

Overview of Complex Networks

Last updated: 2019/01/14, 22:05:08

Complex Networks | @networksvox
CSYS/MATH 303, Spring, 2019

Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center
Vermont Advanced Computing Core | University of Vermont



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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Overview

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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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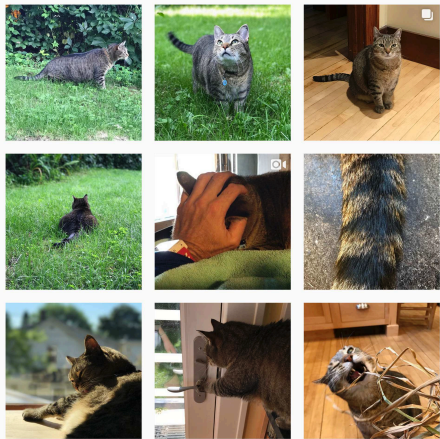


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Overview

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Orientation

Course Information
Projects

The rise of
networks

Models



Resources

Nutshell

References



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 On Instagram at [pratchett_the_cat](https://www.instagram.com/pratchett_the_cat) 



Outline

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Overview

Orientation

Course Information

Projects

Orientation

Course Information

Projects

The rise of networks

The rise of
networks

Models

Models

Resources

Resources

Nutshell

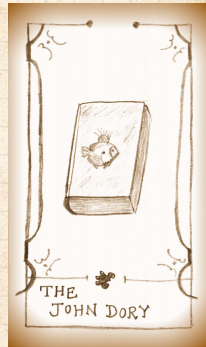
Nutshell

References

References







Peter Dodds

Tyler Gray

Aaron Schwartz

Eric Clark

Ben Emery

David Dewhurst

Colin Van Oort

Abby Ross
Northfield Mount
Hermon School

Chris Fusting
Data Science
Consultant

Ryan Callagher
Northeastern
PhD student

John Ring

compstorylab.org

Chris Danforth

Nick Allgaier
Psychiatry
Postdoc, UVM

Dilan Kiley
Chobanian Group

Tom McAndrew
Cardiovascular
Research Foundation

Emily Cody
Data Scientist
Adobe

Morgan Frank
MIT Media Lab
PhD Student

Cathy Bliss
UVM Lecturer

Mark Ibrahim
Data Scientist
Insight

Ross Lieb-Lappen
Dartmouth PhD
Cold Regions Research
& Engineering Laboratory

Eitan Pecherick

Andy Reagan
Data Scientist
MassMutual

Lewis Mitchell
Adelaide Faculty

Jake Williams
Drexel Faculty

Isabel Kloumann
Cornell PhD
Facebook
Data Scientist

Fletcher Hazlehurst

Sharon Alajajian
Research Scientist
Univ of Pennsylvania

Kameron Harris
Washington
PhD Student

Paul Lessard
Colorado
PhD Student

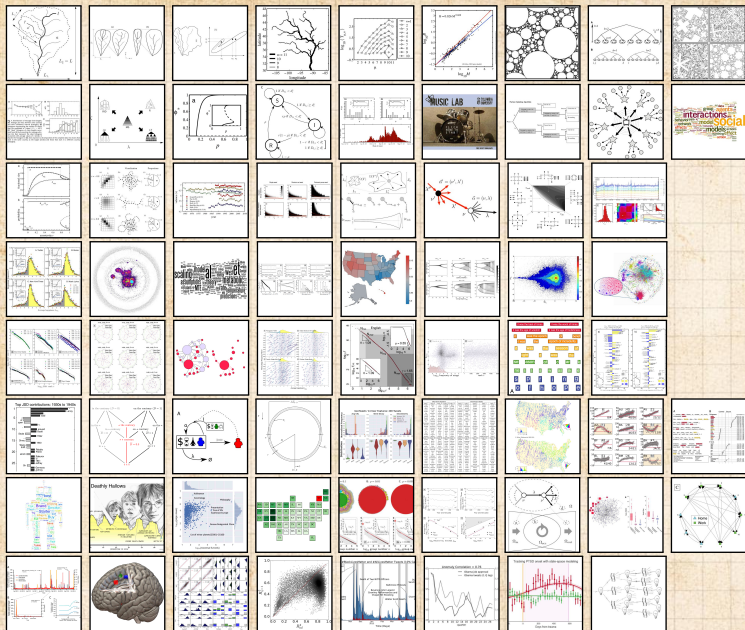
Suma Desu
Apple
Data Scientist

Mike Foley
Northeastern
PhD student

Darcy Glenn
Climate Science
UC London, MS student

Funding: NSF, NASA, MITRE.





Outline

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References











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Basics:

-  Instructor: Prof. Peter Dodds
-  Lecture room and meeting times:
Decision Theater, Farrell Hall, Tuesday and
Thursday, 1:15 pm to 2:30 pm
-  Office: Farrell Hall, second floor, Trinity Campus
-  email: pdodds+coconuts@uvm.edu
-  Course Website:
<http://www.uvm.edu/pdodds/teaching/courses/2019-01UVM-303> 
-  Course Twitter handle: @networksvox
-  Course hashtag: #SpringCOcoNuTS2019

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References





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Potential paper products:

 The Syllabus  and a Poster .

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References





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Office hours:

 10:05 am to 12:00 pm, Tuesday and Thursday,
Farrell Hall, second floor, Trinity Campus

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References






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Graduate Certificate:

 Principles of Complex Systems is one of two core requirements for UVM's five course Certificate of Graduate Study in Complex Systems .

 Other required course: Prof. Maggie Eppstein's "Modelling Complex Systems" (CSYS/CS 302).

 coCoNuTS: The Sequel to PoCS: "Complex Networks" (CSYS/MATH 303).



Details regarding these artisanal slides:



Three versions (all in pdf):

1. Presentation,
2. Flat Presentation,
3. Handout (3x2 slides per page).

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Some books will be linked to on amazon.



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








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Brought to you by a frightening melange of X_YAT_EX , Beamer , perl , PerlTeX , fevered command-line madness , and an almost fanatical devotion  to the indomitable emacs .



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







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#evilsuperpowers




More super exciting details:

 We use Open Sans and make math look good:

```
\setmainfont[Ligatures=TeX]{Open Sans}  
\setsansfont[Ligatures=TeX]{Open Sans}  
\usefonttheme[onlymath]{serif}
```

 Working towards putting the course on Github.

 And writing a book. A few books.




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Yet more super exciting details:

 This is Season 9 of Complex Networks.

 Lectures will be called Episodes.

 All lectures are bottle  episodes .

 Other tropes  will be involved.

 Last coCoNuTs Episodes are here .







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Wonderful foundational support for PoCS and CoNKS has come from the NSF:

-  "CAREER: Explorations of Complex Social and Psychological Phenomena through Multiscale Online Sociological Experiments, Empirical Studies, and Theoretical Models." 2009–2015.
-  SES Division of Social and Economic Sciences
SBE Directorate for Social, Behavioral & Economic Sciences
-  Abstract is here .

 Last season's Episodes are here .



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Team coCoNuTs

We'll be carrying on with the PoCS Slack:

- Place for discussions about all things PoCS/coCoNuTs including assignments and projects.

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References






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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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-  Everyone will behave wonderfully.



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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References




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Grading breakdown:

 **Projects/talks (36%)**—Students will work on semester-long projects. Students will develop a proposal in the first few weeks of the course which will be discussed with the instructor for approval. Details: 12% for the first talk, 12% for the final talk, and 12% for the written project.





 **Assignments (60%)**—All assignments will be of equal weight and there will be 10 ± 1 of them.

 **General attendance/Class participation (4%)**



How grading works:

Questions are worth 3 points according to the following scale:

-  3 = correct or very nearly so.
-  2 = acceptable but needs some revisions.
-  1 = needs major revisions.
-  0 = way off.



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Important things:

1. Classes run from Tuesday, January 16 to Thursday, May 4.
2. Add/Drop, Audit, Pass/No Pass deadline—Monday, January 29.
3. Last day to withdraw—Monday, April 2 (Never!).
4. Reading and Exam period—Monday, May 7 to Friday, May 11.

Do check the course Twitter account, @networksvox, for updates regarding the course (part of the course site).

Academic assistance: Anyone who requires assistance in any way (as per the ACCESS program or due to athletic endeavors), please see or contact me as soon as possible.



Schedule in detail:

Week number (dates)	Tuesday	Thursday
1 (1/16 and 1/18)	overview, branching networks I	branching networks I and II
2 (1/23 and 1/25)	branching networks II	optimal supply networks I and II
3 (1/30 and 2/1)	optimal supply networks II	optimal supply networks II
4 (2/6 and 2/8)	optimal supply networks II	optimal supply networks III
5 (2/13 and 2/15)	optimal supply networks III, random networks	random networks
6 (2/20 and 2/22)	generating functions	random bipartite networks
7 (2/27 and 3/1)	Town meeting day	project presentations [†]
8 (3/6 and 3/8)	Spring Recess	Spring Recess
9 (3/13 and 3/15)	random networks	bipartite networks
10 (3/20 and 3/22)	contagion	contagion
11 (3/27 and 3/29)	contagion	chaotic contagion
12 (4/3 and 4/5)	multilayer networks	multilayer networks
13 (4/10 and 4/12)	assortativity	mixed random networks
14 (4/17 and 4/19)	centrality	structure detection
15 (4/24 and 4/26)	structure detection	structure detection
16 (5/1 and 5/3)	organizational networks	special topics

†: 3-4 minutes each + 1 or 2 questions;

Outline

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

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Overview

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References




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Projects

 Semester-long projects, teams (maybe multiple)

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Overview

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References





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Projects

-  Semester-long projects, teams (maybe multiple)
-  Big themes: Stories, Narratives, and Language.

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Overview

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References






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Overview

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References







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Overview

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References








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- Massive data sets available, including Twitter.
- Academic output (journal papers) resulting from Principles of Complex Systems and Complex Networks can be found here . Add more!



The narrative hierarchy—Stories and Storytelling on all Scales: ↗



-  1 to 3 word encapsulation = a soundbite = a buzzframe,
-  1 sentence, title,
-  few sentences, a haiku,
-  a paragraph, abstract,
-  short paper, essay,
-  long paper,
-  chapter,
-  book,
-  ...



Key Observation:



Many **complex systems** can be viewed as **complex networks** of physical or abstract interactions.

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References





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Key Observation:

-  Many **complex systems** can be viewed as **complex networks** of physical or abstract interactions.
-  Opens door to mathematical and numerical analysis.

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References






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Key Observation:

-  Many **complex systems** can be viewed as **complex networks** of physical or abstract interactions.
-  Opens door to mathematical and numerical analysis.
-  Dominant approach of last decade of a **theoretical-physics/stat-mechish** flavor.



Key Observation:

-  Many **complex systems** can be viewed as **complex networks** of physical or abstract interactions.
-  Opens door to mathematical and numerical analysis.
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-  Mindboggling amount of work published on complex networks since 1998 ...



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- ...due to your typical theoretical physicist:



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 *Piranha physicist*




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 *Piranha physicus*

 Hunt in packs.



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- ...due to your typical theoretical physicist:



- Piranha physicus*
- Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)



Popularity (according to Google Scholar)

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References

“Collective dynamics of ‘small-world’ networks”^[10]

Duncan Watts and Steve Strogatz

Nature, 1998

Times cited: _____  (as of January 15, 2018)

“Emergence of scaling in random networks”^[3]

László Barabási and Réka Albert

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models


Resources

Nutshell

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources


Nutshell

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Times cited: **30,242**  (as of January 15, 2018)



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Models

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References

Some important models:



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Some important models:

1. generalized random networks (touched on in PoCS)



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Some important models:

1. generalized random networks (touched on in PoCS)
2. scale-free networks ↗ (partly covered in PoCS)



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3. small-world networks ↗ (covered in PoCS)



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4. statistical generative models (p^*)



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3. small-world networks ↗ (covered in PoCS)
4. statistical generative models (p^*)
5. generalized affiliation networks (covered in PoCS)

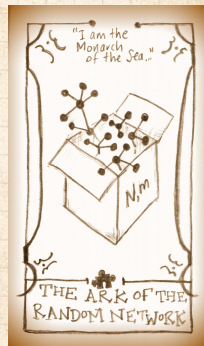


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1. generalized random networks:




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1. generalized random networks:

 Arbitrary degree distribution P_k .





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1. generalized random networks:

-  Arbitrary degree distribution P_k .
-  Wire nodes together randomly.






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1. generalized random networks:

-  Arbitrary degree distribution P_k .
-  Wire nodes together randomly.
-  Create ensemble to test deviations from randomness.







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1. generalized random networks:

-  Arbitrary degree distribution P_k .
-  Wire nodes together randomly.
-  Create ensemble to test deviations from randomness.
-  Interesting, applicable, rich mathematically.








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1. generalized random networks:

-  Arbitrary degree distribution P_k .
-  Wire nodes together randomly.
-  Create ensemble to test deviations from randomness.
-  Interesting, applicable, rich mathematically.
-  We will have fun with these things ...



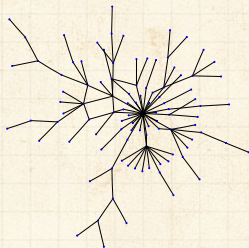
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2. 'scale-free networks':



$$\gamma = 2.5, \langle k \rangle = 1.8, \\ N = 150$$



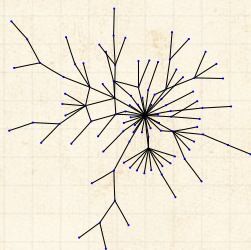
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Introduced by Barabasi and Albert ^[3]

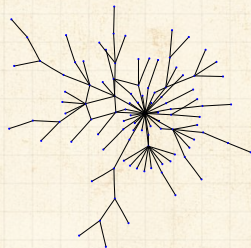


Generative model

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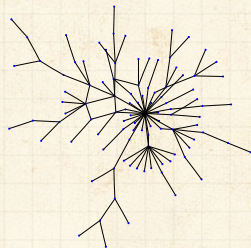


Preferential attachment model with growth:

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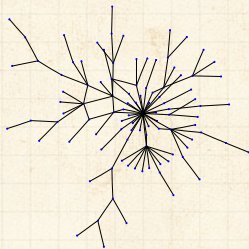


$P[\text{attachment to node } i] \propto k_i^\alpha$.

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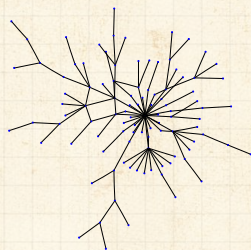


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- Preferential attachment model with growth:
- $P[\text{attachment to node } i] \propto k_i^\alpha$.
- Produces $P_k \sim k^{-\gamma}$ when $\alpha = 1$.
- Trickiness: other models generate skewed degree distributions.




3. small-world networks

 Introduced by Watts and Strogatz ^[10]



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Two scales:




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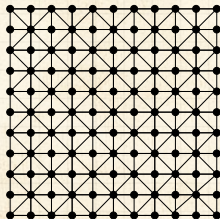


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 **local regularity** (an individual's friends know each other)




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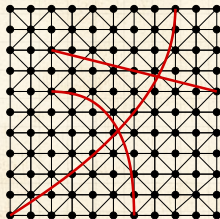
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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References




CoNKs

Complex Networks
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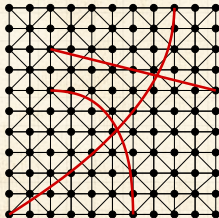
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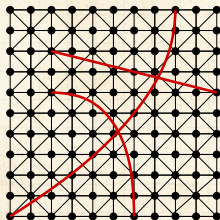
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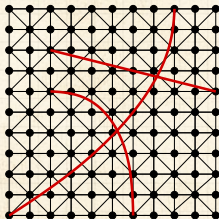
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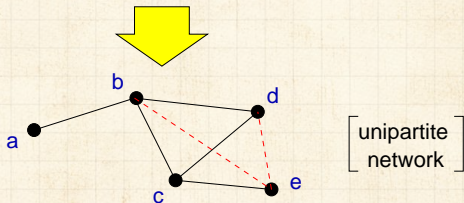
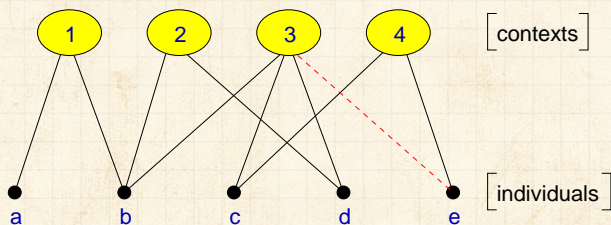
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 Facilitates synchronization



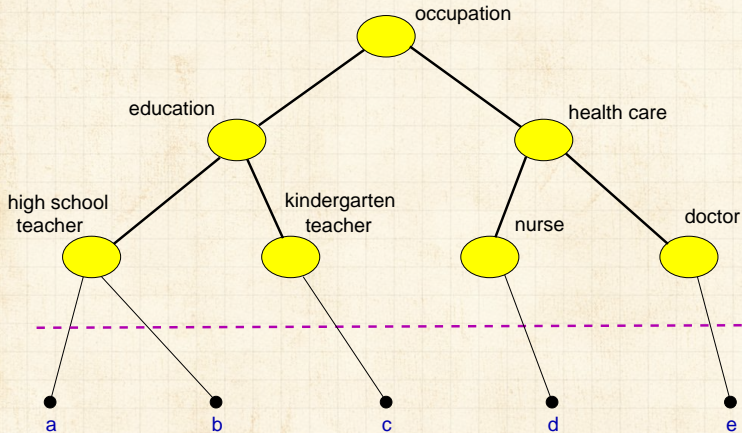
5. generalized affiliation networks



Bipartite affiliation networks: boards and directors, movies and actors.



5. generalized affiliation networks



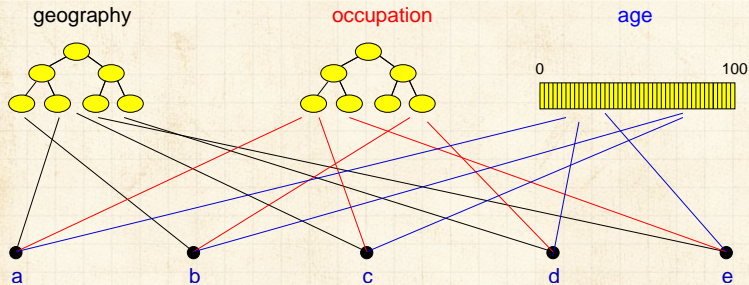
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5. generalized affiliation networks



Blau & Schwartz ^[4], Simmel ^[8], Breiger ^[6], Watts *et al.* ^[9]



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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources


Nutshell

References

Textbooks:



Mark Newman (Physics, Michigan)

"Networks: An Introduction" 



David Easley and Jon Kleinberg (Economics and
Computer Science, Cornell)

"Networks, Crowds, and Markets: Reasoning About a
Highly Connected World" 



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Bonus materials:

Review articles:


 S. Boccaletti et al.,
Physics Reports, 2006,
"Complex networks: structure and dynamics" [5]
Times cited: **7,897**  (as of January 15, 2018)

 M. Newman,
SIAM Review, 2003,
"The structure and function of complex
networks" [7]
Times cited: **16,768**  (as of January 15, 2018)

 R. Albert and A.-L. Barabási
Reviews of Modern Physics, 2002,
"Statistical mechanics of complex networks" [1]
Times cited: **20,656**  (as of January 15, 2018)





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-  Three main (blurred) categories:
 1. **Physical** (e.g., river networks),
 2. **Interactional** (e.g., social networks),
 3. **Abstract** (e.g., thesauri).





Overview Key Points (cont.):

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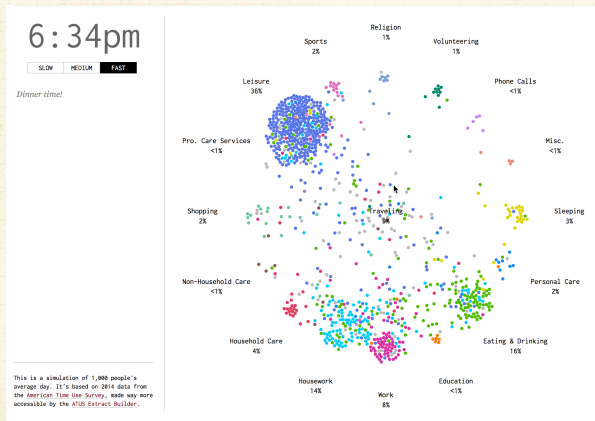


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Visualizing a day in the life of Americans ↗



Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Source: Flowing Data/Nathan Yau.



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Rev. Mod. Phys., 74:47–97, 2002. [pdf](#) 
- [2] P. W. Anderson.
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Science, 177(4047):393–396, 1972. [pdf](#) 
- [3] A.-L. Barabási and R. Albert.
Emergence of scaling in random networks.
Science, 286:509–511, 1999. [pdf](#) 
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Crosscutting Social Circles.
Academic Press, Orlando, FL, 1984.



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References III

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Overview

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References

- [9] D. J. Watts, P. S. Dodds, and M. E. J. Newman.
Identity and search in social networks.
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- [10] D. J. Watts and S. J. Strogatz.
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[Nature](#), 393:440–442, 1998. pdf ↗



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