Overview of Complex Networks

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Principles of Complex Systems, Vols. 1 & 2 CSYS/MATH 300 and 303, 2021–2022 |@pocsvox

Prof. Peter Sheridan Dodds | @peterdodds

Computational Story Lab | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont



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Overview of Complex Networks

Complex Networks Basics Etymology Popularity Graph theory? Basic definitions

Examples of Complex Networks Physical networks Interaction networks Relational networks

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Outline

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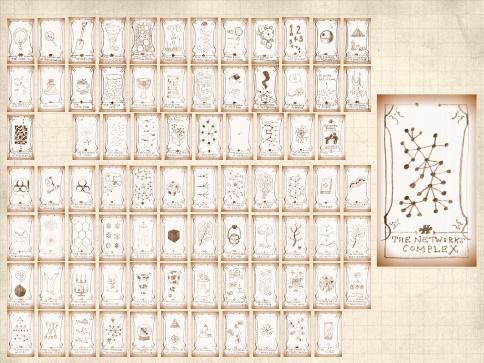
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net•work |'net_iwərk|

noun

1 an arrangement of intersecting horizontal and vertical lines.

• a complex system of roads, railroads, or other transportation routes : *a network of railroads*.

2 a group or system of interconnected people or things : a trade network.

- a group of people who exchange information, contacts, and experience for professional or social purposes : a support network.
- a group of broadcasting stations that connect for the simultaneous broadcast of a program : the introduction of a second TV network | [as adj.] network television.
- a number of interconnected computers, machines, or operations : *specialized computers that manage multiple outside connections to a network* | *a local cellular phone network*.
- a system of connected electrical conductors.

verb [trans.]

connect as or operate with a network : the stock exchanges have proven to be resourceful in networking these deals.

• link (machines, esp. computers) to operate interactively : [as adj.] (**networked**) networked workstations.

• [intrans.] [often as n.] (**networking**) interact with other people to exchange information and develop contacts, esp. to further one's career : *the skills of networking, bargaining, and negotiation.*

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Thesaurus deliciousness:

network

noun

 a network of arteries WEB, lattice, net, matrix, mesh, crisscross, grid, reticulum, reticulation; Anatomy plexus.
 a network of lanes MAZE, labyrinth, warren, tangle.
 a network of friends SYSTEM, complex, nexus, web, webwork.

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Ancestry:

From Keith Briggs's excellent etymological investigation:



🚳 Opus reticulatum: \lambda A Latin origin?



[http://serialconsign.com/2007/11/we-put-net-

network]

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Ancestry:

First known use: Geneva Bible, 1560 'And thou shalt make unto it a grate like networke of brass (Exodus xxvii 4).'

From the OED via Briggs:

- 🚳 1658–: reticulate structures in animals
- 🚳 1839–: rivers and canals
- \lambda 1869–: railways
- \lambda 1883–: distribution network of electrical cables
- 🗞 1914–: wireless broadcasting networks

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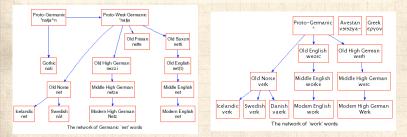
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Ancestry: Net and Work are venerable old words: 'Net' first used to mean spider web (King Ælfréd, 888).

Work' appear to have long meant purposeful action.



 'Network' = something built based on the idea of natural, flexible lattice or web.
 c.f., ironwork, stonework, fretwork.

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Key Observation:

- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...
- …largely due to your typical theoretical physicist:



- 🗃 Piranha physicus
- 🝞 Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)



See also: https://xkcd.com/793/

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Popularity (according to Google Scholar)



"Collective dynamics of 'small-world' networks" Watts and Strogatz, Nature, **393**, 440–442, 1998.^[16]

Times cited: $\Box \sim 37,460$ (as of October 24, 2018)



"Emergence of scaling in random networks" Barabási and Albert, Science, **286**, 509–511, 1999.^[2]

Times cited: 27 ~ 32,093 (as of October 24, 2018)

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Review articles:



"Complex Networks: Structure and Dynamics" Boccaletti et al., Physics Reports, **424**, 175–308, 2006. ^[3]

Times cited: 🗹 ~ 8,533 (as of October 24, 2018)



"The structure and function of complex networks" M. E. J. Newman, SIAM Rev., **45**, 167–256, 2003. ^[12]

Times cited: 27 ~ 17,782 (as of October 24, 2018)



"Statistical mechanics of complex networks" Albert and Barabási, Rev. Mod. Phys., **74**, 47–97, 2002. ^[1]

Times cited: C ~ 20,531 (as of October 24, 2018)

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Popularity according to textbooks:



"Networks" **3** C by Mark Newman (2018).^[11]





"Networks, crowds, and markets: Reasoning about a highly connected world" **3**, by Easley and Kleinberg (2010). ^[7]

http://cs.cornell.edu/home/kleinber/networks-book/

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Popularity according to books:



GLADWELL

(it is different into " - Political

The Tipping Point: How Little Things can make a Big Difference—Malcolm Gladwell^[8]



Nexus: Small Worlds and the Groundbreaking Science of Networks—Mark Buchanan

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Popularity according to books:

Haw Everything In Connected to Exceptions Else and What Is Means for Datasets, Science, and Everyday Life



Albert-Lészló Berebési

Linked: How Everything Is Connected to Everything Else and What It Means—Albert-Laszlo Barabási



Six Degrees: The Science of a Connected Age—Duncan Watts^[15]

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Numerous others ...

- Complex Social Networks—F. Vega-Redondo^[14]
- Fractal River Basins: Chance and Self-Organization—I. Rodríguez-Iturbe and A. Rinaldo^[13]
- 🚳 Random Graph Dynamics—R. Durette
- 🗞 Scale-Free Networks—Guido Caldarelli
- Evolution and Structure of the Internet: A Statistical Physics Approach—Romu Pastor-Satorras and Alessandro Vespignani
- 🗞 Complex Graphs and Networks—Fan Chung
- Social Network Analysis—Stanley Wasserman and Kathleen Faust
- Handbook of Graphs and Networks—Eds: Stefan Bornholdt and H. G. Schuster^[5]
- Evolution of Networks—S. N. Dorogovtsev and J. F. F. Mendes^[6]

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More observations

But surely networks aren't new ... Graph theory is well established ... 🚓 Study of social networks started in the 1930's ... So why all this 'new' research on networks? Answer: Oodles of Easily Accessible Data. 🚳 We can now inform (alas) our theories with a much more measurable reality.* A worthy goal: establish mechanistic explanations. *If this is upsetting, maybe string theory is for you ...

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More observations

Web-scale data sets can be overly exciting.

Witness:

- The End of Theory: The Data Deluge Makes the Scientific Theory Obsolete (Anderson, Wired)
- "The Unreasonable Effectiveness of Data," Halevy et al. ^[9].
- c.f. Wigner's "The Unreasonable Effectiveness of Mathematics in the Natural Sciences" [17]

But:

For scientists, description is only part of the battle.We still need to understand.

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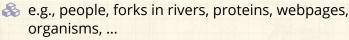
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Super Basic definitions

Nodes = A collection of entities which have properties that are somehow related to each other



Links = Connections between nodes

Links may be directed or undirected.
 Links may be binary or weighted.

Other spiffing words: vertices and edges.

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Super Basic definitions

Node degree = Number of links per node

- \aleph Notation: Node *i*'s degree = k_i .
- $\& k_i = 0, 1, 2,$
- Notation: the average degree of a network = $\langle k \rangle$ (and sometimes *z*)
- Connection between number of edges m and average degree:

$$\langle k \rangle = \frac{2m}{N}.$$

 \mathfrak{S} Defn: \mathcal{N}_i = the set of *i*'s k_i neighbors

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Super Basic definitions

Adjacency matrix:

We represent a directed network by a matrix A with link weight a_{ij} for nodes i and j in entry (i, j).
 e.g.,

	ΓΟ	1	1	1	0 7	
	$\begin{bmatrix} 0\\0\\1\\0\\0 \end{bmatrix}$	0	1	0	1	24 11 11
A =	1	0	0	0	0	
	0	1	0	0	1	
		1	0	1	0	

(n.b., for numerical work, we always use sparse matrices.)

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So what passes for a complex network?

- 🗞 Complex networks are large (in node number)
- Complex networks are sparse (low edge to node ratio)
- Complex networks are usually dynamic and evolving
- Complex networks can be social, economic, natural, informational, abstract, ...

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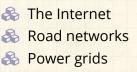
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Physical networks



🙈 River networks 🙈 Neural networks A Trees and leaves Blood networks









Distribution (branching) versus redistribution (cyclical)

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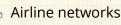


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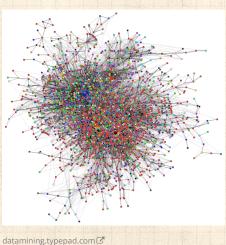
Interaction networks



- 🚳 The Blogosphere
 - Biochemical networks
- Gene-protein networks
- 🙈 Food webs: who eats whom
- 🙈 The World Wide Web (?)



Call networks (AT&T)The Media



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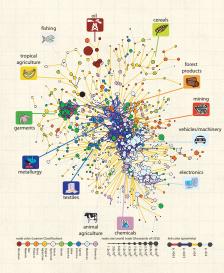
topics:

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Hidalgo et al.'s "The Product Space Conditions the Development of Nations" ^[10]

How do products depend on each other, and how does this network evolve?

How do countries depend on each other for water, energy, people (immigration), investments?



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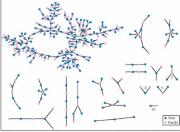
References



Interaction networks: social networks



- 🚳 Snogging
- \lambda Friendships
 - Acquaintances
 - Boards and directors
- Organizations 🔧 facebook 🖸 twitter 🖸



The Structure of Romantic and Sexual Relations at "Jefferson High School"

Each circle represents a student and lines connecting students represent romantic relations occuring within the 6 months preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

(Bearman et al., 2004)

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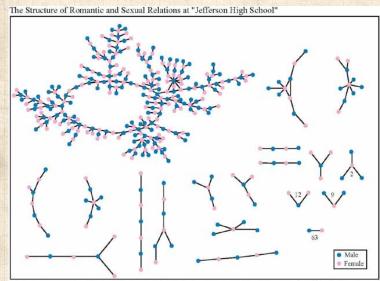
References



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🚳 'Remotely sensed' by: email activity, instant messaging, phone logs (*cough*).



Each circle represents a student and lines connecting students represent romantic relations occuring within the 6 months preceding the interview. Numbers under the figure count the number of times that pattern was observed (i.e. we found 63 pairs unconnected to anyone else).

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Relational networks

- Consumer purchases (Walmart, Target, Amazon, ...)
- Thesauri: Networks of words generated by meanings
- 🗞 Knowledge/Databases/Ideas
- 🗞 Metadata—Tagging: bit.ly 🗹 flickr 🗹

common tags cloud | list

community daily dictionary education **encyclopedia** english free imported info information internet knowledge learning news **reference** research resource resources search tools useful web web2.0 **Wiki wikipedia** PoCS @pocsvox

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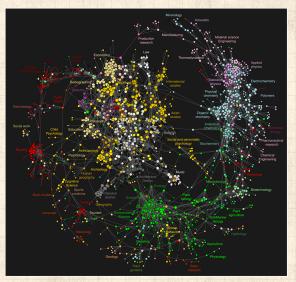
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Clickworthy Science:



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"Clickstream Data Yields High-Resolution Maps of Science", Bollen et al. ^[4], 2009.



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