Small-world networks

Last updated: 2021/10/07, 17:44:59 EDT

Principles of Complex Systems, Vols. 1 & 2 CSYS/MATH 300 and 303, 2021–2022 |@pocsvox

The PoCSverse Small-world networks 1 of 68

Small-world networks Experiments Theory Generalized affiliation networks Nurshell

References

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont





Licensed under the Creative Commons Attribution-NonCommercial-ShareAlike 3.0 License.

These slides are brought to you by:

Sealie & Lambie Productions

The PoCSverse Small-world networks 2 of 68

Small-world networks Experiments Theory Generalized affiliation networks Nutshell



These slides are also brought to you by:

Special Guest Executive Producer



On Instagram at pratchett_the_cat

The PoCSverse Small-world networks 3 of 68

Small-world networks Experiments Theory Generalized affiliation networks Nurshell



Outline

Small-world networks

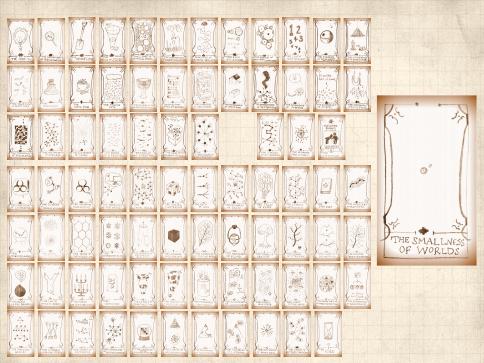
Experiments Theory Generalized affiliation networks Nutshell

References

0°

The PoCSverse Small-world networks 4 of 68

Small-world networks Experiments Theory Generalized affiliation networks Nutshell



Outline

Small-world networks Experiments

Generalized affiliation networks Nutshell The PoCSverse Small-world networks 6 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

ruconcil



People thinking about people: How are social networks structured?

- How do we define and measure connections?
- Methods/issues of self-report and remote sensing.

The PoCSverse Small-world networks 7 of 68

Small-world networks

Experiments

Generalized affiliation networks



People thinking about people: How are social networks structured?

- How do we define and measure connections?
- Methods/issues of self-report and remote sensing.

What about the dynamics of social networks?

- How do social networks/movements begin & evolve?
- How does collective problem solving work?
- How does information move through social networks?
- Which rules give the best 'game of society?'

The PoCSverse Small-world networks 7 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



People thinking about people: How are social networks structured?

- How do we define and measure connections?
- Methods/issues of self-report and remote sensing.

What about the dynamics of social networks?

- How do social networks/movements begin & evolve?
- How does collective problem solving work?
- How does information move through social networks?
- Which rules give the best 'game of society?'

Sociotechnical phenomena and algorithms:

What can people and computers do together? (google)
 Use Play + Crunch to solve problems. Which problems?

The PoCSverse Small-world networks 7 of 68

Small-world networks

Experiments Theory

Generalized anniation networks Nutshell



Social Search

A small slice of the pie:

Q. Can people pass messages between distant individuals using only their existing social connections? The PoCSverse Small-world networks 8 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Social Search

A small slice of the pie:

- Q. Can people pass messages between distant individuals using only their existing social connections?
- \lambda A. Apparently yes ...

The PoCSverse Small-world networks 8 of 68

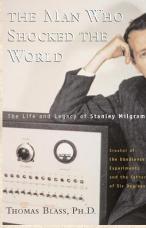
Small-world networks

Experiments Theory

Generalized affiliation networks



Milgram's social search experiment (1960s)



http://www.stanleymilgram.com

 Target person = Boston stockbroker.
 296 senders from Boston and Omaha. The PoCSverse Small-world networks 9 of 68

Small-world networks

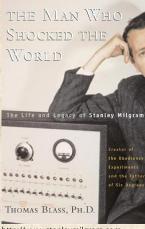
Experiments Theory

Generalized affiliation networks

Nutshell



Milgram's social search experiment (1960s)



http://www.stanleymilgram.com

- Target person = Boston stockbroker.
- 296 senders from Boston and Omaha.
- 20% of senders reached target.
- 🚳 chain length \simeq 6.5.

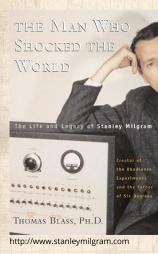
The PoCSverse Small-world networks 9 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

Milgram's social search experiment (1960s)



- Target person = Boston stockbroker.
- 296 senders from Boston and Omaha.
- 20% of senders reached target.
- \clubsuit chain length \simeq 6.5.

Popular terms:

- The Small World Phenomenon;
- 🗞 "Six Degrees of Separation."



Small-world networks

Experiments Theory

Generalized affiliation networks



From Frigyes Karinthy's "Chain-links" C in "Everything is Different", 1929:

'A fascinating game grew out of this discussion. One of us suggested performing the following experiment to prove that the population of the Earth is closer together now than they have ever been before. We should select any person from the 1.5 billion inhabitants of the Earth-anyone, anywhere at all. He bet us that, using no more than five individuals, one of whom is a personal acquaintance, he could contact the selected individual using nothing except the network of personal acquaintances. For example, "Look, you know Mr. X.Y., please ask him to contact his friend Mr. Q.Z., whom he knows, and so forth."

The PoCSverse Small-world networks 10 of 68

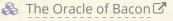
Small-world networks

Experiments Theory

Generalized affiliation networks



It's a game C: "Kevin Bacon is the Center of the Universe"



Six Degrees of Paul Erdös:



Academic papers.
Erdös Number C
Erdös Number Project C

The PoCSverse Small-world networks 11 of 68

Small-world networks

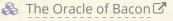
Experiments Theory

Generalized affiliation networks





It's a game C: "Kevin Bacon is the Center of the Universe"



Six Degrees of Paul Erdös:



Academic papers.
Erdös Number C
Erdös Number Project C

🗞 So naturally we must have the Erdös-Bacon Number 🗹.



The PoCSverse Small-world networks 11 of 68

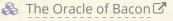
Small-world networks

Experiments Theory

Generalized affiliation networks



It's a game C: "Kevin Bacon is the Center of the Universe"



Six Degrees of Paul Erdös:



Academic papers.
 Erdös Number C
 Erdös Number Project C

& So naturally we must have the Erdös-Bacon Number \mathbb{Z} . & One Story Lab alum has EB# $< \infty$.



The PoCSverse Small-world networks 11 of 68

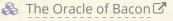
Small-world networks

Experiments Theory

Generalized affiliation networks



It's a game C: "Kevin Bacon is the Center of the Universe"



Six Degrees of Paul Erdös:



Academic papers.
Erdös Number C
Erdös Number Project C

So naturally we must have the Erdös-Bacon Number ^I.
One Story Lab alum has EB# < ∞.
Natalie Hershlag's (Portman's) EB# = 5 + 2 = 7.

The PoCSverse Small-world networks 11 of 68

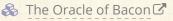
Small-world networks

Experiments Theory

Generalized affiliation networks



It's a game C: "Kevin Bacon is the Center of the Universe"



Six Degrees of Paul Erdös:



Academic papers.
 Erdös Number C
 Erdös Number Project C

So naturally we must have the Erdös-Bacon Number .
One Story Lab alum has EB# < ∞.
Natalie Hershlag's (Portman's) EB# = 5 + 2 = 7.
The EBS# is also a thing: erdosbaconsabbath.com .



The PoCSverse Small-world networks 11 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

Good Will Hunting:

The PoCSverse Small-world networks 12 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References



Boardwork by Dan Kleitman C, EB# = 1 + 2 = 3.

See Kleitman's sidebar in Mark Saul's Movie Review (Notices of the AMS, Vol. 45, 1998.)



You may already be a winner in NSA's "three-degrees" surveillance sweepstakes! NSA's probes could cover hundreds of millions of Americans. Thanks, Kevin Bacon.

by Sean Gallagher - July 18 2013, 4:00pm EDT





Aurich Lawson



\lambda Many people 🗹 are within three degrees from a random person ...

The PoCSverse Small-world networks 13 of 68

Small-world networks

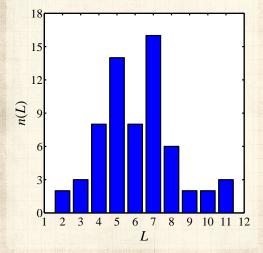
Experiments

Generalized affiliation

Nutshell



Lengths of successful chains:



The PoCSverse Small-world networks 14 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References

From Travers and Milgram (1969) in Sociometry: ^[9] "An Experimental Study of the Small World Problem."



The PoCSverse Small-world networks 15 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

References

Two features characterize a social 'Small World':



The PoCSverse Small-world networks 15 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References

Two features characterize a social 'Small World':

1. Short paths exist, and



The PoCSverse Small-world networks 15 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References

Two features characterize a social 'Small World':

1. Short paths exist,

and

2. People are good at finding them.



The PoCSverse Small-world networks 15 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

References

Two features characterize a social 'Small World':

- 1. Short paths exist, (= Geometric piece) and
- 2. People are good at finding them.



The PoCSverse Small-world networks 15 of 68

Small-world networks

Experiments Theory

Nutshell

References

Two features characterize a social 'Small World':

- 1. Short paths exist, (= Geometric piece) and
- People are good at finding them. (= Algorithmic piece)



Social Search

Milgram's small world experiment with email:



The PoCSverse Small-world networks 16 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

Nutshell

References





"An Experimental study of Search in Global Social Networks" Dodds, Muhamad, and Watts, Science, **301**, 827–829, 2003. ^[4]

60,000+ participants in 166 countries

The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments

networks Nutshell



60,000+ participants in 166 countries 18 targets in 13 countries including

The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments

networks Nutshell



left for the second sec 18 targets in 13 countries including a professor at an Ivy League university, The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments

Generalized affiliation Nutshell



60,000+ participants in 166 countries
 18 targets in 13 countries including
 a professor at an Ivy League university,
 an archival inspector in Estonia,

The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



60,000+ participants in 166 countries
 18 targets in 13 countries including
 a professor at an Ivy League university,
 an archival inspector in Estonia,
 a technology consultant in India,

The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments Theory

Generalized amiliation networks



60,000+ participants in 166 countries
18 targets in 13 countries including
a professor at an Ivy League university,
an archival inspector in Estonia,
a technology consultant in India,
a policeman in Australia,

The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



- 60,000+ participants in 166 countries
- 🗞 18 targets in 13 countries including
 - a professor at an Ivy League university,
 - 📦 an archival inspector in Estonia,
 - 🟹 a technology consultant in India,
 - a policeman in Australia, and
 - a veterinarian in the Norwegian army.

The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



- 🚳 60,000+ participants in 166 countries
- 18 targets in 13 countries including
 - a professor at an lvy League university,
 - an archival inspector in Estonia,
 - a technology consultant in India,
 - a policeman in Australia, and
 - a veterinarian in the Norwegian army.
- A 24,000+ chains

The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments



- 🚳 60,000+ participants in 166 countries
- 🗞 18 targets in 13 countries including
 - a professor at an lvy League university,
 - 🗊 an archival inspector in Estonia,
 - a technology consultant in India,
 - a policeman in Australia, and
 - a veterinarian in the Norwegian army.
- 🗞 24,000+ chains

We were lucky and contagious (more later):

"Using E-Mail to Count Connections" C, Sarah Milstein, New York Times, Circuits Section (December, 2001) The PoCSverse Small-world networks 17 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



All targets:

Table S1

Target	City	Country	Occupation	Gender	N	$N_c(\%)$	r (r ₀)	<l></l>
1	Novosibirsk	Russia	PhD student	F	8234	20(0.24)	64 (76)	4.05
2	New York	USA	Writer	F	6044	31 (0.51)	65 (73)	3.61
3	Bandung	Indonesia	Unemployed	М	8151	0	66 (76)	n/a
4	New York	USA	Journalist	F	5690	44 (0.77)	60 (72)	3.9
5	Ithaca	USA	Professor	М	5855	168 (2.87)	54 (71)	3.84
6	Melbourne	Australia	Travel Consultant	F	5597	20 (0.36)	60 (71)	5.2
7	Bardufoss	Norway	Army veterinarian	М	4343	16 (0.37)	63 (76)	4.25
8	Perth	Australia	Police Officer	М	4485	4 (0.09)	64 (75)	4.5
9	Omaha	USA	Life Insurance	F	4562	2 (0.04)	66 (79)	4.5
			Agent					
10	Welwyn Garden City	UK	Retired	М	6593	1 (0.02)	68 (74)	4
11	Paris	France	Librarian	F	4198	3 (0.07)	65 (75)	5
12	Tallinn	Estonia	Archival Inspector	М	4530	8 (0.18)	63(79)	4
13	Munich	Germany	Journalist	М	4350	32 (0.74)	62 (74)	4.66
14	Split	Croatia	Student	М	6629	0	63 (77)	n/a
15	Gurgaon	India	Technology	М	4510	12 (0.27)	67 (78)	3.67
			Consultant					
16	Managua	Nicaragua	Computer analyst	М	6547	2 (0.03)	68 (78)	5.5
17	Katikati	New Zealand	Potter	М	4091	12 (0.3)	62 (74)	4.33
18	Elderton	USA	Lutheran Pastor	М	4438	9 (0.21)	68 (76)	4.33
Totals			an and she had		98,847	384 (0.4)	63 (75)	4.05

The PoCSverse Small-world networks 18 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Milgram's participation rate was roughly 75%

The PoCSverse Small-world networks 19 of 68

Small-world networks

Experiments

Generalized affiliation networks



Milgram's participation rate was roughly 75%
 Email version: Approximately 37% participation rate.

The PoCSverse Small-world networks 19 of 68

Small-world networks

Experiments

Generalized affiliation networks



The PoCSverse Small-world networks 19 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

References

- Milgram's participation rate was roughly 75%
 Email version: Approximately 37% participation rate.
- Probability of a chain of length 10 getting through:

 $.37^{10}\simeq 5\times 10^{-5}$



The PoCSverse Small-world networks 19 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References

- Milgram's participation rate was roughly 75%
 Email version: Approximately 37% participation rate.
- Probability of a chain of length 10 getting through:

 $.37^{10}\simeq 5\times 10^{-5}$

 \Rightarrow 384 completed chains (1.6% of all chains).

line and the second sec

The PoCSverse Small-world networks 20 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



The PoCSverse Small-world networks 20 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

References

Motivation/Incentives/Perception matter.
 If target *seems* reachable
 participation more likely.



The PoCSverse Small-world networks 20 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

References

local Motivation/Incentives/Perception matter.

- ♣ If target seems reachable ⇒ participation more likely.
- Small changes in attrition rates ⇒ large changes in completion rates



The PoCSverse Small-world networks 20 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

References

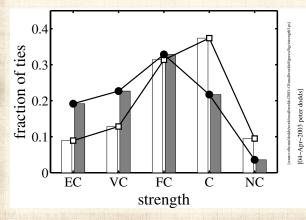
location/Incentives/Perception matter.

- ♣ If target seems reachable ⇒ participation more likely.
- Small changes in attrition rates
 ⇒ large changes in completion rates
- \mathfrak{F} e.g., \searrow 15% in attrition rate
 - \Rightarrow \nearrow 800% in completion rate



Comparing successful to unsuccessful chains:

🚳 Successful chains used relatively weaker ties:



The PoCSverse Small-world networks 21 of 68

Small-world networks

Experiments

Generalized affiliation networks



Successful chains disproportionately used:



Small-world networks

Experiments

Generalized affiliation networks

Nutshell



Successful chains disproportionately used:

🚳 Weak ties, Granovetter [5]

The PoCSverse Small-world networks 22 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

Nutshell



Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter [5]
- Professional ties (34% vs. 13%)

The PoCSverse Small-world networks 22 of 68

Small-world networks

Experiments

Generalized affiliation networks



Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter [5]
- Professional ties (34% vs. 13%)
- Ties originating at work/college



Small-world networks

Experiments

Generalized affiliation networks Nutshell



Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter [5]
- Professional ties (34% vs. 13%)
- Ties originating at work/college
- 🗞 Target's work (65% vs. 40%)

The PoCSverse Small-world networks 22 of 68

Small-world networks

Experiments

Generalized affiliation networks



Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter [5]
- Professional ties (34% vs. 13%)
- Ties originating at work/college
- 🗞 Target's work (65% vs. 40%)

...and disproportionately avoided



Small-world networks

Experiments Theory

Generalized affiliation networks



Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter [5]
- Professional ties (34% vs. 13%)
- Ties originating at work/college
- 🗞 Target's work (65% vs. 40%)

...and disproportionately avoided

\lambda hubs (8% vs. 1%) (+ no evidence of funnels)

The PoCSverse Small-world networks 22 of 68

Small-world networks

Experiments Theory

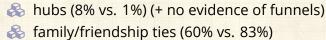
Generalized affiliation networks



Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter [5]
- Professional ties (34% vs. 13%)
- Ties originating at work/college
- 🗞 Target's work (65% vs. 40%)

...and disproportionately avoided



The PoCSverse Small-world networks 22 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter [5]
- Professional ties (34% vs. 13%)
- Ties originating at work/college
- 🗞 Target's work (65% vs. 40%)

...and disproportionately avoided

hubs (8% vs. 1%) (+ no evidence of funnels)
 family/friendship ties (60% vs. 83%)

 $\textbf{Geography} \rightarrow \textbf{Work}$

The PoCSverse Small-world networks 22 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

Senders of successful messages showed little absolute dependency on



🚳 age, gender

The PoCSverse Small-world networks 23 of 68

Small-world networks

Experiments

Generalized affiliation

Nutshell



Senders of successful messages showed little absolute dependency on



\delta age, gender

🚳 country of residence

The PoCSverse Small-world networks 23 of 68

Small-world networks

Experiments

Generalized affiliation Nutshell



Senders of successful messages showed little absolute dependency on

- 🗞 age, gender
- 🚳 country of residence
- 🚳 income

The PoCSverse Small-world networks 23 of 68

Small-world networks

Experiments

Generalized affiliation networks



Senders of successful messages showed little absolute dependency on

- 🚳 age, gender
- 🚳 country of residence
- 🗞 income
- 🚳 religion



Small-world networks

Experiments

Generalized affiliation networks



Senders of successful messages showed little absolute dependency on

- 🚳 age, gender
- 🚳 country of residence
- 🗞 income
- 🚳 religion
- 🚳 relationship to recipient



Small-world networks

Experiments

Generalized affiliation networks



Senders of successful messages showed little absolute dependency on

- 🚳 age, gender
- 🚳 country of residence
- 🗞 income
- 🚳 religion
- 🚳 relationship to recipient

Range of completion rates for subpopulations:

30% to 40%



The PoCSverse

Small-world networks 23 of 68 Small-world networks



Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain." The PoCSverse Small-world networks 24 of 68

Small-world networks

Experiments

Generalized affiliation networks Nutshell



Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."

Why:

🚳 Specificity important

The PoCSverse Small-world networks 24 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."

Why:

- 🚳 Specificity important
- Successful links used relevant information. (e.g. connecting to someone who shares same profession as target.)

The PoCSverse Small-world networks 24 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Basic results:

 $\langle L \rangle = 4.05$ for all completed chains

The PoCSverse Small-world networks 25 of 68

Small-world networks

Experiments

Generalized affiliation networks

Nutshell



Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- L_{*} = Estimated 'true' median chain length (zero attrition)

The PoCSverse Small-world networks 25 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- L_{*} = Estimated 'true' median chain length (zero attrition)

lntra-country chains: $L_* = 5$

The PoCSverse Small-world networks 25 of 68

Small-world networks

Experiments

Generalized affiliation networks Nutshell



Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- L_{*} = Estimated 'true' median chain length (zero attrition)
- lntra-country chains: $L_* = 5$

lnter-country chains: $L_* = 7$

The PoCSverse Small-world networks 25 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- L_{*} = Estimated 'true' median chain length (zero attrition)
- lntra-country chains: $L_* = 5$
- lnter-country chains: $L_* = 7$
- All chains: $L_* = 7$

The PoCSverse Small-world networks 25 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- L_{*} = Estimated 'true' median chain length (zero attrition)
- lntra-country chains: $L_* = 5$
- lnter-country chains: $L_* = 7$
- All chains: $L_* = 7$
- \clubsuit Milgram: $L_* \simeq 9$

The PoCSverse Small-world networks 25 of 68

Small-world networks

Experiments

Generalized affiliation networks



Harnessing social search:

The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

Nutshell



Harnessing social search:

Can distributed social search be used for something big/good? The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments

Generalized affiliation networks



Harnessing social search:

- Can distributed social search be used for something big/good?
- What about something evil? (Good idea to check.)

The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments

Generalized affiliation networks



Harnessing social search:

- Can distributed social search be used for something big/good?
- What about something evil? (Good idea to check.)
- What about socio-inspired algorithms for information search? (More later.)

The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments

Generalized affiliation networks



Harnessing social search:

- Can distributed social search be used for something big/good?
- What about something evil? (Good idea to check.)
- What about socio-inspired algorithms for information search? (More later.)
- For real social search, we have an incentives problem.

The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Harnessing social search:

- Can distributed social search be used for something big/good?
- What about something evil? (Good idea to check.)
- What about socio-inspired algorithms for information search? (More later.)
- For real social search, we have an incentives problem.
- Which kind of influence mechanisms/algorithms would help propagate search?

The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Harnessing social search:

- Can distributed social search be used for something big/good?
- What about something evil? (Good idea to check.)
- What about socio-inspired algorithms for information search? (More later.)
- For real social search, we have an incentives problem.
- Which kind of influence mechanisms/algorithms would help propagate search?
- 🗞 Fun, money, prestige, ...?

The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Harnessing social search:

- Can distributed social search be used for something big/good?
- What about something evil? (Good idea to check.)
- What about socio-inspired algorithms for information search? (More later.)
- For real social search, we have an incentives problem.
- Which kind of influence mechanisms/algorithms would help propagate search?
- 🗞 Fun, money, prestige, ...?
- 🚳 Must be 'non-gameable.'

The PoCSverse Small-world networks 26 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



A Grand Challenge:

The PoCSverse Small-world networks 27 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks

Nutshell



A Grand Challenge:

1969: The Internet is born (the ARPANET —four nodes!).

The PoCSverse Small-world networks 27 of 68

Small-world networks

Experiments

Generalized affiliation networks Nutshell



A Grand Challenge:

- 1969: The Internet is born (the ARPANET —four nodes!).
- Originally funded by DARPA who created a grand Network Challenge for the 40th anniversary.

The PoCSverse Small-world networks 27 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References



*DARPA = Defense Advanced Research Projects Agency .

A Grand Challenge:

- 1969: The Internet is born (the ARPANET —four nodes!).
- Originally funded by DARPA who created a grand Network Challenge for the 40th anniversary.
- Saturday December 5, 2009: DARPA puts 10 red weather balloons up during the day.

The PoCSverse Small-world networks 27 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References

o'

*DARPA = Defense Advanced Research Projects Agency 🗹.

A Grand Challenge:

- 1969: The Internet is born (the ARPANET —four nodes!).
- Solution of the second second
- Saturday December 5, 2009: DARPA puts 10 red weather balloons up during the day.
- Each 8 foot diameter balloon is anchored to the ground somewhere in the United States.

The PoCSverse Small-world networks 27 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell

References



*DARPA = Defense Advanced Research Projects Agency 🗹.

A Grand Challenge:

- 1969: The Internet is born (the ARPANET —four nodes!).
- Solution of the second second
- Saturday December 5, 2009: DARPA puts 10 red weather balloons up during the day.
- Each 8 foot diameter balloon is anchored to the ground somewhere in the United States.
- Schallenge: Find the latitude and longitude of each balloon.

*DARPA = Defense Advanced Research Projects Agency .

The PoCSverse Small-world networks 27 of 68

Small-world networks

Experiments Theory

Nutshell



A Grand Challenge:

- 1969: The Internet is born (the ARPANET —four nodes!).
- Solution of the second second
- Saturday December 5, 2009: DARPA puts 10 red weather balloons up during the day.
- Each 8 foot diameter balloon is anchored to the ground somewhere in the United States.
- Challenge: Find the latitude and longitude of each balloon.
- 🗞 Prize: \$40,000.

*DARPA = Defense Advanced Research Projects Agency .

The PoCSverse Small-world networks 27 of 68

Small-world networks

Experiments Theory

networks Nutshell



Where the balloons were:



The PoCSverse Small-world networks 28 of 68

Small-world networks

Generalized affiliation

🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments

Generalized affiliation networks

Nucsheir



MIT's Media Lab won in less than 9 hours. ^[7]
 Pickard et al. "Time-Critical Social Mobilization," ^[7]
 Science Magazine, 2011.

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



- 🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



- 🗞 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.
- Idea: Want people to both (1) find the balloons, and (2) involve more people.

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



- 🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.
- Idea: Want people to both (1) find the balloons, and (2) involve more people.
- Recursive incentive structure with exponentially decaying payout:

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



- 🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.
- Idea: Want people to both (1) find the balloons, and (2) involve more people.
- Recursive incentive structure with exponentially decaying payout:
 - \$2000 for correctly reporting the coordinates of a balloon.

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



- 🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.
- Idea: Want people to both (1) find the balloons, and (2) involve more people.
- Recursive incentive structure with exponentially decaying payout:
 - \$2000 for correctly reporting the coordinates of a balloon.
 - ♥ \$1000 for recruiting a person who finds a balloon.

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



- 🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.
- Idea: Want people to both (1) find the balloons, and (2) involve more people.
- Recursive incentive structure with exponentially decaying payout:
 - \$2000 for correctly reporting the coordinates of a balloon.
 - \$1000 for recruiting a person who finds a balloon.
 - \$500 for recruiting a person who recruits the balloon finder, ...

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



- 🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.
- Idea: Want people to both (1) find the balloons, and (2) involve more people.
- Recursive incentive structure with exponentially decaying payout:
 - \$2000 for correctly reporting the coordinates of a balloon.
 - \$1000 for recruiting a person who finds a balloon.
 - \$500 for recruiting a person who recruits the balloon finder, ...
 - 🝞 (Not a Ponzi scheme.)

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

seneralized affiliatio hetworks slutshell



- 🙈 MIT's Media Lab 🗹 won in less than 9 hours. [7]
- Pickard et al. "Time-Critical Social Mobilization," ^[7] Science Magazine, 2011.
- People were virally recruited online to help out.
- Idea: Want people to both (1) find the balloons, and (2) involve more people.
- Recursive incentive structure with exponentially decaying payout:
 - \$2000 for correctly reporting the coordinates of a balloon.
 - \$1000 for recruiting a person who finds a balloon.
 - \$500 for recruiting a person who recruits the balloon finder, ...
 - (Not a Ponzi scheme.)

True victory: Colbert interviews Riley Crane 🗹

The PoCSverse Small-world networks 29 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Clever scheme:



🚳 Max payout = \$4000 per balloon.

The PoCSverse Small-world networks 30 of 68

Small-world networks

Experiments

Generalized affiliation networks Nutshell



Clever scheme:

- 🚳 Max payout = \$4000 per balloon.
- lndividuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).



Small-world networks

Experiments Theory

Generalized affiliation networks



Clever scheme:

- 🚳 Max payout = \$4000 per balloon.
- lndividuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).
- 🚳 Gameable?

The PoCSverse Small-world networks 30 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Clever scheme:

- 🚳 Max payout = \$4000 per balloon.
- 🗞 Individuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).
- 🚳 Gameable?
- Limit to how much money a set of bad actors can extract.



Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Clever scheme:

- 🚳 Max payout = \$4000 per balloon.
- 🗞 Individuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).
- 🚳 Gameable?
- Limit to how much money a set of bad actors can extract.

Extra notes:

🚳 MIT's brand helped greatly.



The PoCSverse Small-world networks 30 of 68

Small-world networks

Experiments Theory Generalized affilia

networks Nutshell

Clever scheme:

- 🗞 Max payout = \$4000 per balloon.
- 🗞 Individuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).
- 🚳 Gameable?
- Limit to how much money a set of bad actors can extract.

Extra notes:

- 🚳 MIT's brand helped greatly.
- MIT group first heard about the competition a few days before.



The PoCSverse Small-world networks 30 of 68

Small-world networks

Experiments Theory Generalized affilia

networks Nutshell

Clever scheme:

- 🗞 Max payout = \$4000 per balloon.
- 🗞 Individuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).
- 🚳 Gameable?
- Limit to how much money a set of bad actors can extract.

Extra notes:

- 🚳 MIT's brand helped greatly.
- MIT group first heard about the competition a few days before. Ouch.



The PoCSverse Small-world networks 30 of 68

Small-world networks

Experiments Theory Generalized affilia

networks Nutshell

Clever scheme:

- 🗞 Max payout = \$4000 per balloon.
- 🗞 Individuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).
- 🚳 Gameable?
- Limit to how much money a set of bad actors can extract.

Extra notes:

- 🚳 MIT's brand helped greatly.
- MIT group first heard about the competition a few days before. Ouch.
- line and the set of th

The PoCSverse Small-world networks 30 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Clever scheme:

- 🚳 Max payout = \$4000 per balloon.
- 🗞 Individuals have clear incentives to both
 - 1. involve/source more people (spread), and
 - 2. find balloons (goal action).
- 🚳 Gameable?
- Limit to how much money a set of bad actors can extract.

Extra notes:

- 🚳 MIT's brand helped greatly.
- MIT group first heard about the competition a few days before. Ouch.
- A number of other teams did well C.
 Worthwhile looking at these competing
 - Worthwhile looking at these competing strategies.^[7]

The PoCSverse Small-world networks 30 of 68

Small-world networks

Experiments Theory

Generalized attiliation networks Nutshell



Collective Detective:



🚳 Finding an errant panda 🗹

Once again, social media proved to be a powerful dragnet. Around 1:15 p.m., a Washingtonian posted a picture on Twitter of Rusty in a patch of weeds in the Adams Morgan district, not far from the 163-acre zoo, which was created in 1889 by an act of Congress. "Red panda in our neighborhood," wrote Ashley Foughty, who identified herself as a singer, actress and traveler. "Please come save him!"

Another neighbor posted a photograph of two zoo workers, one in safari shorts standing on a rooftop, one holding a giant butterfly net. Soon the zoo announced: "Rusty the red panda has been recovered, crated & is headed safely back to the National Zoo!"

The PoCSverse Small-world networks 31 of 68

Small-world networks

Experiments

Generalized affiliation Nutshell



Collective Detective:



🚳 Finding an errant panda 🗹

Once again, social media proved to be a powerful dragnet. Around 1:15 p.m., a Washingtonian posted a picture on Twitter of Rusty in a patch of weeds in the Adams Morgan district, not far from the 163-acre zoo, which was created in 1889 by an act of Congress. "Red panda in our neighborhood," wrote Ashley Foughty, who identified herself as a singer, actress and traveler. "Please come save him!"

Another neighbor posted a photograph of two zoo workers, one in safari shorts standing on a rooftop, one holding a giant butterfly net. Soon the zoo announced: "Rusty the red panda has been recovered, crated & is headed safely back to the National Zoo!"

Nature News: "Crowdsourcing in manhunts can work: Despite mistakes over the Boston bombers, social media can help to find people quickly" C by Philip Ball (April 26, 2013)

The PoCSverse Small-world networks 31 of 68

Small-world networks

Experiments

Generalized affiliation Nutshell



Collective Detective:



🚳 Finding an errant panda 🗹

Once again, social media proved to be a powerful dragnet. Around 1:15 p.m., a Washingtonian posted a picture on Twitter of Rusty in a patch of weeds in the Adams Morgan district, not far from the 163-acre zoo, which was created in 1889 by an act of Congress. "Red panda in our neighborhood," wrote Ashley Foughty, who identified herself as a singer, actress and traveler. "Please come save him!"

Another neighbor posted a photograph of two zoo workers, one in safari shorts standing on a rooftop, one holding a giant butterfly net. Soon the zoo announced: "Rusty the red panda has been recovered, crated & is headed safely back to the National Zoo!"

Nature News: "Crowdsourcing in manhunts can work: Despite mistakes over the Boston bombers, social media can help to find people quickly" C by Philip Ball (April 26, 2013)

🚳 Motherboard, Vice: One Degree of Separation in the Forever War 🖸 by Brian Castner (November 11, 2015)

The PoCSverse Small-world networks 31 of 68

Small-world networks

Experiments

Generalized affiliation Nutshell

Outline

Small-world networks

Experiments

Theory

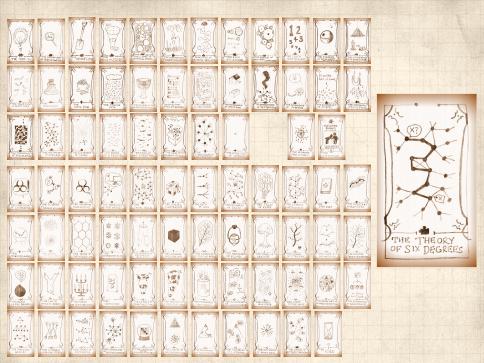
Generalized affiliation network: Nutshell The PoCSverse Small-world networks 32 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks





The social world appears to be small ...why?

Theory: how do we understand the small world property?

Connected random networks have short average path lengths:

$$\langle d_{AB} \rangle \sim \log(N)$$

N = population size,

 d_{AB} = distance between nodes A and B.

The PoCSverse Small-world networks 34 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



The social world appears to be small ...why?

Theory: how do we understand the small world property?

Connected random networks have short average path lengths:

$$\langle d_{AB} \rangle \sim \log(N)$$

- N = population size,
- d_{AB} = distance between nodes A and B.
- 🚳 But: social networks aren't random ...

The PoCSverse Small-world networks 34 of 68

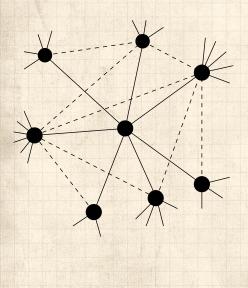
Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell



Simple socialness in a network:



Need "clustering" (your friends are likely to know each other): The PoCSverse Small-world networks 35 of 68

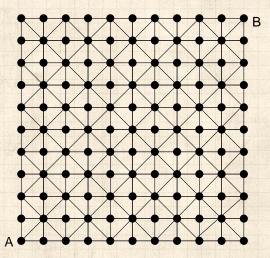
Small-world networks Experiments

Theory Generalized affiliation networks

Nutshell



Non-randomness gives clustering:



The PoCSverse Small-world networks 36 of 68

Small-world networks

Experiments

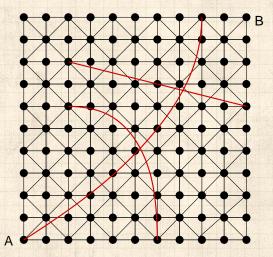
Theory Generalized affiliation networks

References



 $d_{AB} = 10 \rightarrow$ too many long paths.

Randomness + regularity



The PoCSverse Small-world networks 37 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

References



Now have $d_{AB} = 3$

 $\langle d \rangle$ decreases overall

Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."



Small-world networks

Experiments

Theory Generalized affiliation networks

ALC: SPE





Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

🚳 neural network of C. elegans,

The PoCSverse Small-world networks 38 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

- 🗞 neural network of C. elegans,
- 🚳 semantic networks of languages,

The PoCSverse Small-world networks 38 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

- neural network of C. elegans,
 semantic networks of languages,
- actor collaboration graph,

The PoCSverse Small-world networks 38 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

neural network of C. elegans,
 semantic networks of languages,
 actor collaboration graph,

🚳 food webs,

The PoCSverse Small-world networks 38 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

- 🚳 neural network of C. elegans,
- 🚳 semantic networks of languages,
- 🚳 actor collaboration graph,
- 🚳 food webs,
- 🗞 social networks of comic book characters, ...

The PoCSverse Small-world networks 38 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

- 🚳 neural network of C. elegans,
- 🚳 semantic networks of languages,
- 🚳 actor collaboration graph,
- 🚳 food webs,
- 🙈 social networks of comic book characters, ...

Very weak requirements: local regularity The PoCSverse Small-world networks 38 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Introduced by Watts and Strogatz (Nature, 1998)^[11] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

- 🚳 neural network of C. elegans,
- 🚳 semantic networks of languages,
- 🚳 actor collaboration graph,
- 🚳 food webs,
- 🚳 social networks of comic book characters, ...

Very weak requirements:

local regularity + random short cuts

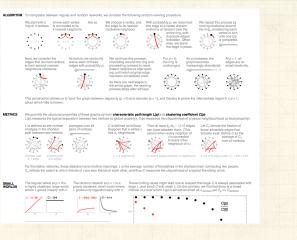
The PoCSverse Small-world networks 38 of 68

Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Papers should be apps:



The PoCSverse Small-world networks 39 of 68

Small-world networks

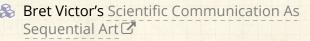
Experiments

Theory Generalized affiliation networks

Nutshell

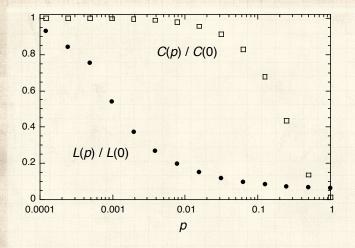
References

The Theory of Str. Decases



Interactive figures and tables = windows into large data sets (empirical or simulated).

The structural small-world property:



The PoCSverse Small-world networks 40 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

References



L(p) = average shortest path length as a function of p
 C(p) = average clustring as a function of p

But are these short cuts findable?

The PoCSverse Small-world networks 41 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Nutshell



But are these short cuts findable?

Nope.^[6]

The PoCSverse Small-world networks 41 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Nutshell



But are these short cuts findable?

Nope.^[6]

Nodes cannot find each other quickly with any local search method.

The PoCSverse Small-world networks 41 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Nutshell



But are these short cuts findable?

Nope.^[6]

Nodes cannot find each other quickly with any local search method.

Need a more sophisticated model ...

The PoCSverse Small-world networks 41 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Nutshell



🚳 What can a local search method reasonably use?



Small-world networks

Experiments

Theory Generalized affiliation networks

Nutshell



What can a local search method reasonably use?How to find things without a map?

The PoCSverse Small-world networks 42 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Nutshell



What can a local search method reasonably use?
How to find things without a map?
Need some measure of distance between friends and the target.

The PoCSverse Small-world networks 42 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks



- What can a local search method reasonably use?
 How to find things without a map?
- Need some measure of distance between friends and the target.

Some possible knowledge:

- Target's identity
 Friends' popularity
- 🚳 Friends' identities
- 🚳 Where message has been



Small-world networks Experiments

Theory Generalized affiliation networks Nutshell



Jon Kleinberg (Nature, 2000)^[6] "Navigation in a small world." The PoCSverse Small-world networks 43 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

A STAT



Jon Kleinberg (Nature, 2000)^[6] "Navigation in a small world."

Allowed to vary:

1. local search algorithm

The PoCSverse Small-world networks 43 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks



Jon Kleinberg (Nature, 2000)^[6] "Navigation in a small world."

Allowed to vary:

- 1. local search algorithm and
- 2. network structure.

The THEORY OF SIX PEGARES

The PoCSverse Small-world networks 43 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Kleinberg's Network:

The PoCSverse Small-world networks 44 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Nutshell



Kleinberg's Network:

1. Start with regular d-dimensional cubic lattice.



Small-world networks

Experiments

Theory Generalized affiliation networks

Nucshen



Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice.
- 2. Add local links so nodes know all nodes within a distance *q*.

The PoCSverse Small-world networks 44 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks Nutshell



Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice.
- 2. Add local links so nodes know all nodes within a distance *q*.
- 3. Add m short cuts per node.

The PoCSverse Small-world networks 44 of 68

Small-world networks Experiments

Theory Generalized affiliation

Nutshell



Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice.
- 2. Add local links so nodes know all nodes within a distance *q*.
- 3. Add m short cuts per node.
- 4. Connect i to j with probability

$$p_{ij} \propto {x_{ij}}^{-\alpha}$$

The PoCSverse Small-world networks 44 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice.
- 2. Add local links so nodes know all nodes within a distance *q*.
- 3. Add m short cuts per node.
- 4. Connect i to j with probability

$$p_{ij} \propto {x_{ij}}^{-\alpha}$$

 $\begin{array}{l} \displaystyle \textcircled{\begin{subarray}{ll} \hline \& & \alpha = 0 \\ \displaystyle \textcircled{\begin{subarray}{ll} \hline \& & \alpha \end{array}} & \alpha \mbox{ large: reinforce local connections.} \\ \displaystyle \textcircled{\begin{subarray}{ll} \hline \& & \alpha = d \\ \displaystyle \end{matrix}} & \mbox{ connections grow logarithmically in space.} \end{array}$

The PoCSverse Small-world networks 44 of 68

Small-world networks Experiments

Theory Generalized affiliation

eneralized affilia hetworks



Theoretical optimal search:

🚳 "Greedy" algorithm.

The PoCSverse Small-world networks 45 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Nucstien



Theoretical optimal search:

- 🚳 "Greedy" algorithm.
- Solution Number of connections grow logarithmically (slowly) in space: $\alpha = d$.

The PoCSverse Small-world networks 45 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks



Theoretical optimal search:

- 🚳 "Greedy" algorithm.
- Solution Number of connections grow logarithmically (slowly) in space: $\alpha = d$.
- 🚳 Social golf.

The PoCSverse Small-world networks 45 of 68

Small-world networks

Experiments Theory

Generalized affiliation networks



Theoretical optimal search:

- 🚳 "Greedy" algorithm.
- Solution Number of connections grow logarithmically (slowly) in space: $\alpha = d$.
- 🚳 Social golf.

Search time grows slowly with system size (like $\log^2 N$).



The PoCSverse Small-world networks 45 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

Theoretical optimal search:

- 🚳 "Greedy" algorithm.
- Number of connections grow logarithmically (slowly) in space: $\alpha = d$.
- 🚳 Social golf.

Search time grows slowly with system size (like $\log^2 N$).

But: social networks aren't lattices plus links.



The PoCSverse Small-world networks 45 of 68

Small-world networks

Experiments

Theory Generalized affiliation networks

If networks have hubs can also search well: Adamic et al. (2001)^[1]

 $P(k_i) \propto k_i^{-\gamma}$

where k = degree of node i (number of friends).

The PoCSverse Small-world networks 46 of 68

Small-world networks Experiments

Theory Generalized affiliation networks

Nutshell



If networks have hubs can also search well: Adamic et al. (2001)^[1]

 $P(k_i) \propto k_i^{-\gamma}$

where k = degree of node i (number of friends).
Basic idea: get to hubs first (airline networks). The PoCSverse Small-world networks 46 of 68

Small-world networks Experiments

Theory Generalized affiliation networks



If networks have hubs can also search well: Adamic et al. (2001)^[1]

 $P(k_i) \propto k_i^{-\gamma}$

where k = degree of node i (number of friends).
Basic idea: get to hubs first (airline networks).
But: hubs in social networks are limited.

The PoCSverse Small-world networks 46 of 68

Small-world networks Experiments

Theory Generalized affiliation networks



Outline

Small-world networks

Generalized affiliation networks

The PoCSverse Small-world networks 47 of 68

Small-world networks Experiments

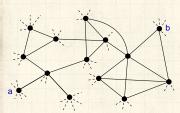
Theory

Generalized affiliation networks Nutshell



The problem

If there are no hubs and no underlying lattice, how can search be efficient?



Which friend of a is closest to the target b?

What does 'closest' mean?

What is 'social distance'?



The PoCSverse Small-world networks 48 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell

One approach: incorporate identity.

The PoCSverse Small-world networks 49 of 68

Small-world networks Experiments

Experiment

Theory

Generalized affiliation networks Nutshell



One approach: incorporate identity.

Identity is formed from attributes such as:

- 🚳 Geographic location
- 🚳 Type of employment
- 🗞 Religious beliefs
- 🚳 Recreational activities.

The PoCSverse Small-world networks 49 of 68

Small-world networks Experiments

experimer

Generalized affiliation networks Nutshell



One approach: incorporate identity.

Identity is formed from attributes such as:

- 🚳 Geographic location
- 🚳 Type of employment
- 🗞 Religious beliefs
- 🚳 Recreational activities.

Groups are formed by people with at least one similar attribute.



The PoCSverse Small-world networks 49 of 68

Small-world networks

cxperimen

Ineory

Generalized affiliation networks Nutshell

One approach: incorporate identity.

Identity is formed from attributes such as:

- 🚳 Geographic location
- 🚳 Type of employment
- 🚳 Religious beliefs
- 🚳 Recreational activities.

Groups are formed by people with at least one similar attribute.

Attributes \Leftrightarrow Contexts \Leftrightarrow Interactions \Leftrightarrow Networks.

The PoCSverse Small-world networks 49 of 68

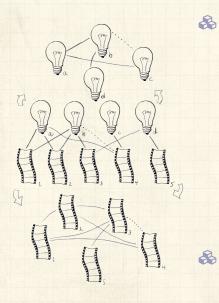
Small-world networks

ть

Generalized affiliation networks Nutshell



Bipartite affiliation structures:



Many real-world networks have an underlying multi-partite structure.

- Stories-tropes.
- Boards and directors.
- Films-actorsdirectors.
- Classes-teachersstudents.
- Upstairsdownstairs.

Unipartite networks may be induced or co-exist. The PoCSverse Small-world networks 50 of 68

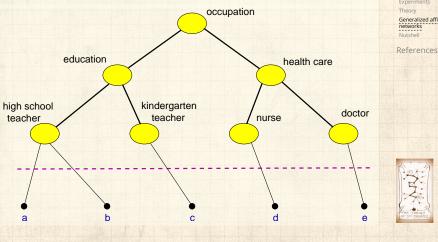
Small-world networks Experiments

Experimen

Generalized affiliation networks Nutshell



Social distance—Context distance



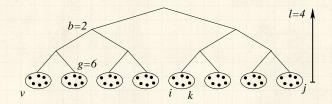
The PoCSverse Small-world networks 51 of 68

Small-world networks

Experiments

Generalized affiliation networks Nutshell

Distance between two individuals x_{ij} is the height of lowest common ancestor.



$$x_{ij} = 3$$
, $x_{ik} = 1$, $x_{iv} = 4$.

The PoCSverse Small-world networks 52 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell



The PoCSverse Small-world networks 53 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell

References

Individuals are more likely to know each other the closer they are within a hierarchy.



Individuals are more likely to know each other the closer they are within a hierarchy.
 Construct *z* connections for each node using

$$p_{ij} = c \exp\{-\alpha x_{ij}\}.$$

The PoCSverse Small-world networks 53 of 68

Small-world networks Experiments

Theony

Generalized affiliation networks Nutshell



Individuals are more likely to know each other the closer they are within a hierarchy.
 Construct *z* connections for each node using

 $p_{ij} = c \exp\{-\alpha x_{ij}\}.$

 $\alpha = 0$: random connections.



The PoCSverse Small-world networks 53 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell

Individuals are more likely to know each other the closer they are within a hierarchy.
 Construct *z* connections for each node using

 $p_{ij} = c \exp\{-\alpha x_{ij}\}.$

 $\begin{array}{l} \displaystyle \textcircled{\&} \ \ \alpha = 0: \mbox{ random connections.} \\ \displaystyle \begin{array}{l} \displaystyle \textcircled{\&} \ \ \alpha \mbox{ large: local connections.} \end{array} \end{array}$



The PoCSverse Small-world networks 53 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell

geography occupation age 0 100 а e \lambda Blau & Schwartz^[2], Simmel^[8], Breiger^[3], Watts *et* al. ^[10]; see also Google+ Circles.

Generalized affiliation networks

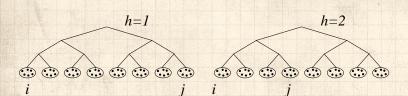


Small-world networks

Experiments

Theory

Generalized affiliation networks Nutshell



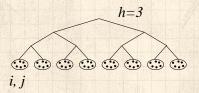
The PoCSverse Small-world networks 55 of 68

Small-world networks Experiments

Experimen

Theory

Generalized affiliation networks Nutshell

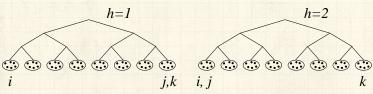


$$\begin{split} \vec{v}_i &= [1 \; 1 \; 1]^T, \vec{v}_j = [8 \; 4 \; 1]^T \\ x^1_{ij} &= 4, \; x^2_{ij} = 3, \; x^3_{ij} = 1. \end{split}$$

Social distance:
$$y_{ij} = \min_h x_{ij}^h$$
.



Triangle inequality doesn't hold:



 $y_{ik} = 4 > y_{ij} + y_{jk} = 1 + 1 = 2.$



The PoCSverse Small-world networks 56 of 68

Small-world networks

Experiments

Theory

Generalized affiliation networks Nutshell

lndividuals know the identity vectors of

The PoCSverse Small-world networks 57 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell



lndividuals know the identity vectors of 1. themselves,

The PoCSverse Small-world networks 57 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell



lndividuals know the identity vectors of

- 1. themselves,
- 2. their friends,

The PoCSverse Small-world networks 57 of 68

Small-world networks Experiments

Experimen

Theory

Generalized affiliation networks Nutshell



lndividuals know the identity vectors of

- 1. themselves,
- 2. their friends, and
- 3. the target.

The PoCSverse Small-world networks 57 of 68

Small-world networks Experiments

Experimen

Theory

Generalized affiliation networks Nutshell



lndividuals know the identity vectors of

- 1. themselves,
- 2. their friends,
 - and
- 3. the target.
- Individuals can estimate the social distance between their friends and the target.

The PoCSverse Small-world networks 57 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell



lndividuals know the identity vectors of

- 1. themselves,
- 2. their friends,
- and a the targe
- 3. the target.
- Individuals can estimate the social distance between their friends and the target.
- Use a greedy algorithm + allow searches to fail randomly.

The PoCSverse Small-world networks 57 of 68

Small-world networks Experiments

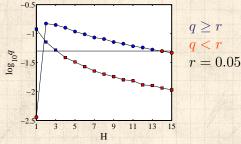
Theony

Generalized affiliation networks Nutshell



The model-results—searchable networks

 $\alpha = 0$ versus $\alpha = 2$ for $N \simeq 10^5$:



The PoCSverse Small-world networks 58 of 68 Small-world networks

Experiments

Theory

Generalized affiliation networks Nutshell

References

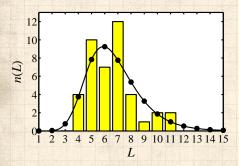
q = probability an arbitrary message chain reaches a target.

- 🚳 A few dimensions help.
- 🗞 Searchability decreases as population increases.
- Precise form of hierarchy largely doesn't matter.



The model-results

Milgram's Nebraska-Boston data:



Model parameters: $N = 10^8$, z = 300, g = 100, b = 10, $\alpha = 1, H = 2$;

 $\left. \begin{array}{l} \bigotimes \ \left< L_{\rm model} \right> \simeq 6.7 \\ \bigotimes \ \ L_{\rm data} \simeq 6.5 \end{array} \right.$



The PoCSverse Small-world networks 59 of 68

Small-world networks Experiments

Theory

Generalized affiliation networks Nutshell

Social search—Data

Adamic and Adar (2003)

For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.



Small-world networks Experiments

- -

Generalized affiliation

networks Nutshell



Social search—Data

Adamic and Adar (2003)

- For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.
- Solution Probability of connection as function of real distance $\propto 1/r$.

The PoCSverse Small-world networks 60 of 68

Small-world networks Experiments

Thoony

Generalized affiliation networks Nutshell



Social Search—Real world uses

Tags create identities for objects

- 🚳 Website tagging: bitly.com 🗹
- 🚳 (e.g., Wikipedia)
- 🚳 Photo tagging: flickr.com
- Dynamic creation of metadata plus links between information objects.
- 🗞 Folksonomy: collaborative creation of metadata



The PoCSverse Small-world networks 61 of 68

Small-world networks

Experimen

Generalized affiliation networks Nutshell

Social Search—Real world uses

Recommender systems:

Amazon uses people's actions to build effective connections between books.

The PoCSverse Small-world networks 62 of 68

Small-world networks Experiments

experimen

Theory

Generalized affiliation networks Nutshell



Social Search—Real world uses

Recommender systems:

- Amazon uses people's actions to build effective connections between books.
- Source of the hoi polloi.

The PoCSverse Small-world networks 62 of 68

Small-world networks Experiments

Experimen

Theory

Generalized affiliation networks Nutshell



Outline

Small-world networks

Experiments Theory Generalized affiliation networks Nutshell The PoCSverse Small-world networks 63 of 68

Small-world networks Experiments Theory Generalized affiliation networks

Nutshell



🚳 Bare networks are typically unsearchable.

The PoCSverse Small-world networks 64 of 68

Small-world networks Experiments Theory Generalized affiliation networks

Nutshell



Bare networks are typically unsearchable.
 Paths are findable if nodes understand how network is formed.

The PoCSverse Small-world networks 64 of 68

Small-world networks Experiments Theory Generalized affiliation networks

Nutshell



- 🚳 Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- lmportance of identity (interaction contexts).

The PoCSverse Small-world networks 64 of 68

Small-world networks Experiments Theory Generalized affiliation networks

Nutshell



- 🚳 Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- lmportance of identity (interaction contexts).
- lmproved social network models.

The PoCSverse Small-world networks 64 of 68

Small-world networks Experiments Theory Generalized affiliation networks

Nutshell



- 🚳 Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- 🚳 Importance of identity (interaction contexts).
- lmproved social network models.
- 🚳 Construction of peer-to-peer networks.

The PoCSverse Small-world networks 64 of 68

Small-world networks Experiments Theory Generalized affiliation networks

Nutshell



- 🚳 Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- 🚳 Importance of identity (interaction contexts).
- 🚳 Improved social network models.
- 🗞 Construction of peer-to-peer networks.
- Construction of searchable information databases.

The PoCSverse Small-world networks 64 of 68

Small-world networks Experiments Theory Generalized affiliation networks

Nutshell



Neural reboot (NR):

Food-induced happiness

The PoCSverse Small-world networks 65 of 68

Small-world networks Experiments Theory

Generalized affiliation networks

Nutshell

References



https://www.youtube.com/watch?v=vC8gJ0_9o4M?rel=0

References I

 L. Adamic, R. Lukose, A. Puniyani, and B. Huberman.
 Search in power-law networks.
 Phys. Rev. E, 64:046135, 2001. pdf C

- [2] P. M. Blau and J. E. Schwartz. Crosscutting Social Circles. Academic Press, Orlando, FL, 1984.
- [3] R. L. Breiger. The duality of persons and groups. <u>Social Forces</u>, 53(2):181–190, 1974. pdf C
- [4] P. S. Dodds, R. Muhamad, and D. J. Watts. An experimental study of search in global social networks. Science, 301:827–829, 2003. pdf

The PoCSverse Small-world networks 66 of 68

Small-world networks Experiments Theory Generalized affiliation networks Nutshell



References II

- [5] M. Granovetter. The strength of weak ties. Am. J. Sociol., 78(6):1360–1380, 1973. pdf C
- [6] J. Kleinberg. Navigation in a small world. Nature, 406:845, 2000. pdf C
- [7] G. Pickard, W. Pan, I. Rahwan, M. Cebrian, R. Crane, A. Madan, and A. Pentland. Time-critical social mobilization. <u>Science</u>, 334:509–512, 2011. pdf

 [8] G. Simmel. The number of members as determining the sociological form of the group. I. American Journal of Sociology, 8:1–46, 1902. The PoCSverse Small-world networks 67 of 68

Small-world networks Experiments Theory Generalized affiliation networks Nutshell



References III

[9] J. Travers and S. Milgram. An experimental study of the small world problem. Sociometry, 32:425–443, 1969. pdf

[10] D. J. Watts, P. S. Dodds, and M. E. J. Newman. Identity and search in social networks. Science, 296:1302–1305, 2002. pdf

[11] D. J. Watts and S. J. Strogatz. Collective dynamics of 'small-world' networks. Nature, 393:440–442, 1998. pdf Pdf The PoCSverse Small-world networks 68 of 68

Small-world networks Experiments Theory Generalized affiliation networks Nutshell

