

Allotaxonomy

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Principles of Complex Systems, Vols. 1, 2, & 3D
CSYS/MATH 300, 303, & 394, 2022-2023 | @pocsvox

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center
Santa Fe Institute | University of Vermont



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A plenitude of
distances

Rank-turbulence
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Probability-
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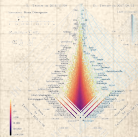
Mechanics of
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Superspreading

Lexical Ultrafame

Turbulent times

References



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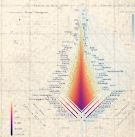
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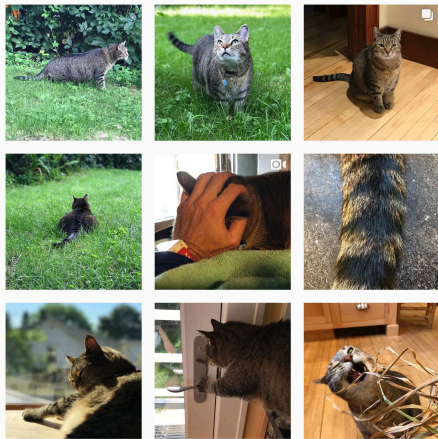
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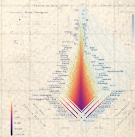
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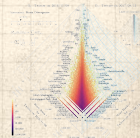
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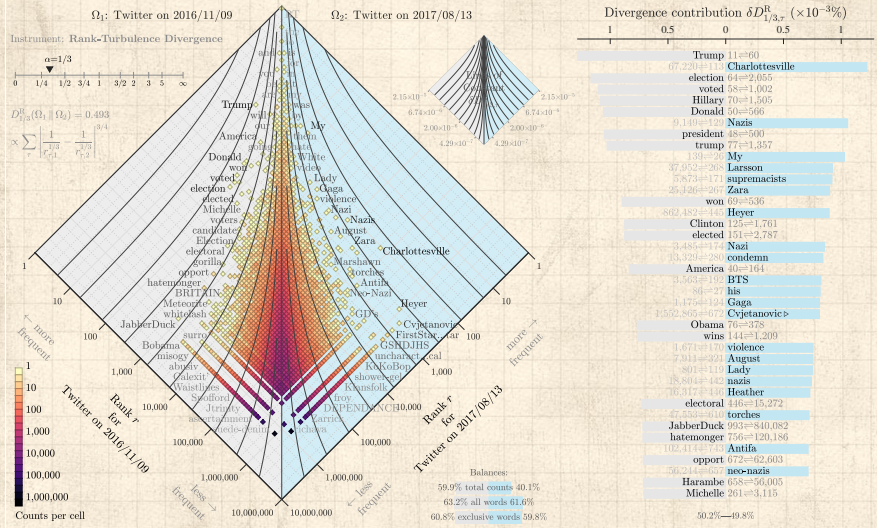
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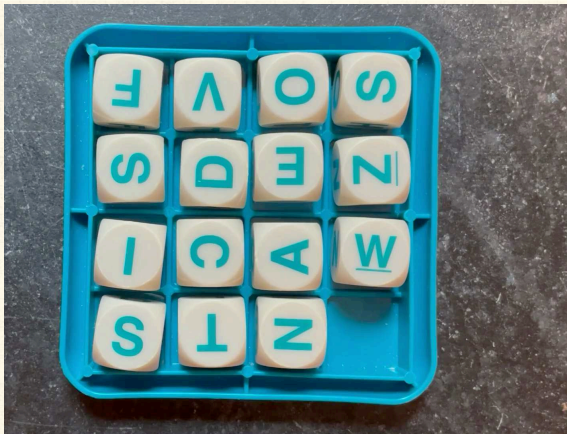
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Goal—Understand this:



The Boggoracle Speaks:



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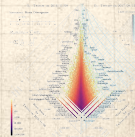
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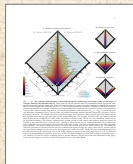
References



Site (papers, examples, code):

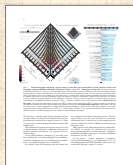
<http://compstorylab.org/allotaxonomy/>

Foundational papers:



"Allotaxonomy and rank-turbulence divergence: A universal instrument for comparing complex systems"

Dodds et al.,
, 2020. ^[11]



"Probability-turbulence divergence: A tunable allotaxonomic instrument for comparing heavy-tailed categorical distributions"

Dodds et al.,
, 2020. ^[13]

Basic science = Describe + Explain:



Dashboards of single scale instruments helps us understand, monitor, and control systems.

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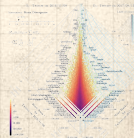
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- 🧱 Archetype: Cockpit dashboard for flying a plane

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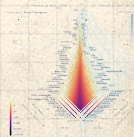
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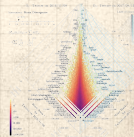
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 Complex systems present two problems for dashboards:

1. Scale with internal diversity of components: We need meters for every species, every company, every word.
2. Tracking change: We need to re-arrange meters on the fly.

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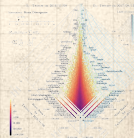
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 Goal—Create comprehensible, dynamically-adjusting, differential dashboards showing two pieces:¹

1. 'Big picture' map-like overview,
2. A tunable ranking of components.

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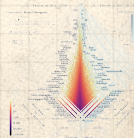
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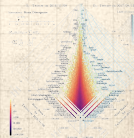
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¹See the [lexicocalorimeter](#) 

Baby names, much studied: [26]

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HOW TO: ABSURD SCIENTIFIC ADVICE FOR COMMON REAL-WORLD PROBLEMS

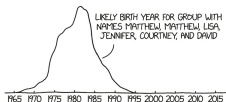
just a decade or so. If you were born in the United States around this year, these are names that are more likely to seem common and generic to you, but are distinctive generational markers.

1890 Will, Maudie, Minnie, May, Cora, Ida, Lela, Hattie, Annie, Ada
1885 Gracey, Maudie, Will, Minnie, Lela, Edie, May, Cora, Lela, Nettie
1880 Maudie, May, Minnie, Edie, Mabel, Bessie, Nettie, Hattie, Lela, Cora
1865 Maudie, Mabel, Minnie, Bessie, Minnie, Myrtle, Hattie, Pearl, Ethel, Bertha
1860 Mabel, Myrtle, Bessie, Minnie, Pearl, Blanche, Gertrude, Ethel, Minnie, Gladys
1855 Gladys, Vada, Mabel, Myrtle, Gertrude, Pearl, Bessie, Blanche, Marnie, Ethel
1910 Thelma, Gladys, Vada, Mildred, Beatrice, Lucille, Gertrude, Agnes, Hazel, Ethel
1915 Mildred, Lucille, Thelma, Helen, Bernice, Pauline, Eleanor, Beatrice, Ruth, Dorothy
1920 Marjorie, Dorothy, Mildred, Lucille, Warren, Thelma, Bernice, Virginia, Helen, Jane
1925 Doris, Jane, Betty, Marjorie, Dorothy, Lorraine, Lisa, Susie, Virginia, Beverly
1930 Dolores, Betty, Joan, Ethel, David, Norma, Lisa, Billy, Jane, Marilyn
1935 Shirley, Marlene, Joan, Dolores, Marilyn, Bobby, Betty, Billy, Joyce, Beverly
1940 Corde, Judith, Judy, Carol, Joyce, Barbara, Joan, Carolyn, Shirley, Jerry
1945 Judy, Judith, Linda, Carol, Sharon, Sandra, Carolyn, Larry, Anita, Dennis
1950 Linda, Deborah, Gill, Andy, Gary, Larry, Diane, Dennis, Brenda, Ankie
1955 Debra, Deborah, Cathy, Kathy, Pamela, Randy, Kim, Cynthia, Diane, Cheryl
1960 Debbie, Kim, Tori, Cindy, Kathy, Cathy, Laverie, Lori, Debra, Ricky
1965 Lisa, Tammy, Lori, Tiffni, Kim, Alexandra, Tracy, Tina, Dana, Michele
1970 Tammy, Tanya, Tracy, Todd, Dana, Tina, Sherry, Stacy, Michele, Lisa
1975 Chad, Jason, Tanya, Heather, Jennifer, Amy, Stacy, Shannon, Sherry, Tara
1980 Brenda, Crystal, April, Susan, Jeremy, Kim, Tiffany, Jamie, Melissa, Jennifer
1985 Crystal, Lindsay, Ashley, Lindsey, Doreen, Jessica, Amanda, Tiffany, Amber
1990 Britany, Chelsea, Kelsey, Cody, Ashley, Courtney, Ryan, Kyle, Megan, Jessica
1995 Taylor, Kelley, Dakota, Austin, Haley, Cody, Tyler, Shelby, Brittany, Kayla
2000 Destiny, Madison, Haley, Sydney, Alexis, Kaitlyn, Hunter, Brianna, Hannah, Alyssa
2005 Aislin, Dkya, Guisli, Hailey, Ethan, Madison, Ava, Isabella, Jayden, Aiden
2010 Jayden, Aislin, Noelle, Addison, Brigid, London, Peyton, Isabella, Ava, Liam
2015 Ari, Harper, Scarlett, Jason, Grayson, Alexander, Hudson, Liam, Zoey, Layla

If kids in your class were named Jeff, Lisa, Michael, Karan, and David, then you were probably born in the mid-1940s. If they were named Jayden, Isabella, Sophia, Ava, and Ethan, then you were probably born somewhere around 2010.

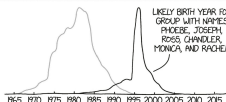
But names can reveal things about age in other ways.

The mid-1990s TV show *Friends* featured six roommates, played by actors named Matthew, Jennifer, Courtney, Lisa, David, and another Matthew. Each of those names has its own popularity curve. If we combine them all, we can guess what year the group of actors was likely born:



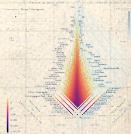
The actors were actually born in the late 1960s, on the very early edge of the popularity of their names. In other words, the actors all have names that were a little before their time. Courtney Cox and Jennifer Aniston had names that didn't really become popular until a decade later. (Maybe people with trendy parents are more likely to wind up in acting.) But the names are generally consistent with their era, if a little ahead of the curve.

We get something very different if we look at the names of their characters—Phoebe, Joseph, Ross, Chandler, Rachel, and Monica:



The show debuted in 1994. There's a clear spike in popularity of the names in 1995 and 1996, which can probably be attributed to the show putting the names in the minds of new parents. But it's not just the show—that name combination was clearly on the rise in the years before *Friends* premiered. It's possible that parents looking for good names for their children are influenced by some of the same cultural trends as TV writers looking for good names for their characters.

How to build a dynamical dashboard that helps sort through a massive number of interconnected time series?

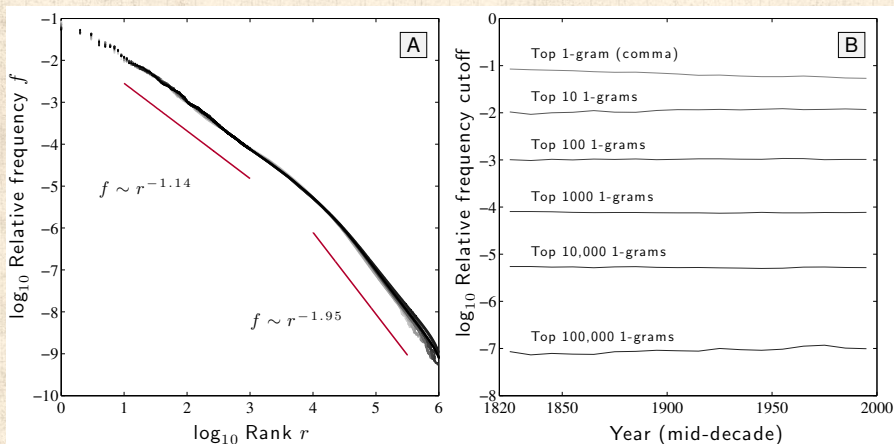




"Is language evolution grinding to a halt? The scaling of lexical turbulence in English fiction suggests it is not" ↗

Pechenick, Danforth, Dodds, Alshaabi, Adams, Dewhurst, Reagan, Danforth, Reagan, and Danforth.

Journal of Computational Science, **21**, 24–37, 2017. [29]



For language, Zipf's law has two scaling regimes: ^[38]

$$f \sim \begin{cases} r^{-\alpha} & \text{for } r \ll r_b, \\ r^{-\alpha'} & \text{for } r \gg r_b, \end{cases}$$

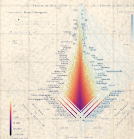
When comparing two texts, define Lexical turbulence as flux of words across a frequency threshold:

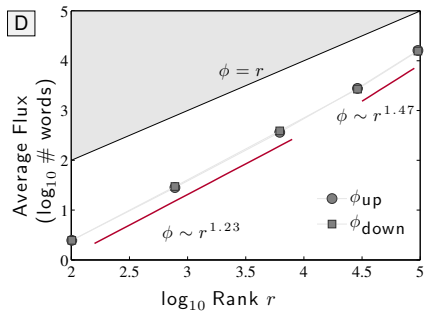
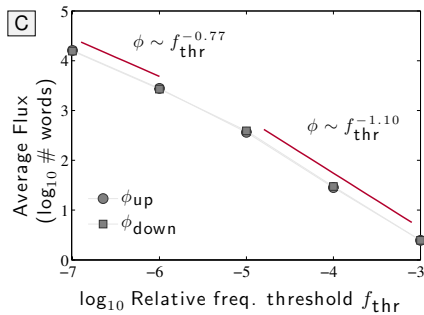
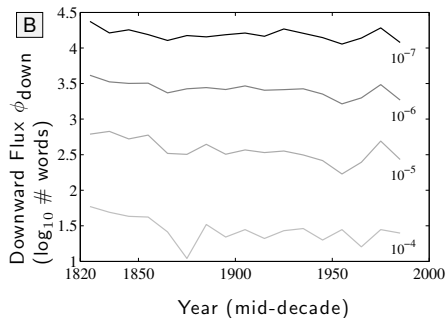
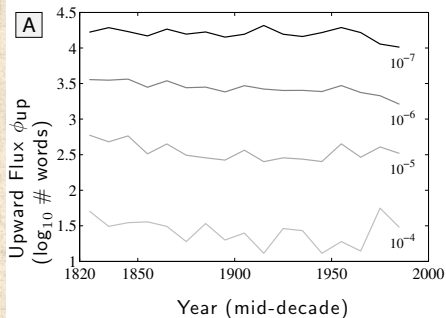
$$\phi \sim \begin{cases} f_{\text{thr}}^{-\mu} & \text{for } f_{\text{thr}} \ll f_b, \\ f_{\text{thr}}^{-\mu'} & \text{for } f_{\text{thr}} \gg f_b, \end{cases}$$

Estimates: $\mu \simeq 0.77$ and $\mu' \simeq 1.10$, and f_b is the scaling break point.

$$\phi \sim \begin{cases} r^\nu = r^{\alpha\mu'} & \text{for } r \ll r_b, \\ r^{\nu'} = r^{\alpha'\mu} & \text{for } r \gg r_b. \end{cases}$$

Estimates: Lower and upper exponents $\nu \simeq 1.23$ and $\nu' \simeq 1.47$.

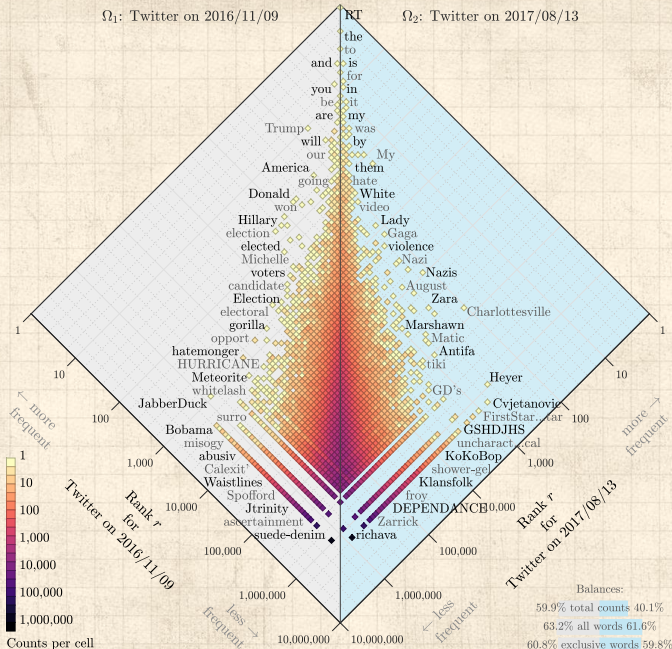




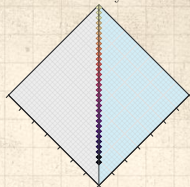
A. Rank-turbulence histogram:

Ω_1 : Twitter on 2016/11/09

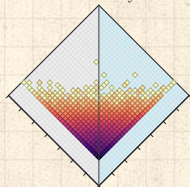
Ω_2 : Twitter on 2017/08/13



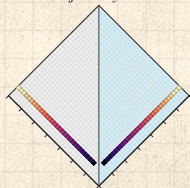
B. Identical systems:



C. Randomized systems:



D. Disjoint systems:



Balances:

59.9% total counts 40.1%

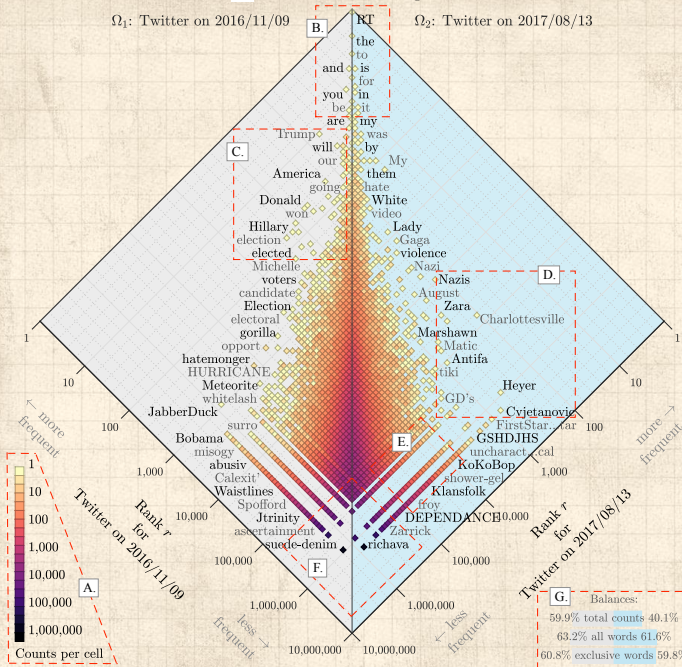
63.2% all words 61.6%

60.8% exclusive words 59.8%

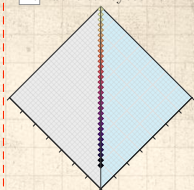
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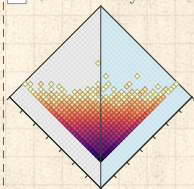
Ω_2 : Twitter on 2017/08/13



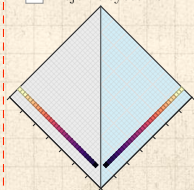
H. Identical systems:



I. Randomized systems:



J. Disjoint systems:



G.

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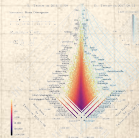
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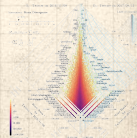
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Exclusive types:

 We call types that are present in one system only 'exclusive types'.

 When warranted, we will use expressions of the form $\Omega^{(1)}$ -exclusive and $\Omega^{(2)}$ -exclusive to indicate to which system an exclusive type belongs.



Probability-turbulence histogram:

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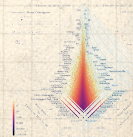
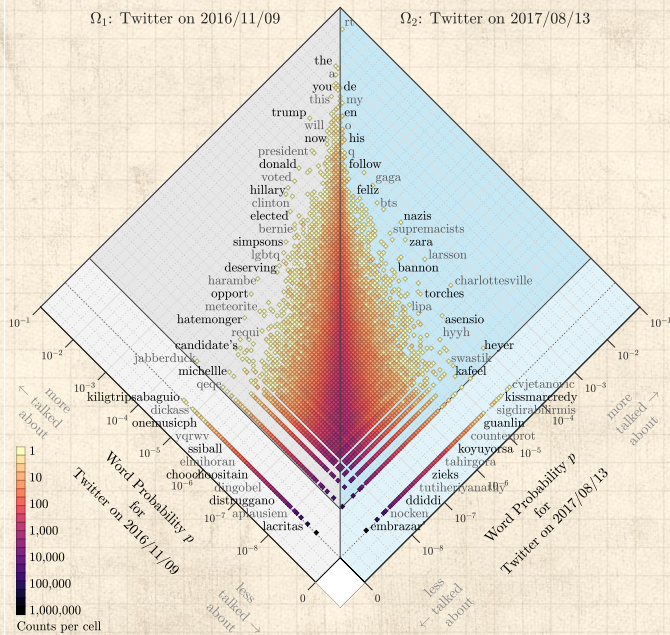
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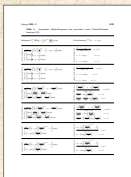
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So, so many ways to compare probability distributions:



"Families of Alpha- Beta- and Gamma-Divergences: Flexible and Robust Measures of Similarities" 

Cichocki and Amari,
Entropy, **12**, 1532-1568, 2010. [8]

"Comprehensive survey on distance/similarity measures between probability density functions" 

Sung-Hyuk Cha,
International Journal of Mathematical Models and Methods in Applied Sciences, **1**, 300-307, 2007. [4]



Comparisons are distances, divergences, similarities, inner products, fidelities ...

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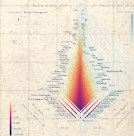
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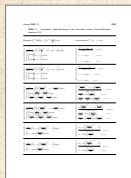
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Measure	Properties
...	...

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Comparisons are distances, divergences, similarities, inner products, fidelities ...



60ish kinds of comparisons grouped into 10 families

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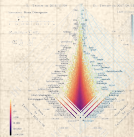
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References




So, so many ways to compare probability distributions:



"Families of Alpha- Beta- and Gamma-Divergences: Flexible and Robust Measures of Similarities" 

Cichocki and Amari,
Entropy, **12**, 1532-1568, 2010. [8]

"Comprehensive survey on distance/similarity measures between probability density functions" 

Sung-Hyuk Cha,
International Journal of Mathematical Models and Methods in Applied Sciences, **1**, 300-307, 2007. [4]



Comparisons are distances, divergences, similarities, inner products, fidelities ...



60ish kinds of comparisons grouped into 10 families



A worry: Subsampled distributions with very heavy tails

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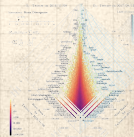
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Quite the festival:

Table 1. L_p Minkowski family

1. Euclidean L_2	$d_{min} = \sqrt{\frac{P-Q}{P+Q}}$ (1)
2. City block L_1	$d_{min} = \frac{1}{2} \left \frac{P-Q}{P+Q} \right $ (2)
3. Minkowski L_p	$d_{min} = \sqrt[p]{\frac{P-Q}{P+Q}}$ (3)
4. Chebyshev L_∞	$d_{min} = \max\{ P-Q \}$ (4)

Table 2. L_p family

5. Sorenson	$d_{min} = \frac{\sum P-Q }{\sum (P+Q)}$ (5)
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6. Gower	$d_{min} = \frac{1}{2} \sqrt{\frac{ P-Q }{P+Q}}$ (6)
	$= \frac{1}{2} \sqrt{\frac{P-Q}{P+Q}}$ (7)

7. Soregol	$d_{min} = \frac{\sum P-Q }{\sum \max(P,Q)}$ (8)
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8. Kulczyński d	$d_{min} = \frac{\sum P-Q }{\sum \min(P,Q)}$ (9)
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9. Canberra	$d_{min} = \sqrt{\frac{ P-Q }{P+Q}}$ (10)
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10. Lovrentzian	$d_{min} = \sum \min\{ P-Q \}$ (11)
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* L_p family \Rightarrow Intersection (13), Wave Hodges (15), Czekanowski (16), Ruszka (21), Tanimoto (23), etc.

Table 3. Intersection family

11. Intersection	$s_{in} = \sum \min(P,Q)$ (12)
	$d_{min} = 1 - s_{in} = \frac{1}{2} \sum P-Q $ (13)
12. Wave Hodges	$d_{min} = \frac{\sum \min(P,Q)}{\sum \max(P,Q)}$ (14)
	$= \frac{\sum P-Q }{\sum \max(P,Q)}$ (15)
13. Czekanowski	$s_{in} = \frac{\sum \min(P,Q)}{\sum (P+Q)}$ (16)
	$d_{min} = 1 - s_{in} = \frac{\sum P-Q }{\sum (P+Q)}$ (17)

Table 4. Inner Product family

18. Inner Product	$s_{in} = P \cdot Q = \sum P_i Q_i$ (24)
19. Harmonic mean	$s_{in} = \frac{\sum P_i Q_i}{\sum (P_i + Q_i)}$ (25)
20. Cosine	$s_{in} = \frac{\sum P_i Q_i}{\sqrt{\sum P_i^2} \sqrt{\sum Q_i^2}}$ (26)

21. Kumar-Hauschok (PCE)	$s_{in} = \frac{\sum P_i Q_i}{\sum P_i^2 + \sum Q_i^2 - \sum P_i Q_i}$ (27)
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22. Jaccard	$s_{in} = \frac{\sum P_i Q_i}{\sum P_i^2 + \sum Q_i^2 - \sum P_i Q_i}$ (28)
-------------	---

23. Dice	$s_{in} = \frac{\sum P_i Q_i}{\sum P_i^2 + \sum Q_i^2}$ (29)
	$d_{min} = 1 - s_{in} = \frac{\sum P-Q ^2}{\sum P_i^2 + \sum Q_i^2}$ (30)

24. Fidelity	$s_{in} = \sum \sqrt{P_i Q_i}$ (32)
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25. Bhattacharyya	$d_{in} = -\ln \sum \sqrt{P_i Q_i}$ (33)
-------------------	--

26. Hellinger	$d_{in} = \sqrt{\frac{1}{2} \sum \sqrt{P_i} \sqrt{Q_i}}$ (34)
	$= \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$ (35)

27. Matusita	$d_{in} = \sqrt{\frac{1}{2} \sum \sqrt{P_i} \sqrt{Q_i} - \sqrt{P_i} \sqrt{Q_i}}$ (36)
	$= \sqrt{1 - \sum \sqrt{P_i Q_i}}$ (37)

28. Squared-chord	$d_{in} = \sqrt{\frac{1}{2} \sum P_i - Q_i ^2}$ (38)
	$s_{in} = 1 - d_{in} = \sqrt{2 \sum \sqrt{P_i Q_i} - 1}$ (39)

29. Squared Euclidean	$d_{in} = \sum (P_i - Q_i)^2$ (40)
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30. Pearson χ^2	$d_{in}(P,Q) = \frac{\sum (P_i - Q_i)^2}{\sum Q_i}$ (41)
----------------------	--

31. Neyman χ^2	$d_{in}(P,Q) = \frac{\sum (P_i - Q_i)^2}{\sum P_i}$ (42)
---------------------	--

32. Squared χ^2	$d_{in} = \frac{\sum (P_i - Q_i)^2}{P_i + Q_i}$ (43)
----------------------	--

33. Probabilistic Symmetric χ^2	$d_{in} = \frac{\sum (P_i - Q_i)^2}{P_i + Q_i}$ (44)
--------------------------------------	--

34. Divergence	$d_{in} = 2 \frac{\sum (P_i - Q_i)^2}{(P_i + Q_i)^2}$ (45)
----------------	--

35. Clark	$d_{in} = \sqrt{\frac{ P-Q }{P+Q}}$ (46)
-----------	--

36. Additive Symmetric χ^2	$d_{in} = \frac{\sum (P_i - Q_i)^2 (P_i + Q_i)}{\sum P_i \sum Q_i}$ (47)
---------------------------------	--

* Squared L_p family \Rightarrow Jaccard (29), Dice (31)

Table 5. Fidelity family or Squared-chord family

24. Fidelity	$s_{in} = \sum \sqrt{P_i Q_i}$ (32)
25. Bhattacharyya	$d_{in} = -\ln \sum \sqrt{P_i Q_i}$ (33)
26. Hellinger	$d_{in} = \sqrt{\frac{1}{2} \sum \sqrt{P_i} \sqrt{Q_i}}$ (34)
	$= \sqrt{\frac{1}{2} \sum \sqrt{P_i Q_i}}$ (35)

Table 6. Squared L_p family or χ^2 family

29. Squared Euclidean	$d_{in} = \sum (P_i - Q_i)^2$ (40)
30. Pearson χ^2	$d_{in}(P,Q) = \frac{\sum (P_i - Q_i)^2}{\sum Q_i}$ (41)
31. Neyman χ^2	$d_{in}(P,Q) = \frac{\sum (P_i - Q_i)^2}{\sum P_i}$ (42)
32. Squared χ^2	$d_{in} = \frac{\sum (P_i - Q_i)^2}{P_i + Q_i}$ (43)
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---------------------------------	--

* Squared L_p family \Rightarrow Jaccard (29), Dice (31)

Table 7. Shannon's entropy family

37. Kullback-Leibler	$d_{in} = \sum P_i \ln \frac{P_i}{Q_i}$ (48)
38. Jeffreys	$d_{in} = \sum (P_i - Q_i) \ln \frac{P_i}{Q_i}$ (49)
39. K. divergence	$d_{in} = \sum P_i \ln \frac{2P_i}{P_i + Q_i}$ (50)

40. Topoc	$d_{in} = \frac{1}{2} \sum P_i \ln \left(\frac{2P_i}{P_i + Q_i} \right) + Q_i \ln \left(\frac{2Q_i}{P_i + Q_i} \right)$ (51)
-----------	--

41. Jensen-Shannon	$d_{in} = \frac{1}{2} \left[\sum P_i \ln \left(\frac{2P_i}{P_i + Q_i} \right) + \sum Q_i \ln \left(\frac{2Q_i}{P_i + Q_i} \right) \right]$ (52)
--------------------	--

42. Jensen divergence	$d_{in} = \frac{1}{2} \left[\sum P_i \ln \frac{P_i - Q_i}{P_i} + \sum Q_i \ln \frac{Q_i - P_i}{Q_i} \right] \ln \left(\frac{P_i + Q_i}{2} \right)$ (53)
-----------------------	---

Table 8. Combinations

43. Taneja	$d_{in} = \frac{\sum (P_i - Q_i)}{2} \ln \left \frac{P_i + Q_i}{2 \sqrt{P_i Q_i}} \right $ (54)
------------	--

44. Kumar-Johnson	$d_{in} = \sum \left[\frac{(P_i - Q_i)^2}{2(P_i Q_i)^2} \right]$ (55)
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45. Avgul(L, L _{in})	$d_{min} = \frac{\sum P-Q + \max\{ P-Q \}}{2}$ (56)
--------------------------------	---

Table 10. Vicissitude

Vicis-Wave Hodges	$d_{min} = \frac{\sum P-Q }{\sum \max(P,Q)}$ (60)
Vicis-Symmetric χ^2	$d_{min} = \frac{\sum P-Q ^2}{\sum \max(P,Q)^2}$ (61)
Vicis-Symmetric χ^2	$d_{min} = \frac{\sum P-Q ^2}{\sum \min(P,Q)^2}$ (62)
Vicis-Symmetric χ^2	$d_{min} = \frac{\sum P-Q ^2}{\sum \max(P,Q)}$ (63)

max-Symmetric	$d_{in} = \max \left(\frac{\sum (P_i - Q_i)^2}{P_i}, \frac{\sum (P_i - Q_i)^2}{Q_i} \right)$ (64)
---------------	--

min-Symmetric	$d_{in} = \min \left(\frac{\sum (P_i - Q_i)^2}{P_i}, \frac{\sum (P_i - Q_i)^2}{Q_i} \right)$ (65)
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Probability-turbulence divergence

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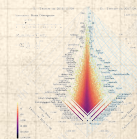
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References




Shannon tried to slow things down in 1956:



"The bandwagon" 

Claude E Shannon,
IRE Transactions on Information Theory, **2**,
3, 1956. ^[34]

 "Information theory has ... become something of a scientific bandwagon."

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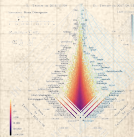
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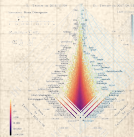
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 "While ... information theory is indeed a valuable tool ... [it] is certainly no panacea for the communication engineer or ... for anyone else."

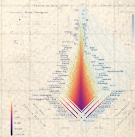


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-  "Information theory has ... become something of a scientific bandwagon."
-  "While ... information theory is indeed a valuable tool ... [it] is certainly no panacea for the communication engineer or ... for anyone else."
-  "A few first rate research papers are preferable to a large number that are poorly conceived or half-finished."





We want two main things:

1. A measure of difference between systems
2. A way of sorting which types/species/words contribute to that difference

Table 1. L_p Minkowski family		
1. Euclidean L_2	$d_{Euc} = \sqrt{\sum_{i=1}^d P_i - Q_i ^2}$	(1)
2. City block L_1	$d_{CB} = \sum_{i=1}^d P_i - Q_i $	(2)
3. Minkowski L_p	$d_{Mk} = \sqrt[p]{\sum_{i=1}^d P_i - Q_i ^p}$	(3)
4. Chebyshev L_∞	$d_{Cheb} = \max_i P_i - Q_i $	(4)

Table 2. L_1 family		
5. Sørensen	$d_{sor} = \frac{\sum_{i=1}^d P_i - Q_i }{\sum_{i=1}^d (P_i + Q_i)}$	(5)

6. Gower	$d_{gow} = \frac{1}{d} \sum_{i=1}^d \frac{ P_i - Q_i }{R_i}$	(6)
	$= \frac{1}{d} \sum_{i=1}^d P_i - Q_i $	(7)

7. Soergel	$d_{sg} = \frac{\sum_{i=1}^d P_i - Q_i }{\sum_{i=1}^d \max(P_i, Q_i)}$	(8)
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8. Kulczynski d	$d_{kul} = \frac{\sum_{i=1}^d P_i - Q_i }{\sum_{i=1}^d \min(P_i, Q_i)}$	(9)
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9. Canberra	$d_{can} = \sum_{i=1}^d \frac{ P_i - Q_i }{P_i + Q_i}$	(10)
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10. Lorentzian	$d_{lor} = \sum_{i=1}^d \ln(1 + P_i - Q_i)$	(11)
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* L_1 family \supset {Intersectoin (13), Wave Hedges (15), Czekanowski (16), Ruzicka (21), Tanimoto (23), etc}.

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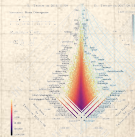
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For sorting, many comparisons give the same ordering.

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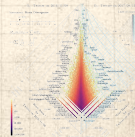
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For sorting, many comparisons give the same ordering.



A few basic building blocks:

$|P_i - Q_i|$ (dominant)

$\max(P_i, Q_i)$

$\min(P_i, Q_i)$

$P_i Q_i$

$|P_i^{1/2} - Q_i^{1/2}|$
(Hellinger)

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--------------------	---	-----

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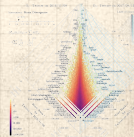
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Information theoretic
sortings are more
opaque

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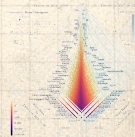
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No tunability

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8. Kulczynski d	$d_{kul} = \frac{\sum_{i=1}^d P_i - Q_i }{\sum_{i=1}^d \min(P_i, Q_i)}$	(9)
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10. Lorentzian	$d_{Lor} = \sum_{i=1}^d \ln(1 + P_i - Q_i)$	(11)
* L_1 family \supset {Intersectoin (13), Wave Hedges (15), Czekanowski (16), Ruzicka (21), Tanimoto (23), etc}.		

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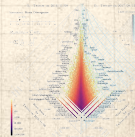
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Shannon's Entropy:

$$H(P) = \langle \log_2 \frac{1}{p_\tau} \rangle = \sum_{\tau \in R_{1,2;\alpha}} p_\tau \log_2 \frac{1}{p_\tau} \quad (1)$$

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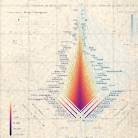
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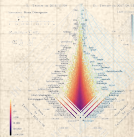


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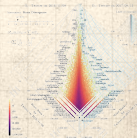
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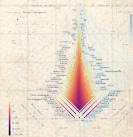
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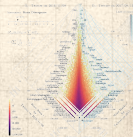
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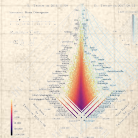
New problem: Re-read solution.



🌀 Jensen-Shannon divergence (JSD): [21, 15, 28, 4]

$$\begin{aligned} D^{\text{JS}}(P_1 \parallel P_2) &= \frac{1}{2} D^{\text{KL}}\left(P_1 \parallel \frac{1}{2}[P_1 + P_2]\right) + \frac{1}{2} D^{\text{KL}}\left(P_2 \parallel \frac{1}{2}[P_1 + P_2]\right) \\ &= \frac{1}{2} \sum_{\tau \in R_{1,2;\alpha}} \left(p_{1,\tau} \log_2 \frac{p_{1,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} + p_{2,\tau} \log_2 \frac{p_{2,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} \right). \end{aligned} \quad (3)$$

🌀 Involving a third intermediate averaged system means JSD is now finite: $0 \leq D^{\text{JS}}(P_1 \parallel P_2) \leq 1$.



🌀 Jensen-Shannon divergence (JSD): [21, 15, 28, 4]

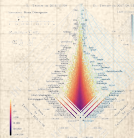
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 &= \frac{1}{2} \sum_{\tau \in R_{1,2;\alpha}} \left(p_{1,\tau} \log_2 \frac{p_{1,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} + p_{2,\tau} \log_2 \frac{p_{2,\tau}}{\frac{1}{2}[p_{1,\tau} + p_{2,\tau}]} \right).
 \end{aligned} \tag{3}$$

🌀 Involving a third intermediate averaged system means JSD is now finite: $0 \leq D^{\text{JS}}(P_1 \parallel P_2) \leq 1$.

🌀 Generalized entropy divergence: [8]

$$\begin{aligned}
 D_{\alpha}^{\text{AS2}}(P_1 \parallel P_2) &= \frac{1}{\alpha(\alpha-1)} \sum_{\tau \in R_{1,2;\alpha}} \left[(p_{\tau,1}^{1-\alpha} + p_{\tau,2}^{1-\alpha}) \left(\frac{p_{\tau,1} + p_{\tau,2}}{2} \right)^{\alpha} - (p_{\tau,1} + p_{\tau,2}) \right].
 \end{aligned} \tag{4}$$

Produces JSD when $\alpha \rightarrow 0$.



Ω_1 : Twitter on 2016/11/09

Ω_2 : Twitter on 2017/08/13

Divergence contribution $\delta D_{0,r}^H$ (%)

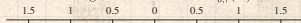
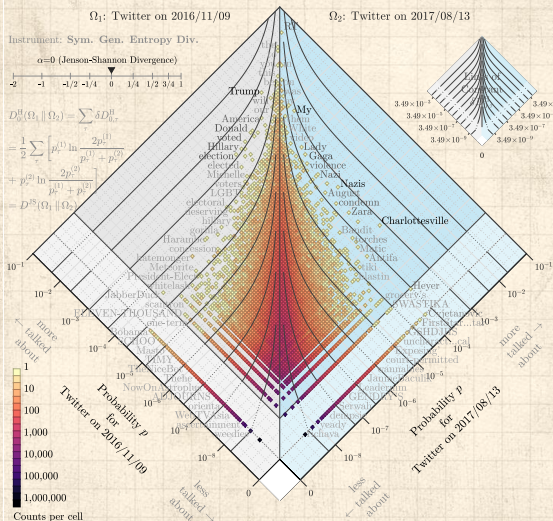
Instrument: Sym. Gen. Entropy Div.

$\alpha=0$ (Jenson-Shannon Divergence)

$$D_{0,r}^H(\Omega_1 || \Omega_2) = \sum_r \delta D_{0,r}^H$$

$$= \frac{1}{2} \sum_r \left[p_r^{(1)} \ln \frac{2p_r^{(1)}}{p_r^{(1)} + p_r^{(2)}} + p_r^{(2)} \ln \frac{2p_r^{(2)}}{p_r^{(1)} + p_r^{(2)}} \right]$$

$$= D^{JS}(\Omega_1 || \Omega_2)$$



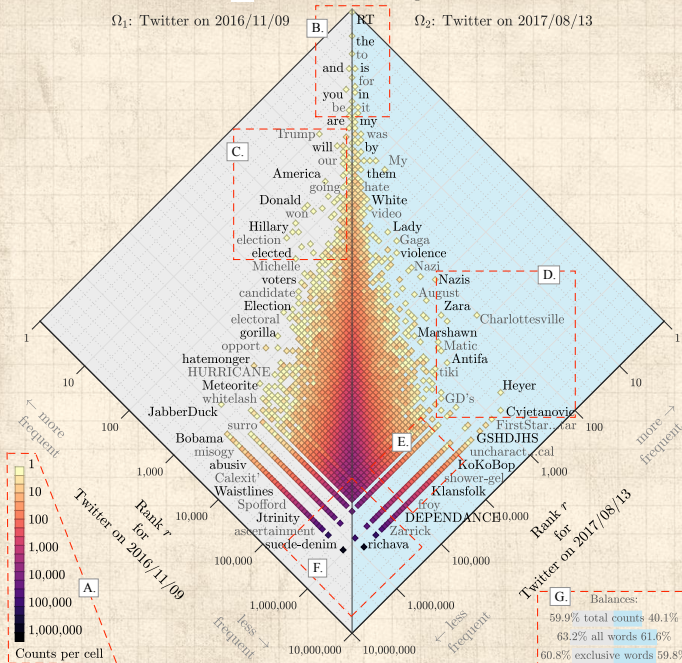
Trump	11=60
voted	58=1,002
Donald	50=566
election	64=2,055
president	48=500
Hillary	70=1,505
trump	77=1,357
America	40=164
won	69=536
67,220=113	Charlottesville
139=20	My
9,149=129	Nazis
Clinton	125=1,761
Obama	76=378
elected	151=2,787
wins	144=1,209
will	23=51
country	71=216
5,873=171	supremacists
1,175=124	Gaga
3,485=174	Nazi
1=1	RT
86=27	his
801=119	Lady
votes	180=1,422
3,563=192	BTS
37,952=268	Larsson
25,126=267	Zara
13,329=280	condem
1,671=170	violence
Michelle	261=3,115
our	41=72
7,911=321	August
President	93=228
voters	306=4,453
1,325=187	supremacy
people	27=45
candidate	362=5,584
1,761=231	police
women	124=315

52.9%—47.1%

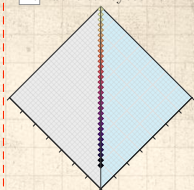
Rank-turbulence histogram:

Ω_1 : Twitter on 2016/11/09

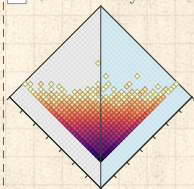
Ω_2 : Twitter on 2017/08/13



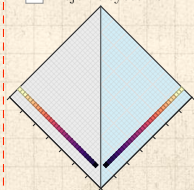
H. Identical systems:



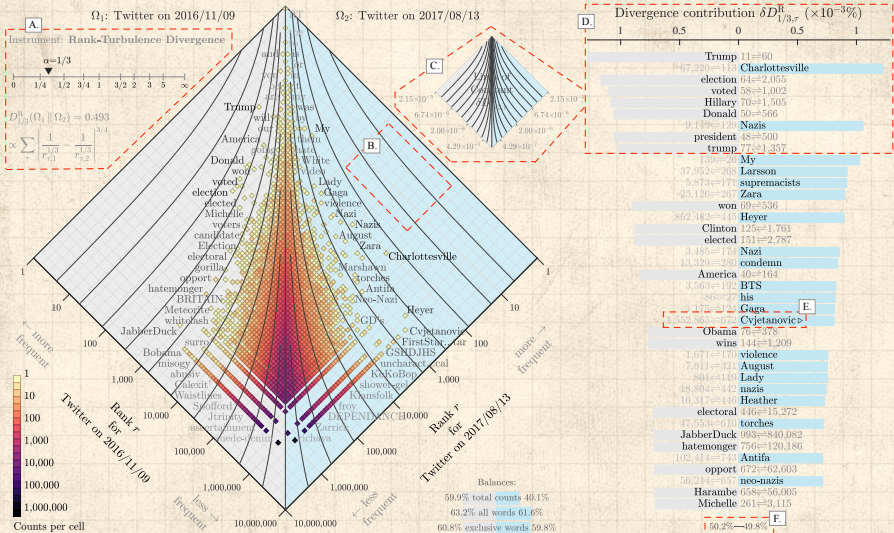
I. Randomized systems:



J. Disjoint systems:



G. Balances:
 59.9% total counts 40.1%
 63.2% all words 61.6%
 60.8% exclusive words 59.8%



Desirable rank-turbulence divergence features:

1. Rank-based.

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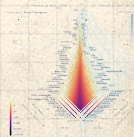
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Desirable rank-turbulence divergence features:

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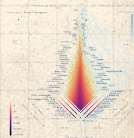
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Desirable rank-turbulence divergence features:

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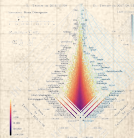
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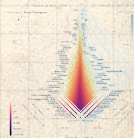
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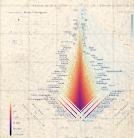
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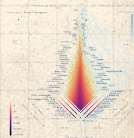
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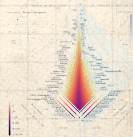
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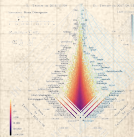
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8. Tunable.
9. Story-finding: Features 1–8 combine to show which component types are most 'important'

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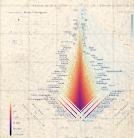
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Some good things about ranks:

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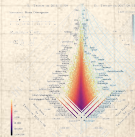
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Some good things about ranks:

 Working with ranks is intuitive

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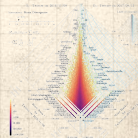
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- Affords some powerful statistics (e.g., Spearman's rank correlation coefficient)

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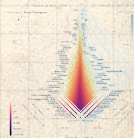
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- Can be used to generalize beyond systems with probabilities

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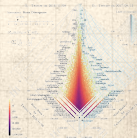
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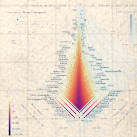
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A start:

$$\left| \frac{1}{r_{\tau,1}} - \frac{1}{r_{\tau,2}} \right|. \quad (5)$$

- Inverse of rank gives an increasing measure of 'importance'
- High rank means closer to rank 1
- We assign tied ranks for components of equal 'size'



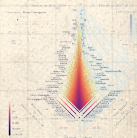
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- We assign tied ranks for components of equal 'size'
- Issue: Biases toward high rank components



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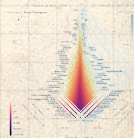
Lexical Ultrafame

Turbulent times

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We introduce a tuning parameter:

$$\left| \frac{1}{[r_{\tau,1}]^{\alpha}} - \frac{1}{[r_{\tau,2}]^{\alpha}} \right|^{1/\alpha} \cdot \quad (6)$$

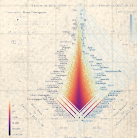


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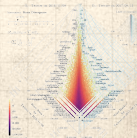
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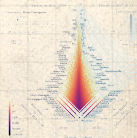
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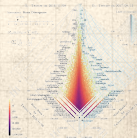
- As $\alpha \rightarrow 0$, high ranked components are increasingly dampened
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- As $\alpha \rightarrow \infty$, high rank components will dominate.



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- For texts, the contributions of rare words will vanish.



Trouble:



The limit of $\alpha \rightarrow 0$ does not behave well for

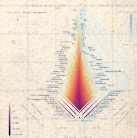
$$\left| \frac{1}{[r_{\tau,1}]^{\alpha}} - \frac{1}{[r_{\tau,2}]^{\alpha}} \right|^{1/\alpha}.$$



The leading order term is:

$$(1 - \delta_{r_{\tau,1} r_{\tau,2}}) \alpha^{1/\alpha} \left| \ln \frac{r_{\tau,1}}{r_{\tau,2}} \right|^{1/\alpha}, \quad (7)$$

which heads toward ∞ as $\alpha \rightarrow 0$.



Trouble:

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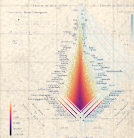
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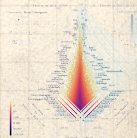
which heads toward ∞ as $\alpha \rightarrow 0$.

🧱 Oops.

🧱 But the insides look nutritious:

$$\left| \ln \frac{r_{\tau,1}}{r_{\tau,2}} \right|$$

is a nicely interpretable log-ratio of ranks.



Some reworking:

$$\delta D_{\alpha, \tau}^R(R_1 \parallel R_2) \propto \frac{\alpha + 1}{\alpha} \left| \frac{1}{[r_{\tau, 1}]^\alpha} - \frac{1}{[r_{\tau, 2}]^\alpha} \right|^{1/(\alpha+1)} \quad (8)$$

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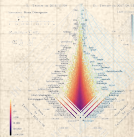
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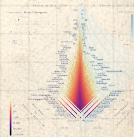
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Large α limit remains the same.

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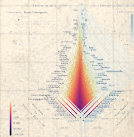
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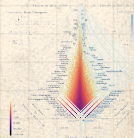
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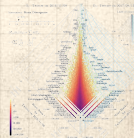
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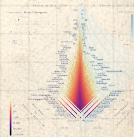
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- Next: Sum over τ to get divergence.



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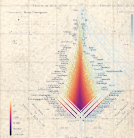
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Rank-turbulence divergence:

$$D_{\alpha}^R(R_1 \parallel R_2) = \frac{1}{\mathcal{N}_{1,2;\alpha}} \sum_{\tau \in R_{1,2;\alpha}} \delta D_{\alpha, \tau}^R(R_1 \parallel R_2) \quad (9)$$



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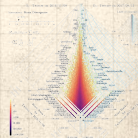
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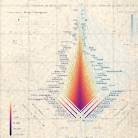
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 Take a data-driven rather than analytic approach
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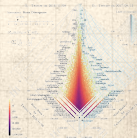
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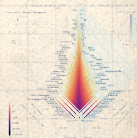
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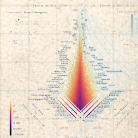
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- Ensures: $0 \leq D_{\alpha}^R(R_1 \parallel R_2) \leq 1$
- Limits of 0 and 1 correspond to the two systems having identical and disjoint Zipf distributions.



Rank-turbulence divergence:

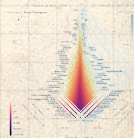
Summing over all types, dividing by a normalization prefactor $\mathcal{N}_{1,2;\alpha}$ we have our prototype:

$$D_{\alpha}^R(R_1 || R_2) = \frac{1}{\mathcal{N}_{1,2;\alpha}} \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_{1,2;\alpha}} \left| \frac{1}{[r_{\tau,1}]^{\alpha}} - \frac{1}{[r_{\tau,2}]^{\alpha}} \right|^{1/(\alpha+1)} \quad (10)$$



General normalization:

☞ If the Zipf distributions are disjoint, then in $\Omega^{(1)}$'s merged ranking, the rank of all $\Omega^{(2)}$ types will be $r = N_1 + \frac{1}{2}N_2$, where N_1 and N_2 are the number of distinct types in each system.



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- ☰ Similarly, $\Omega^{(2)}$'s merged ranking will have all of $\Omega^{(1)}$'s types in last place with rank $r = N_2 + \frac{1}{2}N_1$.

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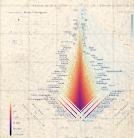
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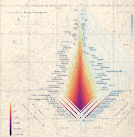
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- ☰ Similarly, $\Omega^{(2)}$'s merged ranking will have all of $\Omega^{(1)}$'s types in last place with rank $r = N_2 + \frac{1}{2}N_1$.
- ☰ The normalization is then:

$$\begin{aligned} \mathcal{N}_{1,2;\alpha} = & \frac{\alpha+1}{\alpha} \sum_{\tau \in R_1} \left| \frac{1}{[r_{\tau,1}]^\alpha} - \frac{1}{[N_1 + \frac{1}{2}N_2]^\alpha} \right|^{1/(\alpha+1)} \\ & + \frac{\alpha+1}{\alpha} \sum_{\tau \in R_2} \left| \frac{1}{[N_2 + \frac{1}{2}N_1]^\alpha} - \frac{1}{[r_{\tau,2}]^\alpha} \right|^{1/(\alpha+1)} \end{aligned} \quad (11)$$




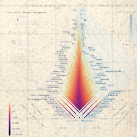
Limit of $\alpha \rightarrow 0$:

$$D_0^R(R_1 \parallel R_2) = \sum_{\tau \in R_{1,2;\alpha}} \delta D_{0,\tau}^R = \frac{1}{\mathcal{N}_{1,2;0}} \sum_{\tau \in R_{1,2;\alpha}} \left| \ln \frac{r_{\tau,1}}{r_{\tau,2}} \right|, \quad (12)$$

where

$$\mathcal{N}_{1,2;0} = \sum_{\tau \in R_1} \left| \ln \frac{r_{\tau,1}}{N_1 + \frac{1}{2}N_2} \right| + \sum_{\tau \in R_2} \left| \ln \frac{r_{\tau,2}}{\frac{1}{2}N_1 + N_2} \right|. \quad (13)$$

 Largest rank ratios dominate.




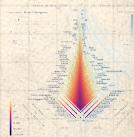
Limit of $\alpha \rightarrow \infty$:

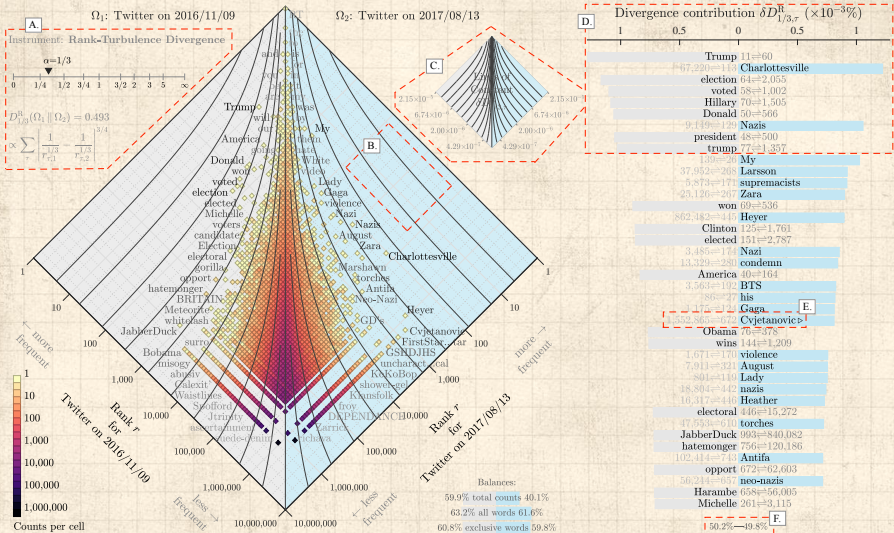
$$\begin{aligned} D_{\infty}^R(R_1 \| R_2) &= \sum_{\tau \in R_{1,2;\alpha}} \delta D_{\infty, \tau}^R \\ &= \frac{1}{N_{1,2;\infty}} \sum_{\tau \in R_{1,2;\alpha}} (1 - \delta_{r_{\tau,1} r_{\tau,2}}) \max_{\tau} \left\{ \frac{1}{r_{\tau,1}}, \frac{1}{r_{\tau,2}} \right\}. \end{aligned} \quad (14)$$

where

$$N_{1,2;\infty} = \sum_{\tau \in R_1} \frac{1}{r_{\tau,1}} + \sum_{\tau \in R_2} \frac{1}{r_{\tau,2}}. \quad (15)$$



 Highest ranks dominate.





Probability-turbulence divergence:

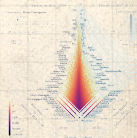
$$D_{\alpha}^{\text{P}}(P_1 \parallel P_2) = \frac{1}{\mathcal{N}_{1,2;\alpha}^{\text{P}}} \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_{1,2;\alpha}} \left| [p_{\tau,1}]^{\alpha} - [p_{\tau,2}]^{\alpha} \right|^{1/(\alpha+1)}. \quad (16)$$

-  For the unnormalized version ($\mathcal{N}_{1,2;\alpha}^{\text{P}}=1$), some troubles return with 0 probabilities and $\alpha \rightarrow 0$.
-  Weep not: $\mathcal{N}_{1,2;\alpha}^{\text{P}}$ will save the day.

Normalization:

With no matching types, the probability of a type present in one system is zero in the other, and the sum can be split between the two systems' types:

$$\mathcal{N}_{1,2;\alpha}^P = \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_1} [p_{\tau,1}]^{\alpha/(\alpha+1)} + \frac{\alpha + 1}{\alpha} \sum_{\tau \in R_2} [p_{\tau,2}]^{\alpha/(\alpha+1)} \quad (17)$$

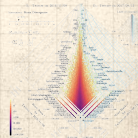


Limit of $\alpha=0$ for probability-turbulence divergence


🧱 if both $p_{\tau,1} > 0$ and $p_{\tau,2} > 0$ then

$$\lim_{\alpha \rightarrow 0} \frac{\alpha + 1}{\alpha} \left| [p_{\tau,1}]^{\alpha} - [p_{\tau,2}]^{\alpha} \right|^{1/(\alpha+1)} = \left| \ln \frac{p_{\tau,2}}{p_{\tau,1}} \right|. \quad (18)$$


🧱 But if $p_{\tau,1} = 0$ or $p_{\tau,2} = 0$, limit diverges as $1/\alpha$.

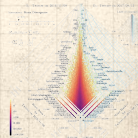


Limit of $\alpha=0$ for probability-turbulence divergence

 Normalization:


$$\mathcal{N}_{1,2;\alpha}^P \rightarrow \frac{1}{\alpha} (N_1 + N_2). \quad (19)$$


 Because the normalization also diverges as $1/\alpha$, the divergence will be zero when there are no exclusive types and non-zero when there are exclusive types.

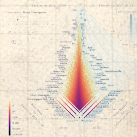


Combine these cases into a single expression:




$$D_0^P(P_1 \parallel P_2) = \frac{1}{(N_1 + N_2)} \sum_{\tau \in R_{1,2;0}} (\delta_{p_{\tau,1},0} + \delta_{0,p_{\tau,2}}). \quad (20)$$

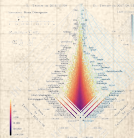
 The term $(\delta_{p_{\tau,1},0} + \delta_{0,p_{\tau,2}})$ returns 1 if either $p_{\tau,1} = 0$ or $p_{\tau,2} = 0$, and 0 otherwise when both $p_{\tau,1} > 0$ and $p_{\tau,2} > 0$.

 Ratio of types that are exclusive to one system relative to the total possible such types,



Type contribution ordering for the limit of $\alpha=0$

-  In terms of contribution to the divergence score, all exclusive types supply a weight of $1/(N_1 + N_2)$. We can order them by preserving their ordering as $\alpha \rightarrow 0$, which amounts to ordering by descending probability in the system in which they appear.
-  And while types that appear in both systems make no contribution to $D_0^P(P_1 \parallel P_2)$, we can still order them according to the log ratio of their probabilities.
-  The overall ordering of types by divergence contribution for $\alpha=0$ is then: (1) exclusive types by descending probability and then (2) types appearing in both systems by descending log ratio.

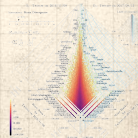


Limit of $\alpha=\infty$ for probability-turbulence divergence





$$D_{\infty}^P(P_1 \parallel P_2) = \frac{1}{2} \sum_{\tau \in R_{1,2;\infty}} (1 - \delta_{p_{\tau,1}, p_{\tau,2}}) \max(p_{\tau,1}, p_{\tau,2}) \quad (21)$$

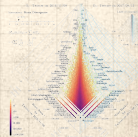
where

$$\mathcal{N}_{1,2;\infty}^P = \sum_{\tau \in R_{1,2;\infty}} (p_{\tau,1} + p_{\tau,2}) = 1 + 1 = 2. \quad (22)$$



Connections for PTD:

-  $\alpha = 0$: Similarity measure Sørensen-Dice coefficient ^[10, 35, 22], F_1 score of a test's accuracy ^[36, 33].
-  $\alpha = 1/2$: Hellinger distance ^[18] and Mautusita distance ^[23].
-  $\alpha = 1$: Many including all $L^{(p)}$ -norm type constructions.
-  $\alpha = \infty$: Motyka distance ^[9].



Ω_1 : Twitter on 2016/11/09

Ω_2 : Twitter on 2017/08/13

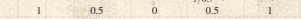
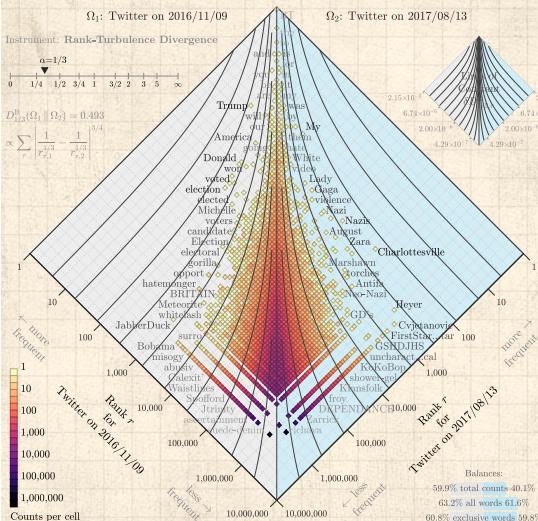
Divergence contribution $\delta D_{1/3,7}^R$ ($\times 10^{-3}\%$)

Instrument: Rank-Turbulence Divergence

$\alpha=1/3$

$$D_{1/3}^R(\Omega_1 || \Omega_2) = 0.493$$

$$\propto \sum_r \left| \frac{1}{r_{-1/3}} - \frac{1}{r_{+1/3}} \right|^{3/4}$$



Trump	11=60
17,220=113	Charlotteville
election	64=2,055
voted	58=1,002
Hillary	70=1,505
Donald	50=566
9,149=129	Nazis
president	48=500
trump	77=1,357
139=20	My
37,952=268	Larsson
5,873=171	supremacists
25,126=267	Zara
won	69=536
862,482=443	Heyer
Clinton	125=1,761
elected	151=2,787
3,485=174	Nazi
13,329=280	condemn
America	40=164
3,503=192	BTS
86=27	his
1,175=124	Gaga
1,562,865=673	Cvjetanovic >
Obama	76=378
wins	144=1,209
1,671=170	violence
7,911=321	August
801=110	Lady
18,804=442	nazis
16,317=140	Heather
electoral	446=15,272
47,558=610	torches
JabberDuck	993=840,082
hatemonger	756=120,186
102,414=743	Antifa
opport	672=62,603
56,244=657	neo-nazis
Harambe	658=56,005
Michelle	261=3,115
50.2%	49.8%

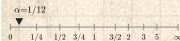
Balances:
 59.9% total counts 40.1%
 63.2% all words 61.6%
 60.8% exclusive words 59.8%

Ω_1 : Twitter on 2016/11/09

Ω_2 : Twitter on 2017/08/13

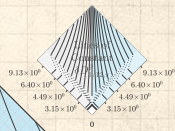
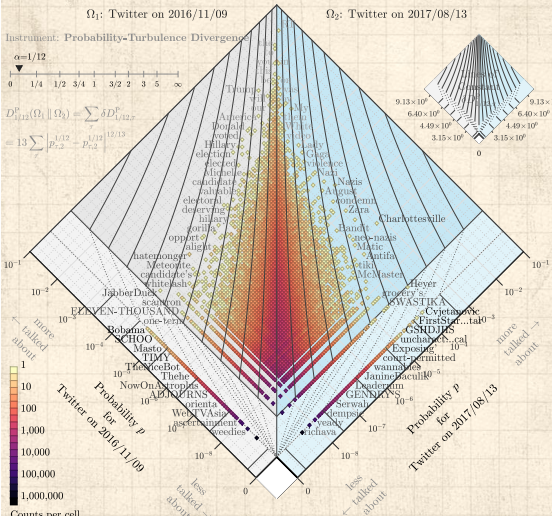
Divergence contribution $\delta D_{1/12,r}^D (\times 10^{-4}\%)$

Instrument: Probability-Turbulence Divergence



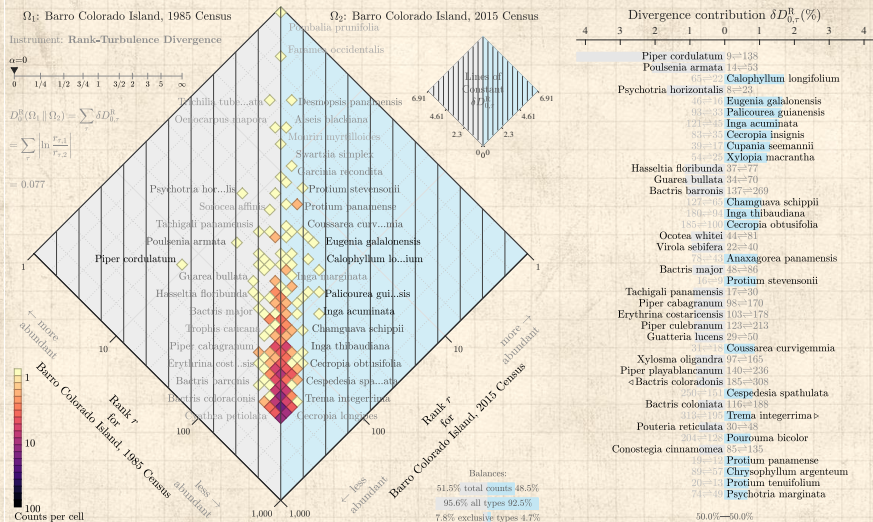
$$D_{1/12}^D(\Omega_1 \parallel \Omega_2) = \sum \delta D_{1/12,r}^D$$

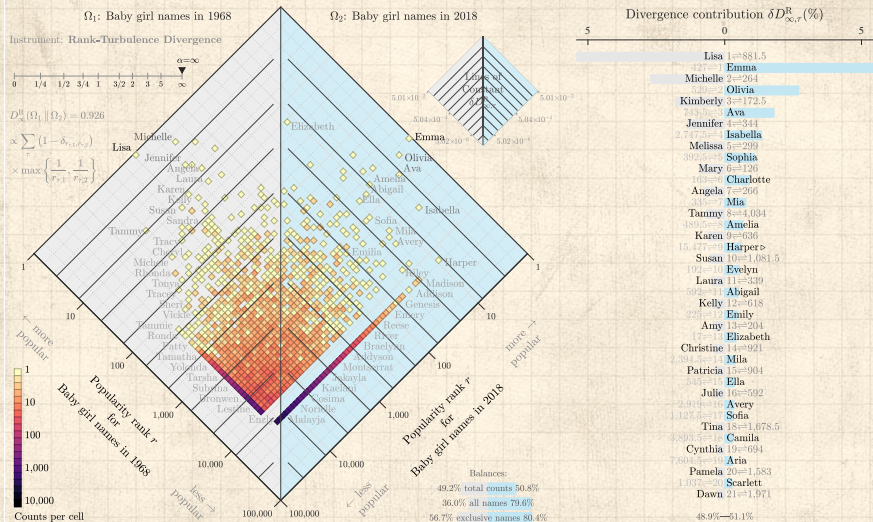
$$= 13 \sum_{P_{r,2}}^{1/12} \frac{1/12}{P_{r,2}} - \frac{1/12}{P_{r,2}^{12/13}}$$

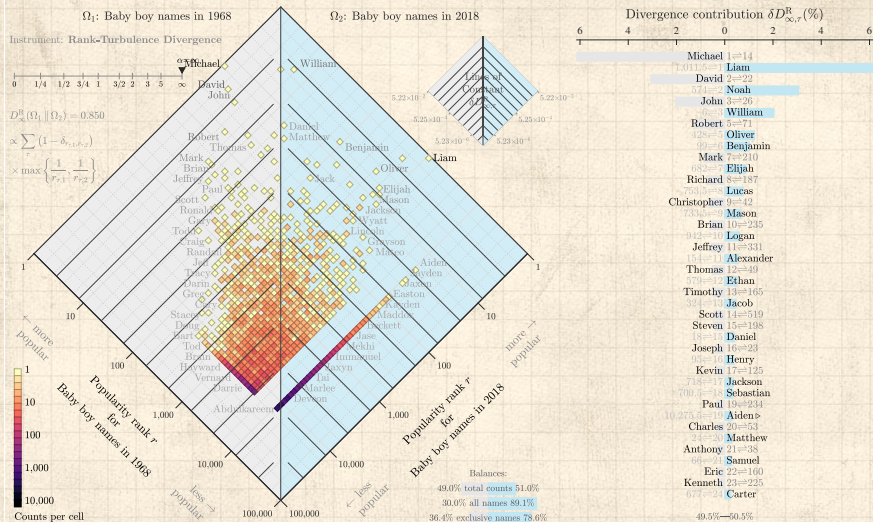


1.552,865=673	Cvjetanovic >
1.552,865=1,110	FirstStarMagicAllStar >
1.552,865=1,47	KISSMARCHED >
1.552,865=1,520	ForAllStarGames >
1.552,865=1,985	Kafeel >
1.552,865=2,021	Starbz >
< Bobama 2,423=1,537,471	
< Oarack 2,425=1,537,471	
< Un-Leashed 2,703=1,537,471	
1.552,865=3,088	GSHDJHS >
1.552,865=3,099	Bodak >
< KiligTripSaBagnio 3,142=1,537,471	
< Somali-American 3,229=1,537,471	
< DICKASS 3,321=1,537,471	
< Michelle 3,412=1,537,471	
1.552,865=3,673	Eastwatch >
< Un-leashed 3,645=1,537,471	
1.552,865=3,983	Heyer's >
< SCHOO 3,921=1,537,471	
1.552,865=4,382	uncharacteristical >
1.552,865=4,518	callejones >
< misogy 4,328=1,537,471	
1.552,865=4,723	TLC >
1.552,865=4,913	SORIBADA >
< tRyNna 4,660=1,537,471	
< aLmoSt 4,671=1,537,471	
1.552,865=5,240	tcas >
< Ruline 5,097=1,537,471	
< Steinger 5,118=1,537,471	
1.552,865=5,436	low-rise >
< climate-denying 5,191=1,537,471	
1.552,865=5,662	CLITORIS >
1.552,865=5,682	Adityanath >
< lambo's 5,383=1,537,471	
1.552,865=5,757	DelHiHasret >
1.552,865=5,757	FikBel >
1.552,865=5,808	Walker-Peters >
< KBAT 5,617=1,537,471	
1.552,865=6,040	UNIDAS >
< stammered 5,653=1,537,471	

49.9%—50.1%





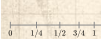


Ω_1 : 1948 Google Books Fiction

Ω_2 : 1987 Google Books Fiction

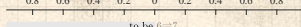
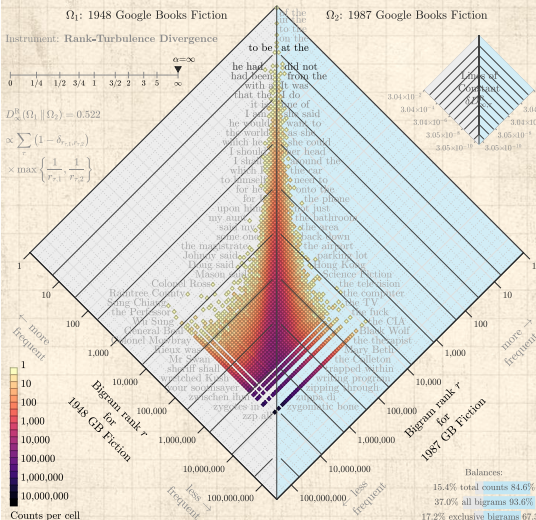
Divergence contribution $\delta D_{\infty,r}^R$ (%)

Instrument: Rank-Turbulence Divergence



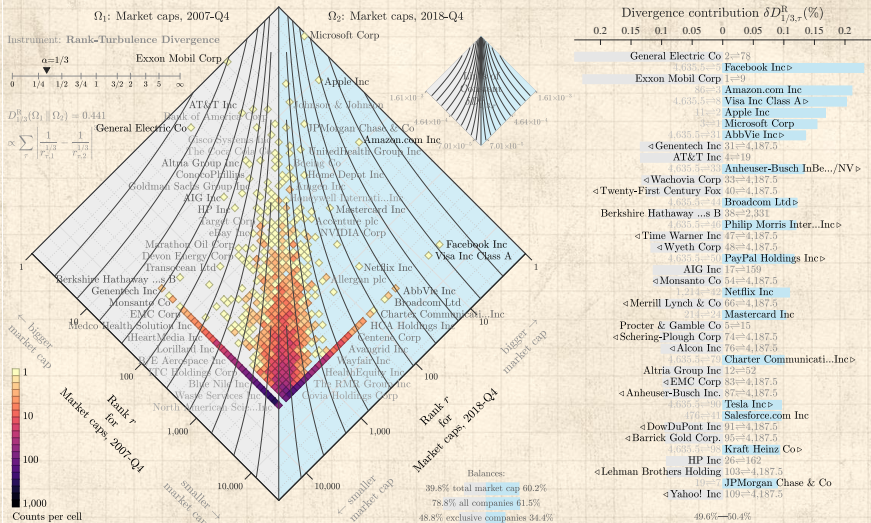
$$D_{\infty}^R(\Omega_1, \Omega_2) = 0.522$$

$$\infty \sum_r (1 - \delta_{r,1} \delta_{r,2}) \times \max\left\{\frac{1}{r_{r,1}}, \frac{1}{r_{r,2}}\right\}$$



- to be 6 \Rightarrow 7
- at the 7 \Rightarrow 8
- had 8 \Rightarrow 19
- did not 12 \Rightarrow 3
- it was 9 \Rightarrow 12
- do not 41 \Rightarrow 9
- of a 10 \Rightarrow 16
- 19 \Rightarrow 10 from the
- he was 13 \Rightarrow 14
- 17 \Rightarrow 13 for the
- had been 15 \Rightarrow 17
- 16 \Rightarrow 15 was a
- of his 18 \Rightarrow 20
- 20 \Rightarrow 18 with the
- with a 21 \Rightarrow 22
- 23 \Rightarrow 21 It was
- that he 22 \Rightarrow 38
- 26 \Rightarrow 23 into the
- by the 24 \Rightarrow 27
- 27 \Rightarrow 24 out of
- in his 25 \Rightarrow 30
- 30 \Rightarrow 25 was not
- 32 \Rightarrow 20 I was
- that the 28 \Rightarrow 35
- 34 \Rightarrow 28 I do
- he said 29 \Rightarrow 33
- 31 \Rightarrow 29 for a
- 43 \Rightarrow 31 she was
- 41 \Rightarrow 33 of her
- and he 33 \Rightarrow 47
- 39 \Rightarrow 34 she had
- and I 35 \Rightarrow 37
- I have 36 \Rightarrow 48
- 37 \Rightarrow 36 could not
- was the 38 \Rightarrow 42
- 47 \Rightarrow 39 one of
- and a 40 \Rightarrow 43
- 80 \Rightarrow 40 going to
- 48 \Rightarrow 41 would be
- it is 42 \Rightarrow 67
- 50.2%—49.8%

Balances:
 15.4% total counts 84.6%
 37.0% all bigrams 93.6%
 17.2% exclusive bigrams 67.3%



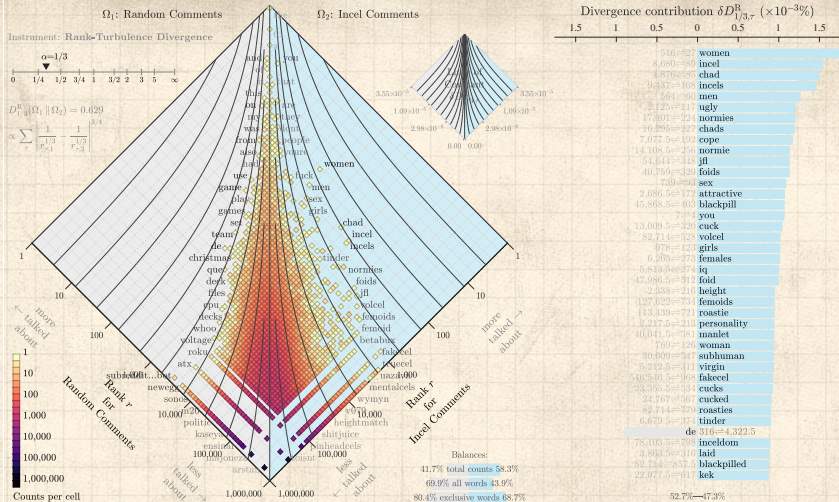
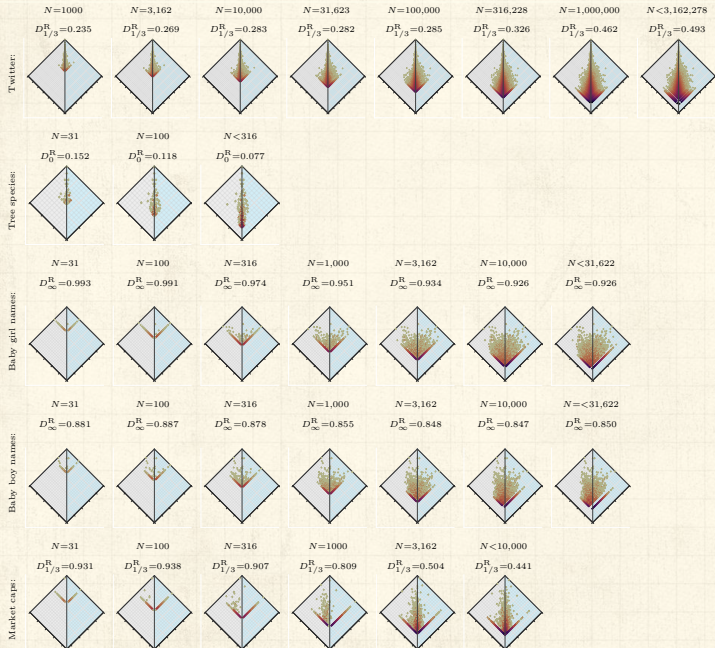


FIG. 8. Rank-turbulence divergence allotaxonograph [34] of word rank distributions in the incel vs random comment corpora. The rank-rank histogram on the left shows the density of words by their rank in the incel comments corpus against their rank in the random comments corpus. Words at the top of the diamond are higher frequency, or lower rank. For example, the word “the” appears at the highest observed frequency, and thus has the lowest rank, 1. This word has the lowest rank in both corpora, so its coordinates lie along the center vertical line in the plot. Words such as “women” diverge from the center line because their rank in the incel corpus is higher than in the random corpus. The top 40 words with greatest divergence contribution are shown on the right. In this comparison, nearly all of the top 40 words are more common in the incel corpus, so they point to the right. The word that has the most notable change in rank from the random to incel corpus is “women”, the object of hatred

Effect of subsampling:



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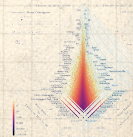
Mechanics of
Fame

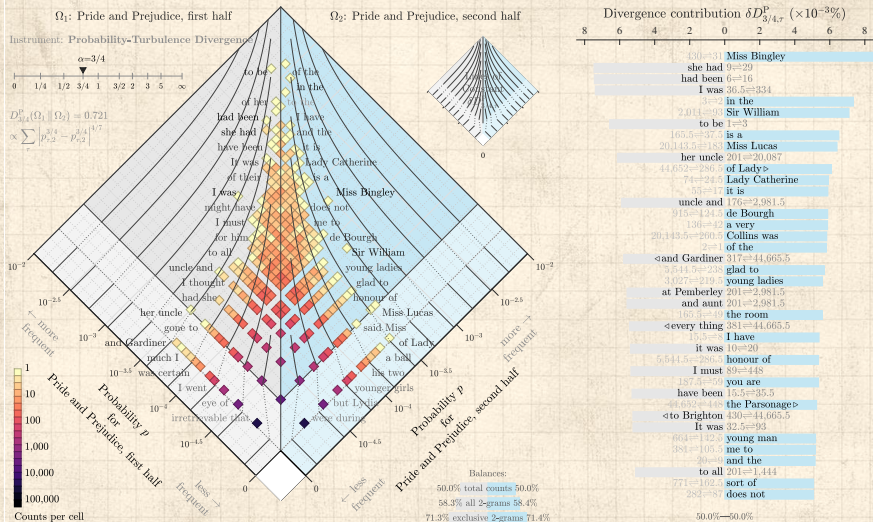
Superspreading

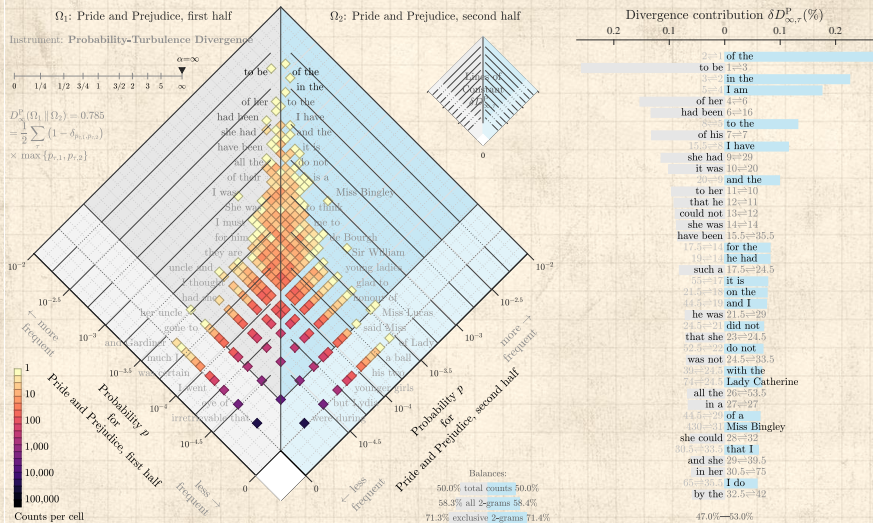
Lexical Ultrafame

Turbulent times

References







Equation-Block:

$$D_{\infty}^P(\Omega_1, \Omega_2) = 0.785$$

$$= \frac{1}{2} \sum_{\tau} (1 - \delta_{p_1, p_{\tau,2}})$$

$$\times \max\{p_{\tau,1}, p_{\tau,2}\}$$

Ω_1 : Twitter on 2020/03/12

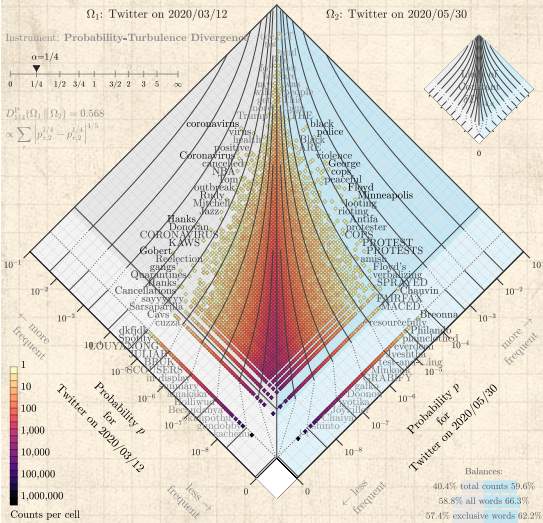
Ω_2 : Twitter on 2020/05/30

Instrument: Probability-Turbulence Divergence

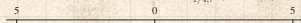


$$D_{1/4}^P(\Omega_1 || \Omega_2) = 0.568$$

$$\propto \sum_p |p_{\Omega_1}^{1/4} - p_{\Omega_2}^{1/4}|^{4/3}$$

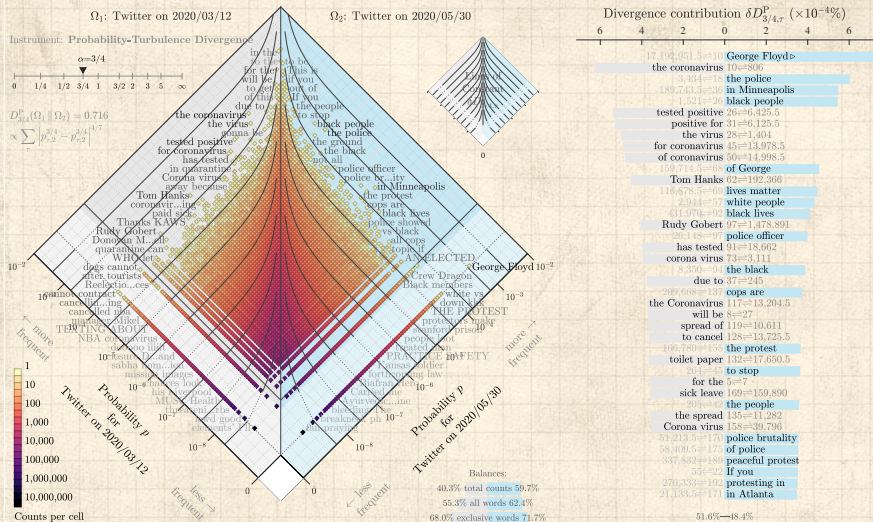


Divergence contribution $\delta D_{1/4,7}^P (\times 10^{-4}\%)$



29,291.5=110	Minneapolis
17,877=117	Floyd
coronavirus	34=708
1,160=40	police
4,689=8	George
14,094.5=150	protesting
6,661=103	cops
4,472=87	protest
19,096.5=194	protestors
12,852.5=160	protesters
22,116.5=223	looting
Gobert	427=164,877.5
Hanks	329=48,943.5
611=40	black
Coronavirus	72=2,352
5,622=137	protests
85,437=579	PROTEST
913,207.5=921	Chauvin
5,274=170	Atlanta
43,060.5=499	Antifa
6,784=206	peaceful
1,717,011.5=1,327	Breonna >
18,219=340	NYPD
619=57	white
tested	118=2,740
40,175.5=520	BLM
129,716.5=798	PROTESTS
22,714=414	rioting
2,797=138	violence
4,488=180	officer
90,270.5=774	ANTIFA
7,926=268	cop
NBA	198=4,648.5
KAWS	852=65,437.5
Rudy	408=13,205.5
gangs	1,232=217,899.5
46,280=76	protester
92,973=1,02	PEACEFUL
220,871.5=1,311	testing
119=1,842	Floyd's
48.6=51.4%	

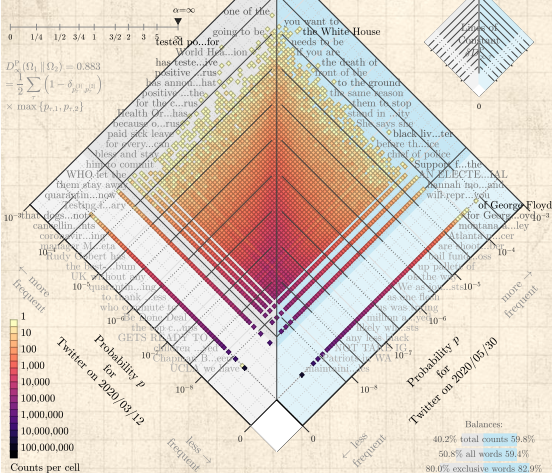
Balances:
 40.4% total counts 59.6%
 58.8% all words 66.3%
 57.4% exclusive words 62.2%



Ω_1 : Twitter on 2020/03/12

Ω_2 : Twitter on 2020/05/30

Instrument: Probability-Turbulence Divergence

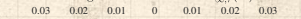


$$D_{\infty}^p(\Omega_1, \Omega_2) = 0.883$$

$$= \frac{1}{2} \sum (1 - \delta_{p, q}^{|\Omega_i|})$$

$$\times \max\{p_{r,1}, p_{r,2}\}$$

Divergence contribution $\delta D_{\infty, r}^p$ (%)





- tested positive for 1=4,975.5
- 40,733,560.5=2 of George Floyd
- 219=2 the White House
- 267=2 in front of
- 2=4 one of the
- has tested positive 3=11,879
- positive for coronavirus 4=14,798
- the spread of 5=7,264.5
- going to be 6=33
- 76=43 out of the
- 687,005=0 black lives matter
- 40,733,560.5=1 community in Minneapolis
- 7=108 is going to
- 108=23 to do with
- 131=49 part of the
- 25=10 you want to
- World Health Organization 8=1,420
- 20,432.5=11 to the ground
- for the coronavirus 9=78,795
- 5,326.5=12 the death of
- 40,733,560.5=13 for George Floyd
- positive for the 10=53,912
- due to the 11=603
- has announced that 12=22,783.5
- 109=14 needs to be
- 3,040,097=13 Support from the
- be able to 13=45
- the rest of 14=143.5
- in the world 15=30
- 52=10 This is the
- because of coronavirus 16=277,424.5
- because of the 17=631.5
- < that dogs cannot 18=43,073,107
- the United States 19=22
- < announced that dogs 20=43,073,107
- Health Organization has 21=172,568
- the corona virus 22=1,421
- < dogs cannot contract 23=43,073,107
- < Organization has an...ced 24=43,073,107
- 40,733,560.5=12 white vs black



Balances:
 40.2% total counts 59.8%
 50.8% all words 59.4%
 80.0% exclusive words 82.9%



Flipbooks for RTD:



Twitter:

[instrument-flipbook-1-rank-div.pdf](#)  

[instrument-flipbook-2-probability-div.pdf](#)  

[instrument-flipbook-3-gen-entropy-div.pdf](#)  







Market caps:

[instrument-flipbook-4-marketcaps-6years-rank-div.pdf](#)  





Baby names:



[instrument-flipbook-5-babynames-girls-50years-rank-div.pdf](#)  

[instrument-flipbook-6-babynames-boys-50years-rank-div.pdf](#)  



Google books:

[instrument-flipbook-7-google-books-onograms-rank-div.pdf](#)  

[instrument-flipbook-8-google-books-bigrams-rank-div.pdf](#)  

[instrument-flipbook-9-google-books-trigrams-rank-div.pdf](#)  

Flipbooks for PTD:



Jane Austen:

[Pride and Prejudice, 1-grams](#)  



[Pride and Prejudice, 2-grams](#)  



[Pride and Prejudice, 3-grams](#)  



Social media:


[Twitter, 1-grams](#)  

[Twitter, 2-grams](#)  

[Twitter, 3-grams](#)  



Ecology:

[Barro Colorado Island](#)  

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divergence

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Stories

Mechanics of
Fame

Superspreading

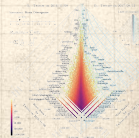
Lexical Ultrafame

Turbulent times

References

Code:

<https://gitlab.com/compstorylab/allotaxonomer>



Claims, exaggerations, reminders:



Needed for comparing large-scale complex systems:

Comprehensible, dynamically-adjusting, differential dashboards

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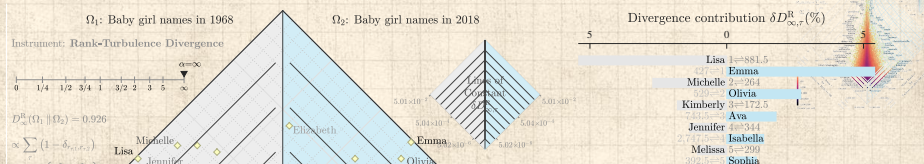
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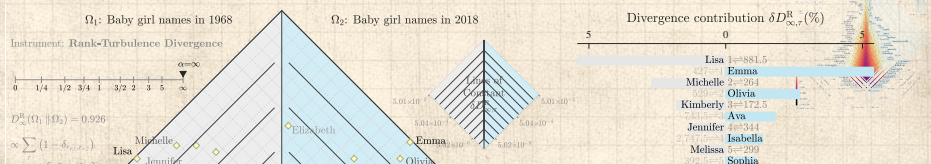


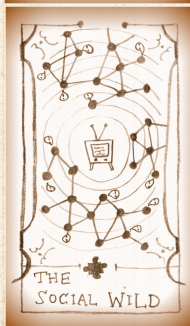
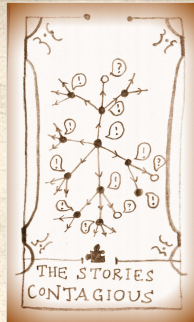
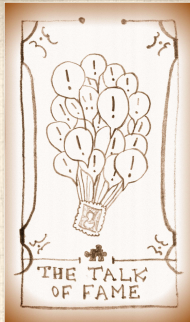
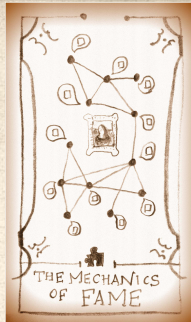
Claims, exaggerations, reminders:

- Needed for comparing large-scale complex systems:
 - Comprehensible, dynamically-adjusting, differential dashboards
- Many measures seem poorly motivated and largely unexamined (e.g., JSD)
- Of value: Combining big-picture maps with ranked lists
- Maybe one day: Online tunable version of rank-turbulence divergence (plus many other instruments)

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- A plenitude of distances
- Rank-turbulence divergence
- Probability-turbulence divergence
- Explorations
- Stories
- Mechanics of Fame
- Superspreading
- Lexical Ultrafame
- Turbulent times
- References





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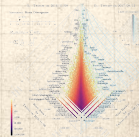
Mechanics of
Fame

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Lexical Ultrafame

Turbulent times

References



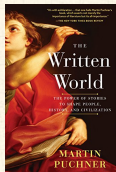
The everywhere-ness of algorithms and stories:



“On the Origin of Stories: Evolution, Cognition, and Fiction” [a](#) [↗](#)
by Brian Boyd (2010). ^[3]



“The Storytelling Animal: How Stories Make Us Human” [a](#) [↗](#)
by Jonathan Gottschall (2013). ^[17]



“The Written World: How Literature Shaped Civilization” [a](#) [↗](#)
by Martin Puchner (2017). ^[31]

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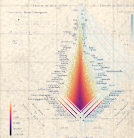
Mechanics of
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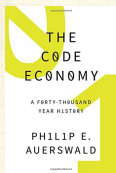
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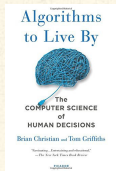


Algorithms, recipes, stories, ...



“The Code Economy: A Forty-Thousand Year History” [a](#)

by Philip E Auerswald (2017). ^[1]



“Algorithms to Live By” [a](#)

by Christian and Griffiths (2016). ^[7]



“Once Upon an Algorithm” [a](#)

by Martin Erwig (2017). ^[16]

Also: Numerical Recipes in C ^[30] and How to Bake π ^[5]

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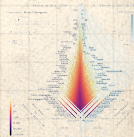
Mechanics of
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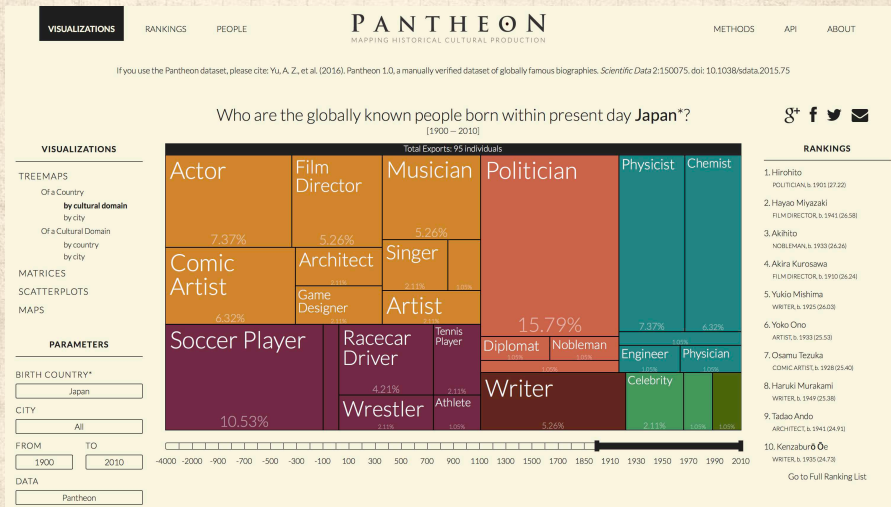
Lexical Ultrafame

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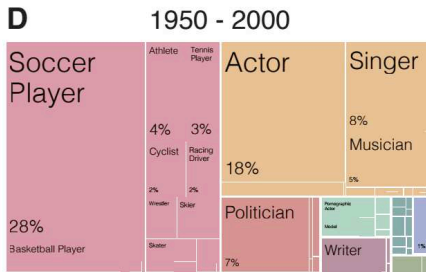
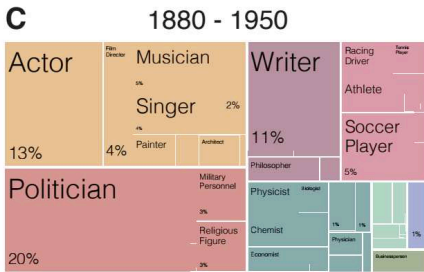
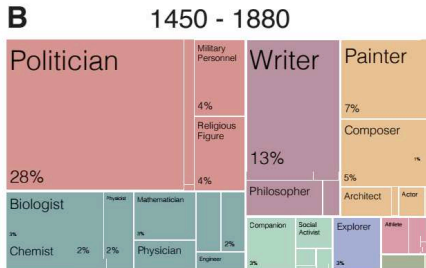
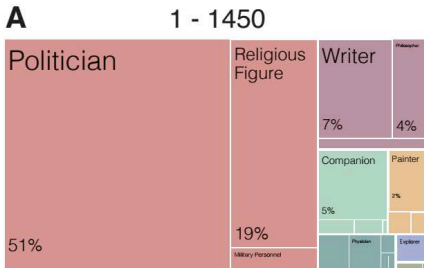


The famous are storytellers—Japan:






For people born 1950–


http://pantheon.media.mit.edu/treemap/country_exports/JP/all/1900/2010/H15/pantheon



Super Survival of the Stories:



-  Study of Agta, Filipino hunter-gatherers.
-  Storytelling valued well above all other skills including hunting.
-  Stories encode prosocial norms such as cooperation.

The Desirability
of
Storytellers ,
The Atlantic,
Ed Yong,
2017-12-05.

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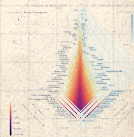
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Lexical Ultrafame





Turbulent times


References



Super Survival of the Stories:



-  Study of Agta, Filipino hunter-gatherers.
-  Storytelling valued well above all other skills including hunting.
-  Stories encode prosocial norms such as cooperation.
-  Like the best stories, the best storytellers reproduce more successfully.

The Desirability
of
Storytellers ,
The Atlantic,
Ed Yong,
2017-12-05.

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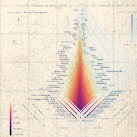
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The most famous painting in the world:



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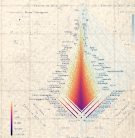
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The dismal predictive powers of editors

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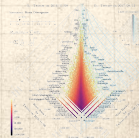
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Twelve ...



The completely unpredicted fall of Eastern Europe:



Timur Kuran: ^[20] "Now Out of Never: The Element of Surprise in the East European Revolution of 1989"

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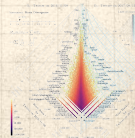
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We understand bushfire stories:



1. Sparks start fires.

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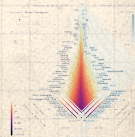
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We understand bushfire stories:



1. Sparks start fires.
2. System properties control a fire's spread.

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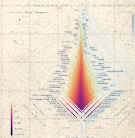
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We understand bushfire stories:



1. Sparks start fires.
2. System properties control a fire's spread.
3. But for three reasons, we make two mistakes about **Social Fires** ...

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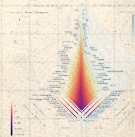
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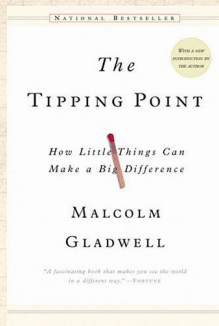
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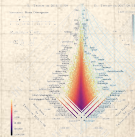
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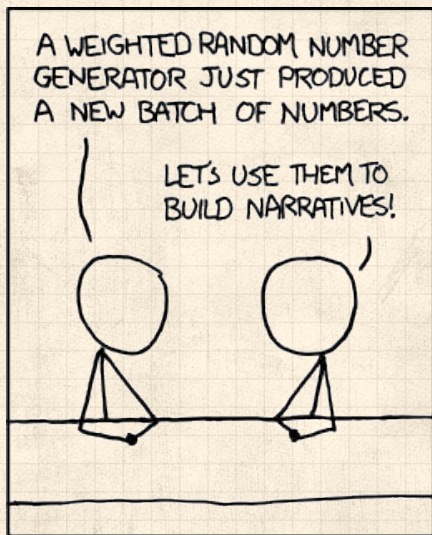
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Reason 1—We are Homo Narrativus.



ALL SPORTS COMMENTARY

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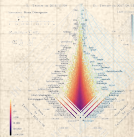
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Reason 2—"We are all individuals."

Archival footage:

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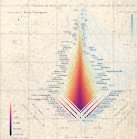
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Individual narratives are not enough to understand distributed, networked minds.



Reason 3—We are spectacular imitators.

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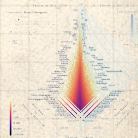
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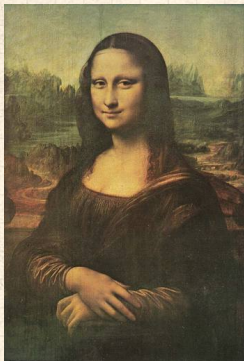
References

BBC/David Attenborough.



Mistake 1:

Success is due to intrinsic properties



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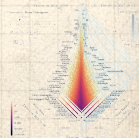
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See "Becoming Mona Lisa" by David Sassoon [↗](#)

Mistake 1: Success is due to intrinsic properties



it's just so disappointingly small

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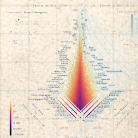
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See "Becoming Mona Lisa" by David Sassoon [↗](#)

Mistake 1: Success is due to intrinsic properties



Stolen in 1913, recovered in 1915.

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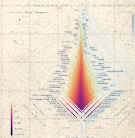
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See "Becoming Mona Lisa" by David Sassoon 

Mistake 1: Success is due to intrinsic properties



Hidden during WWII.

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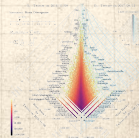
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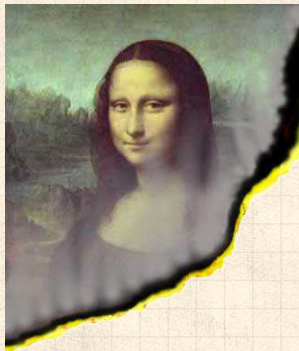
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See "Becoming Mona Lisa" by David Sassoon [↗](#)

Mistake 1: Success is due to intrinsic properties



Repeatedly vandalised and attacked. [↗](#)

See "Becoming Mona Lisa" by David Sassoon [↗](#)

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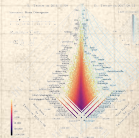
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48 songs
30k participants

Exp 1— weak social

	Exp 1 Mean	Std. Dev.	Exp 2 Mean	Std. Dev.
1. "MUSICALLY "Through it rough?"	20	12	15	10
2. "DEEP ENDING TO ONE "You're cool"	17	11	17	11
3. "THE WIMPY SPONGE "Cool friends"	16	10	17	11
4. "THE BRICKS PROMISE "You're not alone"	15	10	14	10
5. "NO MORE SAMS "You're not alone the answer?"	13	10	14	10
6. "NO MORE AT MY HOME "You're cool?"	9	9	10	10
7. "SOME SHARED "You're cool"	8	10	10	10
8. "NOT FROM BOSTON "You're not alone"	7	10	10	10
9. "SOME SAYS "You're not alone the answer?"	5	10	10	10
10. "PART OF MEAN "You're not alone the answer?"	5	10	10	10
11. "MUSICALLY UNUSUAL "You're not alone the answer?"	4	10	10	10
12. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
13. "SOMEONE WHO'S "You're not alone the answer?"	3	10	10	10
14. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
15. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
16. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
17. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
18. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
19. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
20. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
21. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
22. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
23. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
24. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
25. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
26. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
27. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
28. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
29. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
30. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
31. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
32. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
33. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
34. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
35. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
36. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
37. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10
38. "I CAN'T STOP "You're not alone the answer?"	3	10	10	10

Exp. 2—strong social

	Exp 1 Mean	Std. Dev.	Exp 2 Mean	Std. Dev.
1. "MUSICALLY "You're cool"	20	12	15	10
2. "DEEP ENDING TO ONE "You're cool"	17	11	17	11
3. "THE WIMPY SPONGE "Cool friends"	16	10	17	11
4. "THE BRICKS PROMISE "You're not alone"	15	10	14	10
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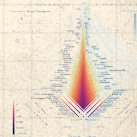
Turbulent times

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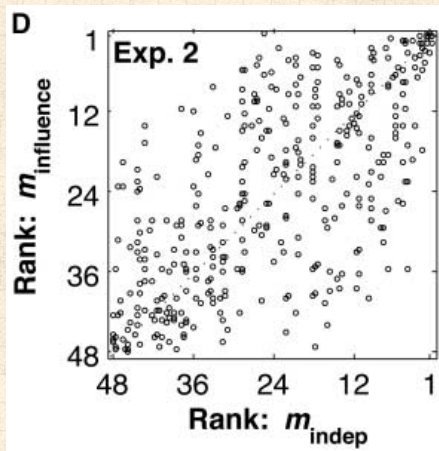


"An experimental study of inequality and unpredictability in an artificial cultural market" ↗

Salganik, Dodds, and Watts,
Science, **311**, 854–856, 2006. [32]



Resolving the paradox:



Increased social awareness leads to
Stronger inequality + Less predictability.

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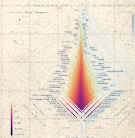
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Payola/Deceptive advertising hurts us all:

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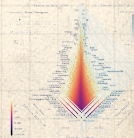
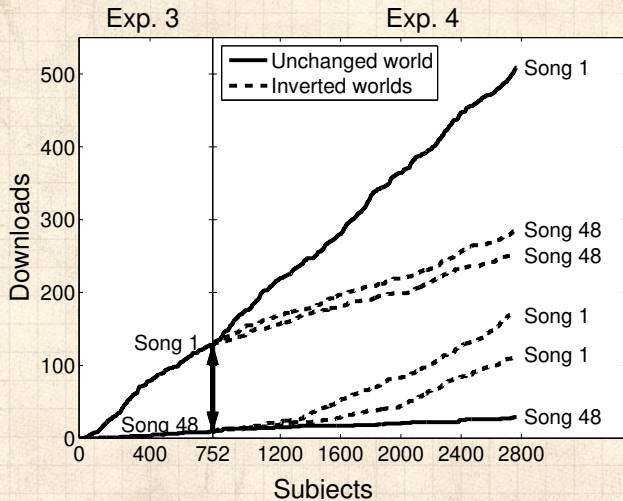
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“Mistake” 2:

Seeing success is ‘due to social’ and
wanting to say ‘all your interactions are
belong to us’



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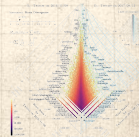
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"This is truly the last time, believe me"

The Washington Post

Business + Analysis



14 years of Mark Zuckerberg saying sorry, not sorry

By Geoffrey A. Fowler and Christy Etkin

Do you trust Mark Zuckerberg?

From the moment the Facebook founder entered the public eye in 2005 for creating a Harvard student hot-or-not rating site, he's been apologizing. So we collected this abbreviated history of his public mea culpas.

It reads like a record on repeat. Zuckerberg, who made "move fast and break things" his slogan, says sorry for being naive, and then promises solutions such as privacy "controls," "transparency" and better policy "enforcement." And then he promises it again the next time. You can track his [apologies to Congress](#) and [apologies to users](#) on the timeline below.

All the while, Facebook's access to our personal data increases and little changes about the way Zuckerberg handles it. So as Zuckerberg prepares to apologize for the first time in front of Congress, the question that lingers is: What will be different this time?

Robert Godwin Sr.

"Our **hearts go out** to the family and friends of Robert Godwin Sr., and we have a lot of work — and **we will keep doing all we can** to prevent tragedies like this from happening."



September 2017

While revealing a **rinse-and-repeat** plan to skip platforms from using Facebook to interfere in one another's elections, noting that the amount of "problematic content" found so far is "relatively small."

"I care deeply about the democratic process and protecting its integrity. ... It is a new challenge for internet communities to deal with



December 2007

After launching Beacon, which opted in everyone to sharing with advertisers what they were doing in outside websites and apps.

"We simply **did a bad job with this release, and I apologize for it. ... People need to be able to explicitly choose what they share.**"

February 2009

After unveiling new terms of service that angered users.

"Over the past couple of days, we received a lot of questions and comments. ... Based on this **feedback, we have decided to return to our previous terms of use** while we resolve the issues."

"We won't prevent all mistakes or abuse, but **we currently make too many errors** enforcing our policies and preventing misuse of our tools. ... **This will be a serious year of self-improvement** and I'm looking forward to learning from working to fix our issues together."

March 2018

After details emerged about Cambridge Analytica taking user data.

"We have a responsibility to **protect your data, and if we can't then we don't deserve to serve you. ... We will learn from this experience to secure our platform further and make our community safer** for everyone going forward."

Commission for deceiving consumers about privacy.

"I'm the first to admit that **we've made a bunch of mistakes. ... Facebook has always been committed to being transparent about the information you have stored with us — and we have led the internet in building tools to give people the ability to see and control what they share.**"



July 2014

After an academic paper exposed that Facebook conducted psychological tests on nearly 700,000 users without their knowledge. (Apology by Facebook COO Sheryl Sandberg)

"It was my mistake, and I'm sorry. ... There's more we can do here to **limit the information developers can access and put more safeguards in place** to prevent abuse."

Related stories

Facebook: Most users may have had public data 'scrapped'

Facebook COO Sheryl Sandberg on data leak: 'I am really sorry, we are late'

As Facebook confronts data misuse, foreign governments might force real change

What if we paid for Facebook — instead of letting it spy on us for free?

About this story

Photoillustrations based on photos by Tony Avelar/Bloomberg News, Drew Angerer/Getty Images, Jeff Blomquist/WI, Jeff Watney/Getty Images, Craig Ruttle/WI, Paul Sotomayor/WI, Stephen Lamy/Reuters, Jose Gomez/Reuters, Richard Drew/AP

233 Comments

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The Facebook ads Russians showed to different groups

Facebook has said these ads were created by the Internet

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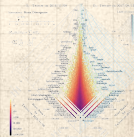
Mechanics of
Fame

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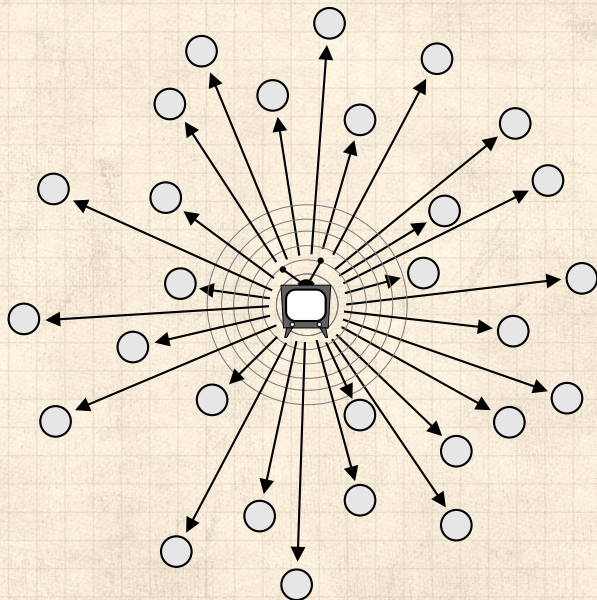
Lexical Ultrafame

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The hypodermic model of influence:



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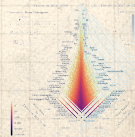
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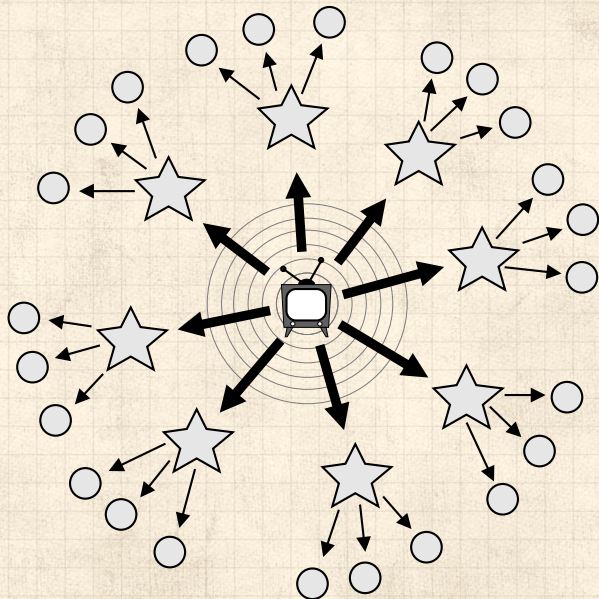
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The two step model of influence: [19]



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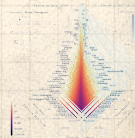
Mechanics of
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Superspreading

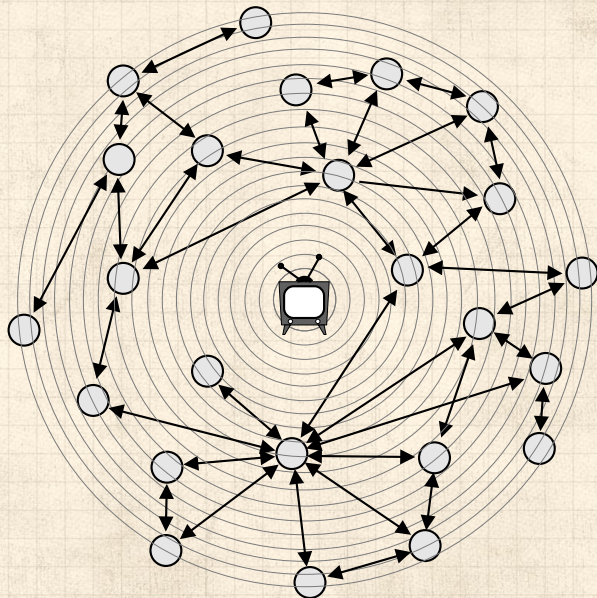
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The network model of influence:



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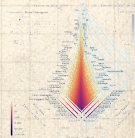
Mechanics of
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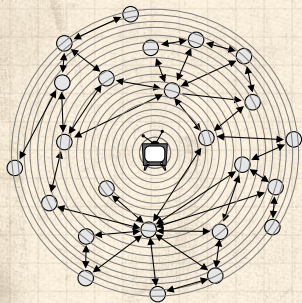
Lexical Ultrafame

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The network model of influence:



How superspreading works:

Many interconnected, average, trusting people must benefit from both **receiving** and **sharing** a message far from its source.



"Influentials, Networks, and Public Opinion Formation" 

Watts and Dodds,

J. Consum. Res., **34**, 441–458, 2007. ^[37]

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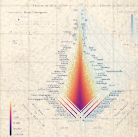
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Etymological clarity:

 **Fate**—from the Latin *fatus*: meaning “spoken”.

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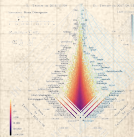
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“It is written”, fore-tell, pre-dict.

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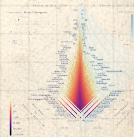
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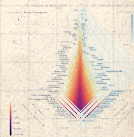
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 Destiny is probablistic.

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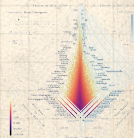
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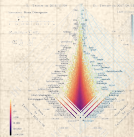
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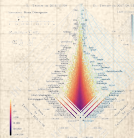
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 Fame is inherently the social discussion about the thing, not the thing itself.





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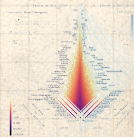
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
 “There is no such thing as fate, only the story of fate.” 

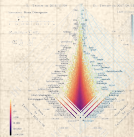
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 Réclame . “Clamo”—Proto-Indo-European: “to shout” (again).






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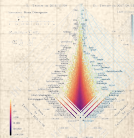
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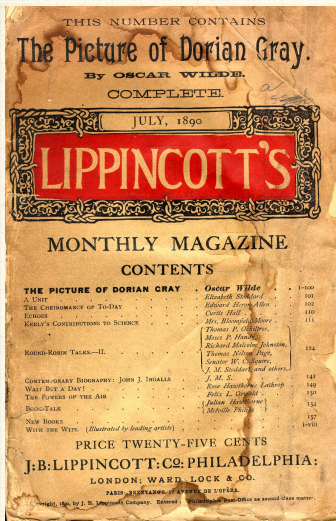
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 Réclame . “Clamo”—Proto-Indo-European: “to shout” (again). Connected to “lowing”.



Oscar Wilde, The Picture of Dorian Gray: Raw Fame



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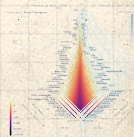
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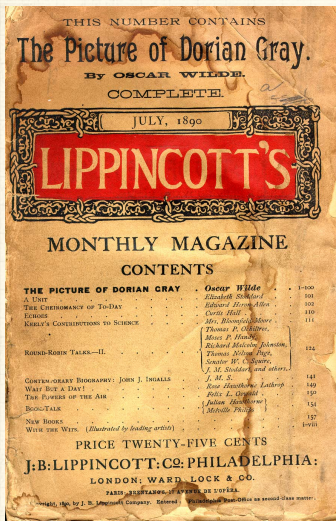
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“There is only one thing in the world

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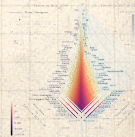
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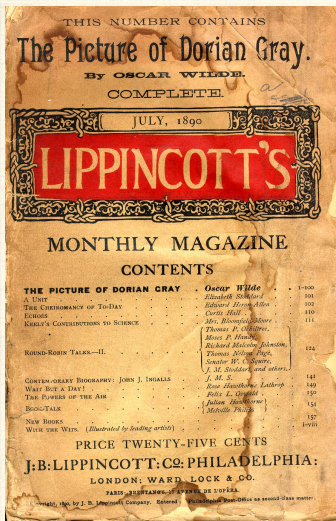
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“There is only one thing in the world worse than being talked about, and that is

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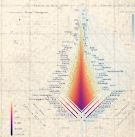
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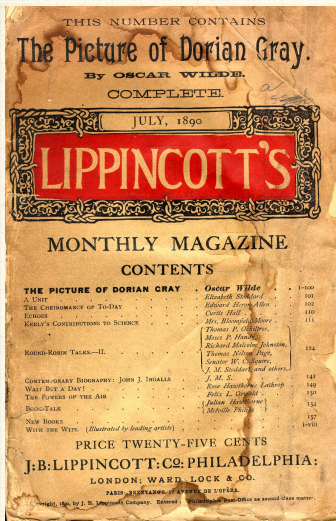
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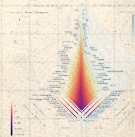
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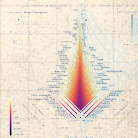
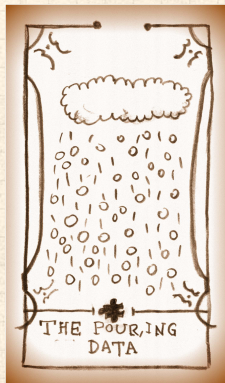
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“Fame and Ultrafame: Measuring and comparing daily levels of ‘being talked about’ for United States’ presidents, their rivals, God, countries, and K-pop”

Dodds et al.,

Available online at

<https://arxiv.org/abs/1910.00149>, 2019. [12]



“Computational timeline reconstruction of the stories surrounding Trump: Story turbulence, narrative control, and collective chronopathy”

Dodds et al.,

, 2020. [14]



POTUSometer with the Smorgasdashbord:

<http://compstorylab.org/potusometer/>



Stories surrounding Trump:

<http://compstorylab.org/trumpstoryturbulence/>

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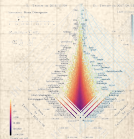
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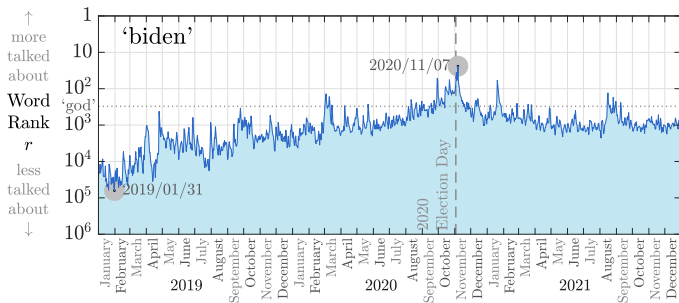
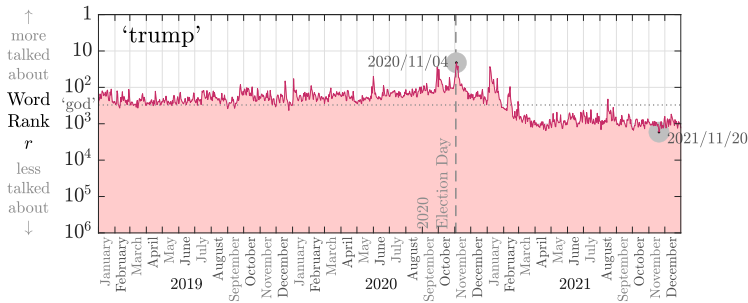
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Ultrafame: Nobody expects the Spanish Inquisition K-pop:



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Vox (2019-04-17):
[BTS, the band that changed K-pop, explained](#) 



Distant reading by smashing texts into storyons:

```
cd ~/work/stories/2019-10story-turbulence-trump/  
261G
```

```
more updateall.sh
```

```
file names:
```

```
compute_rank_turbulence_divergence_sweep_the_leg
```

```
Zip files:
```

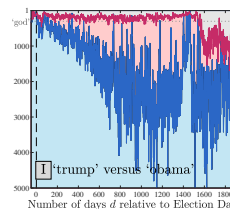
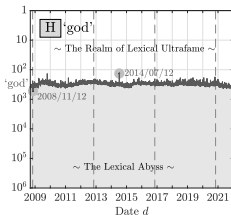
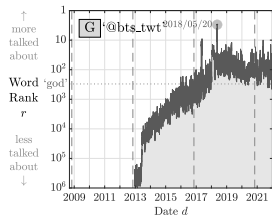
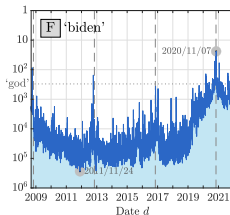
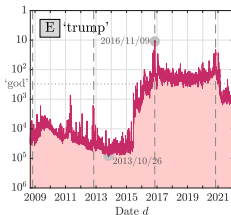
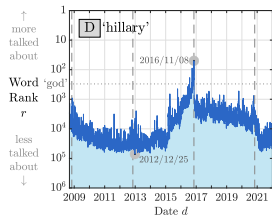
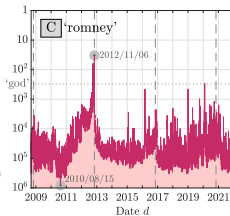
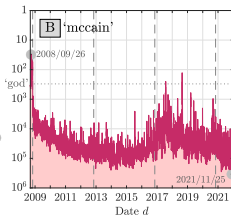
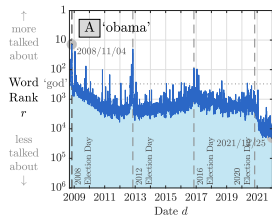
```
zless 2018-01-06/1grams/en_*.tar.tsv
```

```
zless 2021-01-05/1grams/en_*.tar.tsv
```

```
zless 2021-01-06/1grams/en_*.tar.tsv
```

```
zless 2021-01-07/1grams/en_*.tar.tsv
```

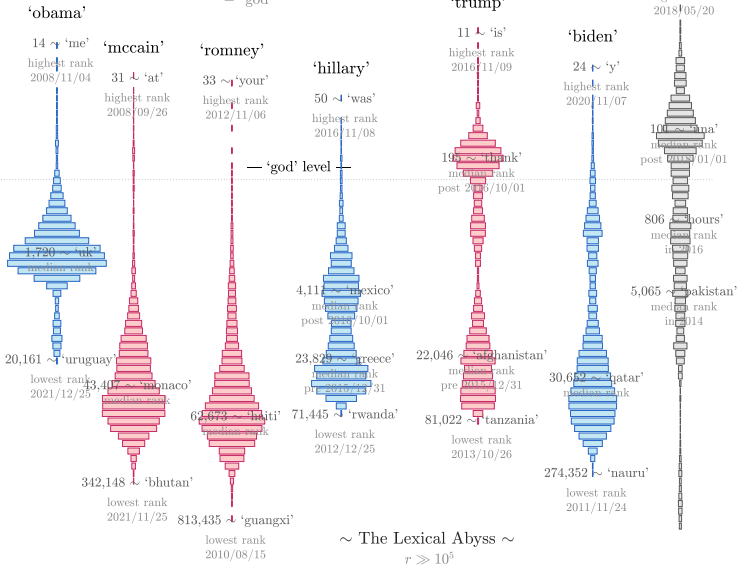






~ The Realm of Lexical Ultraframe ~

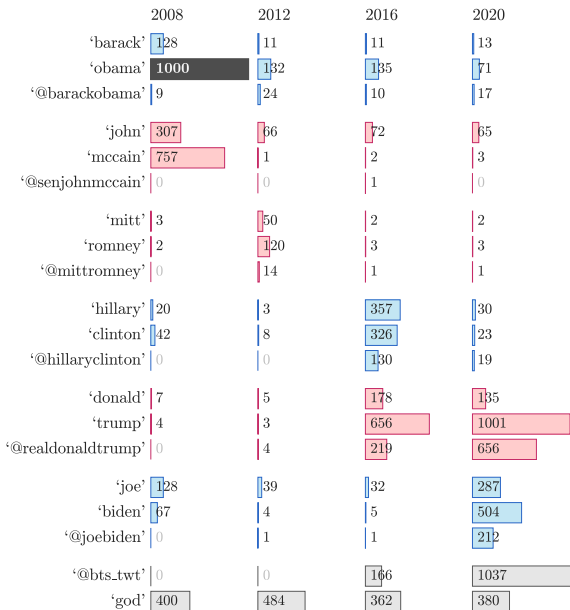
$r \leq r_{\text{god}} = 303$



Ultrafame—Percentage of days per year ranked above 'god'

	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021
'barack'	1.8%	0.3%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%
'obama'	54.4%	6.9%	0.5%	0.5%	2.2%	0.3%	0.0%	0.3%	2.2%	2.2%	0.5%	0.0%	0.3%	0.0%
'@barackobama'	0.0%	0.0%	0.0%	0.0%	0.5%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%
'john'	3.5%	0.6%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.3%	0.8%	0.3%	0.5%	0.0%
'mccain'	39.5%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.3%	1.1%	0.0%	0.0%	0.0%
'@senjohnmccain'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%
'mitt'	0.0%	0.0%	0.0%	0.0%	0.8%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%
'romney'	0.0%	0.0%	0.0%	0.0%	1.6%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.3%	0.0%
'@mittromney'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%
'hillary'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	10.4%	0.0%	0.0%	0.0%	0.0%	0.0%
'clinton'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	7.7%	0.0%	0.0%	0.0%	0.0%	0.0%
'@hillaryclinton'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	1.1%	0.0%	0.0%	0.0%	0.0%	0.0%
'donald'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	2.7%	0.5%	0.0%	0.0%	1.6%	0.6%
'trump'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.5%	47.8%	98.6%	93.7%	92.3%	100.0%	10.2%
'@realdonaldtrump'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	2.7%	26.8%	41.4%	62.7%	90.2%	2.2%
'joe'	3.5%	2.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	8.2%	0.6%
'biden'	1.8%	0.0%	0.0%	0.0%	0.3%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	23.8%	6.1%
'@joebiden'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	4.1%	0.3%
'@bts_twt'	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.5%	8.5%	50.7%	100.0%	100.0%	98.9%	93.1%

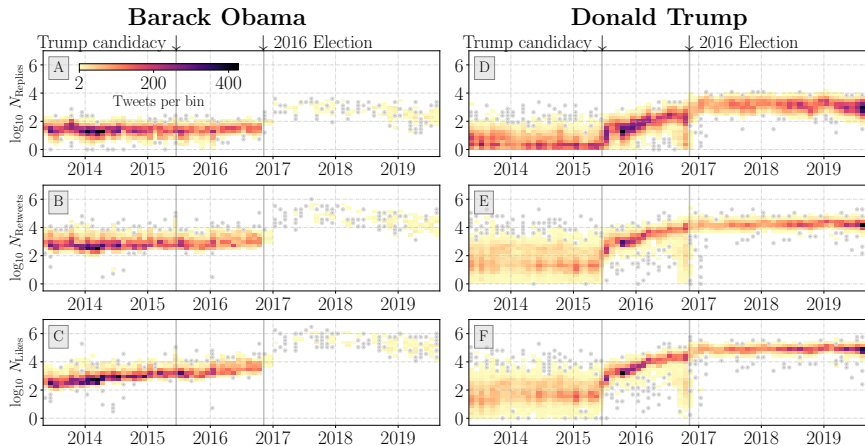
Relative median rates of ‘being talked about’
in the 8 weeks (56 days) pre-election day:



Relative median rates of 'being talked about' per year:

	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021
'barack'	50	38	17	9	10	7	8	11	14	15	14	14	19	3
'obama'	897	379	52	87	97	79	91	103	56	60	129	106	104	17
'@barackobama'	10	8	11	10	17	15	16	13	13	17	17	13	24	5
'john'	405	274	88	26	117	104	113	121	118	29	28	114	108	82
'mccain'	579	11	4	2	2	2	1	1	3	15	7	5	3	2
'@senjohnmccain'	0	2	1	0	0	1	1	1	1	9	2	0	0	0
'mitt'	5	8	5	6	25	6	5	4	4	2	2	3	3	2
'romney'	3	1	1	4	42	2	1	1	4	1	1	3	4	1
'@mittromney'	0	0	0	0	5	0	0	0	1	0	0	1	1	0
'hillary'	28	10	5	3	3	4	6	30	69	72	61	43	33	6
'clinton'	62	25	16	10	8	6	8	27	40	65	62	45	32	8
'@hillaryclinton'	0	0	0	0	0	0	1	11	71	22	19	21	23	3
'donald'	11	17	11	11	8	6	7	44	66	45	14	104	143	43
'trump'	7	20	10	7	4	3	3	77	583	1000	865	808	1134	229
'@realdonaldtrump'	0	0	0	1	2	3	2	32	219	468	555	652	888	1
'joe'	57	87	38	87	66	58	44	46	50	48	44	78	97	117
'biden'	72	7	3	1	2	2	2	3	5	3	4	52	284	221
'@joebiden'	0	0	0	0	0	0	0	0	1	1	2	18	62	28
'@bts_twt'	0	0	0	0	0	5	36	23	242	595	2487	1802	1440	1437
'god'	666	851	687	694	791	719	607	616	601	590	612	611	612	510

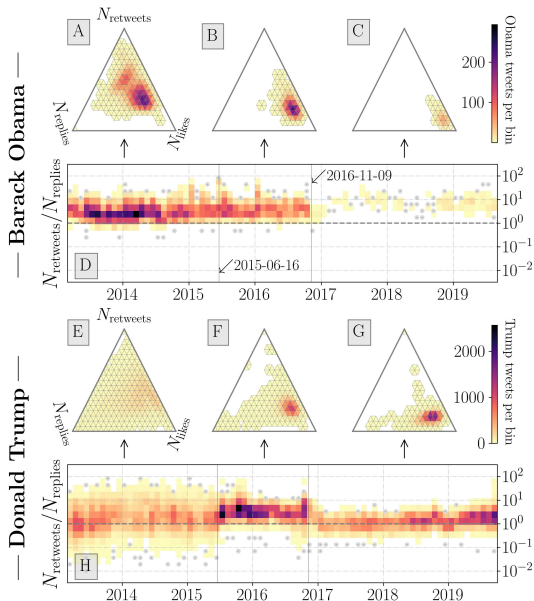
Ratiometrics:



“Ratiometric the President: An exploration of public engagement with Obama and Trump on Twitter,”

Minot et al., 2020 [24]

Ratiometrics:



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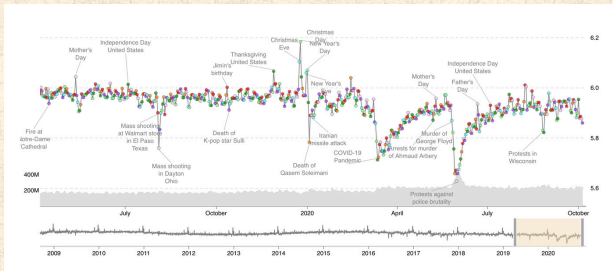
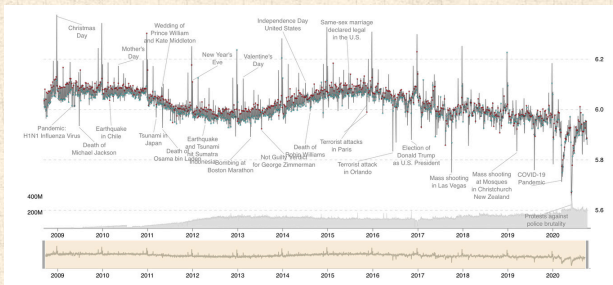
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Emotional turbulence:



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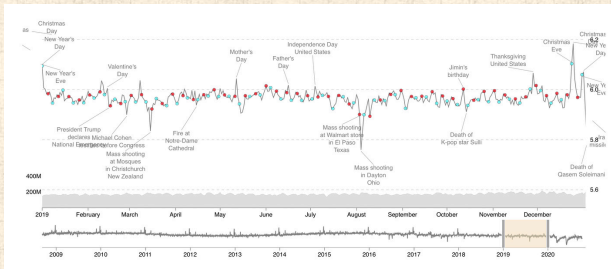
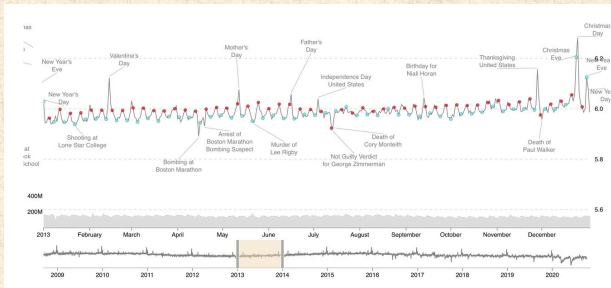
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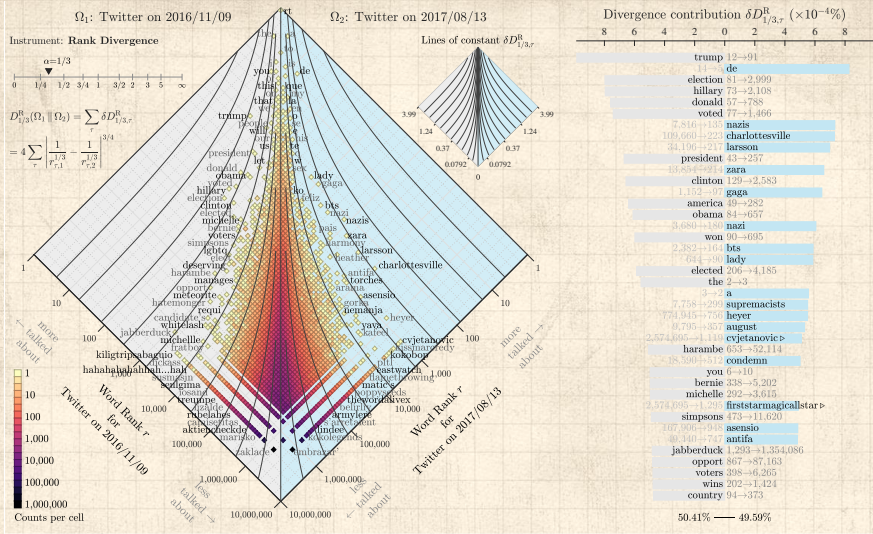
Superspreading

Lexical Ultrafame

Turbulent times

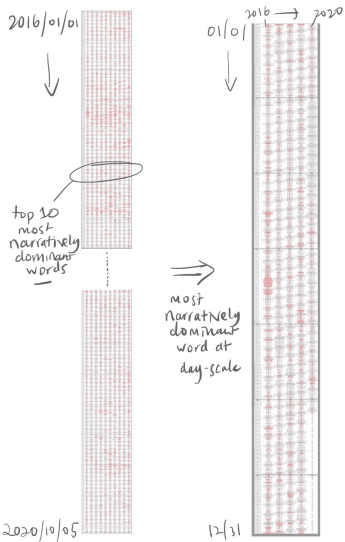
References





Allotaxonomy—
the comparison of complex systems:

<http://compstoriolab.org/allotaxonomy/>



Week	2016	2017	2018	2019	2020
1. 01/01-01/07	Hillary 34.7	hacking 28.6	Bannon 2.2	shutdown 0.0	Iraq 9.6
2. 01/08-01/14	Cruz 1.0	Mercy 5.0	Mueller 0.0	shutdown 0.0	Soleimani 5.9
3. 01/15-01/21	Cruz 10.7	inauguration 0.6	DACA 6.7	Pelosi 6.8	Parnas 0.0
4. 01/22-01/28	Cruz 10.6	inauguration 3.1	Mueller 0.0	Pelosi 2.6	Ukraine 5.5
5. 01/29-02/04	Cruz 11.2	ban 2.1	Mueller 0.0	border 0.0	impeachment 0.0
6. 02/05-02/11	Cruz 5.1	Bannon 0.0	memo 2.3	Whitaker 0.0	Vindjanj 2.5
7. 02/12-02/18	Cruz 6.9	Flynn 0.0	Mueller 0.0	emergency 0.0	Bar 2.2
8. 02/19-02/25	Rubio 3.8	Sweden 4.9	Parkland 0.3	Jussie 0.0	Bloomberg 6.3
9. 02/26-03/04	Rubio 9.2	Russia 6.4	Mueller 0.0	Cohen 3.7	coronavirus 0.0
10. 03/05-03/11	Cruz 1.0	Russia 4.8	Mueller 0.0	Nudge 13.7	coronavirus 0.0
11. 03/12-03/18	Cruz 5.7	tax 1.8	Mueller 2.2	emergency 1.6	coronavirus 0.0
12. 03/19-03/25	Arizona 16.8	Nunes 0.0	Mueller 2.2	Barr 0.0	coronavirus 0.0
13. 03/26-04/01	women 8.3	Russia 9.9	Stormy 0.0	Schiff 5.2	coronavirus 0.5
14. 04/02-04/08	Cruz 1.5	Russia 2.8	Mueller 0.0	returns 0.0	coronavirus 0.0
15. 04/09-04/15	Cruz 1.7	Syria 0.4	Mueller 2.0	Bar 2.4	coronavirus 0.0
16. 04/16-04/22	Cruz 10.5	Russia 0.5	Mueller 0.1	Bar 0.1	coronavirus 0.0
17. 04/23-04/29	Cruz 3.0	days 0.1	Kanye 8.0	Biden 6.0	coronavirus 0.0
18. 04/30-05/06	Indiana 11.5	Trumpcare 0.0	Mueller 0.0	Bar 0.0	coronavirus 0.0
19. 05/07-05/13	Ryan 2.5	Comet 2.8	Iraq 6.6	Bar 0.0	coronavirus 0.0
20. 05/14-05/20	Boris 25.3	Comet 1.0	ZTE 4.5	Bar 0.0	coronavirus 0.0
21. 05/21-05/27	Clinton 9.5	budget 0.0	Korea 18.2	Bar 0.0	pasdemie 0.0
22. 05/28-06/03	Hillary 11.9	Katly 4.4	Roseanne 4.0	USS 3.0	Minneapolis 32.1
23. 06/04-06/10	Clinton 11.1	Comet 0.8	parson 0.0	Memo 27.6	police 4.2
24. 06/11-06/17	Orlando 12.4	Mueller 0.0	Kin 4.1	foreign 2.0	Tuba 4.5
25. 06/18-06/24	Hillary 23.9	Trumpcare 0.0	children 1.0	Iraq 12.9	Tuba 2.1
26. 06/25-07/01	Clinton 13.0	Russia 5.8	Justice 8.3	Moos 29.9	bounties 0.0
27. 07/02-07/08	Cooked 80.6	CNN 0.0	toeddlers 0.0	parade 0.0	Rushmore 2.3
28. 07/09-07/15	Cooked 71.5	Russian 1.2	NATO 13.0	Epstein 0.0	coronavirus 0.0
29. 07/16-07/22	Penet 2.9	Mueller 0.0	Helmski 3.1	nazi 0.8	coronavirus 0.0
30. 07/23-07/29	DNC 6.1	Scouts 0.0	Cohen 0.0	Baltimore 13.6	Portland 11.8
31. 07/30-08/05	Khan 6.5	Mueller 0.0	LeBron 0.7	Baltimore 9.4	pasdemie 0.0
32. 08/06-08/12	Cooked 55.2	Kore 5.8	Omarosa 0.4	Past 7.6	USPS 0.0
33. 08/13-08/19	Manufact 0.0	Charlotteville 1.5	Omarosa 9.5	Greenland 6.9	USPS 0.0
34. 08/20-08/26	Clinton 7.6	Charlotteville 3.8	Cohen 2.7	Greenland 8.0	Biden 6.6
35. 08/27-09/02	Cooked 57.4	Harvey 0.0	Oh 14.0	Dorian 12.2	Kerzhals 9.5
36. 09/03-09/09	Boudi 0.0	DACA 2.4	Kavanaugh 2.1	Dustin 12.6	Atlantic 4.8
37. 09/10-09/16	deplorable 0.0	ESPN 2.7	Puerto 7.5	flavored 0.0	Woodward 2.6
38. 09/17-09/23	Clinton 6.5	Kin 4.9	Kavanaugh 1.7	Kavanaugh 4.5	coronavirus 0.0
39. 09/24-09/30	debate 4.9	Puerto 4.7	Kavanaugh 9.5	Ukraine 6.8	ballots 0.7
40. 10/01-10/07	Penet 4.9	Puerto 2.1	Kavanaugh 6.8	Ukraine 5.1	Covid 0.0
41. 10/08-10/14	sexual 0.3	Puerto 1.8	Kavanaugh 4.3	Kurfs 8.2	
42. 10/15-10/21	rigged 10.1	Puerto 0.2	Puerto 5.3	Kurfs 3.7	
43. 10/22-10/28	star 0.0	Mueller 0.0	Mueller 0.0	caravan 0.0	impeachment 0.0
44. 10/29-11/04	FBI 5.9	Mueller 0.0	caravan 0.0	impeachment 0.0	impeachment 0.0
45. 11/05-11/11	Clinton 0.9	Gillette 12.0	Whitaker 6.2	Ukraine 6.2	Ukraine 5.2
46. 11/12-11/18	Bannon 0.0	sexual 1.7	caravan 0.0	Ukraine 5.2	Ukraine 3.5
47. 11/19-11/25	Hamtop 12.4	LaVar 21.3	Sundi 1.6	Moore 0.0	impeachment 0.0
48. 11/26-11/29	recount 0.0	Moore 0.0	Moore 0.0	Cohen 2.1	impeachment 0.0
49. 12/03-12/09	Taxen 7.8	Mueller 0.0	Cohen 2.1	Cohen 6.9	impeachment 0.0
50. 12/10-12/16	Russia 2.9	Mueller 0.0	wall 9.8	impeachment 1.4	impeachment 1.4
51. 12/17-12/23	inauguration 11.8	Mueller 0.0	wall 20.4	impeachment 1.4	impeachment 1.4
52. 12/24-12/31	inauguration 3.2	Mueller 0.0			

narrative control

Week	2016	2017	2018	2019	2020	2021
1. 01/01-01/07	Hillary 34.7	hacking 28.6	Bannon 2.2	shutdown 0.0	Iran 9.6	Georgia 14.7
2. 01/08-01/14	Cruz 1.0	Meryl 5.0	Mueller 0.0	shutdown 0.0	Soleimani 5.9	Capitol 0.1
3. 01/15-01/21	Cruz 10.7	inauguration 3.6	DACA 6.7	Pelosi 6.8	Parnas 0.0	Capitol 0.0
4. 01/22-01/28	Cruz 10.6	inauguration 3.1	Mueller 0.0	Pelosi 2.6	Ukraine 5.5	insurrection 0.0
5. 01/29-02/04	Cruz 11.2	ban 2.1	Mueller 0.0	border 0.0	impeachment 0.0	Greene 0.0
6. 02/05-02/11	Cruz 5.1	Bannon 0.0	memo 2.3	Whitaker 0.0	Vindman 2.5	insurrection 0.0
7. 02/12-02/18	Cruz 6.9	Flynn 0.0	Mueller 0.0	emergency 0.0	Barr 2.2	Capitol 0.0
8. 02/19-02/25	Rubio 3.8	Sweden 4.9	Parkland 0.3	Jussie 0.0	Bloomberg 6.3	Capitol 0.0
9. 02/26-03/04	Rubio 9.2	Russia 6.4	Mueller 0.0	Cohen 3.7	coronavirus 0.0	Capitol 0.0
10. 03/05-03/11	Cruz 1.0	Russian 4.8	Mueller 0.0	Nadler 13.7	coronavirus 0.0	insurrection 0.0
11. 03/12-03/18	Cruz 5.7	tax 1.8	Mueller 2.2	emergency 1.6	coronavirus 0.0	Biden 0.0
12. 03/19-03/25	Arizona 16.8	Nunes 0.0	Mueller 2.2	Barr 0.0	coronavirus 0.0	Biden 0.0
13. 03/26-04/01	women 8.3	Russia 9.9	Stormy 0.0	Schiff 5.2	coronavirus 0.5	Capitol 0.0
14. 04/02-04/08	Cruz 1.5	Russia 2.8	Mueller 0.0	returns 0.0	coronavirus 0.0	Matt 0.0
15. 04/09-04/15	Cruz 1.7	Syria 4.0	Mueller 2.0	Barf 2.4	coronavirus 0.0	Capitol 0.0
16. 04/16-04/22	Cruz 10.5	Russia 0.5	Mueller 0.1	Barr 0.1	coronavirus 0.0	Capitol 0.0
17. 04/23-04/29	Cruz 3.0	days 0.1	Kanye 8.0	Biden 6.0	coronavirus 0.0	audit 0.0
18. 04/30-05/06	Indiana 11.5	Trumpcare 0.0	Mueller 0.0	Barr 0.0	coronavirus 0.0	Cheeny 0.0
19. 05/07-05/13	Ryan 2.5	Comey 2.8	Iran 6.6	Barr 0.0	coronavirus 0.0	Cheeny 0.0
20. 05/14-05/20	Bernie 25.3	Comey 1.0	ZTE 4.5	Barr 0.0	coronavirus 0.0	Cheeny 0.0
21. 05/21-05/27	Clinton 9.5	budget 0.0	Korea 18.2	Barr 0.0	pandemic 0.0	Weisselberg 0.0
22. 05/28-06/03	Hillary 11.9	Kathy 4.4	Roseanne 4.0	USS 3.0	Minneapolis 32.1	reinstated 0.0
23. 06/04-06/10	Clinton 11.1	Comey 0.8	pardon 0.0	Mexico 27.6	police 4.2	McGahn 0.0
24. 06/11-06/17	Orlando 12.4	Mueller 0.0	Kim 4.1	foreign 2.0	Tulsa 4.5	DOJ 0.0
25. 06/18-06/24	Hillary 23.9	Trumpcare 0.0	children 1.0	Iran 12.9	Tulsa 2.1	Capitol 0.0
26. 06/25-07/01	Clinton 13.0	Russia 5.8	Justice 8.3	Moon 29.9	bounties 0.0	Organization 0.0
27. 07/02-07/08	Crooked 80.6	CNN 0.7	toddlers 0.0	parade 0.0	Rushmore 2.3	Weisselberg 0.0
28. 07/09-07/15	Crooked 71.5	Russian 1.2	NATO 13.0	Epstein 0.0	coronavirus 0.0	CPAC 0.0
29. 07/16-07/22	Pence 2.9	Mueller 0.0	Helsinki 3.1	racist 0.8	coronavirus 0.0	vaccinated 0.0
30. 07/23-07/29	DNC 6.1	Scouts 0.0	Cohen 0.0	Baltimore 13.6	Portland 11.8	Jan 0.0
31. 07/30-08/05	Khan 6.5	Mueller 0.0	LeBron 0.7	Baltimore 9.4	pandemic 0.0	Capitol 0.0
32. 08/06-08/12	Crooked 55.2	Korea 5.8	Omarosa 0.4	Paso 7.6	USPS 0.0	Rosen 0.0
33. 08/13-08/19	Manafort 0.7	Charlottesville 1.5	Omarosa 9.5	Greenland 6.9	USPS 0.0	Taliban 0.0
34. 08/20-08/26	Clinton 7.6	Charlottesville 3.8	Cohen 2.7	Greenland 8.0	Biden 6.6	Taliban 0.0
35. 08/27-09/02	Crooked 57.4	Harvey 0.0	Ohr 14.0	Dorian 12.2	Kenosha 9.5	Taliban 0.0
36. 09/03-09/09	Bondi 0.0	DACA 2.4	Kavanaugh 2.1	Dorian 12.6	Atlantic 4.8	Afghanistan 0.0
37. 09/10-09/16	deplorable 0.0	ESPN 2.7	Puerto 7.5	flavored 0.0	Woodward 2.6	Millie 0.0
38. 09/17-09/23	Clinton 6.5	Kim 4.9	Kavanaugh 1.7	Ukraine 4.5	coronavirus 0.0	Eastman 0.0
39. 09/24-09/30	debate 4.9	Puerto 4.7	Kavanaugh 9.5	Ukraine 6.8	ballots 0.7	audit 0.0
40. 10/01-10/07	Pence 4.9	Puerto 2.1	Kavanaugh 9.8	Ukraine 5.1	Covid 1.4	Bannon 0.0
41. 10/08-10/14	sexual 0.3	Puerto 1.8	Kavanaugh 4.3	Kurds 8.2	COVID 1.4	Jan 0.0
42. 10/15-10/21	rigged 10.1	Puerto 0.2	Saudi 5.3	Kurds 3.7	Biden 8.2	Powell 0.0
43. 10/22-10/28	star 0.0	Mueller 0.0	caravan 0.0	impeachment 0.0	Biden 9.2	Jan 0.0
44. 10/29-11/04	FBI 5.9	Mueller 0.0	caravan 0.0	impeachment 0.0	Biden 10.0	Youngkin 0.0
45. 11/05-11/11	Clinton 0.9	Gillespie 12.0	Whitaker 6.2	Ukraine 6.2	votes 3.4	infrastructure 0.0
46. 11/12-11/18	Bannon 0.0	sexual 1.7	caravan 0.0	Ukraine 5.2	Dominion 23.2	Christie 0.0
47. 11/19-11/25	Hamilton 12.4	LaVar 21.3	Saudi 1.6	Ukraine 3.5	Sidney 0.1	Rittenhouse 0.0
48. 11/26-12/02	recount 0.0	Moore 0.0	Moscow 0.1	impeachment 3.1	votes 24.1	Waukesha 0.0
49. 12/03-12/09	Taiwan 7.8	Mueller 0.0	Cohen 2.1	impeachment 0.0	Georgia 20.2	Meadows 0.0
50. 12/10-12/16	Russia 2.9	Mueller 0.0	Cohen 6.9	impeachment 0.0	vaccine 11.1	Meadows 0.0
51. 12/17-12/23	inauguration 11.8	Mueller 0.0	wall 9.8	impeachment 1.4	vaccine 15.4	Manchin 0.0
52. 12/24-12/31	inauguration 3.2	Mueller 0.0	wall 20.4	impeachment 7.6	Election 60.2	Brandon 0.0

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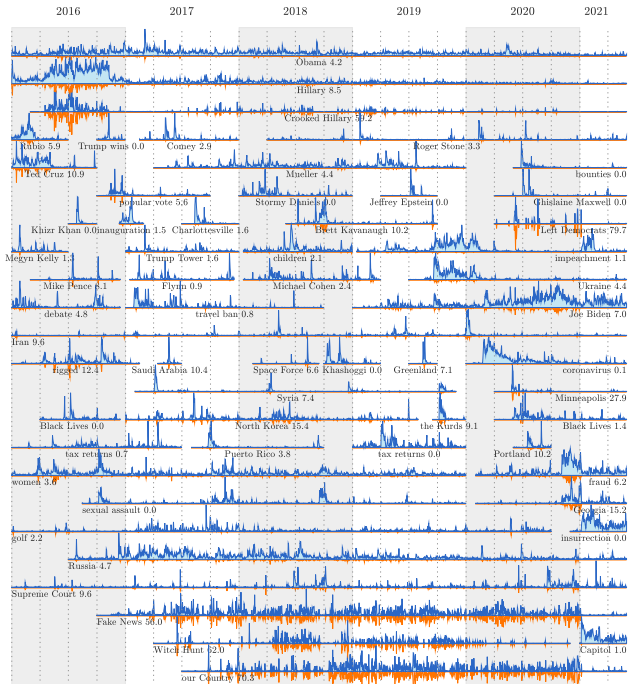
Lexical Ultrafame

Turbulent times

References

Week	2016	2017	2018	2019	2020	2021
1. 01/01-01/07	Hillary Clinton 32.7	plant in 85.1	Steve Bannon 5.7	the government 0.0	a war 6.6	in Georgia 20.2
2. 01/08-01/14	Trump rally 0.0	Meryl Streep 6.6	shithole countries 0.0	the border 1.0	impeachment trial 0.0	the Capitol 0.0
3. 01/15-01/21	Ted Cruz 26.0	Trump's inauguration 0.0	the government 1.4	Cohen to 0.0	impeachment trial 0.0	the Capitol 0.0
4. 01/22-01/28	Megyn Kelly 4.9	executive order 0.0	the FBI 5.6	the government 0.0	impeachment trial 0.0	the Capitol 0.0
5. 01/29-02/04	Ted Cruz 19.7	travel ban 1.6	the FBI 9.4	Ralph Northam 26.0	impeachment trial 0.0	the Capitol 0.0
6. 02/05-02/11	New Hampshire 19.5	travel ban 1.1	military parade 0.0	El Paso 4.7	Alexander Vindman 7.0	the Capitol 0.0
7. 02/12-02/18	Ted Cruz 15.7	Michael Flynn 0.0	school shooting 3.1	national emergency 0.0	Roger Stone 4.0	the Capitol 0.0
8. 02/19-02/25	Ted Cruz 30.1	Trump administration 0.0	the NRA 0.0	Jussie Smollett 0.0	Bernie Sanders 13.6	the Capitol 0.0
9. 02/26-03/04		to Russia 22.0	Hope Hicks 0.0	Michael Cohen 5.3	the coronavirus 0.0	the Capitol 0.0
10. 03/05-03/11		travel ban 0.0	Stormy Daniels 0.0	Tim Apple 0.0	the coronavirus 0.0	voted for 0.0
11. 03/12-03/18		Meals on 0.1	Stormy Daniels 0.0	New Zealand 17.9	the coronavirus 0.0	Lara Trump 0.0
12. 03/19-03/25	Lynin' Ted 66.2	health care 0.0	Cambridge Analytics 0.0	Mueller report 0.0	the coronavirus 0.0	the border 0.0
13. 03/26-04/01	Trump is 0.0	Freedom Caucus 20.8	Stormy Daniels 0.0	Mueller report 0.0	the coronavirus 0.0	Matt Gaetz 0.0
14. 04/02-04/08	Ted Cruz 3.9	Susan Rice 0.3	National Guard 0.0	tax returns 0.0	the coronavirus 0.0	Matt Gaetz 0.0
15. 04/09-04/15	New York 19.3	in Syria 0.2	Michael Cohen 0.0	sanctuary cities 5.3	the coronavirus 0.0	Matt Gaetz 0.0
16. 04/16-04/22	Ted Cruz 28.1	turnout for 0.0	Michael Cohen 2.4	Mueller report 0.0	the coronavirus 0.0	Maxine Waters 0.0
17. 04/23-04/29	Trump rally 0.0	tax plan 0.0	the Korean 0.0	Mueller report 0.0	the coronavirus 0.0	Liz Cheney 0.0
18. 04/30-05/06	Ted Cruz 5.5	health care 0.0	Stormy Daniels 0.0	Mueller report 0.0	treated worse 0.0	Liz Cheney 0.0
19. 05/07-05/13	Paul Ryan 2.0	James Comey 6.7	the Iran 9.0	tax returns 0.0	tested positive 0.0	Liz Cheney 0.0
20. 05/14-05/20	Hillary Clinton 26.5	Saudi Arabia 12.5	are animals 0.0	Lindsay Graham 0.0	the pandemic 0.0	Kevin McCarthy 0.0
21. 05/21-05/27	Hillary Clinton 24.8	Saudi Arabia 8.2	the FBI 23.3	Rance Polosi 12.5	a mask 6.3	the January 0.0
22. 05/28-06/03	Trump University 3.4	Kathy Griffin 5.7	Samantha Bee 4.4	John McCain 0.0	photo op 0.0	Memorial Day 0.0
23. 06/04-06/10	Hillary Clinton 18.6	James Comey 0.2	Justin Trudeau 8.5	with Mexico 39.2	Left Democrats 75.1	Jean Carroll 0.0
24. 06/11-06/17	Trump is 0.0	obstruction of 12.6	their parents 0.0	the FBI 8.5	in Tulsa 7.4	Trump DOJ 0.0
25. 06/18-06/24	Hillary Clinton 20.6	Karen Handel 16.6	their parents 3.4	need soap 0.0	in Tulsa 2.2	the Capitol 0.0
26. 06/25-07/01	Hillary Clinton 20.5	Fake News 37.6	Supreme Court 3.7	Jean Carroll 0.0	American soldiers 0.0	Trump Organization 0.0
27. 07/02-07/08	Crooked Hillary 82.8	North Korea 28.6	Trump administration 0.0	Jeffrey Epstein 0.0	Mount Rushmore 3.9	Ashli Babbitt 0.0
28. 07/09-07/15	Crooked Hillary 73.3	Trump Jr 0.0	Supreme Court 7.9	Jeffrey Epstein 0.0	Roger Stone 0.0	the Capitol 0.0
29. 07/16-07/22	Mike Pence 6.8	Secret Service 0.0	in Helsinki 1.7	a racist 0.0	in Portland 0.0	Tom Barrack 0.0
30. 07/23-07/29	Crooked Hillary 79.6	Boy Scouts 0.0	Walk of 0.0	Elijah Cummings 27.2	in Portland 8.9	the Capitol 0.0
31. 07/30-08/05	Khizr Khan 0.0	Maxine Waters 0.0	enemy of 22.2	El Paso 11.1	the election 3.4	the Capitol 0.0
32. 08/06-08/12	Hillary Clinton 10.5	North Korea 5.7	Space Force 11.1	El Paso 7.7	Social Security 0.0	ouvertun 0.0
33. 08/13-08/19	Trump campaign 0.0	white supremacists 0.0	security clearance 0.0	New Hampshire 26.5	the USPS 0.0	the Taliban 0.0
34. 08/20-08/26	Hillary Clinton 19.1	Joe Arpaio 3.5	Michael Cohen 4.3	Prime Minister 28.7	Joe Biden 5.9	the Taliban 0.0
35. 08/27-09/02	Crooked Hillary 61.8	Hurricane Harvey 0.1	John McCain 0.2	Hurricane Dorian 9.6	Joe Biden 2.7	the Taliban 0.0
36. 09/03-09/09	in Detroit 0.0	to end 0.0	Brett Kavanaugh 7.6	the Taliban 3.0	Joe Biden 3.4	Robert E 0.0
37. 09/10-09/16	tax returns 0.0	white supremacist 0.0	Puerto Rico 8.4	Dan Bishop 37.7	Joe Biden 13.3	the Taliban 0.0
38. 09/17-09/23	Trump Jr 0.0	North Korea 12.8	Blasey Ford 0.0	a foreign 6.4	Supreme Court 7.3	to overturn 0.0
39. 09/24-09/30	Hillary Clinton 7.5	Puerto Rico 5.2	Brett Kavanaugh 15.2	impeachment inquiry 0.0	Supreme Court 5.7	debt ceiling 0.0
40. 10/01-10/07	Mike Pence 8.9	Puerto Rico 2.6	Supreme Court 6.9	Adam Schiff 13.3	Walter Reed 5.7	the debt 0.0
41. 10/08-10/14	sexual assault 0.0	Puerto Rico 2.2	Kanye West 0.0	the Kurds 11.3	Biden is 26.5	the January 0.0
42. 10/15-10/21	Hillary Clinton 19.9	families of 0.0	Saudi Arabia 6.6	the Kurds 3.8	Joe Biden 12.1	the January 0.0
43. 10/22-10/28	Hillary Clinton 11.7	Myshia Johnson 0.0	the bombs 0.0	World Series 0.0	Joe Biden 10.1	Alec Baldwin 0.0
44. 10/29-11/04	Hillary Clinton 6.5	Twitter employee 0.0	birthright citizenship 0.0	the impeachment 0.0	Joe Biden 12.6	in Virginia 0.0
45. 11/05-11/11	Trump wins 0.0	mental health 0.0	Jim Acosta 0.0	pro quo 8.1	the election 2.2	infrastructure bill 0.0
46. 11/12-11/18	Steve Bannon 0.0	ban on 0.0	president who 0.0	impeachment inquiry 0.0	the election 7.5	Chris Christie 0.0
47. 11/19-11/25	Mike Pence 24.3	Roy Moore 0.0	Saudi Arabia 2.5	quid pro 1.3	the election 6.7	Kyle Rittenhouse 0.0
48. 11/26-12/02	popular vote 17.4	Native American 0.1	Trump Tower 2.5	Hong Kong 0.0	voter fraud 32.2	Donald Trump 0.0
49. 12/03-12/09	Air Force 18.2	Roy Moore 3.5	campaign finance 0.0	to impeach 7.7	in Georgia 12.9	Donald Trump 0.0
50. 12/10-12/16	of State 7.6	of sexual 0.0	Michael Cohen 7.8	articles of 0.0	the election 9.0	Mark Meadows 0.0
51. 12/17-12/23	Electoral College 5.8	tax bill 0.0	the wall 13.7	Christianity Today 8.1	election fraud 13.9	the Capitol 0.0





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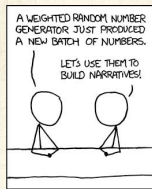
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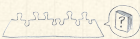
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Understanding the Sociotechnocene—Stories:



xkcd.com/904/



Toward a Science of Stories.



Claim: Homo narrativus—we run on stories.



“What’s the John Dory?”



“They’ve lost the plot/thread”



Narrative hierarchies and scalability of stories



Research: Real-time and offline extraction of metaphors, frames, plots, narratives, conspiracy theories, and stories from large-scale text.



Research: The taxonomy of human stories.



To be built:
Storyscopes—improvable, online, interactive instruments.

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