Mechanisms for Generating Power-Law Size Distributions, Part 3

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Principles of Complex Systems, Vols. 1, 2, & 3D CSYS/MATH 300, 303, & 394, 2022-2023 | @pocsvox

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Outline

Rich-Get-Richer Mechanism

Simon's Model **Analysis** Words Catchphrases First Mover Advantage

References

Aggregation:

- Random walks represent additive aggregation
- Mechanism: Random addition and subtraction
- & Compare across realizations, no competition.
- Next: Random Additive/Copying Processes involving Competition.
- Widespread: Words, Cities, the Web, Wealth, Productivity (Lotka), Popularity (Books, People, ...)
- Competing mechanisms (trickiness)

Pre-Zipf's law observations of Zipf's law @pocsvox Power-Law

Rich-Get-Richer Mechanism Words

References

Mechanisms, Pt. 3

- 🚳 1910s: Word frequency examined re Stenography

 ☐ (or shorthand or brachygraphy or tachygraphy), Jean-Baptiste Estoup [6].
- ♣ 1910s: Felix Auerbach pointed out the Zipfitude of city sizes in
 - "Das Gesetz der Bevölkerungskonzentration" ("The Law of Population Concentration") [1].
- 1924: G. Udny Yule [15]:

Theoretical Work of Yore:

- # Species per Genus (offers first theoretical mechanism)
- 4 1926: Lotka [9]:
 - # Scientific papers per author (Lotka's law)

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References

- 3 1949: Zipf's "Human Behaviour and the Principle of Least-Effort" is published. [16]
- 1953: Mandelbrot [10]: Optimality argument for Zipf's law; focus on language.
- 4 1955: Herbert Simon [14, 16]: Zipf's law for word frequency, city size, income, publications, and species per genus.
- 1965/1976: Derek de Solla Price [4, 13]: Network of Scientific Citations.
- 4 1999: Barabasi and Albert [2]: The World Wide Web, networks-at-large.

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Political scientist (and much more)

Involved in Cognitive Psychology, Computer Science, Public Administration, Economics, Management, Sociology

Herbert Simon 🗗 (1916–2001):

- Coined 'bounded rationality' and 'satisficing'
- Nearly 1000 publications (see Google Scholar
 ♂)
- An early leader in Artificial Intelligence, Information Processing, Decision-Making, Problem-Solving, Attention Economics, Organization Theory, Complex Systems, And Computer Simulation Of Scientific Discovery.
- 4 1978 Nobel Laureate in Economics (his Nobel bio is here \square).

Essential Extract of a Growth Model: @pocsvox Power-Law

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Random Competitive Replication (RCR):

- 1. Start with 1 elephant (or element) of a particular flavor at t=1
- 2. At time t = 2, 3, 4, ..., add a new elephant in one of two ways:
 - \bigcirc With probability ρ , create a new elephant with a new flavor
 - = Mutation/Innovation
 - With probability 1ρ , randomly choose from all existing elephants, and make a copy.
 - = Replication/Imitation
 - Elephants of the same flavor form a group



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Random Competitive Replication:

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Example: Words appearing in a language

- Consider words as they appear sequentially.
- \aleph With probability ρ , the next word has not previously appeared
 - = Mutation/Innovation
- \mathbb{A} With probability $1-\rho$, randomly choose one word from all words that have come before, and reuse this word
 - = Replication/Imitation

Note: This is a terrible way to write a novel.



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For example:



- . 21 words used
- · next word 13 new with prob p
- · next word is a copy with prob 1-P next word : prob: 6/21 ook 4/21 the and 3/21 2/21 penguin library

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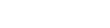
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Some observations:

- Fundamental Rich-get-Richer story;
- Competition for replication between individual elephants is random;
- & Competition for growth between groups of matching elephants is not random;
- Selection on groups is biased by size;
- Random selection sounds easy;
- Possible that no great knowledge of system needed (but more later ...).

Your free set of tofu knives:

- Related to Pólya's Urn Model , a special case of problems involving urns and colored balls .
- Sampling with super-duper replacement and sneaky sneaking in of new colors.

Random Competitive Replication:

Some observations:

- Steady growth of system: +1 elephant per unit time.
- Steady growth of distinct flavors at rate ρ
- & We can incorporate

-Economy-

1. Elephant elimination

Ch. 3: An Urban Mystery, p. 46

distribution should be ..."1, 2

- 2. Elephants moving between groups
- 3. Variable innovation rate ρ
- 4. Different selection based on group size (But mechanism for selection is not as simple...)

"The Self-Organizing Economy" 🚨 🗹

by Paul Krugman (1996). [8]

"...Simon showed—in a completely impenetrable

exposition!—that the exponent of the power law

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Random Competitive Replication:

Definitions:

& k_i = size of a group i

 \aleph $N_{k,t}$ = # groups containing k elephants at time t.

Basic question: How does $N_{k,t}$ evolve with time?

Random Competitive Replication:

 $\Longrightarrow kN_{k-t}$ elephants in size k groups

Random Competitive Replication:

 $N_{k,t}$, the number of groups with k elephants,

Happens with probability $(1-\rho)kN_{k-t}/t$

2. An elephant belonging to a group with k-1

1. An elephant belonging to a group with k elephants

Happens with probability $(1-\rho)(k-1)N_{k-1-t}/t$

belongs to a group of size k:

 N_{k} size k groups

& t elephants overall

changes at time t if

is replicated:

 $N_{k,t+1} = N_{k,t} - 1$

 $N_{k,t+1} = N_{k,t} + 1$

elephants is replicated:

 $P_k(t)$ = Probability of choosing an elephant that

 $P_k(t) = \frac{kN_{k,t}}{t}$.

First:
$$\sum_k k N_{k,\,t} = t = \text{number of elephants}$$
 at time t



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Random Competitive Replication:

Special case for $N_{1,t}$:

- 1. The new elephant is a new flavor: $N_{1,t+1} = N_{1,t} + 1$ Happens with probability ρ
- 2. A unique elephant is replicated:

 $N_{1,t+1} = N_{1,t} - 1$ Happens with probability $(1-\rho)N_{1-t}/t$



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Random Competitive Replication:

Putting everything together: For k > 1:

 $\left\langle N_{k,\,t+1}-N_{k,\,t}\right\rangle = (1-\rho)\left(\frac{(+1)(k-1)\frac{N_{k-1,\,t}}{t}+(-1)k\frac{N_{k,\,t}}{t}}{t}\right)^{\text{Cantiphrason interferences}} element + \frac{N_{k,\,t}}{t}$

For k = 1:

$$\langle N_{1,t+1} - N_{1,t} \rangle = (+1)\rho + (-1)(1-\rho)1 \cdot \frac{N_{1,t}}{t}$$



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Analysis Catchphrases

Random Competitive Replication:

Assume distribution stabilizes: $N_{k,t} = n_k t$ (Reasonable for t large)

- Drop expectations
- Numbers of elephants now fractional
- Okay over large time scales
- \clubsuit For later: the fraction of groups that have size k is n_k/ρ since

$$\frac{N_{k,t}}{\rho t} = \frac{n_k t}{\rho t} = \frac{n_k}{\rho}$$



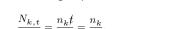
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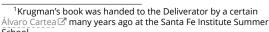
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²Let's use π for probability because π 's not special, right guys?



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Random Competitive Replication:

Stochastic difference equation:

$$\left\langle N_{k,\,t+1}-N_{k,\,t}\right\rangle = (1-\rho)\left((k-1)\frac{N_{k-1,\,t}}{t}-k\frac{N_{k,\,t}}{t}\right)$$

becomes

$$n_k(t+1)-n_kt=(1-\rho)\left((k-1)\frac{n_{k-1}t}{t}-k\frac{n_kt}{t}\right)$$

$$n_k({\color{red} t}+1-{\color{red} t}) = (1-\rho)\left((k-1)\frac{n_{k-1}{\color{red} t}}{\color{red} t} - k\frac{n_k{\color{red} t}}{\color{red} t}\right)$$

$$\Rightarrow n_k = (1-\rho)\left((k-1)n_{k-1} - kn_k\right)$$

$$\Rightarrow n_k \left(1 + \textcolor{red}{(1-\rho)k}\right) = (1-\rho)(k-1)n_{k-1}$$

Random Competitive Replication:

We have a simple recursion:

$$\frac{n_k}{n_{k-1}} = \frac{(k-1)(1-\rho)}{1+(1-\rho)k}$$

- Interested in k large (the tail of the distribution)
- Can be solved exactly.

Insert question from assignment 4 2

& For just the tail: Expand as a series of powers of 1/k

Insert question from assignment 4 2

We (okay, you) find

$$n_k \propto k^{-\frac{(2-\rho)}{(1-\rho)}} = k^{-\gamma}$$

$$\gamma = \frac{(2-\rho)}{(1-\rho)} = 1 + \frac{1}{(1-\rho)}$$

& Micro-to-Macro story with ρ and γ measurable.

$$\gamma = \frac{(2-\rho)}{(1-\rho)} = 1 + \frac{1}{(1-\rho)}$$

- \Leftrightarrow Observe $2 < \gamma < \infty$ for $0 < \rho < 1$.
- A For $\rho \simeq 0$ (low innovation rate):

$$\gamma \simeq 2$$

- & 'Wild' power-law size distribution of group sizes, bordering on 'infinite' mean.
- & For $\rho \simeq 1$ (high innovation rate):

$$\gamma \simeq \infty$$

- All elephants have different flavors.
- Upshot: Tunable mechanism producing a family of universality classes.

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- A Recall Zipf's law: $s_m \sim r^{-\alpha}$ (s_r = size of the rth largest group of elephants)
- \clubsuit We found $\alpha = 1/(\gamma 1)$ so:

$$\alpha = \frac{1}{\gamma - 1} = \frac{1}{1 + \frac{1}{(1 - \rho)} - 1} = 1 - \rho.$$

- $\gamma = 2$ corresponds to $\alpha = 1$
- & We (roughly) see Zipfian exponent [16] of $\alpha = 1$ for many real systems: city sizes, word distributions,
- & Corresponds to $\rho \to 0$, low innovation.
- Still, other guite different mechanisms are
- Must look at the details to see if mechanism makes sense... more later.

What about small k?:

We had one other equation:



$$\left\langle N_{1,t+1} - N_{1,t} \right\rangle = \rho - (1-\rho)1 \cdot \frac{N_{1,t}}{t}$$

- As before, set $N_{1,t} = n_1 t$ and drop expectations

$$n_1(t+1)-n_1t=\rho-(1-\rho)1\cdot\frac{n_1t}{t}$$

$$n_1 = \rho - (1-\rho)n_1$$

Rearrange:

$$n_1 + (1-\rho)n_1 = \rho$$



$$n_1 = \frac{\rho}{2 - \rho}$$

So...
$$N_{1,t} = n_1 t = \frac{\rho t}{2 - \rho}$$

- Recall number of distinct elephants = ρt .
- Fraction of distinct elephants that are unique (belong to groups of size 1):

$$\frac{1}{\rho t} N_{1,t} = \frac{1}{\rho t} \frac{\rho t}{2 - \rho} = \frac{1}{2 - \rho}$$

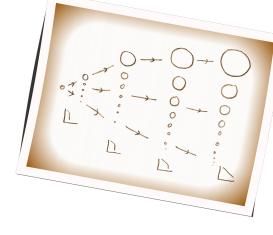
(also = fraction of groups of size 1)

- $\ref{harmonic}$ For ho small, fraction of unique elephants $\sim 1/2$
- Roughly observed for real distributions
- Can show fraction of groups with two elephants

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Estimate $\rho_{est} = \#$ unique words/# all words

For Joyce's Ulysses: $\rho_{\rm est} \simeq 0.115$

N_1 (real)	N_1 (est)	N_2 (real)	N_2 (est)	
16,432	15,850	4,776	4,870	

Words:

From Simon [14]:

N_1 (real)	N_1 (est)	N_2 (real)	N_2 (est)
16,432	15,850	4,776	4,870



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From Simon's introduction:

Evolution of catch phrases:

& Yule's paper (1924) [15]:

Simon's paper (1955) [14]:

It is the purpose of this paper to analyse a class of distribution functions that appear in a wide range of empirical data—particularly data describing sociological, biological and economic phenomena.

conclusions of Dr J. C. Willis, F.R.S."

"A mathematical theory of evolution, based on the

"On a class of skew distribution functions" (snore)

Its appearance is so frequent, and the phenomena so diverse, that one is led to conjecture that if these phenomena have any property in common it can only be a similarity in the structure of the underlying probability mechanisms.



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Evolution of catch phrases:

Derek de Solla Price:

- First to study network evolution with these kinds of models.
- & Citation network of scientific papers
- Price's term: Cumulative Advantage
- Idea: papers receive new citations with probability proportional to their existing # of citations
- Directed network
- Two (surmountable) problems:
 - 1. New papers have no citations
 - 2. Selection mechanism is more complicated

Evolution of catch phrases:

Robert K. Merton: the Matthew Effect

Studied careers of scientists and found credit flowed disproportionately to the already famous

From the Gospel of Matthew:

"For to every one that hath shall be given... (Wait! There's more....)

but from him that hath not, that also which he seemeth to have shall be taken away. And cast the worthless servant into the outer darkness; there men will weep and gnash their

- (Hath = suggested unit of purchasing power.)
- A Matilda effect: Women's scientific achievements are often overlooked

Evolution of catch phrases:

Merton was a catchphrase machine:

- 1. Self-fulfilling prophecy
- 2. Role model
- 3. Unintended (or unanticipated) consequences
- 4. Focused interview \rightarrow focus group
- 5. Obliteration by incorporation **(includes above**) examples from Merton himself)

And just to be clear...

Merton's son, Robert C. Merton, won the Nobel Prize for Economics in 1997.

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- Barabasi and Albert [2]—thinking about the Web
- Independent reinvention of a version of Simon and Price's theory for networks
- Another term: "Preferential Attachment"
- & Considered undirected networks (not realistic but avoids 0 citation problem)
- Still have selection problem based on size (non-random)
- Solution: Randomly connect to a node (easy) ...
- ...and then randomly connect to the node's friends
- Scale-free networks" = food on the table for physicists

Another analytic approach: [5]

- Focus on how the nth arriving group typically grows.
- Analysis gives:

$$S_{n,\,t} \sim \left\{ \begin{array}{l} \frac{1}{\Gamma(2-\rho)} \left[\frac{1}{t}\right]^{-(1-\rho)} \text{ for } n=1, \\ \rho^{1-\rho} \left[\frac{n-1}{t}\right]^{-(1-\rho)} \text{ for } n \geq 2 \end{array} \right.$$

- & Because ρ is usually close to 0, the first element is truly an elephant in the room.
- Appears that this has been missed for 60 years ...

Dodds et al.,

B a = 0.01

$$S_{n,\,t} \sim \left\{ \begin{array}{l} \frac{1}{\Gamma(2-\rho)} \left[\frac{1}{t}\right]^{-(1-\rho)} \text{ for } n=1, \\ \rho^{1-\rho} \left[\frac{n-1}{t}\right]^{-(1-\rho)} \text{ for } n \geq 2. \end{array} \right.$$

- \clubsuit First mover is a factor $1/\rho$ greater than expected.

"Simon's fundamental rich-get-richer model

entails a dominant first-mover advantage"

C. $\rho = 0.001$

Physical Review E, **95**, 052301, 2017. [5]

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Mechanism

D. $\rho = 0.0001$

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Alternate analysis:

 \clubsuit Evolution of the *n*th arriving group's size:

$$\left\langle S_{n,t+1} - S_{n,t} \right\rangle = (1-\rho_t) \cdot \frac{S_{n,t}}{t} \cdot (+1).$$

 \Re For $t \geq t_n^{\text{init}}$, fix $\rho_t = \rho$ and shift t to t-1:

$$S_{n,t} = \left[1 + \frac{(1-\rho)}{t-1}\right] S_{n,t-1}.$$

where $S_{n,t_n^{\text{init}}} = 1$.



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Betafication ensues:

$$\begin{split} S_{n,t} &= \left[1 + \frac{(1-\rho)}{t-1}\right] \left[1 + \frac{(1-\rho)}{t-2}\right] \cdots \left[1 + \frac{(1-\rho)}{t_n^{\mathsf{init}}}\right] \cdot 1 \\ &= \left[\frac{t+1-\rho}{t-1}\right] \left[\frac{t-\rho}{t-2}\right] \cdots \left[\frac{t_n^{\mathsf{init}} + 1 - \rho}{t_n^{\mathsf{init}}}\right] \\ &= \frac{\Gamma(t+1-\rho)\Gamma(t_n^{\mathsf{init}})}{\Gamma(t_n^{\mathsf{init}} + 1 - \rho)\Gamma(t)} \\ &= \frac{B(t_n^{\mathsf{init}}, 1 - \rho)}{B(t, 1 - \rho)}. \end{split}$$



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 \Leftrightarrow For $n \geq 2$ and $\rho \ll 1$, the *n*th group typically arrives

 \mathfrak{S} But $t_1^{\mathsf{init}} = 1$ and the scaling is distinct in form.

The first mover is really different:

 \clubsuit The issue is t_n^{init} in

at $t_n^{\mathsf{init}} \simeq \left[\frac{n-1}{n}\right]$

Simon missed the first mover by working on the size distribution.

 $S_{n,t} = \frac{B(t_n^{\mathsf{init}}, 1 - \rho)}{B(t, 1 - \rho)}$

- & Contribution to $P_{k,t}$ of the first element vanishes
- Note: Does not apply to Barabási-Albert model.



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See visualization at paper's online app-endices



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Variability:

 The probability that the nth arriving group, if of size $S_{n,t} = k$ at time t, first replicates at time $t + \tau$:

$$\begin{split} & \Pr \big(S_{n,t+\tau} = k+1 \, | \, S_{n,t+i} = k \ \text{ for } i = 0, \ldots, \tau-1 \big) \\ & = \prod_{i=0}^{\tau-1} \left[1 - (1-\rho) \frac{k}{t+i} \right] \cdot (1-\rho) \frac{k}{t+\tau} \\ & = k \frac{B(\tau,t)}{B\left(\tau,t-(1-\rho)\right)} \frac{1-\rho}{t+\tau} \propto \frac{\tau^{-(1-\rho)k}}{t+\tau} \sim \tau^{-(2-\rho)k}. \end{split}$$

By Upshot: *n*th arriving group starting at size 1 will on average wait for an infinite time to replicate.

Related papers:

"Organization of Growing Random Networks"

Krapivsky and Redner, Phys. Rev. E, **63**, 066123, 2001. [7]



"The first-mover advantage in scientific publication"

M. E. J. Newman, Europhysics Letters, **86**, 68001, 2009. [11]

Related papers:



"Prediction of highly cited papers" M. E. J. Newman, Europhysics Letters, **105**, 28002, 2014. [12]



"The effect of the initial network configuration on preferential attachment"

Berset and Medo, The European Physical Journal B, 86, 1-7, 2013.[3]

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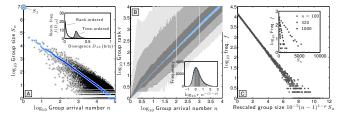
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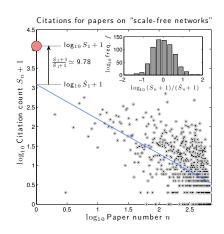
Mechanism



- Any one simulation shows a high amount of
- Two orders of magnitude variation in possible
- Rank ordering creates a smooth Zipf distribution.
- \triangle Size distribution for the *n*th arriving group show exponential decay.

Self-referential citation data:

Arrival variability:



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More mattering:

Rich-get-richerness in social contagion:

- & We love to rank everyone, everything: Top n lists.
- People, wealth, sports, music, movies, books, schools, cities, countries, dogs (13/10) ♂, ...
- Gameable: payola ☑, astroturfing ☑, sockpuppetry , John Barron (the sockpuppet hype man 🗷), ...
- Black-box ranking algorithms make ranking opaque.
- Black boxes are gameable but takes money and commensurate skill.
- Black box algorithms can make things spread rampantly.1
- No "regramming" is a positive feature of Instagram (also: Pratchett the Cat ☑)
- What if a healthier Facebook is just ...

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[1] F. Auerbach. Das gesetz der bevölkerungskonzentration. Petermanns Geogr. Mitteilungen, 59:73-76, 1913.

[2] A.-L. Barabási and R. Albert. Emergence of scaling in random networks. Science, 286:509-511, 1999. pdf

Y. Berset and M. Medo. The effect of the initial network configuration on preferential attachment. The European Physical Journal B, 86(6):1–7, 2013. pdf 🗹

[4] D. J. de Solla Price. Networks of scientific papers. Science, 149:510-515, 1965. pdf



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