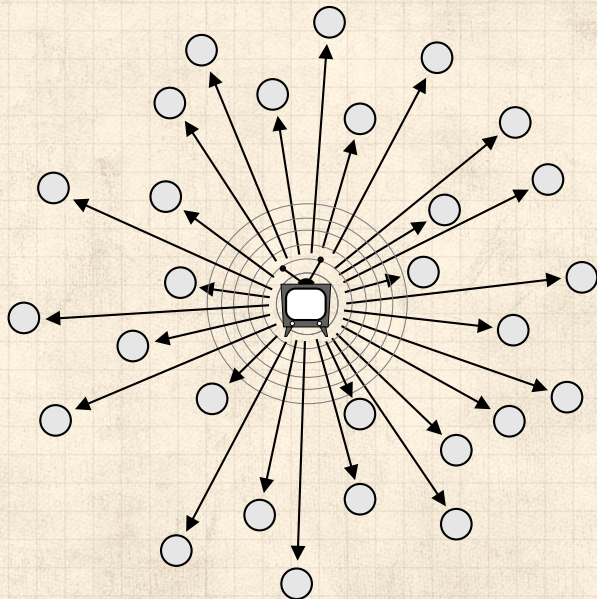
Network version

Final size

Spreading success

Groups

### References



# The two step model of influence [19]

The PoCSverse  
Social Contagion  
25 of 112

Social Contagion  
Models

Background

Granovetter's model

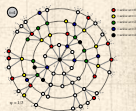
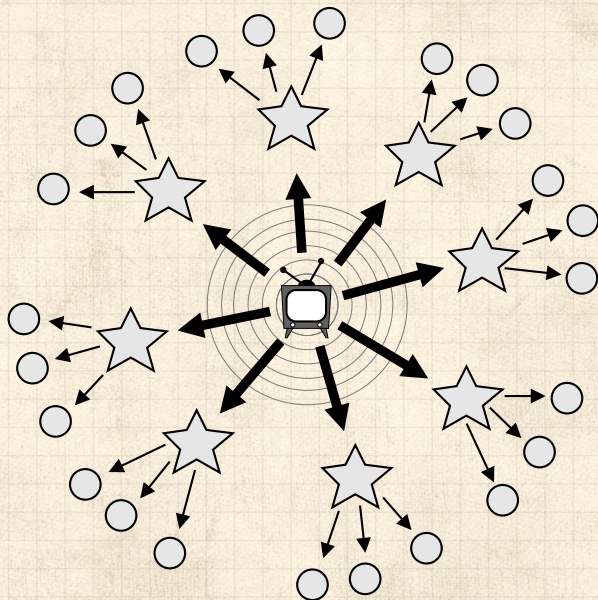
Network version

Final size

Spreading success

Groups

References





# The general model of influence: the Social Wild

The PoCSverse  
Social Contagion  
26 of 112

Social Contagion  
Models

Background

Granovetter's model

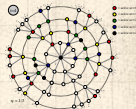
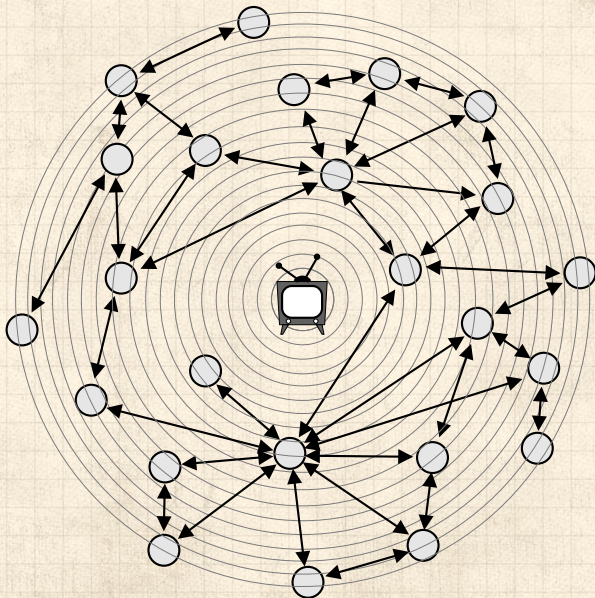
Network version

Final size

Spreading success

Groups

References



## Talking about the social wild:

### Social Contagion Models

#### Background

Granovetter's model

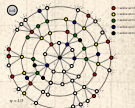
Network version

Final size

Spreading success

Groups

### References



# Why do things spread socially?

The PoCSverse  
Social Contagion  
28 of 112

## Social Contagion Models

### Background

Granovetter's model

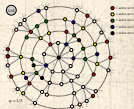
Network version

Final size


Spreading success

Groups

## References



# Why do things spread socially?

 Because of properties of special individuals?

The PoCSverse  
Social Contagion  
28 of 112

Social Contagion  
Models

## Background

Granovetter's model

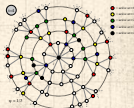
Network version

Final size


Spreading success


Groups

References



# Why do things spread socially?

 Because of properties of special individuals?

 Or system level properties?

The PoCSverse  
Social Contagion  
28 of 112

Social Contagion  
Models

Background

Granovetter's model

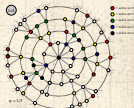
Network version

Final size

Spreading success

Groups

References



## Why do things spread socially?

- Because of properties of special individuals?
- Or system level properties?
- Is the match that lights the fire important?

### Social Contagion Models

#### Background

Granovetter's model

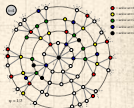
Network version

Final size

Spreading success

Groups

### References



## Why do things spread socially?

- Because of properties of special individuals?
- Or system level properties?
- Is the match that lights the fire important?
- Yes. But only because we are storytellers:  
*homo narrativus* ↗

### Social Contagion Models

#### Background

Granovetter's model

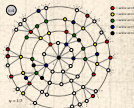
Network version

Final size

Spreading success

Groups

#### References



## Why do things spread socially?

- Because of properties of special individuals?
- Or system level properties?
- Is the match that lights the fire important?
- Yes. But only because we are storytellers:  
*homo narrativus* ↗
- We like to think things happened for reasons ...

Background

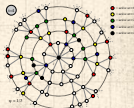
Granovetter's model

Network version

Final size

Spreading success

Groups





## Why do things spread socially?

- Because of properties of special individuals?
- Or system level properties?
- Is the match that lights the fire important?
- Yes. But only because we are storytellers:  
*homo narrativus* ↗
- We like to think things happened for reasons ...
- Reasons for success are usually ascribed to intrinsic properties (examples next).

Background

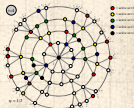
Granovetter's model

Network version


Final size

Spreading success

Groups



## Why do things spread socially?

- Because of properties of special individuals?
- Or system level properties?
- Is the match that lights the fire important?
- Yes. But only because we are storytellers:  
*homo narrativus* 
- We like to think things happened for reasons ...
- Reasons for success are usually ascribed to intrinsic properties (examples next).
- Teleological stories of fame are often easy to generate and believe.

Background

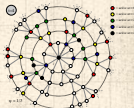
Granovetter's model

Network version

Final size

Spreading success

Groups



## Why do things spread socially?

- Because of properties of special individuals?
- Or system level properties?
- Is the match that lights the fire important?
- Yes. But only because we are storytellers:  
*homo narrativus* ↗
- We like to think things happened for reasons ...
- Reasons for success are usually ascribed to intrinsic properties (examples next).
- Teleological stories of fame are often easy to generate and believe.
- System/group dynamics harder to understand because most of our stories are built around individuals.

Background

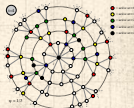
Granovetter's model

Network version

Final size

Spreading success

Groups



## Why do things spread socially?

- Because of properties of special individuals?
- Or system level properties?
- Is the match that lights the fire important?
- Yes. But only because we are storytellers:  
*homo narrativus* ↗.
- We like to think things happened for reasons ...
- Reasons for success are usually ascribed to intrinsic properties (examples next).
- Teleological stories of fame are often easy to generate and believe.
- System/group dynamics harder to understand because most of our stories are built around individuals.
- Always good to examine what is said before and after the fact ...

Background

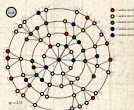
Granovetter's model

Network version

Final size

Spreading success

Groups



# The Mona Lisa

The PoCSverse  
Social Contagion  
29 of 112

Social Contagion  
Models

Background

Granovetter's model

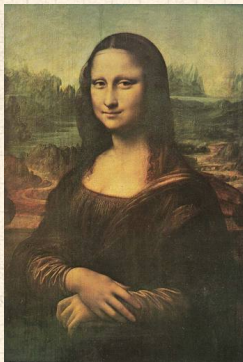
Network version

Final size

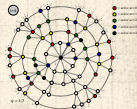
Spreading success

Groups

References



“Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon



# The Mona Lisa

The PoCSverse  
Social Contagion  
29 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

Spreading success

Groups

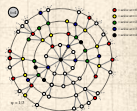
References



“Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon



Not the world's greatest painting from the start...



# The Mona Lisa

The PoCSverse  
Social Contagion  
29 of 112

Social Contagion  
Models

## Background

Granovetter's model

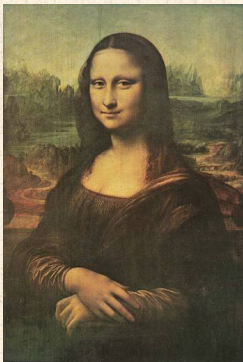
Network version


Final size


Spreading success


Groups

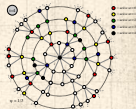
References



 “Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon

 Not the world's greatest painting from the start...

 Escalation through theft, vandalism,



# The Mona Lisa

The PoCSverse  
Social Contagion  
29 of 112

Social Contagion  
Models

## Background

Granovetter's model

Network version

Final size

Spreading success

Groups

References



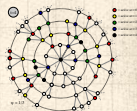
“Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon



Not the world's greatest painting from the start...



Escalation through theft, vandalism, **parody**, ...





# The Mona Lisa

The PoCSverse  
Social Contagion  
29 of 112

Social Contagion  
Models

## Background

Granovetter's model

Network version

Final size

Spreading success

Groups

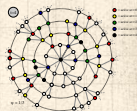
References



🧱 “Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon

🧱 Not the world's greatest painting from the start...

🧱 Escalation through theft, vandalism, **parody**, ...



# The Mona Lisa

The PoCSverse  
Social Contagion  
29 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

Spreading success

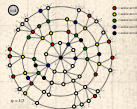
Groups

References




LEONARDO DA VINCI PAINTS MONA LISA — G. LISA

- 🧱 “Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon
- 🧱 Not the world’s greatest painting from the start...
- 🧱 Escalation through theft, vandalism, **parody**, ...



# 'Tattooed Guy' Was Pivotal in Armstrong Case

[nytimes] 



"... LeGrande's doping sparked a series of events  
..."

The PoCverse  
Social Contagion  
30 of 112

Social Contagion  
Models

## Background

Granovetter's model

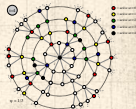
Network version

Final size

Spreading success

Groups

References



# The completely unpredicted fall of Eastern Europe:



Timunr Kuran: <sup>[20, 21]</sup> "Now Out of Never: The Element of Surprise in the East European Revolution of 1989"

The PoCSverse  
Social Contagion  
31 of 112

Social Contagion  
Models

Background

Granovetter's model

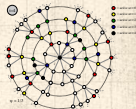
Network version

Final size

Spreading success

Groups

References



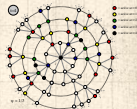
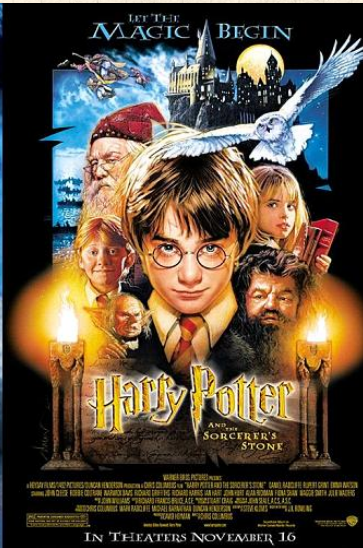
# The dismal predictive powers of editors...

The PoCVerse  
Social Contagion  
32 of 112

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

The PoCSverse  
Social Contagion  
33 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

Spreading success

Groups

References



From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book.

The PoCSverse  
Social Contagion  
33 of 112

Social Contagion  
Models

[Background](#)

[Granovetter's model](#)

[Network version](#)

[Final size](#)

[Spreading success](#)

[Groups](#)

[References](#)



From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice.

The PoCSverse  
Social Contagion  
33 of 112

Social Contagion  
Models

[Background](#)

[Granovetter's model](#)

[Network version](#)

[Final size](#)

[Spreading success](#)

[Groups](#)

[References](#)





From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it.



From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick."

The PoCSverse  
Social Contagion  
33 of 112

Social Contagion  
Models

[Background](#)

[Granovetter's model](#)

[Network version](#)

[Final size](#)

[Spreading success](#)

[Groups](#)

[References](#)



From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti."



From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right.



From a 2013 Believer Magazine [↗](#) interview with  
Maurice Sendak [↗](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then.



From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then. Everyone wanted another Tahitian book, a beach book.



## From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then. Everyone wanted another Tahitian book, a beach book. But then he kept writing deeper and deeper and then came Moby-Dick and people hated it.



## From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then. Everyone wanted another Tahitian book, a beach book. But then he kept writing deeper and deeper and then came Moby-Dick and people hated it. The only ones who liked it were Mr. and Mrs. Nathaniel Hawthorne.

Social Contagion  
Models

[Background](#)

[Granovetter's model](#)

[Network version](#)

[Final size](#)

[Spreading success](#)

[Groups](#)

References





## From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?


MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then. Everyone wanted another Tahitian book, a beach book. But then he kept writing deeper and deeper and then came Moby-Dick and people hated it. The only ones who liked it were Mr. and Mrs. Nathaniel Hawthorne. Moby-Dick didn't get famous until 1930.



## From a 2013 Believer Magazine [interview with Maurice Sendak](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then. Everyone wanted another Tahitian book, a beach book. But then he kept writing deeper and deeper and then came Moby-Dick and people hated it. The only ones who liked it were Mr. and Mrs. Nathaniel Hawthorne. Moby-Dick didn't get famous until 1930.


 Sendak named his dog Herman.




## From a 2013 Believer Magazine [↗](#) interview with Maurice Sendak [↗](#):

BLVR: Did the success of Where the Wild Things Are ever feel like an albatross?

MS: It's a nice book. It's perfectly nice. I can't complain about it. I remember Herman Melville said, "When I die no one is going to mention Moby-Dick. They're all going to talk about my first book, about \*\*\*\*ing maidens in Tahiti." He was right. No mention of Moby-Dick then. Everyone wanted another Tahitian book, a beach book. But then he kept writing deeper and deeper and then came Moby-Dick and people hated it. The only ones who liked it were Mr. and Mrs. Nathaniel Hawthorne. Moby-Dick didn't get famous until 1930.

 Sendak named his dog Herman.

 The essential Colbert interview: [Pt. 1](#) [↗](#) and [Pt. 2](#) [↗](#).



# Drafting success in the NFL: ↗

## Top Players by Round, 1995-2012



1ST ROUND

**Peyton Manning**

1ST OVER ALL, 1998



2ND ROUND

**Drew Brees**

32ND PICK, 2001



3RD ROUND

**Terrell Owens**

89TH PICK, 1996



4TH ROUND

**Jared Allen**

126TH PICK, 2004



5TH ROUND

**Zach Thomas**

154TH PICK, 1996



6TH ROUND

**Tom Brady**

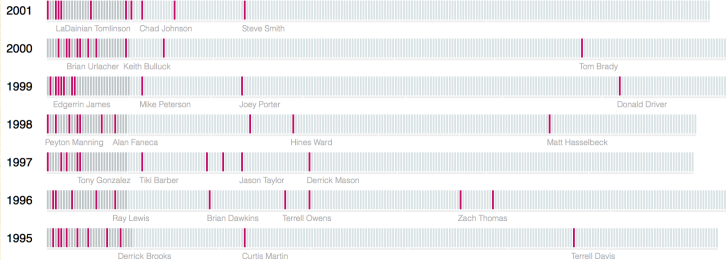
199TH PICK, 2000



7TH ROUND

**Donald Driver**

213TH PICK, 1999



## Social Contagion Models

### Background

Granovetter's model

Network version

Final size

Spreading success

Groups

## References



# Social Contagion

## Messaging with social connections

The PoCSverse  
Social Contagion  
35 of 112

### Social Contagion Models

#### Background

Granovetter's model

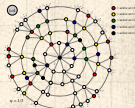
Network version

Final size

Spreading success

Groups


### References



# Social Contagion

The PoCSverse  
Social Contagion  
35 of 112

## Messaging with social connections

 Ads based on message content

Social Contagion  
Models

### Background

Granovetter's model

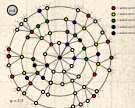
Network version

Final size

Spreading success

Groups

References



# Social Contagion

The PoCSverse  
Social Contagion  
35 of 112

## Messaging with social connections

- 📦 Ads based on message content  
(e.g., Google and email)

Social Contagion  
Models

### Background

Granovetter's model

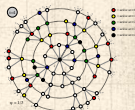
Network version

Final size


Spreading success

Groups





References



## Messaging with social connections

 Ads based on message content  
(e.g., Google and email)

 BzzAgent 

-  Harnessing of BzzAgents to directly market through social ties.
-  Generally: BzzAgents did not reveal their BzzAgent status and did not want to be paid.
-  NYT, 2004-12-05: "The Hidden (in Plain Sight) Persuaders" 

## Social Contagion Models

### Background

Granovetter's model

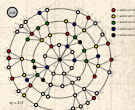
Network version

Final size

Spreading success

Groups

## References





## Messing with social connections



Ads based on message content  
(e.g., Google and email)



BzzAgent

- Harnessing of BzzAgents to directly market through social ties.
- Generally: BzzAgents did not reveal their BzzAgent status and did not want to be paid.
- NYT, 2004-12-05: "The Hidden (in Plain Sight) Persuaders"



One of Facebook's early advertising attempts:  
Beacon

## Social Contagion Models

### Background

Granovetter's model

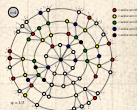
Network version

Final size




Spreading success

Groups

## References



## Messing with social connections

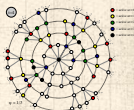
- 📦 Ads based on message content (e.g., Google and email)
- 📦 BzzAgent 
  - 📦 Harnessing of BzzAgents to directly market through social ties.
  - 📦 Generally: BzzAgents did not reveal their BzzAgent status and did not want to be paid.
  - 📦 NYT, 2004-12-05: "The Hidden (in Plain Sight) Persuaders" 
- 📦 One of Facebook's early advertising attempts: Beacon 
- 📦 All of Facebook's advertising attempts.

## Social Contagion Models




### Background

Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References



## Messing with social connections

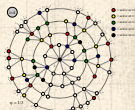
- 📦 Ads based on message content (e.g., Google and email)
- 📦 BzzAgent 
  - 📦 Harnessing of BzzAgents to directly market through social ties.
  - 📦 Generally: BzzAgents did not reveal their BzzAgent status and did not want to be paid.
  - 📦 NYT, 2004-12-05: "The Hidden (in Plain Sight) Persuaders" 
- 📦 One of Facebook's early advertising attempts: Beacon 
- 📦 All of Facebook's advertising attempts.
- 📦 Seriously, Facebook. What could go wrong?

## Social Contagion Models

### Background

- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by Robert Cialdini 

The PoCSverse  
Social Contagion  
36 of 112

Social Contagion  
Models

## Background

Granovetter's model

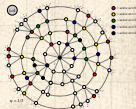
Network version

Final size

Spreading success

Groups

References



# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by Robert Cialdini 

Six modes of influence:

The PoCSverse  
Social Contagion  
36 of 112

Social Contagion  
Models

Background

Granovetter's model

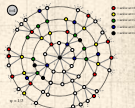
Network version

Final size


Spreading success

Groups

References



# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by Robert Cialdini 

Six modes of influence:

1. **Reciprocation**: *The Old Give and Take... and Take*;  
e.g., Free samples, Hare Krishnas.

Background

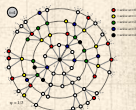
Granovetter's model

Network version

Final size

Spreading success

Groups



# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by [Robert Cialdini](#) ↗

Six modes of influence:

1. **Reciprocation:** *The Old Give and Take... and Take;* e.g., Free samples, Hare Krishnas.
2. **Commitment and Consistency:** *Hobgoblins of the Mind;* e.g., Hazing.

Background

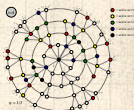
Granovetter's model

Network version

Final size

Spreading success

Groups



# Getting others to do things for you

A very good book: 'Influence' <sup>[8]</sup> by Robert Cialdini ↗

Six modes of influence:

1. **Reciprocation**: *The Old Give and Take... and Take*; e.g., Free samples, Hare Krishnas.
2. **Commitment and Consistency**: *Hobgoblins of the Mind*; e.g., Hazing.
3. **Social Proof**: *Truths Are Us*; e.g., Jonestown ↗, Kitty Genovese ↗ (contested).

Background

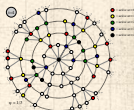
Granovetter's model

Network version

Final size

Spreading success

Groups





# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by [Robert Cialdini](#)

## Six modes of influence:

1. **Reciprocation:** *The Old Give and Take... and Take;* e.g., Free samples, Hare Krishnas.
2. **Commitment and Consistency:** *Hobgoblins of the Mind;* e.g., Hazing.
3. **Social Proof:** *Truths Are Us;* e.g., [Jonestown](#), [Kitty Genovese](#) (contested).
4. **Liking:** *The Friendly Thief;* e.g., Separation into groups is enough to cause problems.

### Background

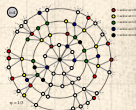
Granovetter's model

Network version

Final size

Spreading success

Groups



# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by [Robert Cialdini](#)

## Six modes of influence:

1. **Reciprocation:** *The Old Give and Take... and Take;* e.g., Free samples, Hare Krishnas.
2. **Commitment and Consistency:** *Hobgoblins of the Mind;* e.g., Hazing.
3. **Social Proof:** *Truths Are Us;* e.g., [Jonestown](#), [Kitty Genovese](#) (contested).
4. **Liking:** *The Friendly Thief;* e.g., Separation into groups is enough to cause problems.
5. **Authority:** *Directed Deference;* e.g., [Milgram's obedience to authority experiment](#).

Social Contagion  
Models

### Background

Granovetter's model

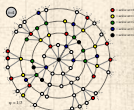
Network version

Final size

Spreading success

Groups

References



# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by [Robert Cialdini](#)

## Six modes of influence:

1. **Reciprocation:** *The Old Give and Take... and Take;* e.g., Free samples, Hare Krishnas.
2. **Commitment and Consistency:** *Hobgoblins of the Mind;* e.g., Hazing.
3. **Social Proof:** *Truths Are Us;* e.g., [Jonestown](#), [Kitty Genovese](#) (contested).
4. **Liking:** *The Friendly Thief;* e.g., Separation into groups is enough to cause problems.
5. **Authority:** *Directed Deference;* e.g., [Milgram's obedience to authority experiment](#).
6. **Scarcity:** *The Rule of the Few;* e.g., Prohibition.

Social Contagion  
Models

### Background

Granovetter's model

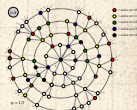
Network version

Final size

Spreading success

Groups

References



## Social proof:

### Social Contagion Models

#### Background

Granovetter's model

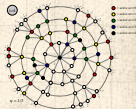
Network version

Final size

Spreading success

Groups

### References



# Social contagion

The PoCSverse  
Social Contagion  
38 of 112

## Social Contagion Models

### Background

Granovetter's model

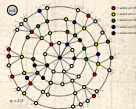
Network version

Final size

Spreading success

Groups

## References



# Social contagion

The PoCSverse  
Social Contagion  
38 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

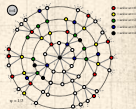
Spreading success

Groups

References



Cialdini's modes are heuristics that help up us get through life.



# Social contagion

The PoCSverse  
Social Contagion  
38 of 112

## Social Contagion Models

### Background

Granovetter's model


Network version


Final size

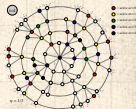
Spreading success

Groups

### References

 Cialdini's modes are heuristics that help up us get through life.

 Useful but can be leveraged...



# Social contagion

The PoCSverse  
Social Contagion  
38 of 112

## Social Contagion Models

### Background

Granovetter's model


Network version


Final size

Spreading success

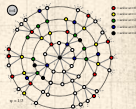
Groups

### References

 Cialdini's modes are heuristics that help up us get through life.

 Useful but can be leveraged...

Other acts of influence:





# Social contagion

The PoCSverse  
Social Contagion  
38 of 112

Social Contagion  
Models

## Background

Granovetter's model


Network version


Final size

Spreading success


Groups

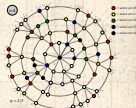
References

 Cialdini's modes are heuristics that help up us get through life.

 Useful but can be leveraged...

Other acts of influence:

 Conspicuous Consumption (Veblen, 1912)



# Social contagion

The PoCSverse  
Social Contagion  
38 of 112

Social Contagion  
Models

Background

Granovetter's model


Network version


Final size

Spreading success


Groups


References

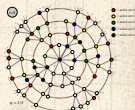
 Cialdini's modes are heuristics that help up us get through life.

 Useful but can be leveraged...

Other acts of influence:

 Conspicuous Consumption (Veblen, 1912)

 Conspicuous Destruction (Potlatch)





Background

Granovetter's model

Network version


Final size

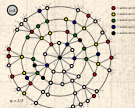
Spreading success

Groups

References

Some important models:

 Tipping models—Schelling (1971) [23, 24, 25]



Background

Granovetter's model

Network version


Final size


Spreading success

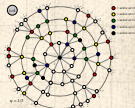
Groups

References

Some important models:

 Tipping models—Schelling (1971) [23, 24, 25]

 Simulation on checker boards



Background

Granovetter's model

Network version


Final size


Spreading success


Groups

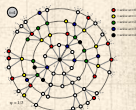
References

## Some important models:

 Tipping models—Schelling (1971) [23, 24, 25]

 Simulation on checker boards

 Idea of thresholds



Background

Granovetter's model


Network version





Final size

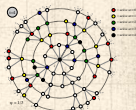
Spreading success

Groups

## Some important models:

 Tipping models—Schelling (1971) [23, 24, 25]

-  Simulation on checker boards
-  Idea of thresholds
-  Polygon-themed online visualization. (Includes optional diversity-seeking proclivity.) 



Background

Granovetter's model

Network version


Final size


Spreading success


Groups



References


## Some important models:

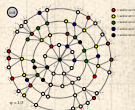
 Tipping models—Schelling (1971) [23, 24, 25]

 Simulation on checker boards

 Idea of thresholds

 Polygon-themed online visualization. (Includes optional diversity-seeking proclivity.) 

 Threshold models—Granovetter (1978) [15]





Background

Granovetter's model

Network version


Final size


Spreading success


Groups



References


## Some important models:


 Tipping models—Schelling (1971) [23, 24, 25]

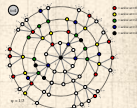
 Simulation on checker boards

 Idea of thresholds

 Polygon-themed online visualization. (Includes optional diversity-seeking proclivity.) 

 Threshold models—Granovetter (1978) [15]

 Herding models—Bikhchandani, Hirschleifer, Welch (1992) [2, 3]



Background

Granovetter's model

Network version

Final size

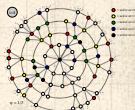
Spreading success

Groups

References

## Some important models:

- 🧱 Tipping models—Schelling (1971) [23, 24, 25]
  - 🧱 Simulation on checker boards
  - 🧱 Idea of thresholds
  - 🧱 Polygon-themed online visualization. (Includes optional diversity-seeking proclivity.) ↗
- 🧱 Threshold models—Granovetter (1978) [15]
- 🧱 Herding models—Bikhchandani, Hirschleifer, Welch (1992) [2, 3]
  - 🧱 Social learning theory, Informational cascades,...



# Social contagion models

## Thresholds

The PoCSverse  
Social Contagion  
41 of 112

### Social Contagion Models

#### Background

Granovetter's model

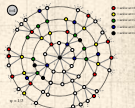
Network version

Final size

Spreading success

Groups

#### References



# Social contagion models

The PoCSverse  
Social Contagion  
41 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version


Final size

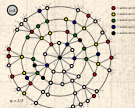
Spreading success

Groups

References

## Thresholds

 Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted



# Social contagion models

The PoCSverse  
Social Contagion  
41 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version


Final size


Spreading success

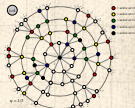
Groups

References

## Thresholds

 Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted

 'Others' may be everyone in a population, an individual's close friends, any reference group.



# Social contagion models

The PoCSverse  
Social Contagion  
41 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

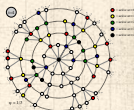
Spreading success

Groups

References





## Thresholds

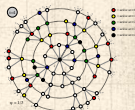
- Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted
- 'Others' may be everyone in a population, an individual's close friends, any reference group.
- Response can be probabilistic or deterministic.



# Social contagion models

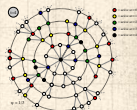
## Thresholds

-  Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted
-  'Others' may be everyone in a population, an individual's close friends, any reference group.
-  Response can be probabilistic or deterministic.
-  Individual thresholds can vary



## Thresholds

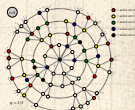
- Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted
- 'Others' may be everyone in a population, an individual's close friends, any reference group.
- Response can be probabilistic or deterministic.
- Individual thresholds can vary
- Assumption: order of others' adoption does not matter...





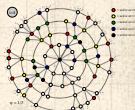
## Thresholds

- Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted
- 'Others' may be everyone in a population, an individual's close friends, any reference group.
- Response can be probabilistic or deterministic.
- Individual thresholds can vary
- Assumption: order of others' adoption does not matter... **(unrealistic)**.



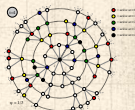
## Thresholds

- Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted
- 'Others' may be everyone in a population, an individual's close friends, any reference group.
- Response can be probabilistic or deterministic.
- Individual thresholds can vary
- Assumption: order of others' adoption does not matter... **(unrealistic)**.
- Assumption: level of influence per person is uniform



## Thresholds

- Basic idea: individuals adopt a behavior when a **certain fraction of others** have adopted
- 'Others' may be everyone in a population, an individual's close friends, any reference group.
- Response can be probabilistic or deterministic.
- Individual thresholds can vary
- Assumption: order of others' adoption does not matter... **(unrealistic)**.
- Assumption: level of influence per person is uniform **(unrealistic)**.



# Social Contagion

The PoCSverse  
Social Contagion  
42 of 112

Some possible origins of thresholds:

Social Contagion  
Models

Background

Granovetter's model

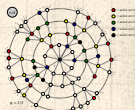
Network version

Final size

Spreading success

Groups

References



# Social Contagion

The PoCSverse  
Social Contagion  
42 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version


Final size

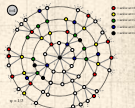
Spreading success

Groups

References

Some possible origins of thresholds:

 Inherent, evolution-devised inclination to coordinate, to conform, to imitate. [1]



# Social Contagion

The PoCSverse  
Social Contagion  
42 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version



Final size

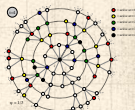
Spreading success

Groups




References

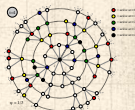
Some possible origins of thresholds:

-  Inherent, evolution-devised inclination to coordinate, to conform, to imitate. [1]
-  **Lack of information:** impute the worth of a good or behavior based on degree of adoption (social proof)







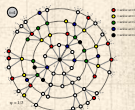
## Some possible origins of thresholds:

-  Inherent, evolution-devised inclination to coordinate, to conform, to imitate. [1]
-  **Lack of information:** impute the worth of a good or behavior based on degree of adoption (social proof)
-  Economics: **Network effects** or **network externalities**








## Some possible origins of thresholds:

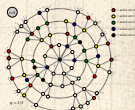
-  Inherent, evolution-devised inclination to coordinate, to conform, to imitate. [1]
-  **Lack of information:** impute the worth of a good or behavior based on degree of adoption (social proof)
-  Economics: **Network effects** or **network externalities**
  -  Externalities = Effects on others not directly involved in a transaction











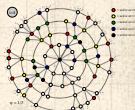
## Some possible origins of thresholds:

-  Inherent, evolution-devised inclination to coordinate, to conform, to imitate. [1]
-  **Lack of information:** impute the worth of a good or behavior based on degree of adoption (social proof)
-  Economics: **Network effects** or **network externalities**
  -  Externalities = Effects on others not directly involved in a transaction
  -  Examples: telephones, fax machine, Facebook, operating systems



## Some possible origins of thresholds:

-  Inherent, evolution-devised inclination to coordinate, to conform, to imitate. <sup>[1]</sup>
-  **Lack of information:** impute the worth of a good or behavior based on degree of adoption (social proof)
-  Economics: **Network effects** or **network externalities**
  -  Externalities = Effects on others not directly involved in a transaction
  -  Examples: telephones, fax machine, Facebook, operating systems
  -  An individual's utility increases with the adoption level among peers and the population in general



# Outline

The PoCSverse  
Social Contagion  
43 of 112

## Social Contagion Models

Background

Granovetter's model

Network version

Final size

Spreading success

Groups

## References

## Social Contagion Models

Background

Granovetter's model

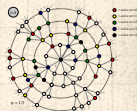
Network version

Final size

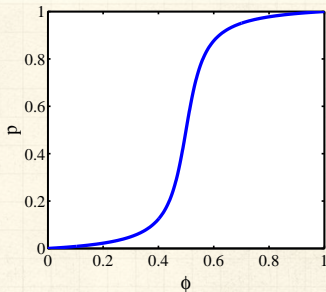
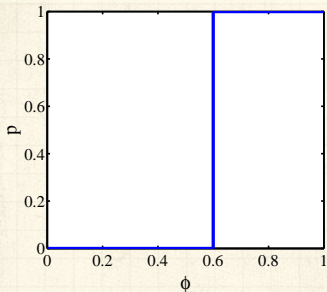
Spreading success

Groups

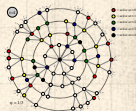
## References



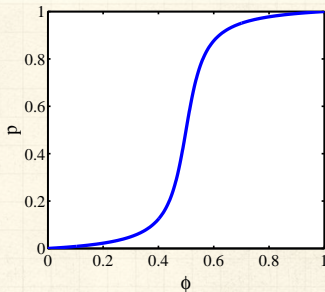
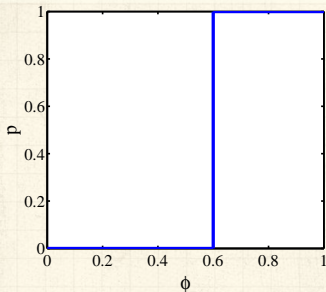
# Threshold models—response functions





Example threshold influence response functions:  
**deterministic** and **stochastic**

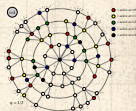


# Threshold models—response functions

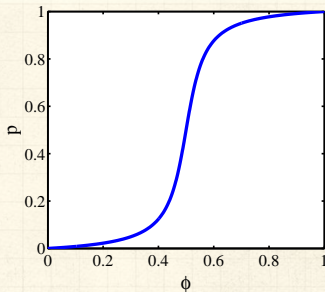
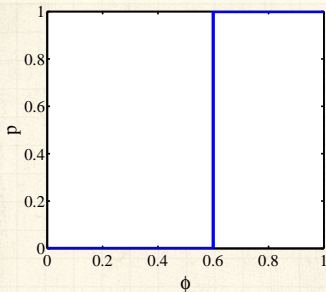



 Example threshold influence response functions:  
**deterministic** and **stochastic**


  $\phi$  = fraction of contacts 'on' (e.g., rioting)




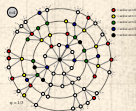
# Threshold models—response functions



 Example threshold influence response functions:  
**deterministic** and **stochastic**

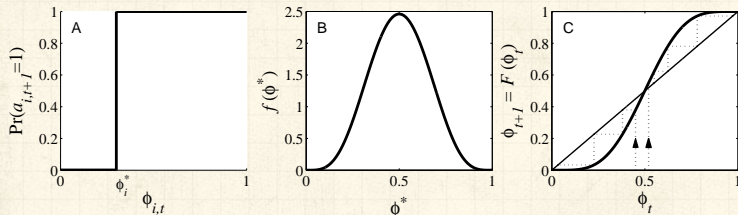
  $\phi$  = fraction of contacts 'on' (e.g., rioting)

 Two states: S and I.



# Threshold models

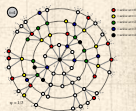
Action based on perceived behavior of others:



Two states: S and I.

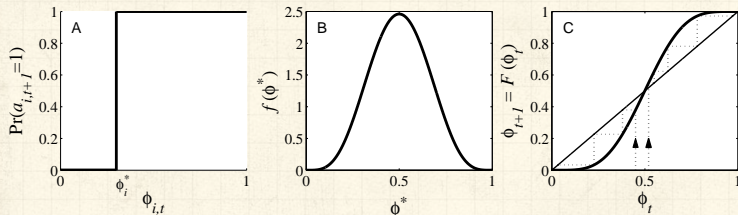


$\phi$  = fraction of contacts 'on' (e.g., rioting)



# Threshold models

Action based on perceived behavior of others:



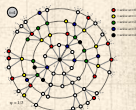
Two states: S and I.



$\phi$  = fraction of contacts 'on' (e.g., rioting)



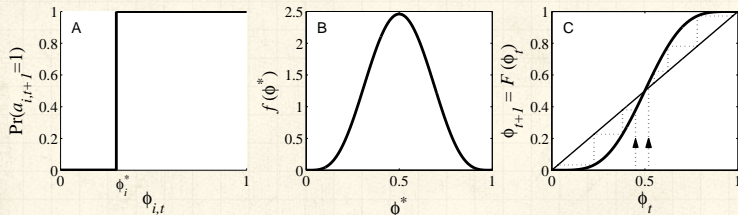
Discrete time update (strong assumption!)





# Threshold models

Action based on perceived behavior of others:



Two states: S and I.



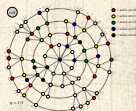
$\phi$  = fraction of contacts 'on' (e.g., rioting)



Discrete time update (strong assumption!)



This is a **Critical mass model**



# Threshold models

## Social Contagion Models

Background

Granovetter's model

Network version

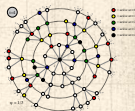
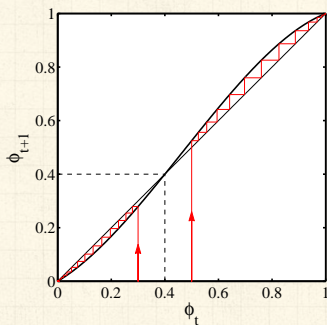
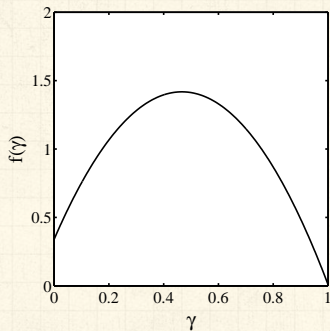
Final size

Spreading success

Groups

References

Another example of critical mass model:



# Threshold models

## Social Contagion Models

Background

Granovetter's model

Network version

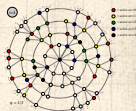
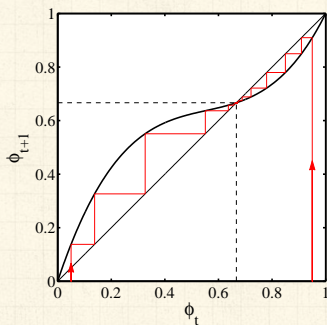
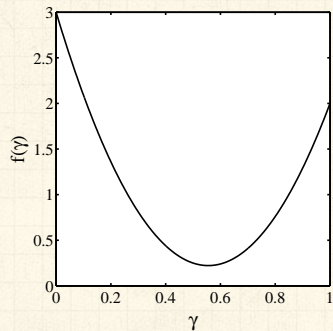
Final size

Spreading success

Groups

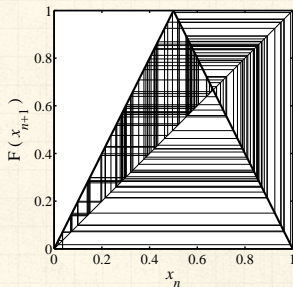
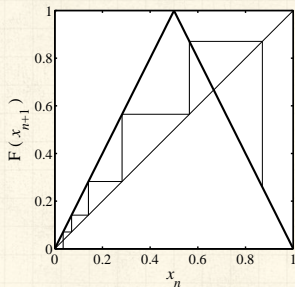
References

Example of single stable state model:



# Threshold models

Chaotic behavior possible [17, 16, 9, 18]



## Social Contagion Models

Background

Granovetter's model

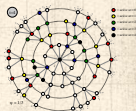
Network version

Final size

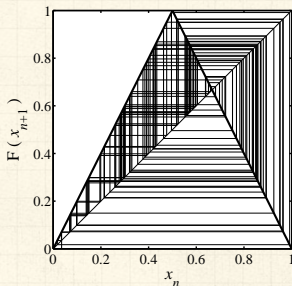
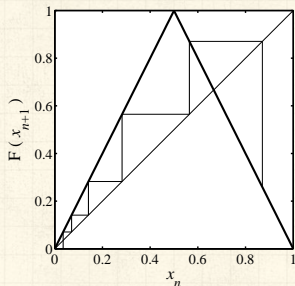
Spreading success

Groups

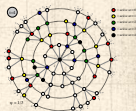
## References



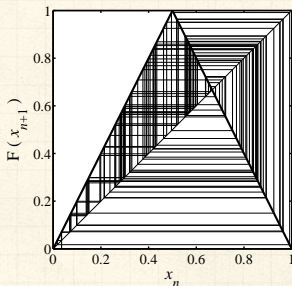
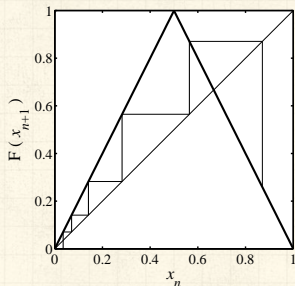
Chaotic behavior possible [17, 16, 9, 18]





Period doubling arises as map amplitude  $r$  is increased.



## Chaotic behavior possible [17, 16, 9, 18]



 Period doubling arises as map amplitude  $r$  is increased.

 Synchronous update assumption is crucial

## Social Contagion Models

Background

Granovetter's model

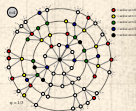
Network version

Final size

Spreading success

Groups

## References



# Threshold models—Nutshell

The PoCSverse  
Social Contagion  
49 of 112

## Social Contagion Models

Background

Granovetter's model

Network version

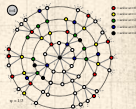
Final size

Spreading success

Groups

## References

Implications for collective action theory:



# Threshold models—Nutshell

The PoCSverse  
Social Contagion  
49 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

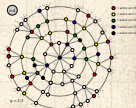
Spreading success

Groups

References

Implications for collective action theory:

1. Collective uniformity  $\nRightarrow$  individual uniformity





# Threshold models—Nutshell

The PoCSverse  
Social Contagion  
49 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

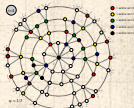
Spreading success

Groups

References

## Implications for collective action theory:

1. Collective uniformity  $\nRightarrow$  individual uniformity
2. Small individual changes  $\Rightarrow$  large global changes



# Threshold models—Nutshell

The PoCSverse  
Social Contagion  
49 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

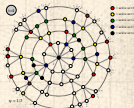
Spreading success

Groups

References

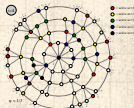
## Implications for collective action theory:

1. Collective uniformity  $\nRightarrow$  individual uniformity
2. Small individual changes  $\Rightarrow$  large global changes
3. The stories/dynamics of complex systems are conceptually inaccessible for individual-centric narratives.



## Implications for collective action theory:

1. Collective uniformity  $\nRightarrow$  individual uniformity
2. Small individual changes  $\Rightarrow$  large global changes
3. The stories/dynamics of complex systems are conceptually inaccessible for individual-centric narratives.
4. System stories live in left null space of our stories—we can't even see them.



# Threshold models—Nutshell

The PoCSverse  
Social Contagion  
49 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

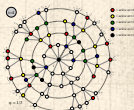
Spreading success

Groups

References

## Implications for collective action theory:

1. Collective uniformity  $\nRightarrow$  individual uniformity
2. Small individual changes  $\Rightarrow$  large global changes
3. The stories/dynamics of complex systems are conceptually inaccessible for individual-centric narratives.
4. System stories live in left null space of our stories—we can't even see them.
5. But we happily impose simplistic, individual-centric stories—we can't help ourselves ↗.



# Outline

The PoCSverse  
Social Contagion  
50 of 112

## Social Contagion Models

Background

Granovetter's model

**Network version**

Final size

Spreading success

Groups

## Social Contagion Models

Background

Granovetter's model

**Network version**

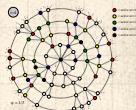
Final size

Spreading success

Groups

## References

## References



# Many years after Granovetter and Soong's work:



"A simple model of global cascades on random networks"

D. J. Watts. Proc. Natl. Acad. Sci., 2002 [27]

The PoCSverse  
Social Contagion  
51 of 112

Social Contagion  
Models

Background

Granovetter's model

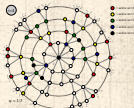
Network version

Final size

Spreading success

Groups

References



# Many years after Granovetter and Soong's work:



"A simple model of global cascades on random networks"

D. J. Watts. Proc. Natl. Acad. Sci., 2002 [27]



Mean field model  $\rightarrow$  network model

The PoCSverse  
Social Contagion  
51 of 112

Social Contagion  
Models

Background

Granovetter's model

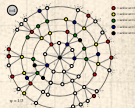
Network version

Final size

Spreading success

Groups

References



## Many years after Granovetter and Soong's work:



"A simple model of global cascades on random networks"

D. J. Watts. Proc. Natl. Acad. Sci., 2002 [27]



Mean field model → network model



Individuals now have a limited view of the world

The PoCSverse  
Social Contagion  
51 of 112

Social Contagion  
Models

Background

Granovetter's model

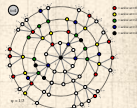
Network version

Final size

Spreading success

Groups

References





## Many years after Granovetter and Soong's work:



"A simple model of global cascades on random networks"

D. J. Watts. Proc. Natl. Acad. Sci., 2002 [27]



Mean field model → network model



Individuals now have a limited view of the world

## We'll also explore:



"Seed size strongly affects cascades on random networks" [14]

Gleeson and Cahalane, Phys. Rev. E, 2007.

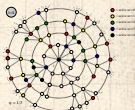


"Direct, physically motivated derivation of the contagion condition for spreading processes on generalized random networks" [10] Dodds, Harris, and Payne, Phys. Rev. E, 2011



"Influentials, Networks, and Public Opinion Formation" [28]

Watts and Dodds, J. Cons. Res., 2007.



# Threshold model on a network

The PoCSverse  
Social Contagion  
52 of 112

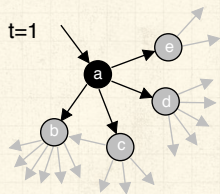
## Social Contagion Models


Background  
Granovetter's model

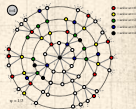
Network version  
Final size

Spreading success  
Groups

## References



 All nodes have threshold  $\phi = 0.2$ .



# Threshold model on a network

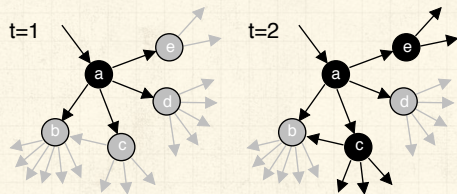
## Social Contagion Models


Background  
Granovetter's model

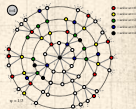
Network version  
Final size

Spreading success  
Groups

References



 All nodes have threshold  $\phi = 0.2$ .



# Threshold model on a network

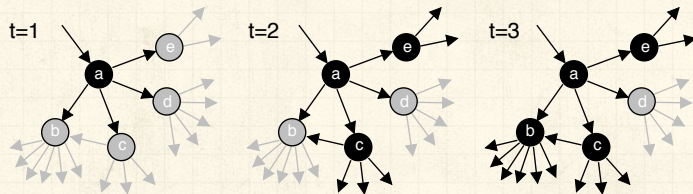
## Social Contagion Models


Background  
Granovetter's model

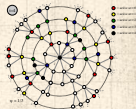
Network version  
Final size

Spreading success  
Groups


References



 All nodes have threshold  $\phi = 0.2$ .



# Threshold model on a network

 Interactions between individuals now represented by a network.

The PoCSverse  
Social Contagion  
53 of 112

Social Contagion  
Models

Background

Granovetter's model

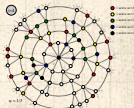
Network version

Final size


Spreading success


Groups

References



# Threshold model on a network

 Interactions between individuals now represented by a network.

 Network is **sparse**.

The PoCSverse  
Social Contagion  
53 of 112

Social Contagion  
Models

Background

Granovetter's model

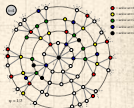
Network version

Final size

Spreading success

Groups

References



# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.

The PoCSverse  
Social Contagion  
53 of 112

## Social Contagion Models

Background

Granovetter's model

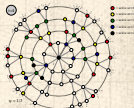
Network version

Final size

Spreading success

Groups

References



# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.

## Social Contagion Models

Background

Granovetter's model

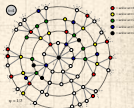
Network version

Final size

Spreading success

Groups

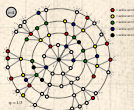
References





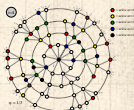
# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.
- Each individual  $i$  has a fixed threshold  $\phi_i$ .



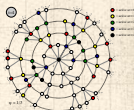
# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.
- Each individual  $i$  has a fixed threshold  $\phi_i$ .
- Individuals repeatedly poll contacts on network.



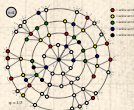
# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.
- Each individual  $i$  has a fixed threshold  $\phi_i$ .
- Individuals repeatedly poll contacts on network.
- Synchronous, discrete time updating.



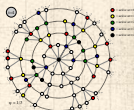
# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.
- Each individual  $i$  has a fixed threshold  $\phi_i$ .
- Individuals repeatedly poll contacts on network.
- Synchronous, discrete time updating.
- Individual  $i$  becomes active when fraction of active contacts  $\frac{a_i}{k_i} \geq \phi_i$ .



# Threshold model on a network

- Interactions between individuals now represented by a network.
- Network is **sparse**.
- Individual  $i$  has  $k_i$  contacts.
- Influence on each link is **reciprocal** and of **unit weight**.
- Each individual  $i$  has a fixed threshold  $\phi_i$ .
- Individuals repeatedly poll contacts on network.
- Synchronous, discrete time updating.
- Individual  $i$  becomes active when fraction of active contacts  $\frac{a_i}{k_i} \geq \phi_i$ .
- Individuals remain active when switched (no recovery = SI model).



# Snowballing

The PoCSverse  
Social Contagion  
54 of 112

## Social Contagion Models

Background

Granovetter's model

**Network version**

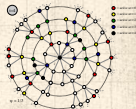
Final size

Spreading success

Groups

## References

First study random networks:



# Snowballing

## Social Contagion Models


Background  
Granovetter's model

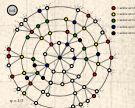
**Network version**  
Final size

Spreading success  
Groups

References

First study random networks:

 Start with  $N$  nodes with a degree distribution  $P_k$



# Snowballing

## Social Contagion Models

Background  
Granovetter's model

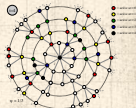
**Network version**  
Final size

Spreading success  
Groups

References

First study random networks:

- Start with  $N$  nodes with a degree distribution  $P_k$
- Nodes are randomly connected (carefully so)





# Snowballing

## Social Contagion Models

Background  
Granovetter's model

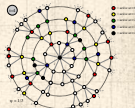
**Network version**  
Final size

Spreading success  
Groups

References

First study random networks:

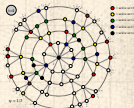
- Start with  $N$  nodes with a degree distribution  $P_k$
- Nodes are randomly connected (carefully so)
- Aim: Figure out when activation will propagate



# Snowballing

## First study random networks:

- Start with  $N$  nodes with a degree distribution  $P_k$
- Nodes are randomly connected (carefully so)
- Aim: Figure out when activation will propagate
- Determine a **cascade condition**



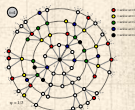
# Snowballing

## First study random networks:

- Start with  $N$  nodes with a degree distribution  $P_k$
- Nodes are randomly connected (carefully so)
- Aim: Figure out when activation will propagate
- Determine a **cascade condition**

## The Cascade Condition:

1. If one individual is initially activated, what is the probability that an activation will spread over a network?



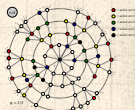
# Snowballing

## First study random networks:

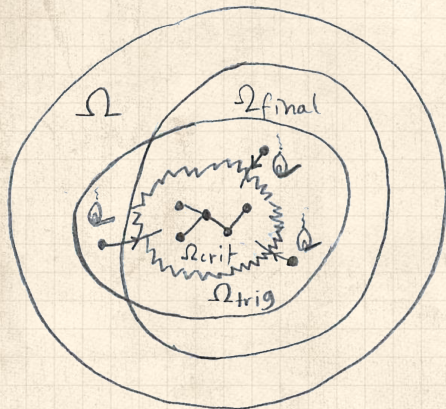
- Start with  $N$  nodes with a degree distribution  $P_k$
- Nodes are randomly connected (carefully so)
- Aim: Figure out when activation will propagate
- Determine a **cascade condition**


## The Cascade Condition:


1. If one individual is initially activated, what is the probability that an activation will spread over a network?
2. What features of a network determine whether a cascade will occur or not?





# Example random network structure:

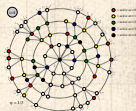


  $\Omega_{crit} = \Omega_{vuln} =$   
critical mass =  
global  
vulnerable  
component

  $\Omega_{trig} =$   
triggering  
component

  $\Omega_{final} =$   
potential  
extent of  
spread

  $\Omega =$  entire  
network



$$\Omega_{crit} \subset \Omega_{trig}; \Omega_{crit} \subset \Omega_{final}; \text{ and } \Omega_{trig}, \Omega_{final} \subset \Omega.$$

# Snowballing

The PoCSverse  
Social Contagion  
56 of 112

## Social Contagion Models

Background

Granovetter's model

**Network version**

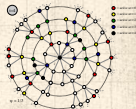
Final size

Spreading success

Groups

## References

Follow active links



# Snowballing

The PoCSverse  
Social Contagion  
56 of 112

## Social Contagion Models


Background  
Granovetter's model

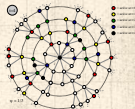
Network version  
Final size

Spreading success  
Groups


## References


## Follow active links

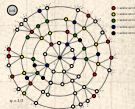
 An active link is a link connected to an activated node.



## Follow active links




 An active link is a link connected to an activated node.

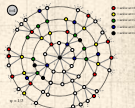
 If an infected link leads to **at least 1 more infected link**, then **activation spreads**.





## Follow active links

-  An active link is a link connected to an activated node.
-  If an infected link leads to **at least 1 more infected link**, then **activation spreads**.
-  We need to understand which nodes can be activated when only one of their neighbors becomes active.



# The most gullible

Vulnerables:

The PoCverse  
Social Contagion  
57 of 112

Social Contagion  
Models

Background

Granovetter's model

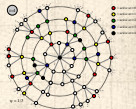
Network version

Final size

Spreading success

Groups

References



# The most gullible

The PoCSverse  
Social Contagion  
57 of 112

## Social Contagion Models

Background  
Granovetter's model

Network version  
Final size

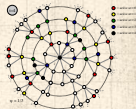
Spreading success  
Groups

References

## Vulnerables:



We call individuals who can be activated by just one contact being active **vulnerables**



# The most gullible

## Social Contagion Models


Background  
Granovetter's model


**Network version**  
Final size

Spreading success  
Groups

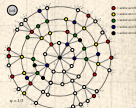
References

## Vulnerables:

 We call individuals who can be activated by just one contact being active **vulnerables**


 The vulnerability condition for node  $i$ :


$$1/k_i \geq \phi_i$$




# The most gullible

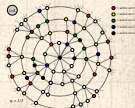
## Vulnerables:

 We call individuals who can be activated by just one contact being active **vulnerables**

 The vulnerability condition for node  $i$ :


$$1/k_i \geq \phi_i$$


 Which means # contacts  $k_i \leq \lfloor 1/\phi_i \rfloor$




# The most gullible


## Vulnerables:

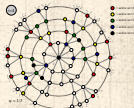
 We call individuals who can be activated by just one contact being active **vulnerables**

 The vulnerability condition for node  $i$ :

$$1/k_i \geq \phi_i$$


 Which means # contacts  $k_i \leq \lfloor 1/\phi_i \rfloor$


 For global cascades on random networks, must have a *global cluster of vulnerables* <sup>[27]</sup>




# The most gullible


## Vulnerables:

 We call individuals who can be activated by just one contact being active **vulnerables**

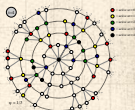
 The vulnerability condition for node  $i$ :

$$1/k_i \geq \phi_i$$

 Which means # contacts  $k_i \leq \lfloor 1/\phi_i \rfloor$


 For global cascades on random networks, must have a *global cluster of vulnerables* <sup>[27]</sup>


 **Cluster of vulnerables = critical mass**




# The most gullible


## Vulnerables:


 We call individuals who can be activated by just one contact being active **vulnerables**


 The vulnerability condition for node  $i$ :

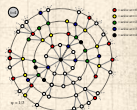
$$1/k_i \geq \phi_i$$

 Which means # contacts  $k_i \leq \lfloor 1/\phi_i \rfloor$

 For global cascades on random networks, must have a *global cluster of vulnerables* <sup>[27]</sup>

 **Cluster of vulnerables = critical mass**

 Network story: 1 node  $\rightarrow$  critical mass  $\rightarrow$  everyone.





# Cascade condition

Back to following a link:

The PoCSverse  
Social Contagion  
58 of 112

Social Contagion  
Models

Background

Granovetter's model

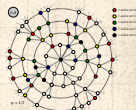
**Network version**

Final size

Spreading success


Groups

References



# Cascade condition

## Back to following a link:

 A randomly chosen link, traversed in a random direction, leads to a degree  $k$  node with probability  $\propto kP_k$ .

## Social Contagion Models

Background

Granovetter's model

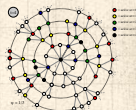
Network version

Final size

Spreading success



Groups

## References



# Cascade condition

## Back to following a link:

-  A randomly chosen link, traversed in a random direction, leads to a degree  $k$  node with probability  $\propto kP_k$ .
-  Follows from there being  $k$  ways to connect to a node with degree  $k$ .

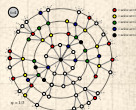
## Social Contagion Models

Background  
Granovetter's model

Network version  
Final size




Spreading success  
Groups

## References



# Cascade condition

## Back to following a link:

-  A randomly chosen link, traversed in a random direction, leads to a degree  $k$  node with probability  $\propto kP_k$ .
-  Follows from there being  $k$  ways to connect to a node with degree  $k$ .
-  Normalization:

$$\sum_{k=0}^{\infty} kP_k = \langle k \rangle$$

## Social Contagion Models

Background

Granovetter's model

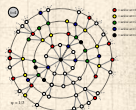
Network version

Final size

Spreading success




Groups

## References



# Cascade condition

## Back to following a link:

-  A randomly chosen link, traversed in a random direction, leads to a degree  $k$  node with probability  $\propto kP_k$ .
-  Follows from there being  $k$  ways to connect to a node with degree  $k$ .
-  Normalization:

$$\sum_{k=0}^{\infty} kP_k = \langle k \rangle$$

-  So

$$P(\text{linked node has degree } k) = \frac{kP_k}{\langle k \rangle}$$

## Social Contagion Models

Background

Granovetter's model

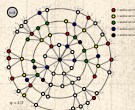
Network version

Final size

Spreading success

Groups

## References



# Cascade condition

The PoCSverse  
Social Contagion  
59 of 112

## Social Contagion Models

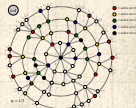
Background  
Granovetter's model

Network version  
Final size


Spreading success  
Groups

## References

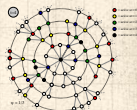
Next: Vulnerability of linked node



Next: Vulnerability of linked node

 Linked node is **vulnerable** with probability

$$\beta_k = \int_{\phi'_*=0}^{1/k} f(\phi'_*) d\phi'_*$$




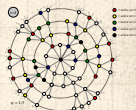
# Cascade condition

## Next: Vulnerability of linked node

 Linked node is **vulnerable** with probability

$$\beta_k = \int_{\phi'_*=0}^{1/k} f(\phi'_*) d\phi'_*$$

 If linked node is **vulnerable**, it produces  $k - 1$  new outgoing active links







# Cascade condition

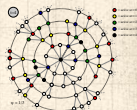
## Next: Vulnerability of linked node

 Linked node is **vulnerable** with probability

$$\beta_k = \int_{\phi'_*=0}^{1/k} f(\phi'_*) d\phi'_*$$

 If linked node is **vulnerable**, it produces  $k - 1$  **new** outgoing active links

 If linked node is **not vulnerable**, it produces **no** active links.



# Cascade condition


## Social Contagion Models

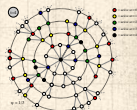
- Background
- Granovetter's model
- Network version**
- Final size

- Spreading success
- Groups

## References


Putting things together:

 Expected number of active edges produced by an active edge:

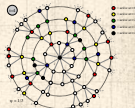


# Cascade condition

Putting things together:


 Expected number of active edges produced by an active edge:

$$R = \left[ \sum_{k=1}^{\infty} \underbrace{(k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle}}_{\text{success}} + \right]$$

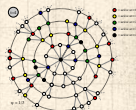


# Cascade condition

Putting things together:


 Expected number of active edges produced by an active edge:

$$R = \left[ \sum_{k=1}^{\infty} \underbrace{(k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle}}_{\text{success}} + \underbrace{0 \cdot (1 - \beta_k) \cdot \frac{kP_k}{\langle k \rangle}}_{\text{failure}} \right]$$

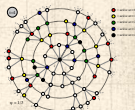


# Cascade condition

Putting things together:

 Expected number of active edges produced by an active edge:


$$R = \left[ \sum_{k=1}^{\infty} \underbrace{(k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle}}_{\text{success}} + \underbrace{0 \cdot (1 - \beta_k) \cdot \frac{kP_k}{\langle k \rangle}}_{\text{failure}} \right]$$
$$= \sum_{k=1}^{\infty} (k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle}$$




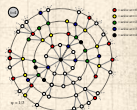
# Cascade condition

So... for random networks with fixed degree distributions, cascades take off when:

$$\sum_{k=1}^{\infty} (k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

  $\beta_k$  = probability a degree  $k$  node is vulnerable.

  $P_k$  = probability a node has degree  $k$ .



# Cascade condition

Two special cases:

The PoCverse  
Social Contagion  
62 of 112

Social Contagion  
Models

Background

Granovetter's model

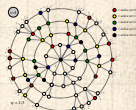
**Network version**

Final size

Spreading success

Groups

References



# Cascade condition

## Social Contagion Models


Background  
Granovetter's model

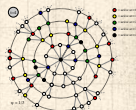
Network version  
Final size

Spreading success  
Groups

References

Two special cases:


 (1) Simple disease-like spreading succeeds:  $\beta_k = \beta$



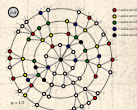


# Cascade condition

Two special cases:

 (1) Simple disease-like spreading succeeds:  $\beta_k = \beta$

$$\beta \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$



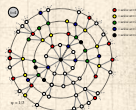
# Cascade condition

Two special cases:

🧱 (1) Simple disease-like spreading succeeds:  $\beta_k = \beta$


$$\beta \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

🧱 (2) Giant component exists:  $\beta = 1$




# Cascade condition

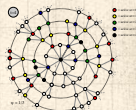
## Two special cases:

 (1) Simple disease-like spreading succeeds:  $\beta_k = \beta$

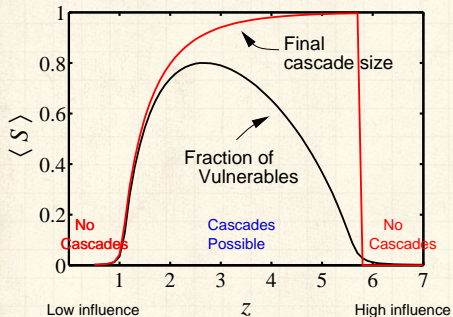
$$\beta \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

 (2) Giant component exists:  $\beta = 1$

$$1 \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

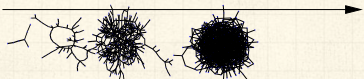


# Cascades on random networks

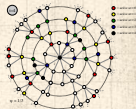


Cascades occur only if size of max vulnerable cluster  $> 0$ .

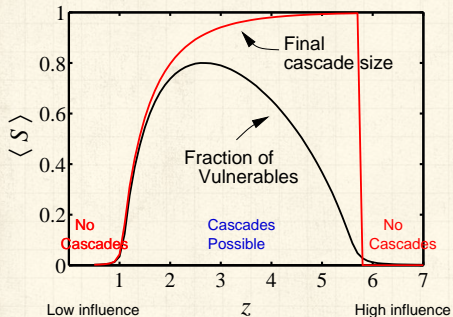
Low influence  $z$  High influence



Example networks



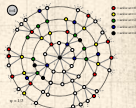
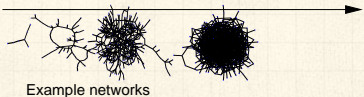
# Cascades on random networks



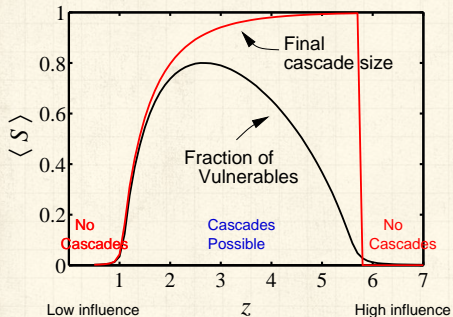
Cascades occur only if size of max vulnerable cluster  $> 0$ .



System may be 'robust-yet-fragile'.



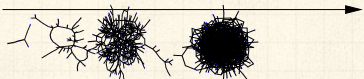
# Cascades on random networks



Low influence

$z$

High influence



Example networks



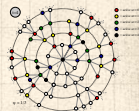
Cascades occur only if size of max vulnerable cluster  $> 0$ .



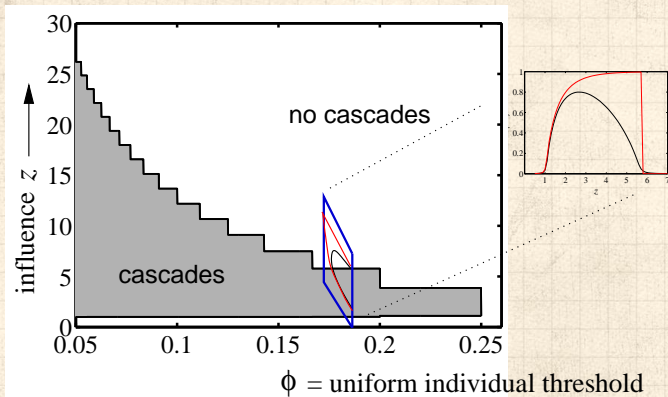
System may be 'robust-yet-fragile'.





'Ignorance' facilitates spreading.

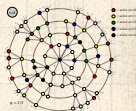


# Cascade window for random networks

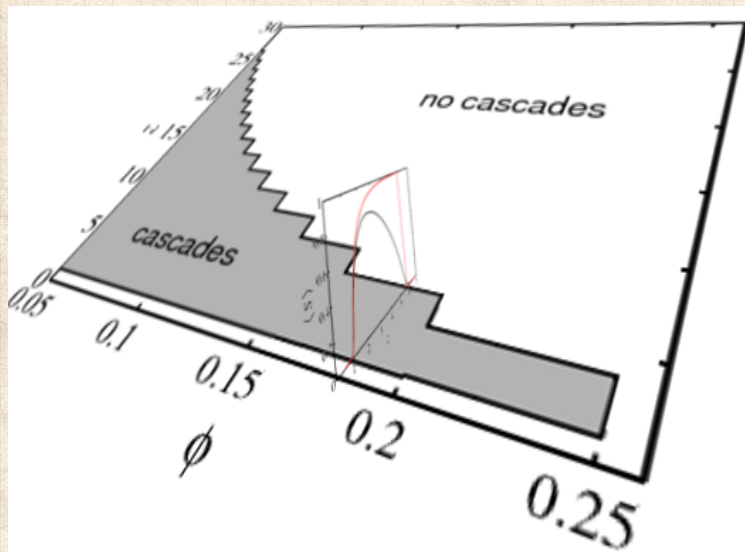


 'Cascade window' widens as threshold  $\phi$  decreases.

 Lower thresholds enable spreading.



# Cascade window for random networks



The PoCSverse  
Social Contagion  
65 of 112

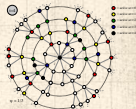
Social Contagion  
Models

Background  
Granovetter's model

**Network version**  
Final size

Spreading success  
Groups

References





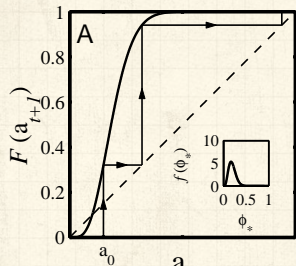
# All-to-all versus random networks

## Social Contagion Models

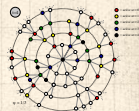
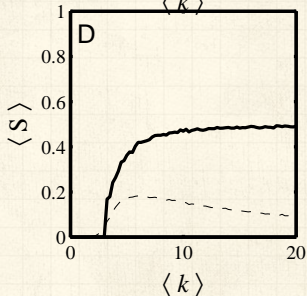
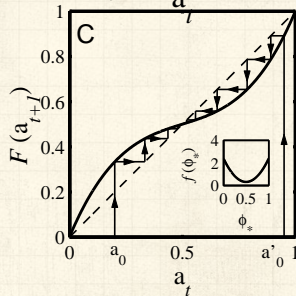
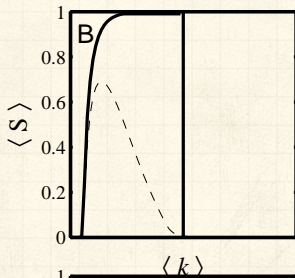
- Background
- Granovetter's model
- Network version**
- Final size
- Spreading success
- Groups

## References

all-to-all networks



random networks



# Cascade window—summary

The PoCSverse  
Social Contagion  
67 of 112

## Social Contagion Models

Background

Granovetter's model

**Network version**

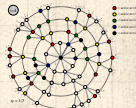
Final size

Spreading success

Groups

## References

For our simple model of a uniform threshold:



# Cascade window—summary

The PoCSverse  
Social Contagion  
67 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

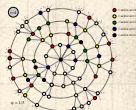
Spreading success

Groups

References

For our simple model of a uniform threshold:

1. **Low  $\langle k \rangle$ :** No cascades in poorly connected networks.  
No global clusters of any kind.



# Cascade window—summary

The PoCSverse  
Social Contagion  
67 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

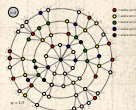
Spreading success

Groups

References

For our simple model of a uniform threshold:

1. **Low  $\langle k \rangle$ :** No cascades in poorly connected networks.  
No global clusters of any kind.
2. **High  $\langle k \rangle$ :** Giant component exists but not enough vulnerables.



# Cascade window—summary

The PoCSverse  
Social Contagion  
67 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

Final size

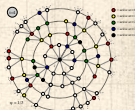
Spreading success

Groups

References

For our simple model of a uniform threshold:

1. **Low  $\langle k \rangle$** : No cascades in poorly connected networks.  
No global clusters of any kind.
2. **High  $\langle k \rangle$** : Giant component exists but not enough vulnerables.
3. **Intermediate  $\langle k \rangle$** : Global cluster of vulnerables exists.  
Cascades are possible in **"Cascade window."**



# Outline

The PoCSverse  
Social Contagion  
68 of 112

## Social Contagion Models

Background

Granovetter's model

Network version

**Final size**

Spreading success

Groups

## Social Contagion Models

Background

Granovetter's model

Network version

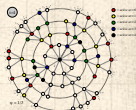
Final size

Spreading success

Groups

## References

## References



# Threshold contagion on random networks

The PoCSverse  
Social Contagion  
69 of 112

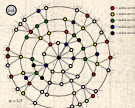
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



**Next:** Find expected fractional size of spread.



# Threshold contagion on random networks


The PoCSverse  
Social Contagion  
69 of 112


## Social Contagion Models

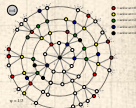
Background  
Granovetter's model  
Network version  
Final size

Spreading success  
Groups

## References

 **Next:** Find expected fractional size of spread.

 Not obvious even for uniform threshold problem.





# Threshold contagion on random networks

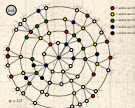
The PoCSverse  
Social Contagion  
69 of 112

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

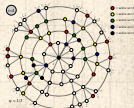
## References

- Next: Find expected fractional size of spread.
- Not obvious even for uniform threshold problem.
- Difficulty is in figuring out if and when nodes that need  $\geq 2$  hits switch on.



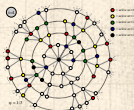
# Threshold contagion on random networks

- Next: Find expected fractional size of spread.
- Not obvious even for uniform threshold problem.
- Difficulty is in figuring out if and when nodes that need  $\geq 2$  hits switch on.
- Problem **beautifully solved** for infinite seed case by Gleeson and Cahalane:  
"Seed size strongly affects cascades on random networks," Phys. Rev. E, 2007. <sup>[14]</sup>




# Threshold contagion on random networks

- Next: Find expected fractional size of spread.
- Not obvious even for uniform threshold problem.
- Difficulty is in figuring out if and when nodes that need  $\geq 2$  hits switch on.
- Problem **beautifully solved** for infinite seed case by Gleeson and Cahalane:  
"Seed size strongly affects cascades on random networks," Phys. Rev. E, 2007. <sup>[14]</sup>
- Developed further by Gleeson in "Cascades on correlated and modular random networks," Phys. Rev. E, 2008. <sup>[13]</sup>



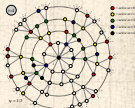
# Determining expected size of spread:

 Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



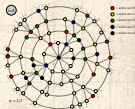
# Determining expected size of spread:

- ☰ Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- ☰ Capitalize on local branching network structure of random networks (again)

## Social Contagion Models

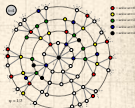
- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



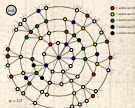
# Determining expected size of spread:

- ☰ Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- ☰ Capitalize on local branching network structure of random networks (again)
- ☰ Now think about what must happen for a specific node  $i$  to become active at time  $t$ :



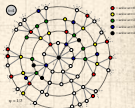
# Determining expected size of spread:

- Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- Capitalize on local branching network structure of random networks (again)
- Now think about what must happen for a specific node  $i$  to become active at time  $t$ :
  - $t = 0$ :  $i$  is one of the seeds (prob =  $\phi_0$ )



# Determining expected size of spread:

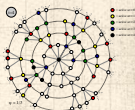
- Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- Capitalize on local branching network structure of random networks (again)
- Now think about what must happen for a specific node  $i$  to become active at time  $t$ :
  - $t = 0$ :  $i$  is one of the seeds (prob =  $\phi_0$ )
  - $t = 1$ :  $i$  was not a seed but enough of  $i$ 's friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.





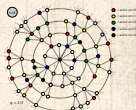
# Determining expected size of spread:

- Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- Capitalize on local branching network structure of random networks (again)
- Now think about what must happen for a specific node  $i$  to become active at time  $t$ :
  - $t = 0$ :  $i$  is one of the seeds (prob =  $\phi_0$ )
  - $t = 1$ :  $i$  was not a seed but enough of  $i$ 's friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.
  - $t = 2$ : enough of  $i$ 's friends and friends-of-friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.



# Determining expected size of spread:

- ☰ Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- ☰ Capitalize on local branching network structure of random networks (again)
- ☰ Now think about what must happen for a specific node  $i$  to become active at time  $t$ :
  - $t = 0$ :  $i$  is one of the seeds (prob =  $\phi_0$ )
  - $t = 1$ :  $i$  was not a seed but enough of  $i$ 's friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.
  - $t = 2$ : enough of  $i$ 's friends and friends-of-friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.
  - $t = n$ : enough nodes within  $n$  hops of  $i$  switched on at  $t = 0$  and their effects have propagated to reach  $i$ .

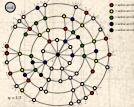
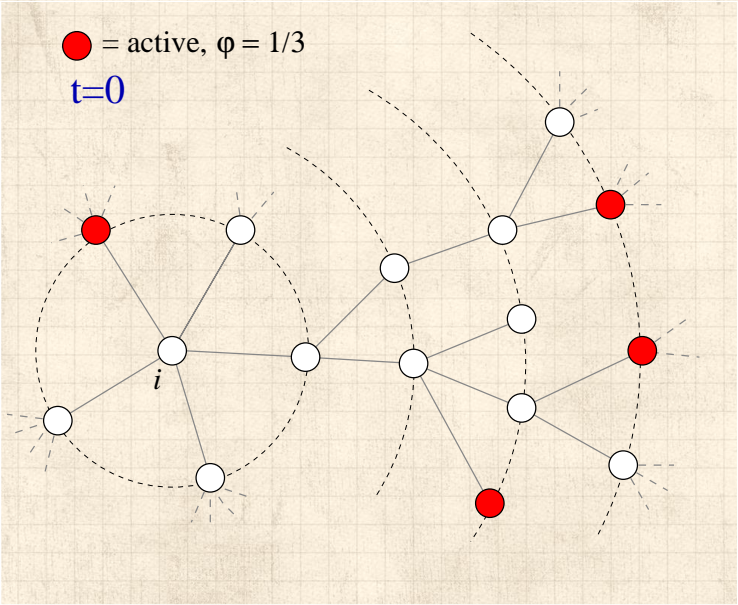


# Expected size of spread

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups

## References



# Expected size of spread

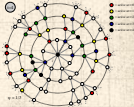
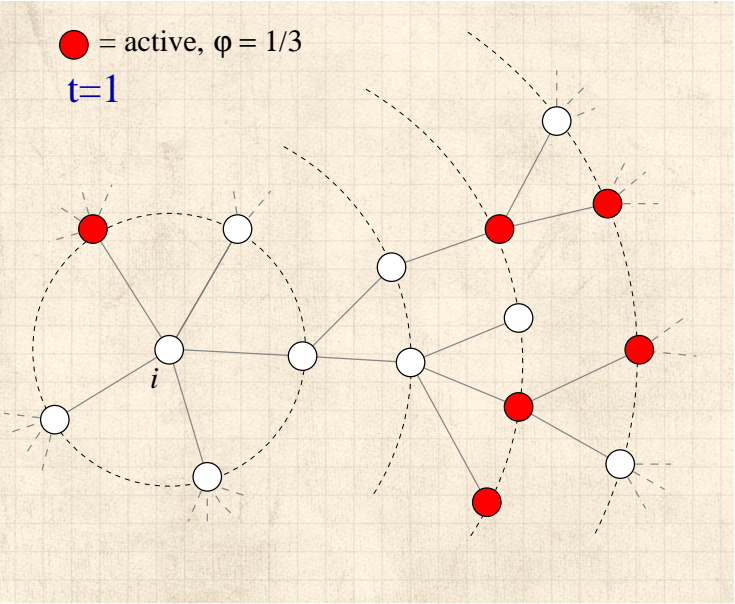
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups

## References

● = active,  $\phi = 1/3$

$t=1$

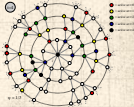
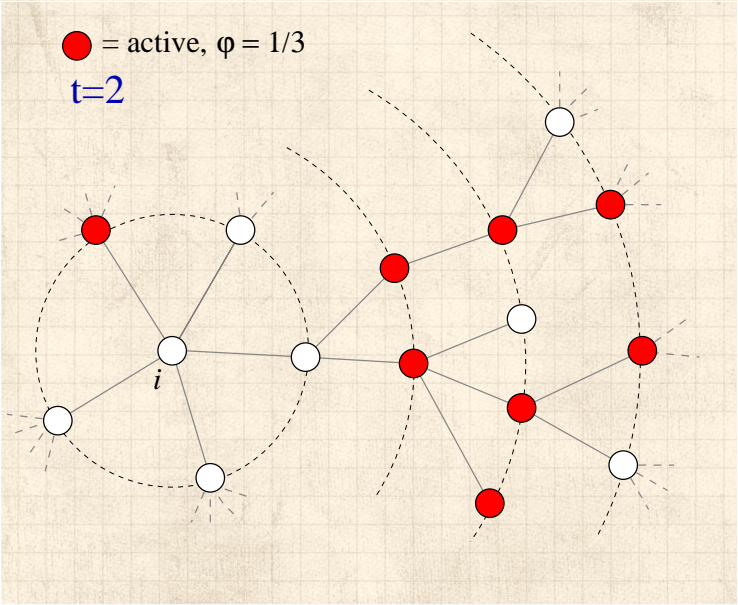


# Expected size of spread

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



# Expected size of spread

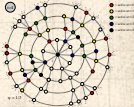
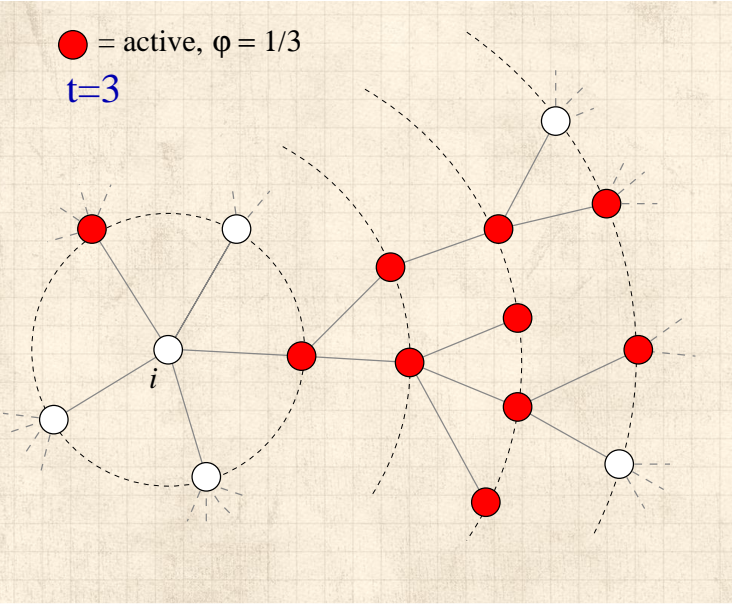
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups

## References

● = active,  $\phi = 1/3$

$t=3$

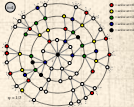
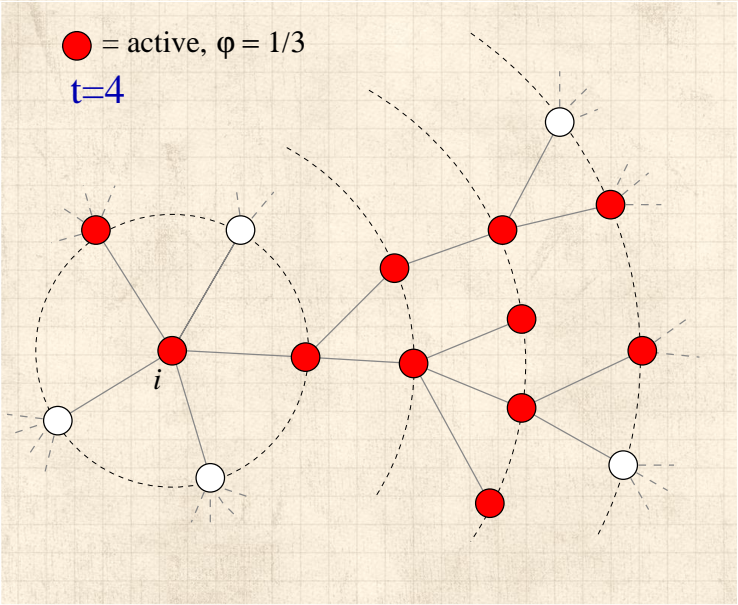


# Expected size of spread

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups

## References



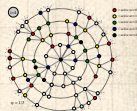
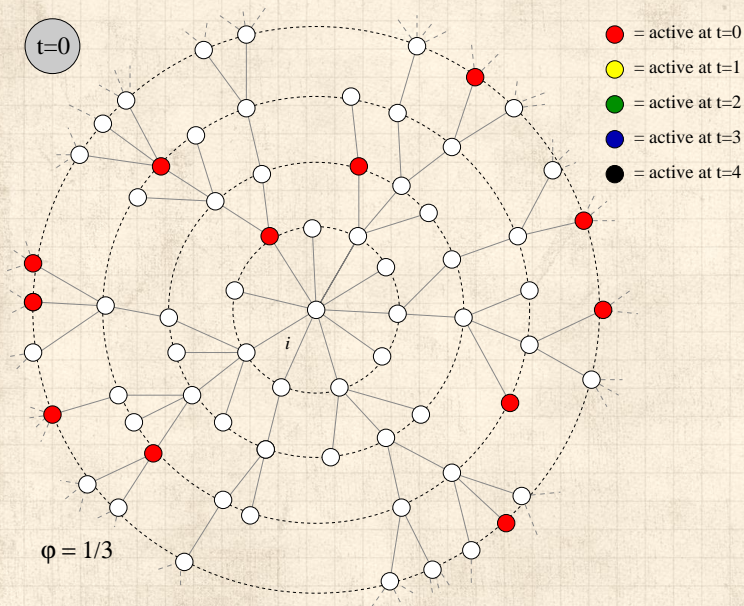
# Expected size of spread

The PoCSverse  
Social Contagion  
72 of 112

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References



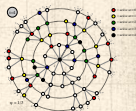
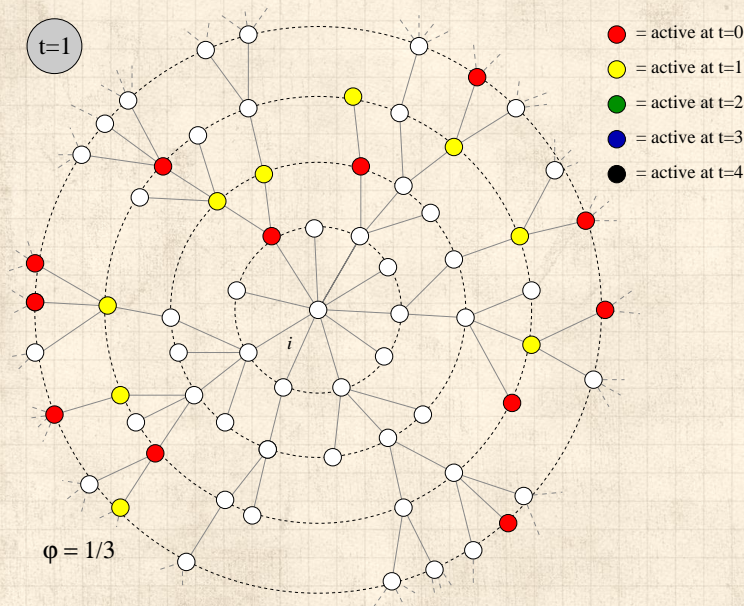


# Expected size of spread

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References



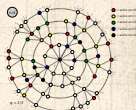
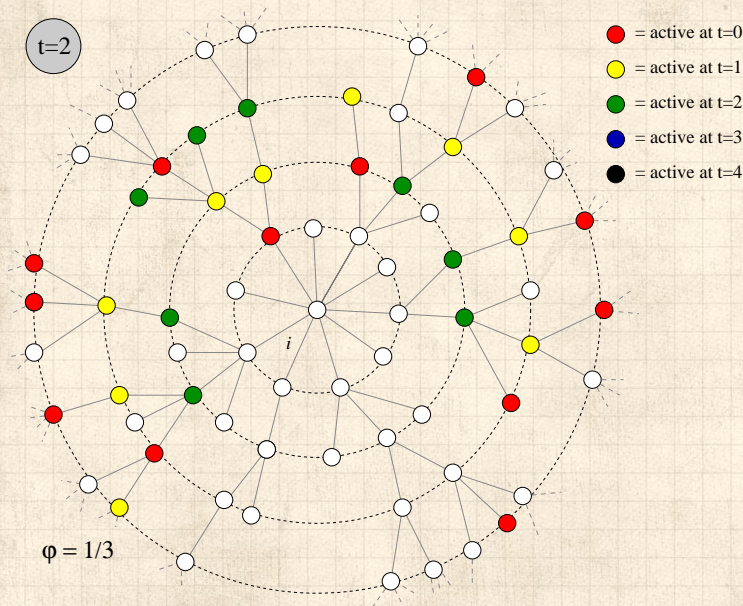
# Expected size of spread

The PoCSverse  
Social Contagion  
72 of 112

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References

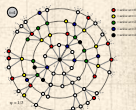
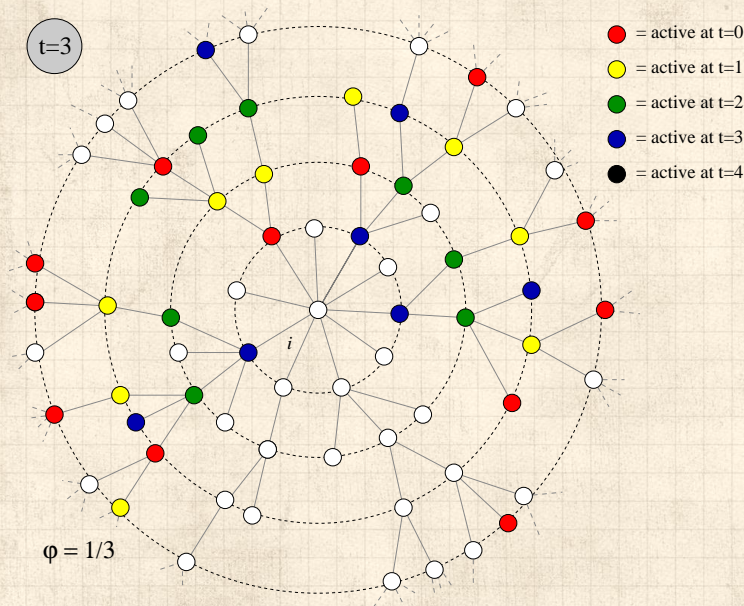


# Expected size of spread

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References

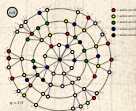
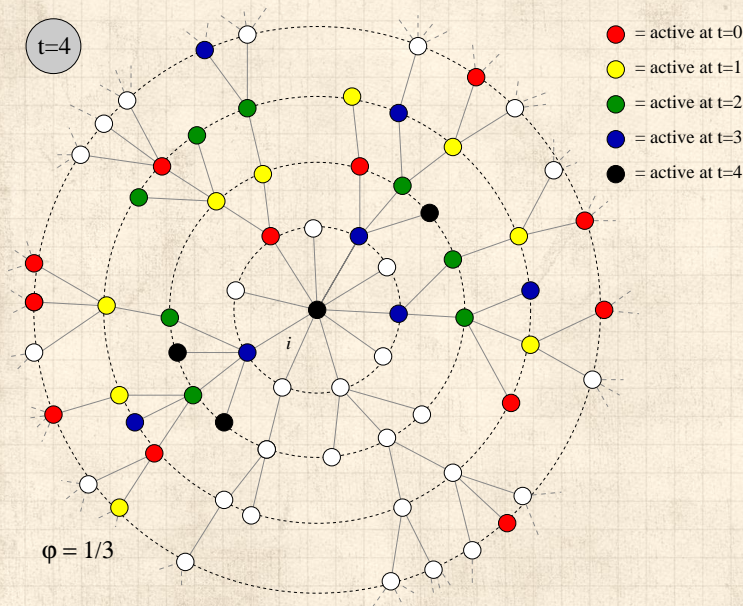


# Expected size of spread

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References



# Expected size of spread

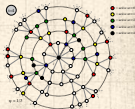
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References

### Notes:

- Calculations are possible if nodes do not become inactive (strong restriction).



# Expected size of spread

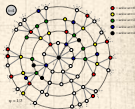
## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References

### Notes:

- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.



# Expected size of spread

The PoCSverse  
Social Contagion  
73 of 112

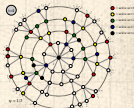
## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References

### Notes:

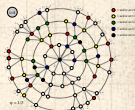
- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.
- We can analytically determine the entire time evolution, not just the final size.



# Expected size of spread

## Notes:

- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.
- We can analytically determine the entire time evolution, not just the final size.
- We can in fact determine **Pr**(node of degree  $k$  switching on at time  $t$ ).

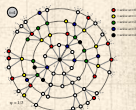




# Expected size of spread


## Notes:

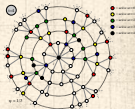
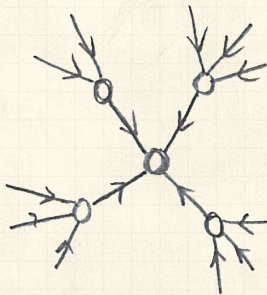
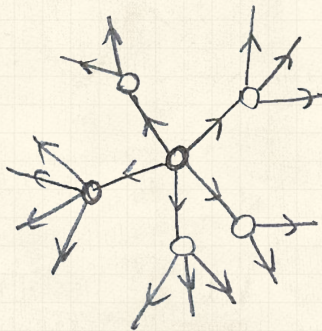
- Calculations are possible if nodes do not become inactive (strong restriction).
- Not just for threshold model—works for a wide range of contagion processes.
- We can analytically determine the entire time evolution, not just the final size.
- We can in fact determine **Pr**(node of degree  $k$  switching on at time  $t$ ).
- Asynchronous updating can be handled too.



# Expected size of spread

Pleasantness:

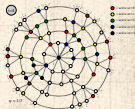
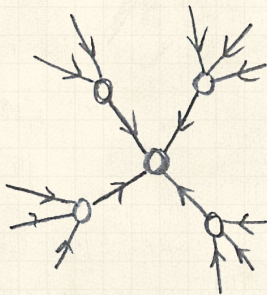
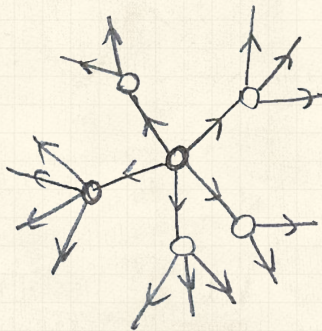
 Taking off from a single seed story is about **expansion** away from a node.



# Expected size of spread

## Pleasantness:

- Taking off from a single seed story is about **expansion** away from a node.
- Extent of spreading story is about **contraction** at a node.



# Expected size of spread



**Notation:**

$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).

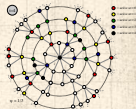
The PoCSverse  
Social Contagion  
75 of 112

Social Contagion  
Models

Background  
Granovetter's model  
Network version

Final size  
Spreading success  
Groups

References



# Expected size of spread

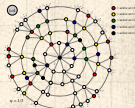


**Notation:**

$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).



**Notation:**  $B_{kj} = \mathbf{Pr}$  (a degree  $k$  node becomes active if  $j$  neighbors are active).



# Expected size of spread



**Notation:**

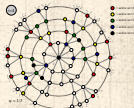
$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).



**Notation:**  $B_{kj} = \mathbf{Pr}$  (a degree  $k$  node becomes active if  $j$  neighbors are active).



Our starting point:  $\phi_{k,0} = \phi_0$ .



# Expected size of spread



**Notation:**

$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).



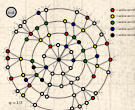
**Notation:**  $B_{kj} = \mathbf{Pr}$  (a degree  $k$  node becomes active if  $j$  neighbors are active).



Our starting point:  $\phi_{k,0} = \phi_0$ .



$\binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} = \mathbf{Pr}$  ( $j$  of a degree  $k$  node's neighbors were seeded at time  $t = 0$ ).



# Expected size of spread



**Notation:**

$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).



**Notation:**  $B_{kj} = \mathbf{Pr}$  (a degree  $k$  node becomes active if  $j$  neighbors are active).



Our starting point:  $\phi_{k,0} = \phi_0$ .



$\binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} = \mathbf{Pr}$  ( $j$  of a degree  $k$  node's neighbors were seeded at time  $t = 0$ ).

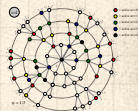


Probability a degree  $k$  node was a seed at  $t = 0$  is  $\phi_0$  (as above).

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References





# Expected size of spread



**Notation:**

$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).



**Notation:**  $B_{kj} = \mathbf{Pr}$  (a degree  $k$  node becomes active if  $j$  neighbors are active).



Our starting point:  $\phi_{k,0} = \phi_0$ .



$\binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} = \mathbf{Pr}$  ( $j$  of a degree  $k$  node's neighbors were seeded at time  $t = 0$ ).



Probability a degree  $k$  node was a seed at  $t = 0$  is  $\phi_0$  (as above).

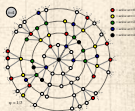


Probability a degree  $k$  node was not a seed at  $t = 0$  is  $(1 - \phi_0)$ .

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



# Expected size of spread



**Notation:**

$\phi_{k,t} = \mathbf{Pr}$ (a degree  $k$  node is active at time  $t$ ).



**Notation:**  $B_{kj} = \mathbf{Pr}$  (a degree  $k$  node becomes active if  $j$  neighbors are active).



Our starting point:  $\phi_{k,0} = \phi_0$ .



$\binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} = \mathbf{Pr}$  ( $j$  of a degree  $k$  node's neighbors were seeded at time  $t = 0$ ).



Probability a degree  $k$  node was a seed at  $t = 0$  is  $\phi_0$  (as above).



Probability a degree  $k$  node was not a seed at  $t = 0$  is  $(1 - \phi_0)$ .



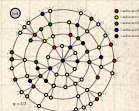
Combining everything, we have:


$$\phi_{k,1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^k \binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} B_{kj}.$$

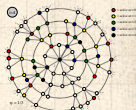
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



 For general  $t$ , we need to know the probability an edge coming into a degree  $k$  node at time  $t$  is active.



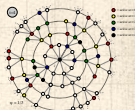
Social Contagion  
Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

References

For general  $t$ , we need to know the probability an edge coming into a degree  $k$  node at time  $t$  is active.

**Notation:** call this probability  $\theta_t$ .



Social Contagion  
Models

Background  
Granovetter's model  
Network version

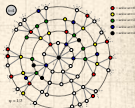
Final size  
Spreading success  
Groups

References

For general  $t$ , we need to know the probability an edge coming into a degree  $k$  node at time  $t$  is active.

**Notation:** call this probability  $\theta_t$ .

We already know  $\theta_0 = \phi_0$ .



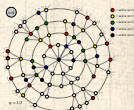
For general  $t$ , we need to know the probability an edge coming into a degree  $k$  node at time  $t$  is active.

**Notation:** call this probability  $\theta_t$ .

We already know  $\theta_0 = \phi_0$ .

Story analogous to  $t = 1$  case. For node  $i$ :

$$\phi_{i,t+1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^{k_i} \binom{k_i}{j} \theta_t^j (1 - \theta_t)^{k_i-j} B_{k_i j}.$$



For general  $t$ , we need to know the probability an edge coming into a degree  $k$  node at time  $t$  is active.

**Notation:** call this probability  $\theta_t$ .

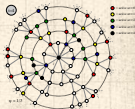
We already know  $\theta_0 = \phi_0$ .

Story analogous to  $t = 1$  case. For node  $i$ :

$$\phi_{i,t+1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^{k_i} \binom{k_i}{j} \theta_t^j (1 - \theta_t)^{k_i-j} B_{k_i j}.$$

Average over all nodes to obtain expression for  $\phi_{t+1}$ :

$$\phi_{t+1} = \phi_0 + (1 - \phi_0) \sum_{k=0}^{\infty} P_k \sum_{j=0}^k \binom{k}{j} \theta_t^j (1 - \theta_t)^{k-j} B_{k j}.$$



For general  $t$ , we need to know the probability an edge coming into a degree  $k$  node at time  $t$  is active.

**Notation:** call this probability  $\theta_t$ .

We already know  $\theta_0 = \phi_0$ .

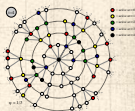
Story analogous to  $t = 1$  case. For node  $i$ :

$$\phi_{i,t+1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^{k_i} \binom{k_i}{j} \theta_t^j (1 - \theta_t)^{k_i-j} B_{k_i j}.$$

Average over all nodes to obtain expression for  $\phi_{t+1}$ :

$$\phi_{t+1} = \phi_0 + (1 - \phi_0) \sum_{k=0}^{\infty} P_k \sum_{j=0}^k \binom{k}{j} \theta_t^j (1 - \theta_t)^{k-j} B_{k j}.$$

So we need to compute  $\theta_t$ ...





For general  $t$ , we need to know the probability an edge coming into a degree  $k$  node at time  $t$  is active.

**Notation:** call this probability  $\theta_t$ .

We already know  $\theta_0 = \phi_0$ .

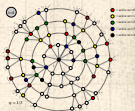
Story analogous to  $t = 1$  case. For node  $i$ :

$$\phi_{i,t+1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^{k_i} \binom{k_i}{j} \theta_t^j (1 - \theta_t)^{k_i-j} B_{k_i j}.$$

Average over all nodes to obtain expression for  $\phi_{t+1}$ :


$$\phi_{t+1} = \phi_0 + (1 - \phi_0) \sum_{k=0}^{\infty} P_k \sum_{j=0}^k \binom{k}{j} \theta_t^j (1 - \theta_t)^{k-j} B_{k j}.$$

So we need to compute  $\theta_t$ ... massive excitement...





# Expected size of spread


First connect  $\theta_0$  to  $\theta_1$ :

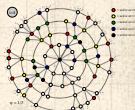
  $\theta_1 = \phi_0 +$

$$(1 - \phi_0) \sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_0^j (1 - \theta_0)^{k-1-j} B_{kj}$$

  $\frac{k P_k}{\langle k \rangle} = R_k = \mathbf{Pr}$  (edge connects to a degree  $k$  node).


  $\sum_{j=0}^{k-1}$  piece gives  $\mathbf{Pr}$ (degree node  $k$  activates) of its neighbors  $k - 1$  incoming neighbors are active.

  $\phi_0$  and  $(1 - \phi_0)$  terms account for state of node at time  $t = 0$ .





# Expected size of spread


First connect  $\theta_0$  to  $\theta_1$ :


  $\theta_1 = \phi_0 +$

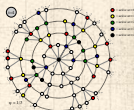
$$(1 - \phi_0) \sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_0^j (1 - \theta_0)^{k-1-j} B_{kj}$$

  $\frac{k P_k}{\langle k \rangle} = R_k = \mathbf{Pr}$  (edge connects to a degree  $k$  node).

  $\sum_{j=0}^{k-1}$  piece gives  $\mathbf{Pr}$ (degree node  $k$  activates) of its neighbors  $k - 1$  incoming neighbors are active.

  $\phi_0$  and  $(1 - \phi_0)$  terms account for state of node at time  $t = 0$ .

 See this all generalizes to give  $\theta_{t+1}$  in terms of  $\theta_t \dots$



# Expected size of spread

Two pieces: edges first, and then nodes

$$1. \theta_{t+1} = \underbrace{\phi_0}_{\text{exogenous}}$$

$$+(1 - \phi_0) \underbrace{\sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_t^j (1 - \theta_t)^{k-1-j} B_{kj}}_{\text{social effects}}$$

with  $\theta_0 = \phi_0$ .

$$2. \phi_{t+1} =$$

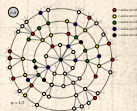
$$\underbrace{\phi_0}_{\text{exogenous}} + (1 - \phi_0) \underbrace{\sum_{k=0}^{\infty} P_k \sum_{j=0}^k \binom{k}{j} \theta_t^j (1 - \theta_t)^{k-j} B_{kj}}_{\text{social effects}}$$

Social Contagion  
Models

Background  
Granovetter's model  
Network version

Final size  
Spreading success  
Groups

References



# Expected size of spread

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

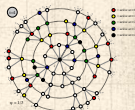
## References

Iterative map for  $\theta_t$  is key:


$$\theta_{t+1} = \underbrace{\phi_0}_{\text{exogenous}}$$

$$+(1 - \phi_0) \underbrace{\sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_t^j (1 - \theta_t)^{k-1-j} B_{kj}}_{\text{social effects}}$$

$$= G(\theta_t; \phi_0)$$



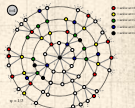
# Expected size of spread:

 Retrieve cascade condition for spreading from a single seed in limit  $\phi_0 \rightarrow 0$ .

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



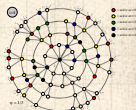
# Expected size of spread:

- Retrieve cascade condition for spreading from a single seed in limit  $\phi_0 \rightarrow 0$ .
- Depends on map  $\theta_{t+1} = G(\theta_t; \phi_0)$ .

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References

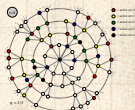


# Expected size of spread:

- Retrieve cascade condition for spreading from a single seed in limit  $\phi_0 \rightarrow 0$ .
- Depends on map  $\theta_{t+1} = G(\theta_t; \phi_0)$ .
- First: if self-starters are present, some activation is assured:

$$G(0; \phi_0) = \sum_{k=1}^{\infty} \frac{kP_k}{\langle k \rangle} \bullet B_{k0} > 0.$$

meaning  $B_{k0} > 0$  for at least one value of  $k \geq 1$ .





# Expected size of spread:

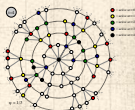
- Retrieve cascade condition for spreading from a single seed in limit  $\phi_0 \rightarrow 0$ .
- Depends on map  $\theta_{t+1} = G(\theta_t; \phi_0)$ .
- First: if self-starters are present, some activation is assured:

$$G(0; \phi_0) = \sum_{k=1}^{\infty} \frac{kP_k}{\langle k \rangle} \bullet B_{k0} > 0.$$

meaning  $B_{k0} > 0$  for at least one value of  $k \geq 1$ .


- If  $\theta = 0$  is a fixed point of  $G$  (i.e.,  $G(0; \phi_0) = 0$ ) then spreading occurs if

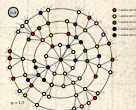
$$G'(0; \phi_0) = \sum_{k=0}^{\infty} \frac{kP_k}{\langle k \rangle} \bullet (k-1) \bullet B_{k1} > 1.$$



# Expected size of spread:

In words:

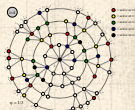
 If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.



# Expected size of spread:

In words:

- 🧱 If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.
- 🧱 If  $G$  has an **unstable fixed point** at  $\theta = 0$ , then cascades are also always possible.



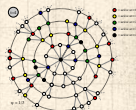
# Expected size of spread:

In words:

- 🧱 If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.
- 🧱 If  $G$  has an **unstable fixed point** at  $\theta = 0$ , then cascades are also always possible.

Non-vanishing seed case:

- 🧱 Cascade condition is more complicated for  $\phi_0 > 0$ .



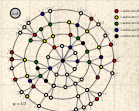
# Expected size of spread:

In words:

- 🧱 If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.
- 🧱 If  $G$  has an **unstable fixed point** at  $\theta = 0$ , then cascades are also always possible.

Non-vanishing seed case:

- 🧱 Cascade condition is more complicated for  $\phi_0 > 0$ .
- 🧱 If  $G$  has a **stable fixed point** at  $\theta = 0$ , and an **unstable fixed point** for some  $0 < \theta_* < 1$ , then for  $\theta_0 > \theta_*$ , spreading takes off.



# Expected size of spread:

## In words:

- 🧱 If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.
- 🧱 If  $G$  has an **unstable fixed point** at  $\theta = 0$ , then cascades are also always possible.

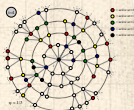
## Non-vanishing seed case:

- 🧱 Cascade condition is more complicated for  $\phi_0 > 0$ .
- 🧱 If  $G$  has a **stable fixed point** at  $\theta = 0$ , and an **unstable fixed point** for some  $0 < \theta_* < 1$ , then for  $\theta_0 > \theta_*$ , spreading takes off.
- 🧱 Tricky point:  $G$  depends on  $\phi_0$ , so as we change  $\phi_0$ , we also change  $G$ .

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References



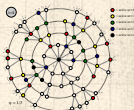
# Expected size of spread:

## In words:

- 🧱 If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.
- 🧱 If  $G$  has an **unstable fixed point** at  $\theta = 0$ , then cascades are also always possible.

## Non-vanishing seed case:

- 🧱 Cascade condition is more complicated for  $\phi_0 > 0$ .
- 🧱 If  $G$  has a **stable fixed point** at  $\theta = 0$ , and an **unstable fixed point** for some  $0 < \theta_* < 1$ , then for  $\theta_0 > \theta_*$ , spreading takes off.
- 🧱 Tricky point:  $G$  depends on  $\phi_0$ , so as we change  $\phi_0$ , we also change  $G$ .
- 🧱 A version of a critical mass model again.

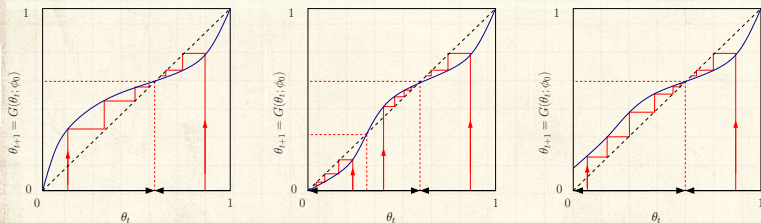



# General fixed point story:

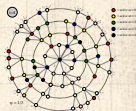
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups

## References



 Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.



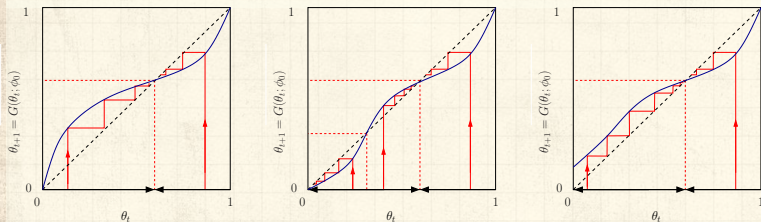



# General fixed point story:


## Social Contagion Models

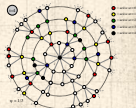
- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups

## References



 Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.

 n.b., adjacent fixed points must have opposite stability types.

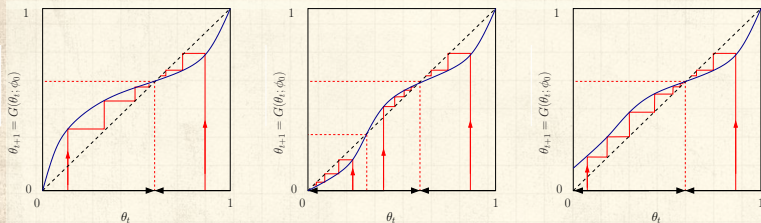


# General fixed point story:

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups

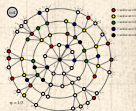
## References



Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.

n.b., adjacent fixed points must have opposite stability types.

**Important:** Actual form of  $G$  depends on  $\phi_0$ .

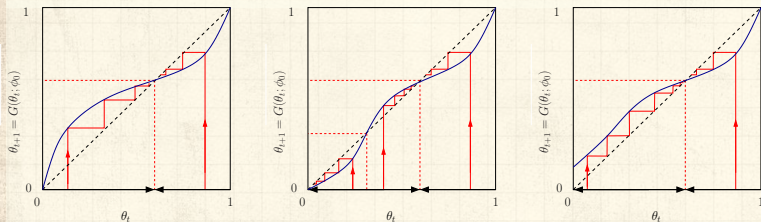



# General fixed point story:


## Social Contagion Models


- Background
- Granovetter's model
- Network version
- Final size**
- Spreading success
- Groups


## References

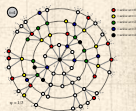


 Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.

 n.b., adjacent fixed points must have opposite stability types.

 **Important:** Actual form of  $G$  depends on  $\phi_0$ .

 So choice of  $\phi_0$  dictates both  $G$  and starting point—can't start anywhere for a given  $G$ .



# Outline

The PoCSverse  
Social Contagion  
83 of 112

## Social Contagion Models

Background

Granovetter's model

Network version

Final size

**Spreading success**

Groups

## Social Contagion Models

Background

Granovetter's model

Network version

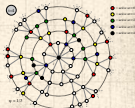
Final size

**Spreading success**

Groups

## References

## References



# Early adopters—degree distributions

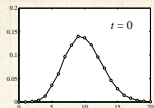
The PoCSverse  
Social Contagion  
84 of 112

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success**
- Groups

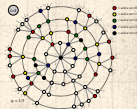
## References

$t = 0$



$P_{k,t}$  versus  $k$

Unpublished?



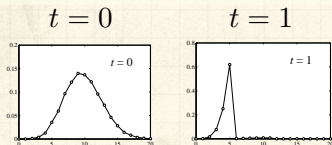
# Early adopters—degree distributions

The PoCSverse  
Social Contagion  
84 of 112

## Social Contagion Models

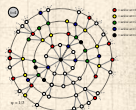
- Background
- Granovetter's model
- Network version
- Final size
- Spreading success**
- Groups

## References



$P_{k,t}$  versus  $k$

Unpublished?



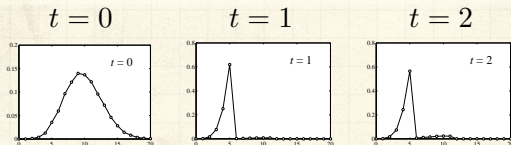
# Early adopters—degree distributions

The PoCSverse  
Social Contagion  
84 of 112

## Social Contagion Models

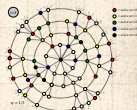
- Background
- Granovetter's model
- Network version
- Final size
- Spreading success**
- Groups

## References



$P_{k,t}$  versus  $k$

Unpublished?

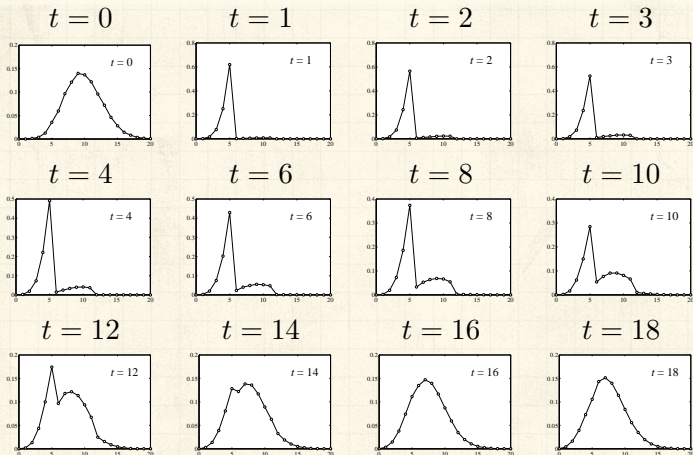


# Early adopters—degree distributions

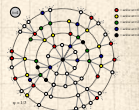
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success**
- Groups

## References



$P_{k,t}$  versus  $k$







Unpublished?

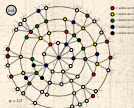




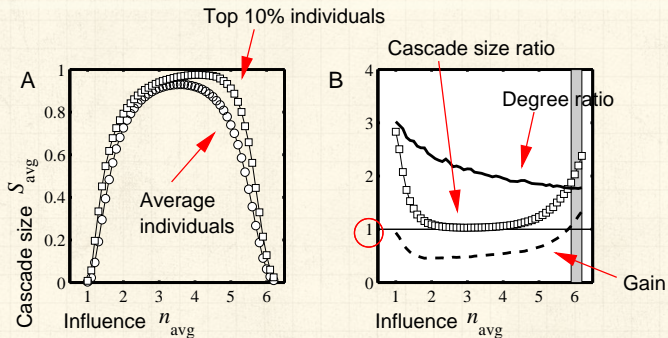
## "Influentials, Networks, and Public Opinion Formation"

Watts and Dodds,  
J. Consum. Res., **34**, 441–458, 2007. [28]

-  Exploration of threshold model of social contagion on various networks.
-  "Influentials" are limited in power.
-  Connected groups of weakly influential-vulnerable" individuals are key.
-  Average individuals can have more power than well connected ones.

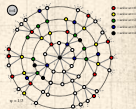


# The multiplier effect:



🧱 Fairly uniform levels of individual influence.

🧱 Multiplier effect is mostly below 1.

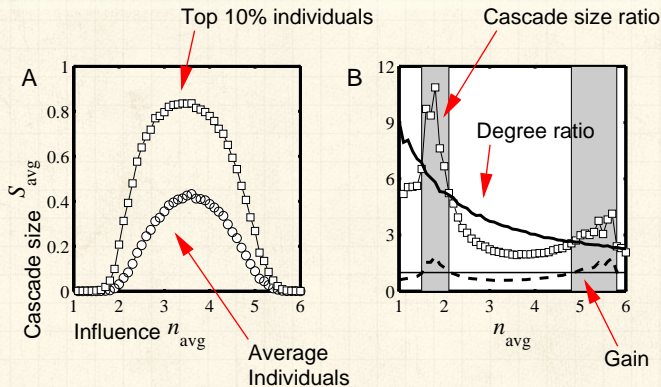


# The multiplier effect:

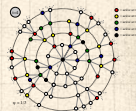
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



Skewed influence distribution example.



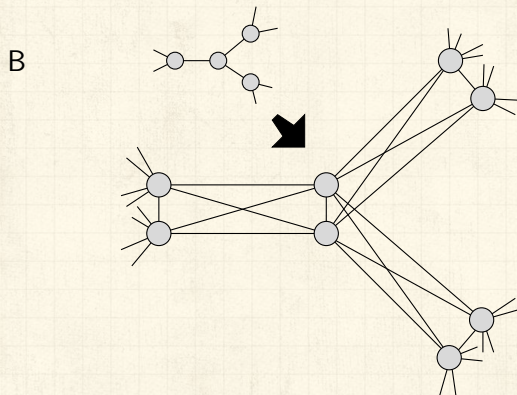
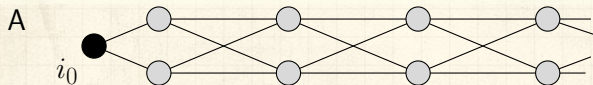
# Special subnetworks can act as triggers


The PoCSverse  
Social Contagion  
88 of 112

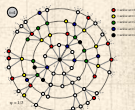
## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
**Spreading success**  
Groups

## References



  $\phi = 1/3$  for all nodes



# Outline

The PoCSverse  
Social Contagion  
89 of 112

## Social Contagion Models

Background

Granovetter's model

Network version

Final size

Spreading success

**Groups**

## Social Contagion Models

Background

Granovetter's model

Network version

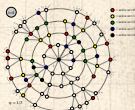
Final size

Spreading success


**Groups**

## References

## References



# The power of groups...



**TEAMWORK**

A FEW HARMLESS FLAKES WORKING TOGETHER CAN  
UNLEASH AN AVALANCHE OF DESTRUCTION.

[www.despair.com](http://www.despair.com)

[despair.com](http://despair.com)

The PoCSverse  
Social Contagion  
90 of 112

Social Contagion  
Models

Background

Granovetter's model

Network version

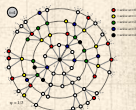
Final size

Spreading success

Groups

References

"A few harmless flakes working together can unleash an avalanche of destruction."

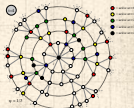





[“Threshold Models of Social Influence”](#) ↗  
Watts and Dodds,  
The Oxford Handbook of Analytical  
Sociology, **34**, 475–497, 2009. [29]



Assumption of sparse interactions is good





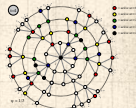
"Threshold Models of Social Influence"   
Watts and Dodds,  
The Oxford Handbook of Analytical  
Sociology, **34**, 475–497, 2009. <sup>[29]</sup>



Assumption of sparse interactions is good







Degree distribution is (generally) key to a  
network's function

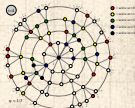











"Threshold Models of Social Influence"   
Watts and Dodds,  
The Oxford Handbook of Analytical  
Sociology, **34**, 475–497, 2009. <sup>[29]</sup>

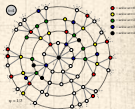
-  Assumption of sparse interactions is good
-  Degree distribution is (generally) key to a network's function
-  Still, random networks don't represent all networks





"Threshold Models of Social Influence"   
Watts and Dodds,  
The Oxford Handbook of Analytical  
Sociology, **34**, 475–497, 2009. <sup>[29]</sup>

-  Assumption of sparse interactions is good
-  Degree distribution is (generally) key to a network's function
-  Still, random networks don't represent all networks
-  Major element missing: **group structure**



# Group structure—Ramified random networks

The PoCSverse  
Social Contagion  
92 of 112

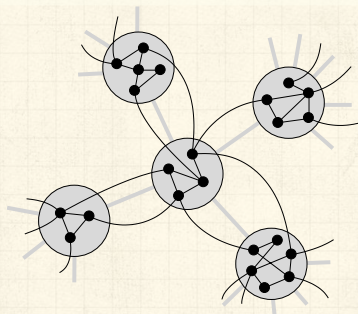
Social Contagion  
Models

Background  
Granovetter's model  
Network version  
Final size

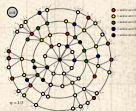
Spreading success

Groups

References



$p$  = intergroup connection probability  
 $q$  = intragroup connection probability.

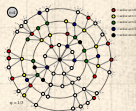
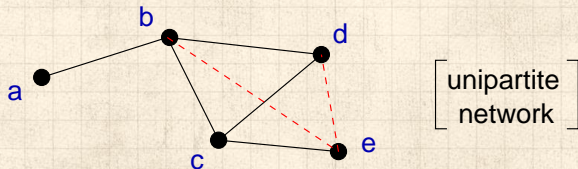
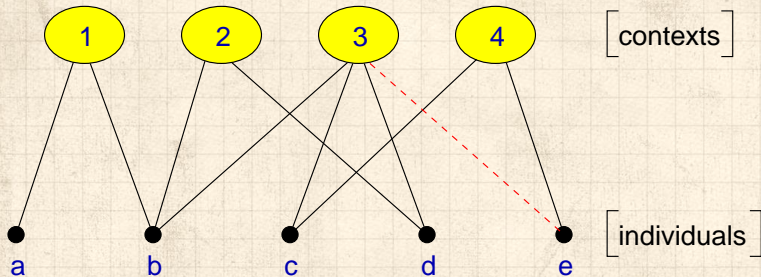


# Bipartite networks

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups
- 

References

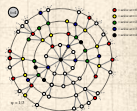
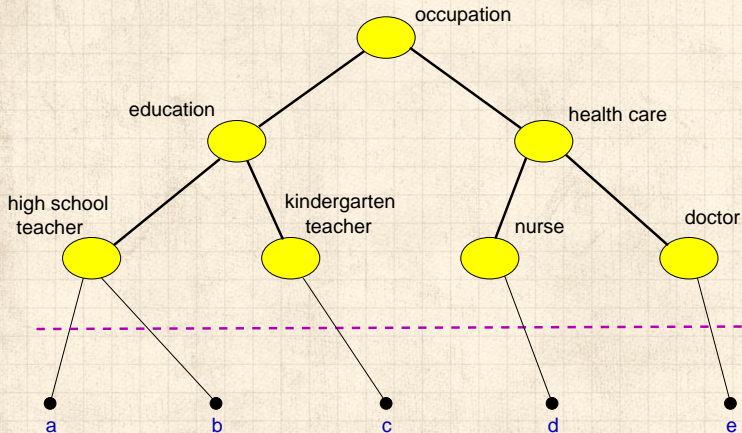


# Context distance

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References

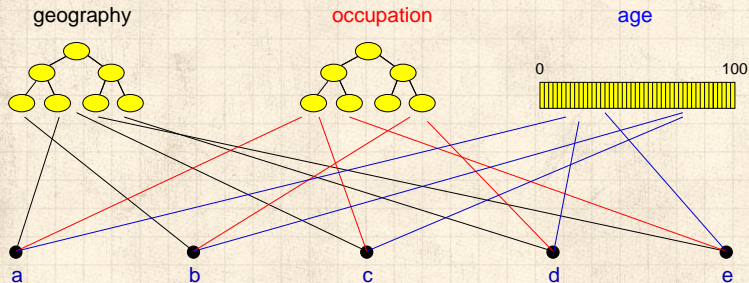


# Generalized affiliation model

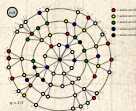
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



(Blau & Schwartz, Simmel, Breiger)



# Generalized affiliation model networks with triadic closure

The PoCSverse  
Social Contagion  
96 of 112

Social Contagion  
Models

Background  
Granovetter's model  
Network version  
Final size

Spreading success  
Groups

References



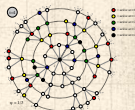
Connect nodes with probability  $\propto e^{-\alpha d}$

where

$\alpha$  = homophily parameter

and

$d$  = distance between nodes (height of lowest common ancestor)



# Generalized affiliation model networks with triadic closure



Connect nodes with probability  $\propto e^{-\alpha d}$

where

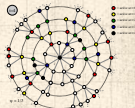
$\alpha$  = homophily parameter

and

$d$  = distance between nodes (height of lowest common ancestor)



$\tau_1$  = intergroup probability of friend-of-friend connection





# Generalized affiliation model networks with triadic closure



Connect nodes with probability  $\propto e^{-\alpha d}$

where

$\alpha$  = homophily parameter

and

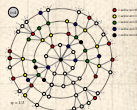
$d$  = distance between nodes (height of lowest common ancestor)



$\tau_1$  = intergroup probability of friend-of-friend connection



$\tau_2$  = intragroup probability of friend-of-friend connection

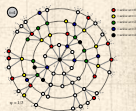
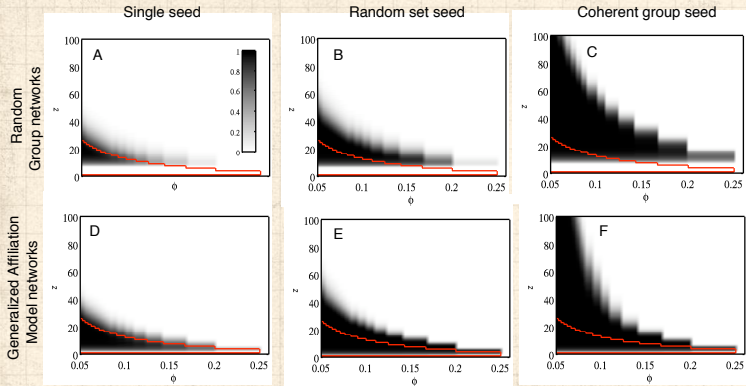


# Cascade windows for group-based networks

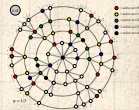
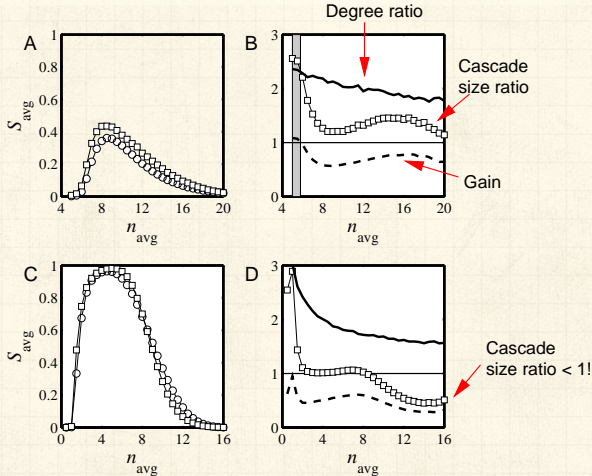
## Social Contagion Models


- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups
- 

## References



# Multiplier effect for group-based networks:



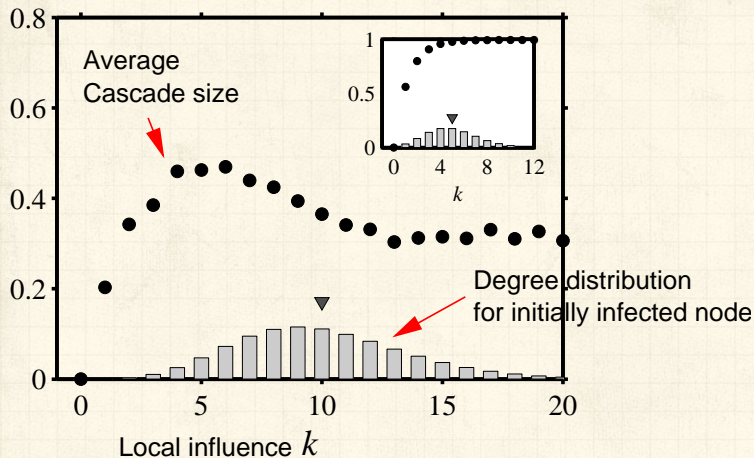
 Multiplier almost always below 1.


# Assortativity in group-based networks

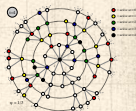
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



 The most connected nodes aren't always the most 'influential.'

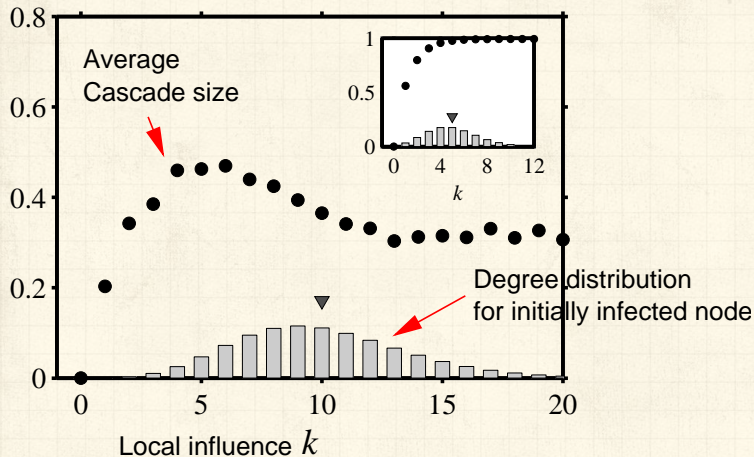



# Assortativity in group-based networks

## Social Contagion Models

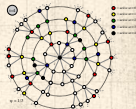
- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References



 The most connected nodes aren't always the most 'influential.'

 Degree assortativity is the reason.



# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

## Summary

 **'Influential vulnerables'** are key to spread.

The PoCSverse  
Social Contagion  
100 of 112

Social Contagion  
Models

Background

Granovetter's model

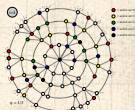
Network version

Final size

Spreading success

Groups


References




# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

## Summary

 **'Influential vulnerables'** are key to spread.

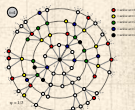
 Early adopters are mostly vulnerables.

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success

### Groups

References



# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

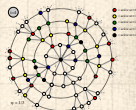
## Summary

- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups**

## References





# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

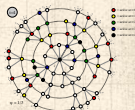
## Summary

- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.
- 🧱 Groups may greatly facilitate spread.

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups**

## References



# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

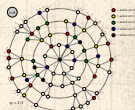
## Summary

- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.
- 🧱 Groups may greatly facilitate spread.
- 🧱 Seems that cascade condition is a global one.

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups**

## References



# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

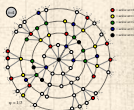
## Summary

- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.
- 🧱 Groups may greatly facilitate spread.
- 🧱 Seems that cascade condition is a global one.
- 🧱 Most extreme/unexpected cascades occur in highly connected networks

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

## References



# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

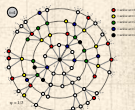
## Summary

- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.
- 🧱 Groups may greatly facilitate spread.
- 🧱 Seems that cascade condition is a global one.
- 🧱 Most extreme/unexpected cascades occur in highly connected networks
- 🧱 'Influentials' are posterior constructs.

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success

## References



# Social contagion

“Without followers, evil cannot spread.” –Leonard Nimoy

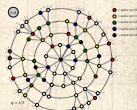
## Summary

- 🧱 **'Influential vulnerables'** are key to spread.
- 🧱 Early adopters are mostly vulnerables.
- 🧱 Vulnerable nodes important but not necessary.
- 🧱 Groups may greatly facilitate spread.
- 🧱 Seems that cascade condition is a global one.
- 🧱 Most extreme/unexpected cascades occur in highly connected networks
- 🧱 'Influentials' are posterior constructs.
- 🧱 Many potential influentials exist.

## Social Contagion Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success

## References



# Social contagion

The PoCSverse  
Social Contagion  
101 of 112

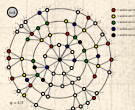
## Implications

 Focus on the influential vulnerables.

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups**

## References



# Social contagion

The PoCSverse  
Social Contagion  
101 of 112

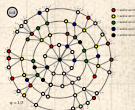
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References

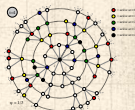
## Implications

- Focus on the influential vulnerables.
- Create entities that can be transmitted successfully through many individuals rather than broadcast from one 'influential.'



## Implications

- Focus on **the influential vulnerables**.
- Create entities that can be transmitted successfully through many individuals rather than broadcast from one 'influential.'
- Only **simple ideas** can spread by word-of-mouth.  
(Idea of opinion leaders spreads well...)





# Social contagion

The PoCSverse  
Social Contagion  
101 of 112

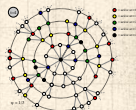
Social Contagion  
Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success

-----  
Groups  
References

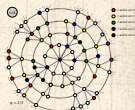
## Implications

- Focus on **the influential vulnerables**.
- Create entities that can be transmitted successfully through many individuals rather than broadcast from one 'influential.'
- Only **simple ideas** can spread by word-of-mouth.  
(Idea of opinion leaders spreads well...)
- Want enough individuals who will adopt and display.



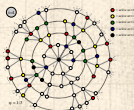
## Implications

- Focus on **the influential vulnerables**.
- Create entities that can be transmitted successfully through many individuals rather than broadcast from one 'influential.'
- Only **simple ideas** can spread by word-of-mouth.  
(Idea of opinion leaders spreads well...)
- Want enough individuals who will adopt and display.
- Displaying can be **passive** = free (yo-yo's, fashion), or **active** = harder to achieve (political messages).



## Implications

- Focus on **the influential vulnerables**.
- Create entities that can be transmitted successfully through many individuals rather than broadcast from one 'influential.'
- Only **simple ideas** can spread by word-of-mouth.  
(Idea of opinion leaders spreads well...)
- Want enough individuals who will adopt and display.
- Displaying can be **passive** = free (yo-yo's, fashion), or **active** = harder to achieve (political messages).
- Entities can be novel or designed to combine with others, e.g. block another one.



# Spreading and unspreading: Empires

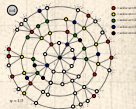
## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success


### ----- Groups

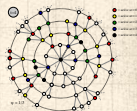
## References

<http://www.youtube.com/watch?v=FEaCflp9qR4?rel=0>






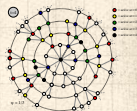
# References I



- [1] A. Bentley, M. Earls, and M. J. O'Brien.  
I'll Have What She's Having: Mapping Social Behavior.  
MIT Press, Cambridge, MA, 2011.
- [2] S. Bikhchandani, D. Hirshleifer, and I. Welch.  
A theory of fads, fashion, custom, and cultural change as informational cascades.  
J. Polit. Econ., 100:992–1026, 1992.
- [3] S. Bikhchandani, D. Hirshleifer, and I. Welch.  
Learning from the behavior of others:  
Conformity, fads, and informational cascades.  
J. Econ. Perspect., 12(3):151–170, 1998. pdf 

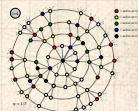


# References II

- [4] J. M. Carlson and J. Doyle.  
Highly optimized tolerance: A mechanism for  
power laws in designed systems.  
[Phys. Rev. E, 60\(2\):1412–1427, 1999. pdf](#) 
- [5] J. M. Carlson and J. Doyle.  
Highly optimized tolerance: Robustness and  
design in complex systems.  
[Phys. Rev. Lett., 84\(11\):2529–2532, 2000. pdf](#) 
- [6] N. A. Christakis and J. H. Fowler.  
The spread of obesity in a large social network  
over 32 years.  
[New England Journal of Medicine, 357:370–379,  
2007. pdf](#) 



- [7] N. A. Christakis and J. H. Fowler.  
The collective dynamics of smoking in a large  
social network.  
[New England Journal of Medicine, 358:2249–2258,  
2008. pdf](#) 
- [8] R. B. Cialdini.  
[Influence: Science and Practice.](#)  
Allyn and Bacon, Boston, MA, 4th edition, 2000.
- [9] P. S. Dodds, K. D. Harris, and C. M. Danforth.  
Limited Imitation Contagion on random networks:  
Chaos, universality, and unpredictability.  
[Phys. Rev. Lett., 110:158701, 2013. pdf](#) 



# References IV

- [10] P. S. Dodds, K. D. Harris, and J. L. Payne.  
Direct, physically motivated derivation of the  
contagion condition for spreading processes on  
generalized random networks.

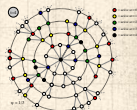
[Phys. Rev. E, 83:056122, 2011. pdf](#)

- [11] J. H. Fowler and N. A. Christakis.  
Dynamic spread of happiness in a large social  
network: longitudinal analysis over 20 years in  
the Framingham Heart Study.

[BMJ, 337:article #2338, 2008. pdf](#)

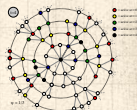
- [12] M. Gladwell.  
The Tipping Point.

[Little, Brown and Company, New York, 2000.](#)






- [13] J. P. Gleeson.  
Cascades on correlated and modular random networks.  
[Phys. Rev. E, 77:046117, 2008. pdf](#)
- [14] J. P. Gleeson and D. J. Cahalane.  
Seed size strongly affects cascades on random networks.  
[Phys. Rev. E, 75:056103, 2007. pdf](#)
- [15] M. Granovetter.  
Threshold models of collective behavior.  
[Am. J. Sociol., 83\(6\):1420–1443, 1978. pdf](#)




# References VI


- [16] M. Granovetter and R. Soong.  
Threshold models of diversity: Chinese  
restaurants, residential segregation, and the  
spiral of silence.

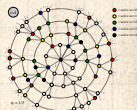
[Sociological Methodology, 18:69–104, 1988. pdf](#) 

- [17] M. S. Granovetter and R. Soong.  
Threshold models of interpersonal effects in  
consumer demand.


[J. Econ. Behav. Organ., 7:83–99, 1986. pdf](#) 

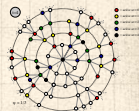
- [18] K. D. Harris, C. M. Danforth, and P. S. Dodds.  
Dynamical influence processes on networks:  
General theory and applications to social  
contagion.

[Phys. Rev. E, 88:022816, 2013. pdf](#) 





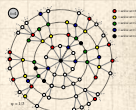
## References VII

- [19] E. Katz and P. F. Lazarsfeld.  
Personal Influence.  
The Free Press, New York, 1955.
- [20] T. Kuran.  
Now out of never: The element of surprise in the  
east european revolution of 1989.  
World Politics, 44:7-48, 1991. [pdf](#) 
- [21] T. Kuran.  
Private Truths, Public Lies: The Social  
Consequences of Preference Falsification.  
Harvard University Press, Cambridge, MA, Reprint  
edition, 1997.
- [22] T. Pratchett.  
The Truth.  
HarperCollins, 2000.



# References VIII

- [23] T. C. Schelling.  
Dynamic models of segregation.  
[J. Math. Sociol.](#), 1:143–186, 1971. [pdf](#) 
- [24] T. C. Schelling.  
Hockey helmets, concealed weapons, and  
daylight saving: A study of binary choices with  
externalities.  
[J. Conflict Resolut.](#), 17:381–428, 1973. [pdf](#) 
- [25] T. C. Schelling.  
[Micromotives and Macrobehavior.](#)  
Norton, New York, 1978.
- [26] D. Sornette.  
[Critical Phenomena in Natural Sciences.](#)  
Springer-Verlag, Berlin, 1st edition, 2003.



# References IX

[27] D. J. Watts.

A simple model of global cascades on random networks.

[Proc. Natl. Acad. Sci., 99\(9\):5766–5771, 2002.](#)

[pdf](#) 

[28] D. J. Watts and P. S. Dodds.


Influentials, networks, and public opinion formation.

[Journal of Consumer Research, 34:441–458, 2007.](#)

[pdf](#) 

[29] D. J. Watts and P. S. Dodds.

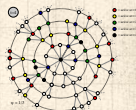
Threshold models of social influence.

In P. Hedström and P. Bearman, editors, [The Oxford Handbook of Analytical Sociology](#), chapter 20, pages 475–497. Oxford University Press, Oxford, UK, 2009. [pdf](#) 

Social Contagion  
Models

Background  
Granovetter's model  
Network version  
Final size  
Spreading success  
Groups

[References](#)



# References X

The PoCSverse  
Social Contagion  
112 of 112

## Social Contagion Models

- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

## References

