

# Organizational Networks: Information Exchange and Robustness

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Principles of Complex Systems, Vols. 1 & 2  
CSYS/MATH 300 and 303, 2021-2022 | @pocsvox

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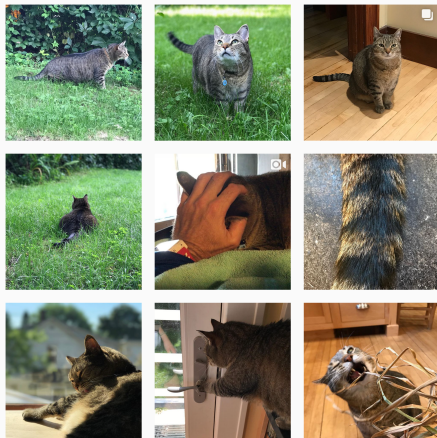
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 On Instagram at [pratchett\\_the\\_cat](https://www.instagram.com/pratchett_the_cat) 

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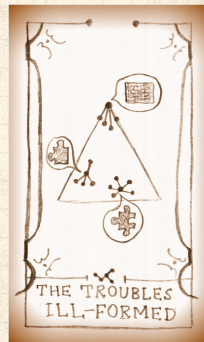
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# Overview

The basic idea/problem/motivation/history:

 Organizations as information exchange entities.

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The basic idea/problem/motivation/history:

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The basic idea/problem/motivation/history:

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-  Catastrophe recovery.
-  Solving ambiguous, ill-defined problems.

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## The basic idea/problem/motivation/history:

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-  Solving ambiguous, ill-defined problems.
-  Robustness as 'optimal' design feature.

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## A model of organizational networks:

- Network construction algorithm.



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## A model of organizational networks:

- Network construction algorithm.
- Task specification.
- Message routing algorithm.

## Results:

- Performance measures.



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# February, 1997:

Aisin (eye-sheen), maker of brake valve parts for Toyota, burns to ground. [4]

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Aisin (eye-sheen), maker of brake valve parts for Toyota, burns to ground. [4]

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- 14,000 cars per day  $\rightarrow$  0 cars per day.
- 6 months before new machines would arrive.
- Recovered in 5 days.

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- 🧱 14,000 cars per day  $\rightarrow$  0 cars per day.
- 🧱 6 months before new machines would arrive.
- 🧱 Recovered in 5 days.

🧱 Case study performed by Nishiguchi and Beaudet [4]


"Fractal Design: Self-organizing Links in Supply Chain"

in "Knowledge Creation: A New Source of Value"



# February, 1997:

## Some details:

 36 suppliers, 150 subcontractors

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# February, 1997:

## Some details:

 36 suppliers, 150 subcontractors

 50 supply lines

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## Some details:

 36 suppliers, 150 subcontractors

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 Sewing machine maker with no experience in car parts spent about 500 man hours refitting a milling machine to produce 40 valves a day.



# February, 1997:

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## Some details:

- 36 suppliers, 150 subcontractors
- 50 supply lines
- Sewing machine maker with no experience in car parts spent about 500 man hours refitting a milling machine to produce 40 valves a day.
- Recovery depended on horizontal links which arguably provided:



# February, 1997:

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-  36 suppliers, 150 subcontractors
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  1. robustness



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## Some details:

-  36 suppliers, 150 subcontractors
-  50 supply lines
-  Sewing machine maker with no experience in car parts spent about 500 man hours refitting a milling machine to produce 40 valves a day.
-  Recovery depended on horizontal links which arguably provided:
  1. robustness
  2. searchability



# Some things fall apart:



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LEHMAN BROTHERS



# Rebirth:

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# Motivation

Recovery from catastrophe involves solving problems that are:

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# Motivation

Recovery from catastrophe involves solving problems that are:

 Unanticipated,

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# Motivation

Recovery from catastrophe involves solving problems that are:

-  Unanticipated,
-  Unprecedented,

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# Motivation

Recovery from catastrophe involves solving problems that are:

-  Unanticipated,
-  Unprecedented,
-  Ambiguous (nothing is obvious),

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# Motivation

Recovery from catastrophe involves solving problems that are:

- 🧱 Unanticipated,
- 🧱 Unprecedented,
- 🧱 Ambiguous (nothing is obvious),
- 🧱 Distributed (knowledge/people/resources),



# Motivation

Recovery from catastrophe involves solving problems that are:

- 🧱 Unanticipated,
- 🧱 Unprecedented,
- 🧱 Ambiguous (nothing is obvious),
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Recovery from catastrophe involves solving problems that are:

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Recovery from catastrophe involves solving problems that are:

- 🧱 Unanticipated,
- 🧱 Unprecedented,
- 🧱 Ambiguous (nothing is obvious),
- 🧱 Distributed (knowledge/people/resources),
- 🧱 Limited by existing resources,
- 🧱 Critical for survival.

Frame:

- 🧱 Collective solving of ambiguous problems



# Motivation

## Ambiguity:



Question much less answer is not well understood.

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# Motivation

## Ambiguity:

- Question much less answer is not well understood.
- Back and forth search process rephrases question.

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# Motivation

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## Ambiguity:

- Question much less answer is not well understood.
- Back and forth search process rephrases question.
- Leads to iterative process of query reformulation.



# Motivation






## Ambiguity:

-  Question much less answer is not well understood.
-  Back and forth search process rephrases question.
-  Leads to iterative process of query reformulation.
-  Ambiguous tasks are inherently not decomposable.



# Motivation

## Ambiguity:

-  Question much less answer is not well understood.
-  Back and forth search process rephrases question.
-  Leads to iterative process of query reformulation.
-  Ambiguous tasks are inherently not decomposable.
-  How do individuals collectively work on an ambiguous organization-scale problem?



# Motivation

## Ambiguity:

- Question much less answer is not well understood.
- Back and forth search process rephrases question.
- Leads to iterative process of query reformulation.
- Ambiguous tasks are inherently not decomposable.
- How do individuals collectively work on an ambiguous organization-scale problem?
- How do we define ambiguity?



# Let's modelify:

Modeling ambiguous problems is hard...

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# Let's modelify:


Modeling ambiguous problems is hard...


 Model response instead...



# Let's modelify:

Modeling ambiguous problems is hard...

 Model response instead...

 Individuals need novel information and must communicate with others outside of their usual contacts.



# Let's modelify:

## Modeling ambiguous problems is hard...

- Model response instead...
- Individuals need novel information and must communicate with others outside of their usual contacts.
- Creative search is intrinsically inefficient.



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Modeling ambiguous problems is hard...

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Focus on robustness:



# Let's modelify:

## Modeling ambiguous problems is hard...

- Model response instead...
- Individuals need novel information and must communicate with others outside of their usual contacts.
- Creative search is intrinsically inefficient.

## Focus on robustness:

- Avoidance of individual failures.



# Let's modelify:

## Modeling ambiguous problems is hard...

- Model response instead...
- Individuals need novel information and must communicate with others outside of their usual contacts.
- Creative search is intrinsically inefficient.

## Focus on robustness:

- Avoidance of individual failures.
- Survival of organization even when failures do occur.



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# Why organizations exist:



"The Nature of the Firm" 

Ronald H. Coase,  
*Economica*, **New Series**, 4, 386–405, 1937. [1]

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# Why organizations exist:



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Notion of Transaction Costs ↗

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Notion of Transaction Costs



More efficient for individuals to cooperate outside of the market.

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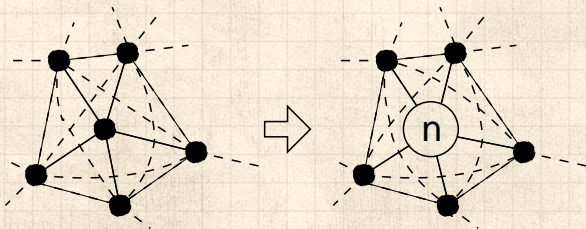
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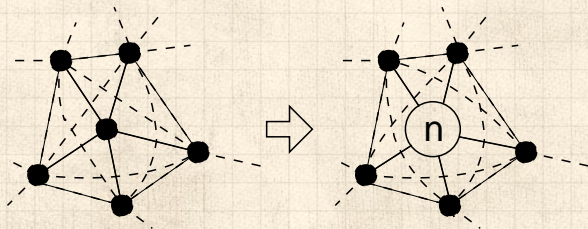


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# Real organizations—Extremes

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## Hierarchy:

-  Maximum efficiency,
-  Suited to static environment,
-  Brittle.



# Real organizations—Extremes

## Hierarchy:

- Maximum efficiency,
- Suited to static environment,
- Brittle.


## Market:


- Resilient,
- Suited to rapidly changing environment,
- Requires costless or low cost interactions.



# Organizations as efficient hierarchies

 Economics: Organizations  $\equiv$  Hierarchies.

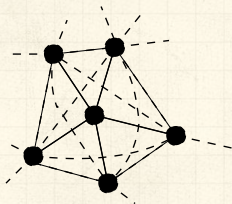
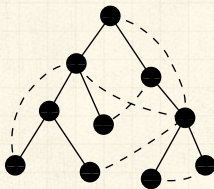
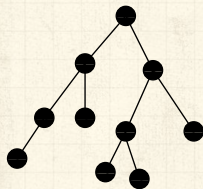
 e.g., Radner (1993)<sup>[5]</sup>, Van Zandt (1998)<sup>[7]</sup>

 Hierarchies performing associative operations:



# Real organizations...

But real, complex organizations are in the middle...



["Heterarchy"](#)

David Stark,

The Biology of Business: Decoding the Natural Laws of the Enterprise., **New Series**, 4, 153–, 1999. [6]



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# Optimal network topologies for local search



“Optimal network topologies for local search with congestion” 

Guimerà et al.,  
Phys. Rev. Lett., **89**, 248701, 2002. <sup>[3]</sup>

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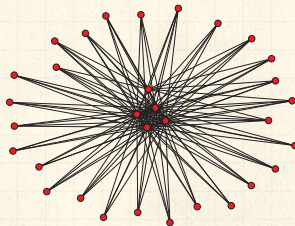
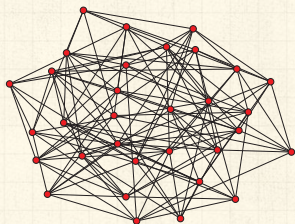
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Parallel search and congestion.



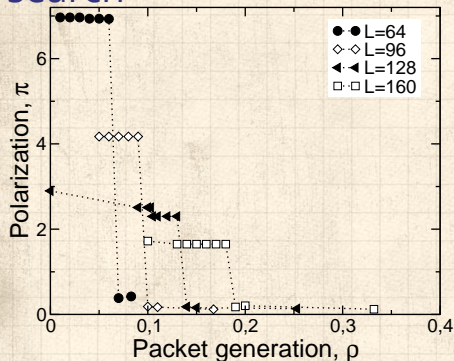
Queueing and network collapse.



Exploration of random search mechanisms.



# Optimal network topologies for local search



Betweenness:  $\beta$ .

Polarization:

$$\pi = \frac{\max \beta}{\langle \beta \rangle} - 1.$$

$L$  = number of links.

Goal: minimize average search time.

Few searches  $\Rightarrow$  hub-and-spoke network.

Many searches  $\Rightarrow$  decentralized network.

Phase transition?



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# Desirable organizational qualities:

1. Low cost (requiring few links).

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# Desirable organizational qualities:

1. Low cost (requiring few links).
2. Scalability.

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# Desirable organizational qualities:

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# Desirable organizational qualities:

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# Desirable organizational qualities:

1. Low cost (requiring few links).
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3. Ease of construction—existence is plausible.
4. Searchability.
5. **'Ultra-robustness'**:

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# Desirable organizational qualities:

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5. **'Ultra-robustness'**:
  - I Congestion robustness  
(Resilience to failure due to information exchange);



# Desirable organizational qualities:

1. Low cost (requiring few links).
2. Scalability.
3. Ease of construction—existence is plausible.
4. Searchability.
5. **'Ultra-robustness'**:
  - I Congestion robustness  
(Resilience to failure due to information exchange);
  - II Connectivity robustness  
(Recoverability in the event of failure).



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## Small world problem:

- Can individuals pass a message to a target individual using only personal connections?
- Yes, large scale networks searchable if nodes have identities.
- "Identity and Search in Social Networks," Watts, Dodds, & Newman, 2002. [8]



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# "Information exchange and the robustness of organizational networks" ↗

Dodds, Watts, and Sabel,

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## Formal organizational structure:

 Underlying hierarchy:

 branching ratio  $b$

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## Formal organizational structure:

 Underlying hierarchy:

-  branching ratio  $b$
-  depth  $L$

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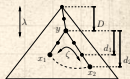
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Dodds, Watts, and Sabel,  
Proc. Natl. Acad. Sci., **100**, 12516–12521,  
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## Formal organizational structure:

 Underlying hierarchy:

 branching ratio  $b$

 depth  $L$

  $N = (b^L - 1)/(b - 1)$  nodes

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## Formal organizational structure:

 Underlying hierarchy:

-  branching ratio  $b$
-  depth  $L$
-   $N = (b^L - 1)/(b - 1)$  nodes
-   $N - 1$  links

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## Formal organizational structure:

 Underlying hierarchy:

-  branching ratio  $b$
-  depth  $L$
-   $N = (b^L - 1)/(b - 1)$  nodes
-   $N - 1$  links

 Additional informal ties:

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 Underlying hierarchy:

-  branching ratio  $b$
-  depth  $L$
-   $N = (b^L - 1)/(b - 1)$  nodes
-   $N - 1$  links

 Additional informal ties:

-  Choose  $m$  links according to a two parameter probability distribution

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## Formal organizational structure:

Underlying hierarchy:

- branching ratio  $b$
- depth  $L$
- $N = (b^L - 1)/(b - 1)$  nodes
- $N - 1$  links

Additional informal ties:

- Choose  $m$  links according to a two parameter probability distribution
- $0 \leq m \leq (N - 1)(N - 2)/2$



# Model—underlying hierarchy

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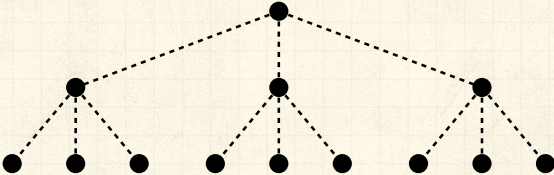
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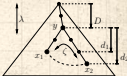
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## Model—formal structure:



$$b = 3, \quad L = 3, \quad N = 13$$





# Model—addition of links

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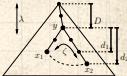
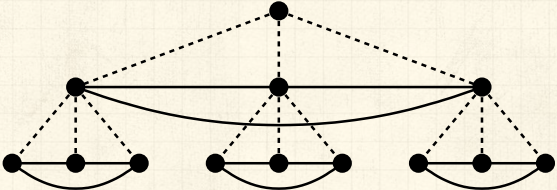
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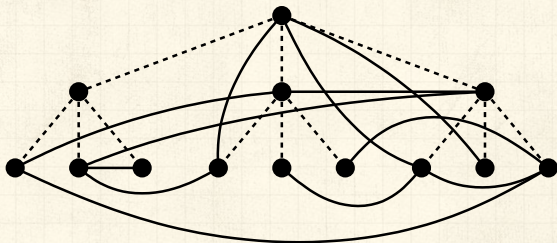
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## Team-based networks ( $m = 12$ ):



# Model—addition of links

Random networks ( $m = 12$ ):



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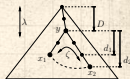
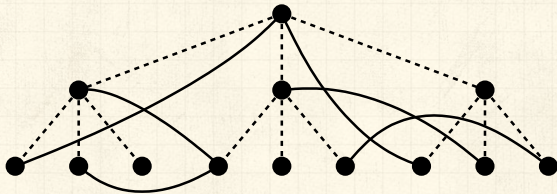
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Random interdivisional networks ( $m = 6$ ):



# Model—addition of links

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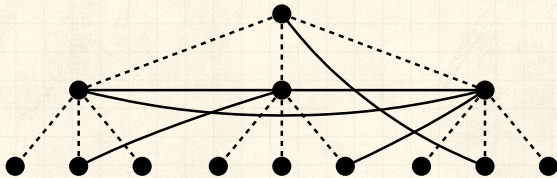
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Core-periphery networks ( $m = 6$ ):



# Model—addition of links

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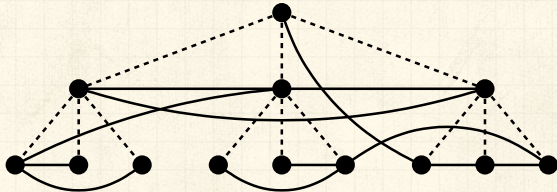
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Multiscale networks ( $m = 12$ ):



# Model—construction

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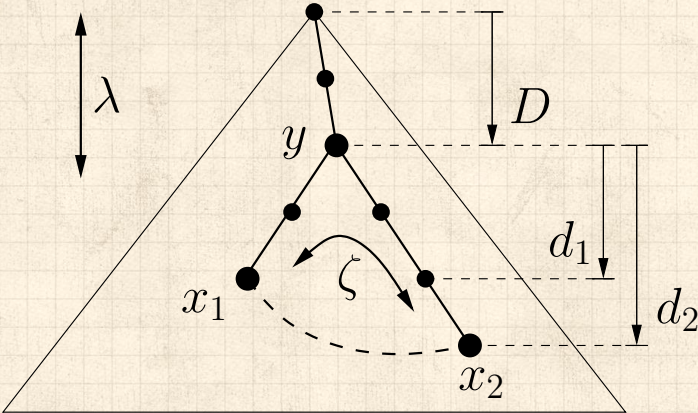
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 Link addition probability:

$$P(D, d_1, d_2) \propto e^{-D/\lambda} e^{-f(d_1, d_2)/\zeta}$$

 First choose  $(D, d_1, d_2)$ .

 Randomly choose  $(y, x_1, x_2)$  given  $(D, d_1, d_2)$ .

 Choose links without replacement.



# Model—construction

Requirements for  $f(d_1, d_2)$ :

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# Model—construction

Requirements for  $f(d_1, d_2)$ :

1.  $f \geq 0$  for  $d_1 + d_2 \geq 2$

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Requirements for  $f(d_1, d_2)$ :

1.  $f \geq 0$  for  $d_1 + d_2 \geq 2$
2.  $f$  increases monotonically with  $d_1, d_2$ .



# Model—construction

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Requirements for  $f(d_1, d_2)$ :

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3.  $f(d_1, d_2) = f(d_2, d_1)$ .



# Model—construction

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Requirements for  $f(d_1, d_2)$ :

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3.  $f(d_1, d_2) = f(d_2, d_1)$ .
4.  $f$  is maximized when  $d_1 = d_2$ .



# Model—construction

## Requirements for $f(d_1, d_2)$ :

1.  $f \geq 0$  for  $d_1 + d_2 \geq 2$
2.  $f$  increases monotonically with  $d_1, d_2$ .
3.  $f(d_1, d_2) = f(d_2, d_1)$ .
4.  $f$  is maximized when  $d_1 = d_2$ .

## Simple function satisfying 1-4:

$$f(d_1, d_2) = (d_1^2 + d_2^2 - 2)^{1/2}$$
$$\Rightarrow P(y, x_1, x_2) \propto e^{-D/\lambda} e^{-(d_1^2 + d_2^2 - 2)^{1/2} / \zeta}$$



# Model—limiting cases

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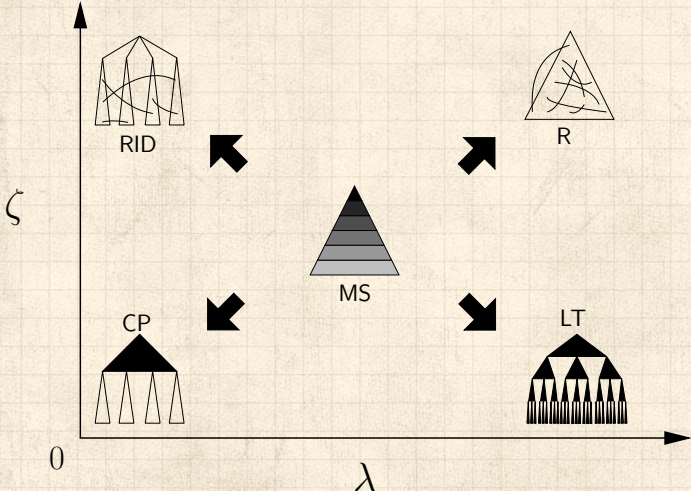
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# Message passing pattern



Each of  $T$  time steps, each node generates a message with probability  $\mu$ .

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# Message passing pattern

- Each of  $T$  time steps, each node generates a message with probability  $\mu$ .
- Recipient of message chosen based on distance from sender.

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# Message passing pattern

 Each of  $T$  time steps, each node generates a message with probability  $\mu$ .

 Recipient of message chosen based on distance from sender.



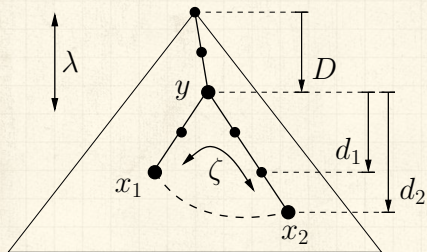
$$P(\text{recipient at distance } d) \propto e^{-d/\xi}.$$

1.  $\xi$  = measure of uncertainty;
2.  $\xi = 0$ : local message passing;
3.  $\xi = \infty$ : random message passing.



# Message passing pattern:

Distance  $d_{12}$  between two nodes  $x_1$  and  $x_2$ :



$$d_{12} = \max(d_1, d_2) = 3$$



Measure unchanged with presence of informal ties.

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# Message passing pattern

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## Simple message routing algorithm:


- Look ahead one step: always choose neighbor closest to recipient node.



# Message passing pattern

## Simple message routing algorithm:

 Look ahead one step: always choose neighbor closest to recipient node.

 Pseudo-global knowledge:

1. Nodes understand hierarchy.
2. Nodes know only local informal ties.



# Message passing pattern

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Interpretations:

1. Sender knows specific recipient.



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## Interpretations:

1. Sender knows specific recipient.
2. Sender requires certain kind of recipient.



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## Interpretations:

1. Sender knows specific recipient.
2. Sender requires certain kind of recipient.
3. Sender seeks specific information but recipient unknown.





# Message passing pattern

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## Interpretations:

1. Sender knows specific recipient.
2. Sender requires certain kind of recipient.
3. Sender seeks specific information but recipient unknown.
4. Sender has a problem but information/recipient unknown.



# Message passing pattern

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Performance:

 Measure Congestion Centrality  $\rho_i$ , fraction of messages passing through node  $i$ .



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## Performance:

 Measure Congestion Centrality  $\rho_i$ , fraction of messages passing through node  $i$ .

 Similar to betweenness centrality.



# Message passing pattern


## Performance:


- Measure Congestion Centrality  $\rho_i$ , fraction of messages passing through node  $i$ .
- Similar to betweenness centrality.
- However: depends on
  1. Search algorithm;




# Message passing pattern

## Performance:

 Measure Congestion Centrality  $\rho_i$ , fraction of messages passing through node  $i$ .

 Similar to betweenness centrality.

 However: depends on

1. Search algorithm;
2. Task specification  $(\mu, \xi)$ .



# Message passing pattern

## Performance:

- Measure Congestion Centrality  $\rho_i$ , fraction of messages passing through node  $i$ .
- Similar to betweenness centrality.
- However: depends on
  - Search algorithm;
  - Task specification  $(\mu, \xi)$ .
- Congestion robustness comes from minimizing  $\rho_{\max}$ .



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Parameter settings (unless varying):

 Underlying hierarchy:  $b = 5, L = 6, N = 3096$ ;





# Performance testing:

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## Parameter settings (unless varying):

 Underlying hierarchy:  $b = 5, L = 6, N = 3096$ ;

 Number of informal ties:  $m = N$ .



# Performance testing:

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## Parameter settings (unless varying):

 Underlying hierarchy:  $b = 5, L = 6, N = 3096$ ;

 Number of informal ties:  $m = N$ .

 Link addition algorithm:  $\lambda = \zeta = 0.5$ .



# Performance testing:

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## Parameter settings (unless varying):

- Underlying hierarchy:  $b = 5, L = 6, N = 3096$ ;
- Number of informal ties:  $m = N$ .
- Link addition algorithm:  $\lambda = \zeta = 0.5$ .
- Message passing:  $\xi = 1, \mu = 10/N, T = 1000$ .



# Results—congestion robustness

## Overview

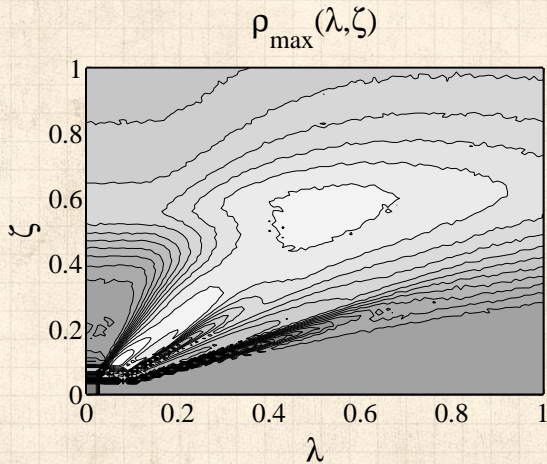
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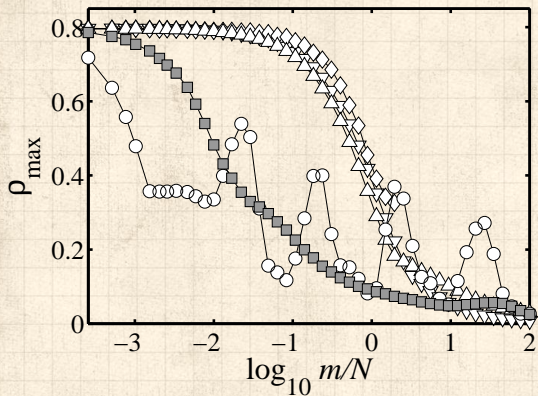
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# Results—varying number of links added:



◇=TB

▽=R

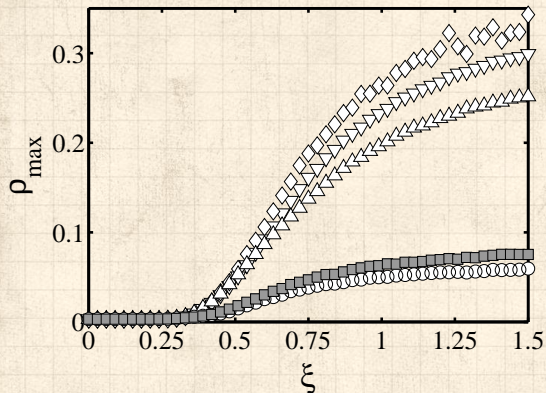
△=RID

○=CP

□=MS



# Results—varying message passing pattern



◇=TB

▽=R


△=RID

○=CP

□=MS



# Results—Maximum firm size

 Congestion may increase with size of network.

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# Results—Maximum firm size

- 🧱 Congestion may increase with size of network.
- 🧱 Fix rate of message passing ( $\mu$ ) and Message pattern ( $\xi$ ).

## Overview

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# Results—Maximum firm size

- 🧱 Congestion may increase with size of network.
- 🧱 Fix rate of message passing ( $\mu$ ) and Message pattern ( $\xi$ ).
- 🧱 Fix branching ratio of hierarchy and add more levels.



# Results—Maximum firm size

- 🧱 Congestion may increase with size of network.
- 🧱 Fix rate of message passing ( $\mu$ ) and Message pattern ( $\xi$ ).
- 🧱 Fix branching ratio of hierarchy and add more levels.
- 🧱 Individuals have limited capacity  $\Rightarrow$  limit to firm size.



# Scalability in complete uncertainty: $\xi = \infty$

## Overview

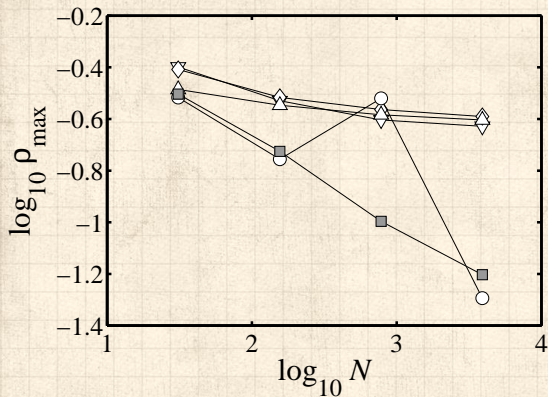
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◇=TB

▽=R


△=RID

○=CP

□=MS





## Inducing catastrophic failure:

 Remove  $N_r$  nodes and measure relative size of largest component  $C = S/(N - N_r)$ .



## Inducing catastrophic failure:

 Remove  $N_r$  nodes and measure relative size of largest component  $C = S/(N - N_r)$ .

 Four deletion sequences:

1. Top-down;
2. Random;
3. Hub;
4. Cascading failure.



## Inducing catastrophic failure:

Remove  $N_r$  nodes and measure relative size of largest component  $C = S/(N - N_r)$ .

Four deletion sequences:

1. Top-down;
2. Random;
3. Hub;
4. Cascading failure.

Results largely independent of sequence.



# Results—Connectivity Robustness

## Overview

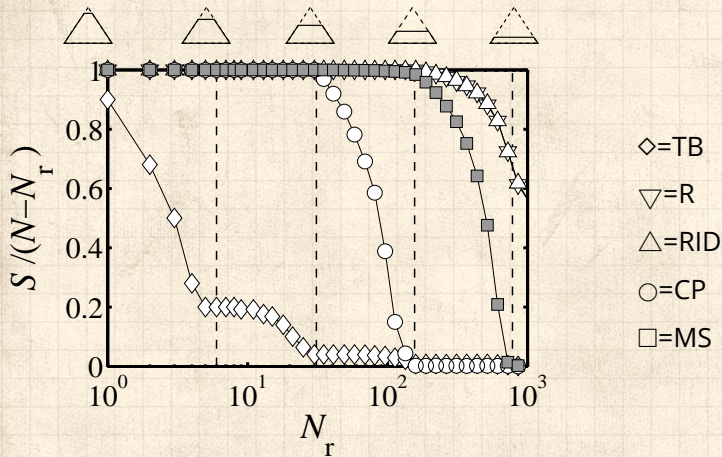
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# Summary of results

Feature	Congestion Robustness	Connectivity Robustness	Scalability
Core-periphery	good	average	average
Random	poor	good	poor
Rand. Interdivisional	poor	good	poor
Team-based	poor	poor	poor
Multiscale	good	good	good





# Conclusory moments

## Multi-scale networks:

1. Possess good Congestion Robustness and Connectivity  
Robustness  $\Rightarrow$  Ultra-robust;

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## Multi-scale networks:

1. Possess good Congestion Robustness and Connectivity  
Robustness  $\Rightarrow$  Ultra-robust;
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3. Relatively insensitive to parameter choice;



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## Multi-scale networks:

1. Possess good Congestion Robustness and Connectivity  
Robustness  $\Rightarrow$  Ultra-robust;
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3. Relatively insensitive to parameter choice;

 Above suggests existence of multi-scale structure is plausible.



# Conclusory moments



Foregoing is an attempt to model what organizations might look like beyond simple hierarchies (2003).

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# Conclusory moments

- ⊞ Foregoing is an attempt to model what organizations might look like beyond simple hierarchies (2003).
- ⊞ Possible work: develop 'bottom up' model of organizational networks based on social search, identity (emergent searchability).

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- ⊞ Foregoing is an attempt to model what organizations might look like beyond simple hierarchies (2003).
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- ⊞ Balance of **generalists versus specialists**—how many middle managers does an organization need?

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- ⊞ Foregoing is an attempt to model what organizations might look like beyond simple hierarchies (2003).
- ⊞ Possible work: develop 'bottom up' model of organizational networks based on social search, identity (emergent searchability).
- ⊞ Balance of **generalists versus specialists**—how many middle managers does an organization need?
- ⊞ Still a need for data on real organizations...

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