Data from our man Zipf

Last updated: 2021/10/06, 20:25:28 EDT Principles of Complex Systems, Vols. 1 & 2

CSYS/MATH 300 and 303, 2021-2022 | @pocsvox

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont

000 Licensed under the Creative Commons Attribution-NonCommercial-ShareAlike 3.0 License.

Outline

Zipf in brief

Zipfian empirics

Yet more Zipfian Empirics

References

George Kingsley Zipf:

In brief:

- 🖧 Zipf 🗹 (1902–1950) was a linguist at Harvard, specializing in Chinese languages.
- local passion for statistical analysis of texts.
- 🚯 Studied human behavior much more generally ...

Zipf's masterwork:

- 🚓 "Human Behavior and the Principle of Least Effort" Addison-Wesley, 1949 Cambridge, MA^[2]
- 🚳 Bonus field of study: Glottometrics. 🗹
- 🚳 Bonus 'word' word: Glossolalia. 🗹

PoCS @pocsvox Data from our

man Zipf

Zipf in brief

Zipfian empiric

Yet more Zipfiar Empirics

Human Behavior/Principle of Least Effort:

From the Preface—

Nearly twenty-five years ago it occurred to me that we might gain considerable insight into the mainsprings of human behavior if we viewed it purely as a natural phenomenon like everything else in the universe, ...

And—

... the expressed purpose of this book is to establish The Principle of Least Effort as the primary principle that governs our entire individual and collective behavior ...

"... a person in solving his immediate problems will

view these against the background of his probable

"... he will strive ... to minimize the total work that he

must expend in solving both his immediate problems

"[he will strive to] minimize the probable average rate of

future problems as estimated by himself."

and his probable future problems."

(m) [8]

PoCS

@pocsvox

man Zipf

Zipf in brief

0

PoCS

@pocsvox

man Zipf

Zipf in brief

UM |8

Data from our

Zipfian empirics

Yet more Zipfiar

Data from our

୬ ବ ଦ 1 of 38

The Principle of Least Effort:

Zipf's framing (p. 1):



• ୨ ۹ (२ 5 of 38

Rampaging research

his work-expenditure..."

- Within Human Behavior and the Principle of Least Effort:
- 🚳 City sizes
- Yet more Zipfian # retail stores in cities
 - 🚳 # services (barber shops, beauty parlors, cleaning, ...)
 - # people in occupations
 - 🚓 # one-way trips in cars and trucks vs. distance
 - Observed general dependency of 'interactions' between cities A and B on $P_A P_B / D_{AB}$ where P_A and P_B are population size and D_{AB} is distance between A and B. \Rightarrow 'Gravity Law.'

Zipfian empirics:

PoCS

@pocsvox

man Zipf

Zipf in brief

References

(m) [8]

PoCS

@pocsvox

man Zipf

Zipf in brief

Reference

Zipfian empirics

Yet more Zipfiar

Data from our

Zipfian empirics

Yet more Zipfiar

Data from our

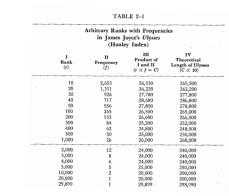
\clubsuit vocabulary balance: $f \sim r^{-1} \rightarrow r \cdot f \sim \text{constant}$ (f = frequency, r = rank).

Zipfian empirics:

Zipf's basic idea:

tasks.

 $f \sim r^{-1}$ for word frequency:



Data from our man Zipf Zipf in brief

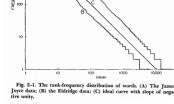
00

PoCS

@pocsvo>

• n q ∩ • 7 of 38

Zipfian empirics Yet more Zipfiai References



00 • n q (+ 8 of 38

PoCS @pocsvox Data from our man Zipf

- Zipf in brief Zipfian empirics Yet more Zipfia Empirics
- listener if all pieces of information correspond to different words (or morphemes).
- Analogy: a specialized tool for every task. Decoding is simple but encoding is hard

Forces of Unification and Diversification:

Easiest for the speaker to use just one word.

Encoding is simple but decoding is hard

Zipf uses the analogy of tools: one tool for all

- Zipf thereby argues for a tension that should lead to an uneven distribution of word usage.
- No formal theory beyond this... (more later [1])

PoCS @pocsvo> Data from our man Zipf

Zipf in brief

References

Zipfian empirics Yet more Zipfiar

References



References

- # telephone messages between cities
- 🚓 # people moving vs. distance
 - 🚓 # marriages vs. distance

(in 18

man Zipf Zipf in brief

PoCS

@pocsvox

Data from our

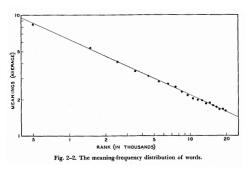
Zipfian empirics Yet more Zipfiar

(I) (S

new items by dateline

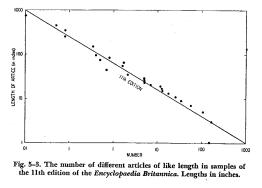
line weight moved between cities by rail

 \clubsuit Number of meanings $m_r \propto f_r^{1/2}$ where r is rank and f_r is frequency.



Zipfian empirics:

Article length in the Encyclopedia Britannica:

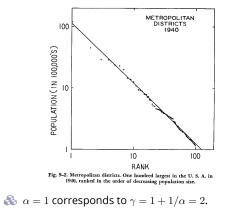


🗞 Not a rank-ordered plot; flipped frequency distribution.

(?) slope of -3/5 corresponds to $\gamma = 5/3$.

Zipfian empirics:

Population size of districts:



Zipfian empirics: Data from our

PoCS

@pocsvox

man Zipf

Zipf in brief

References

8

PoCS

@pocsvox

man Zipf

Zipf in brief

References

PoCS

@pocsvox

man Zipf

Zipf in brief

Empirics

References

୍ଲା 👸

• ୨ ୦ (୦ 12 of 38

Zipfian empirics

Yet more Zipfian

Data from our

Zipfian empirics

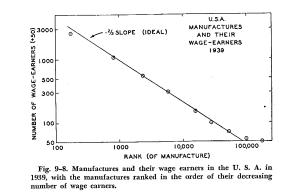
Yet more Zipfian Empirics

Data from our

Zipfian empirics

Yet more Zipfiar Empirics

Number of employees in organizations



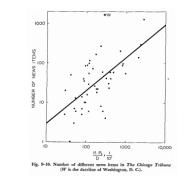
 $\alpha = 2/3$ corresponds to $\gamma = 1 + 1/\alpha = 5/2$. ୬ ବ ଦ 10 of 38

Zipfian empirics:

 \Re # news items as a function of population P_2 of location in the Chicago Tribune

 $\bigotimes D$ = distance, P_1 = Chicago's population

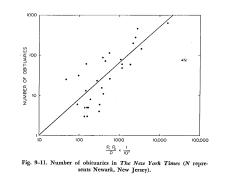
🚯 Solid line = +1 exponent.



Zipfian empirics:

obituaries in the New York Times for locations with population P_2 .

 $\gtrsim D$ = distance, P_1 = New York's population 🚳 Solid line = +1 exponent.



Zipfian empirics:

Zipfian empirics:

corresponds to $\gamma = 2$.

PoCS

@pocsvox

man Zipf

Zipf in brief

Zipfian empirics

Yet more Zipfiar Empirics

References

(I) (S

PoCS

@pocsvox

man Zipf

Zipf in brief

Empirics

References

PoCS

@pocsvox

Data from our

୬ < ເ∾ 15 of 38

Zipfian empirics

Yet more Zipfiar

Data from our

Data from our

- A Movement of stuff between cities
- $\bigotimes D$ = distance, P_1 and P_2 = city populations.
- 🗞 Solid line = +1 exponent.

AP, 10 Fig. 9-14, Railway ailway express. The movement by weight (less carload lots) ween 13 arbitrary cities in the U. S. A., May 1939.

length of trip versus frequency of trip.

Not a rank-ordered plot; flipped frequency

distribution. Solid line = -1/2 exponent



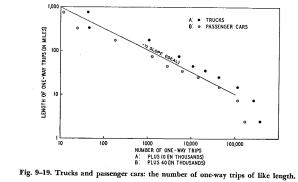
Zipf in brief Zipfian empirics Yet more Zipfiar References

00

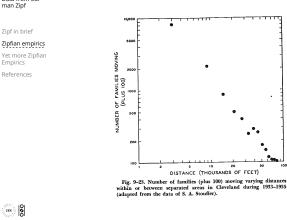
PoCS @pocsvox Data from our man Zipf

Zipf in brief

Zipfian empirics Yet more Zipfiai References



Zipfian empirics:



PoCS @pocsvox Data from our man Zipf

8

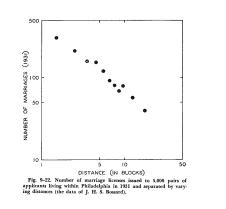
UIN

Zipf in brief Zipfian empirics Yet more Zipfiar

Empirics References



The probability of marriage? $\gg \gamma = 1?$



Comment #60 in Math and the City 🕑 by Strogatz, NYT:

60. May 20, 2009 9:26 am

Link

George Kingsley Zipf was my teacher at Harvard...He had given a class project where we were to see if Chemical Companies when ranked by the number of different chemicles they produced, followed his Law of Least Effort. I missed turning in my assignment due to the accidental death of my father When I returned from the funeral I was given a message to call Dr. Zipf immediately. I did and when I explained why I was late turning in the data. He said, "Well, your father's gone and I (Zipf) have no pipeline to God. I expect the data will be on my desk tomorrow morning!".....My mother, sister and extended family spread huge books of trade magazines on the kitchen and dining room tables and furiously went to work We worked until late in the night and finished the project I drove to Harvard the next morning and angrily gave the hundreds of 'three by five cards' to Zipf. All he said was, "Thank you." Years later, I wondered whether his'meaness' had really been his way of helping me and my family to take our minds of our grief that day and concentrate on finishing my assignment. In my youth I thought not, but now as I approach 80, I like to think his seemingly hurtful attitude was really an act of kindness,,,,,

- Jim Terry

PoCS

@pocsvox

man Zipf

Zipf in brief

Empirics

References

(in |

Zipfian empirics

Yet more Zipfian

Data from our

Zipfian empirics:



I Frequency (f)	Calculated N(f ² - 1/4)		
	II Ulyssea	III Plautus	
1	12,324	4,075	
2	15,410	4,490	
3	19,193	4,280	
4	20,239	4,750	
5	22,424	3,985	
6	22,773	4,504	
7	23,546	4,241	
8	23,651	4,399	
9	24,063	4,366	
10	22,145	4,289	
15	21,576	2,922	
20	27,844	5,996	
30	18,000	3,600	
40	25,600	4,800	
50	22,500	5,000	

Zipfian empirics:

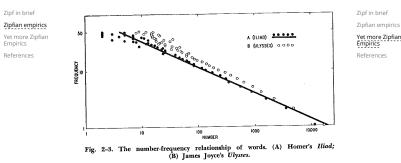
Data from our man Zipf

PoCS

@pocsvox

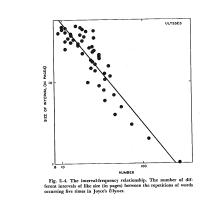
Zipf in brief

References









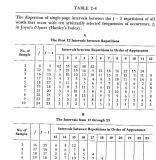
Zipfian empirics:

Calculated values of negative slopes, errors, and Y-intercepts of the er, N, of interval-sizes, I_p between the repetition of words in 14 freque lasses, f_i as fitted to the equation $aX + Y = C$ where $X = \log N$ as $= \log I_p$ and where I_i has integral values from 1 through 21 inclusive						
I No. of Analysis	II Frequency of Occur. (f)	III No. of Different Words of like f	IV Slope of Best Line of Y's (negative) (Y = log It)	V Error (root-mean- square)	VI Y-intercep (antilog thereof)	
1	5	906	1.21	.151	716	
2	6	637	1.20	.169	666	
3	10	222	1.27	.106	677	
4	12	155	1.24	.111	491	
5	15	96	1.15	,096	328	
6	16	86	.96	.124	153	
7	17	79	1.22	.174	422	
8	18	62	1.20	.120	264	
9	19	63	1.21	.148	350	
10	20	69	1.29	.124	944	
11	21	52	1.05	.138	212	
12	22	50	1.10	.117	264	
13	23	44	1.24	.113	352	
14F	24	34	1.01	.158	136	
15Z	24	34	1.05	.147	153	

PoCS @pocsvox Data from our man Zipf

Zipfian empirics:

Zipfian empirics:





PoCS

@pocsvox

man Zipf

Data from our

References

• ୨ ۹ (№ 25 of 38

PoCS @pocsvox Data from our man Zipf

Zipf in brief Zipfian empirics Yet more Zipfian Empirics References



ring twenty-four times in James Joyce's Ulysses

8 ∙∕) q (२ 23 of 38

PoCS

Zipf in brief

Empirics

(in |

୬ ୦ ୦ € 24 of 38

References

Zipfian empirics

Yet more Zipfian

(III)

@pocsvox

man Zipf

Zipf in brief

Empirics

References

Zipfian empirics

Yet more Zipfian

Data from our

୬ ବ. ତ 22 of 38 PoCS

@pocsvox Data from our man Zipf

Zipfian empirics:

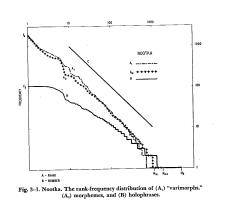
୬ ବ 🕫 26 of 38 PoCS @pocsvox

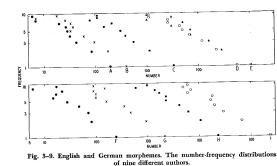
() ()

Data from our man Zipf

TABLE 3-1 Zipf in brief The Frequencies and Average Lengths of Words (A) in terms of the number of phonemes, and (B) in terms of the num-ber of syllables in (A) American newspaper English and in (B) the Latin of Plautus. Zipfian empirics (A) AMERICAN NEWSPAPER ENGLISH (B) LATIN OF PLAUTUS Yet more Zipfian (According to R. C. Eldridge) Empirics Numbe of Occur-Average Number of Numb of Occur Numbe of Occur-rences Average Number of Syllables Number of Occur-rences Average Number Number of of Words Syllables Number of Words Number of Words Average Number of Number of Words References 5429 1198 492 299 161 126 87 2976 1079 516 294 212 151 105 84 86 45 (3.23) (2.92) (2.05) (2.60) (2.53) (2.35) (2.35) (2.30) (2.30) (2.30) (2.30) (2.30) (2.30) (2.30) (2.07) (2.07) (2.40) (2.09) (2.09) (2.01) (6.656) (6.151) (6.015) (6.081) (5.768) (5.768) (5.333) (5.654) (5.377) (4.825) (5.459) (5.367) (4.825) (5.469) (5.500) (5.00) (5.500) (5.500) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.00) (5.333) (5.564) (5.337) (5.564) (5.337) (5.564) (5.367) (5. (2.05 2 (\$ 903) (1.70 (2,08)(3.333) (3.455) (1.40) 61-4290 12 666 62-514 33.094 (2,00) 8.43

Zipfian empirics:

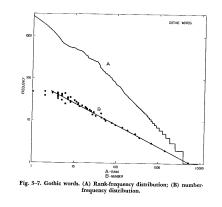








Zipfian empirics:



PoCS @pocsvox

man Zipf

PoCS

@pocsvox

man Zipf

Zipf in brief

References

Zipfian empirics

Yet more Zipfian Empirics

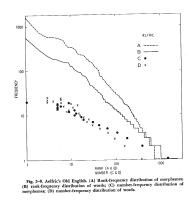
Data from our



Zipf in brief Zipfian empirics Yet more Zipfian Empirics References

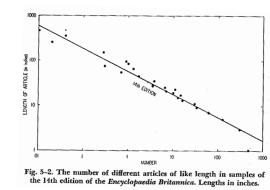


Zipfian empirics:



Zipfian empirics (p. 176):

🗞 Article length in the Encylopedia Brittanica



Zipfian empirics: @pocsvox Data from our

PoCS

man Zipf

Zipf in brief

Zipfian empirics

Yet more Zipfian Empirics

References

() ()

PoCS

@pocsvox

man Zipf

Zipf in brief

Empirics

References

Zipfian empirics

Yet more Zipfian

Data from our

୬ ବ. ତ 31 of 38

TABLE 6-1

The X Number of Different Genera of Like Y Number of Different Species of the Flora of Ceylon (After J. C. Willis)

No. of Genera X

573

176

85

49

36

20

etc.

No. of Species

1

2

3

4

5

6

Yet more Zipfian Empirics References

Zipf in brief

Zipfian empirics





NUMBER EMPLOYEES (FULL-TIME) . GROSS RECEIPTS IN \$1,000'S PAYROLL (TOTAL) pirics lipfian DOHL N MOUNT 4 3 5 30 .50 5 10 RANK 30 50 3 5 IÓ RANK 30 50 100

Fig. 9-9. Gross receipts, number of full-time employees, and total payroll of service establishments in the U.S.A. in 1939 when the service establishments are ranked in the order of their decreasing number of members as in Fig. 9-4 supra.



PoCS

@pocsvox

man Zipf

Zipf in brief

Empirics

References

Zipfian empirics

Yet more Zipfian

Data from our



Zipfian empirics:

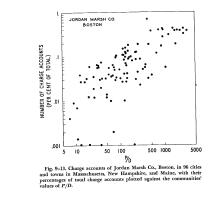
PoCS @pocsvox Data from our man Zipf

わく(~ 35 of 38

() ()

Zipf in brief

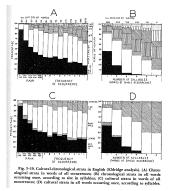
Zipfian empirics Yet more Zipfian Empirics References





PoCS @pocsvox Data from our man Zipf

Zipfian empirics:





Zipf in brief

References

ି । ତି

•ე < (~ 30 of 38

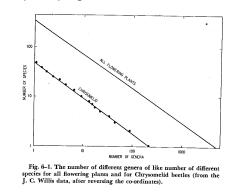
Zipfian empirics

Yet more Zipfian Empirics

(in | 10 Rank



🗞 # species per genera:





References I	PoCS @pocsvox Data from our man Zipf
 [1] R. Ferrer-i-Cancho and R. V. Solé. Least effort and the origins of scaling in human language. Proc. Natl. Acad. Sci, 100:788–791, 2003. pdf 	Zipf in brief Zipfian empirics Yet more Zipfian Empirics References
 [2] G. K. Zipf. Human Behaviour and the Principle of Least-Effort. Addison-Wesley, Cambridge, MA, 1949. 	

୍ତ୍ତି । ୬.୨.୧ 37 of 38

PoCS @pocsvox

Data from our man Zipf

Zipf in brief

References

Zipfian empirics

Yet more Zipfian Empirics

