Overview of Complex Networks

Last updated: 2019/01/14, 23:14:28

Complex Networks | @networksvox CSYS/MATH 303, Spring, 2019

Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont



Licensed under the Creative Commons Attribution-NonCommercial-ShareAlike 3.0 License.

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References





These slides are brought to you by:

Sealie & Lambie Productions

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



990 2 of 45

UVN OO

These slides are also brought to you by:

Special Guest Executive Producer



On Instagram at pratchett_the_cat

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References





990 3 of 45

Outline

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

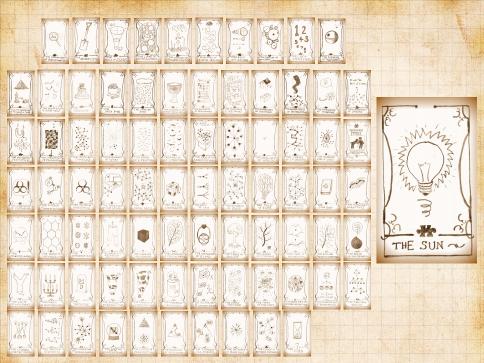
Resources

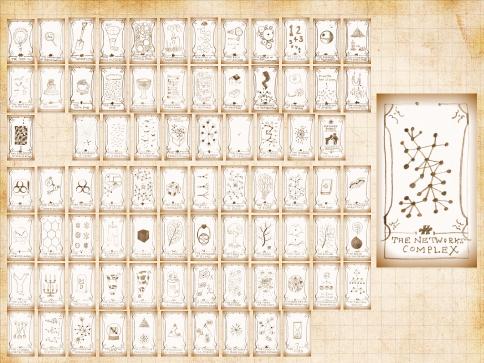
Nutshell

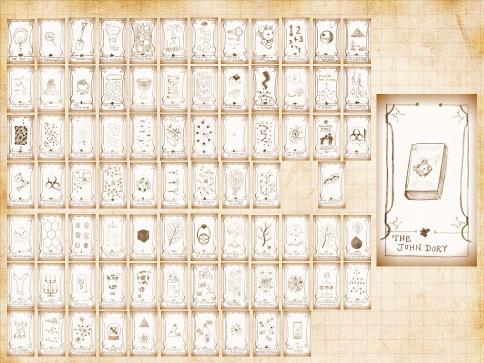
References



200 4 of 45









Peter Dodds



Psychiatry Postdoc, UVM



Lewis Mitchell Adelaide Faculty



Dilan Kiley

Chobanian Group

lake Williams Drexel Faculty



Isabel Kloumann Fletcher Hazlehurst



Emily Cody

Data Scientist

Aaron Schwartz

Chris Fusting

Data Science

Consultant

Tyler Gray

Abby Ross

Northfield Mount

Hermon School

Tom McAndrew

Cardiovascular

Fric Clark

Northeastern

PhD student

Sharon Alaiaiian **Research Scientist**

Morgan Frank

MIT Media Lab

Univ of Pennsylvania PhD Student



Cathy Bliss

UVM Lecturer

Ben Emery

John Ring

Kameron Harris Washington

Paul Lessard Colorado PhD Student

Insight

David

Dewhurst



Apple Data Scientist



Suma Desu



Mike Foley Darcy Glenn Northeastern Climate Science PhD student UC London, MS student



Eitan Pechenick

Chris Danforth

Data Scientist

MassMutual

The rise of

Resources

CocoNuTs Complex Networks Gnetworksvox

DQ @ 8 of 45



COCONUTS @networksvox

Overview

Orientation Course Information

networks

Models

Nutshell





Ross Lieb-Lappen Dartmouth PhD



& Engineering Laboratory

Mark Ibrahim Data Scientist Cold Regions Research



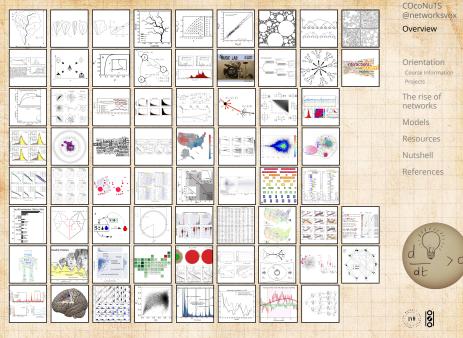
compstorylab.org

Colin

Van Oort

@ Computational

Story Lab



200 9 of 45

Basics:

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References





DQ @ 11 of 45

A Instructor: Prof. Peter Dodds Lecture room and meeting times: Decision Theater, Farrell Hall, Tuesday and Thursday, 1:15 pm to 2:30 pm Office: Farrell Hall, second floor, Trinity Campus 🗞 email: pdodds+coconuts@uvm.edu Course Website: http://www.uvm.edu/pdodds/teaching/courses/2019-01UVM-303 Course Twitter handle: @networksvox Course hashtag: #SpringCOcoNuTS2019

Office hours:

10:05 am to 12:00 pm, Tuesday and Thursday, Farrell Hall, second floor, Trinity Campus

Graduate Certificate:

- Principles of Complex Systems is one of two core requirements for UVM's five course Certificate of Graduate Study in Complex Systems .
- Other required course: Prof. Maggie Eppstein's "Modelling Complex Systems" (CSYS/CS 302).
- coCoNuTS: The Sequel to PoCS: "Complex Networks" (CSYS/MATH 303).

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References





2 a a 12 of 45

Details regarding these artisanal slides:

- 🚳 Three versions (all in pdf):
 - 1. Presentation,
 - 2. Flat Presentation,
 - 3. Handout (3x2 slides per page).
- Presentation versions are hyperly navigable: $\mathfrak{OQC} \equiv back + search + forward.$
- 🗞 Web links look like this 🗹 and are eminently clickable.
 - References in slides link to full citation at end.^[2]
- litations contain links to pdfs for papers (if available).
- 🚳 Some books will be linked to on amazon.
- Brought to you by a frightening melange of X_MT_XC, BeamerC, perIC, PerITeXC, fevered command-line madnessC, and an almost fanatical devotionC to the indomitable emacsC. #evilsuperpowers

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



2 a a 13 of 45

More super exciting details:

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

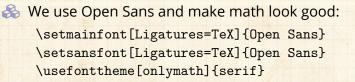
The rise of networks

Models

Resources

Nutshell

References



Working towards putting the course on Github.
 And writing a book. A few books.



Dac 14 of 45

Yet more super exciting details:

- This is Season 9 of Complex Networks.
 Lectures will be called Episodes.
- All lectures are bottle C episodes C.
 Other tropes C will be involved.

🗞 Last coCoNuTs Episodes are here 🗹.

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



200 15 of 45

Wonderful foundational support for PoCS and CoNKS has come from the NSF:

- line and "CAREER: Explorations of Complex Social and Psychological Phenomena through Multiscale **Online Sociological Experiments, Empirical** Studies, and Theoretical Models." 2009-2015.
- SES Division of Social and Economic Sciences SBE Directorate for Social, Behavioral & Economic Sciences

Abstract is here 📿.



🚳 Last season's Episodes are here 🗹.

COCONUTS @networksvox

Overview

Orientation Course Information

The rise of networks

Models

Nutshell

References



29 CP 16 of 45

Team coCoNuTs

We'll be carrying on with the PoCS Slack:

- Place for discussions about all things PoCS/coCoNuTs including assignments and projects.
- Once invited, please sign up here: http://teampocs.slack.com
- line tablets, Wery good: Install Slack app on laptops, tablets, phone.



Everyone will behave wonderfully.



COCONUTS @networksvox

Overview

Orientation Course Information

The rise of networks

Models

Resources

Nutshell

References





Dac 17 of 45

Grading breakdown:

Projects/talks (36%)—Students will work on semester-long projects. Students will develop a proposal in the first few weeks of the course which will be discussed with the instructor for approval. Details: 12% for the first talk, 12% for the final talk, and 12% for the written project.

Assignments (60%)—All assignments will be of equal weight and there will be 10 ± 1 of them.

General attendance/Class participation (4%)

COcoNuTS @networksvox Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



na @ 18 of 45

How grading works:

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



- 3 = correct or very nearly so.
- 2 = acceptable but needs some revisions.
- 4 1 = needs major revisions.
- 🚳 0 = way off.

Complex Networks @networksvox Everything is connected

ク へ 19 of 45

Important things:

- 1. Classes run from Tuesday, January 16 to Thursday, May 4.
- Add/Drop, Audit, Pass/No Pass deadline—Monday, January 29.
- 3. Last day to withdraw—Monday, April 2 (Never!).
- 4. Reading and Exam period—Monday, May 7 to Friday, May 11.

Do check the course Twitter account, @networksvox, for updates regarding the course (part of the course site).

Academic assistance: Anyone who requires assistance in any way (as per the ACCESS program or due to athletic endeavors), please see or contact me as soon as possible. COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



うへで 20 of 45

WN OS

Schedule in detail:

Week number (dates)	Tuesday	Thursday
1 (1/16 and 1/18)	overview, branching networks I	branching networks I and II
2 (1/23 and 1/25)	branching networks II	optimal supply networks I and II
3 (1/30 and 2/1)	optimal supply networks II	optimal supply networks II
4 (2/6 and 2/8)	optimal supply networks II	optimal supply networks III
5 (2/13 and 2/15)	optimal supply networks III, random net- works	random networks
6 (2/20 and 2/22)	generating functions	random bipartite networks
7 (2/27 and 3/1)	Town meeting day	project presentations [†]
8 (3/6 and 3/8)	Spring Recess	Spring Recess
9 (3/13 and 3/15)	random networks	bipartite networks
10 (3/20 and 3/22)	contagion	contagion
11 (3/27 and 3/29)	contagion	chaotic contagion
12 (4/3 and 4/5)	multilayer networks	multilayer networks
13 (4/10 and 4/12)	assortativity	mixed random networks
14 (4/17 and 4/19)	centrality	structure detection
15 (4/24 and 4/26)	structure detection	structure detection
16 (5/1 and 5/3)	organizational networks	special topics

+: 3-4 minutes each + 1 or 2 questions;

Projects

- Semester-long projects, teams (maybe multiple)
- Big themes: Stories, Narratives, and Language.
- Big goal: Aim to submit to arXiv/journal by end of semester.
- Continue from PoCS/Develop proposal in first few weeks
- May range from novel research to investigation of an established area of complex systems.
- Two talks + written piece + Project on Github Pages.
- Usage of the VACC is encouraged (ability to code well = super powers).
- 🚳 Massive data sets available, including Twitter.
- Academic output (journal papers) resulting from Principles of Complex Systems and Complex Networks can be found here . Add more!

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References





23 of 45

The narrative hierarchy—Stories and Storytelling on all Scales:

-

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



Dac 24 of 45

UVN SO

1 to 3 word encapsulation = a soundbite = a buzzframe, 🚳 1 sentence, title, 🚳 few sentences, a haiku, 🚳 a paragraph, abstract, 🚳 short paper, essay, long paper, chapter, book, 2 ...

Key Observation:

- Many complex systems can be viewed as complex networks of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.
- Mindboggling amount of work published on complex networks since 1998 ...
- 🚓 ...due to your typical theoretical physicist:



Piranha physicus

- Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



25 of 45

Popularity (according to Google Scholar)

"Collective dynamics of 'small-world' networks" [10]

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



Duncan Watts and Steve Strogatz

Times cited: 35,226 C (as of January 15, 2018)

Nature, 1998



26 of 45

Some important models:

- 1. generalized random networks (touched on in PoCS)
- 2. scale-free networks C (partly covered in PoCS)
- 3. small-world networks C (covered in PoCS)
- 4. statistical generative models (p^*)
- 5. generalized affiliation networks (covered in PoCS)

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

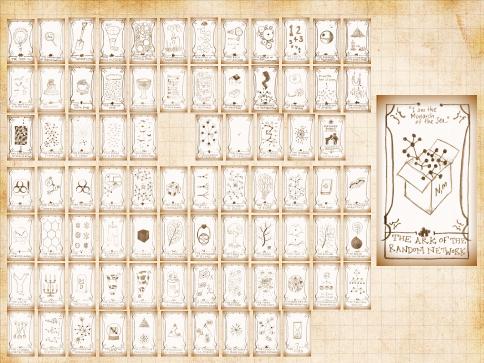
The rise of networks

Models Resources Nutshell

References



na 27 of 45



COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models Resources

Nutshell

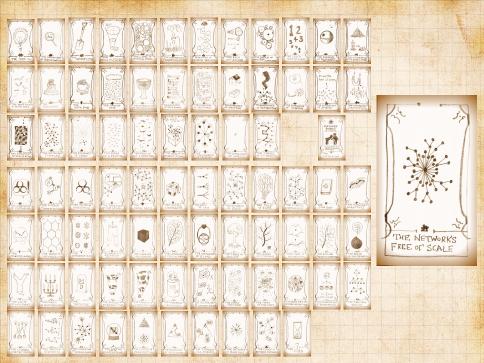
References



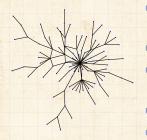
1. generalized random networks:

- \mathfrak{S} Arbitrary degree distribution P_k .
- 🚳 Wire nodes together randomly.
- Create ensemble to test deviations from randomness.
- lnteresting, applicable, rich mathematically.
- 🚳 We will have fun with these things ...

nac 29 of 45



2. 'scale-free networks':



 γ = 2.5, $\langle k \rangle$ = 1.8, N = 150

Introduced by Barabasi and Albert^[3]
Generative model
Preferential attachment model with growth: *P*[attachment to node *i*] ∝ k_i^α.
Produces P_k ~ k^{-γ} when α = 1.
Trickiness: other models

Trickiness: other models generate skewed degree distributions. COcoNuTS @networksvox

Overview

Orientation Course Information Projects

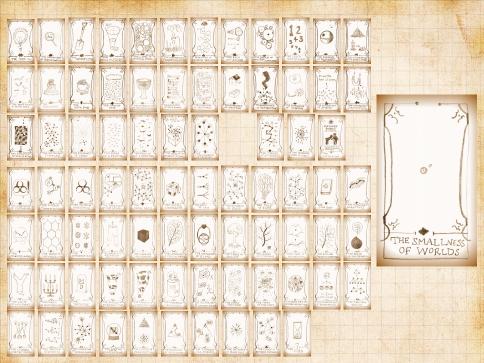
The rise of networks

Models Resources

Nutshell References



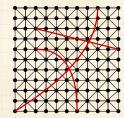
うへ 31 of 45



3. small-world networks
 Introduced by Watts and Strogatz^[10]

Two scales:

- Iocal regularity (an individual's friends know each other)
- 🗞 global randomness (shortcuts).
- Shortcuts allow disease to jump
 - Number of infectives increases exponentially in time
 - Facilitates synchronization



COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

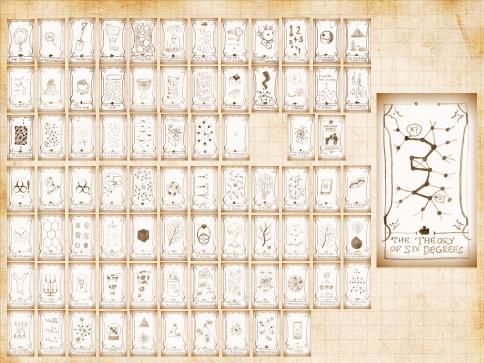
Resources

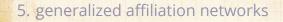
Nutshell

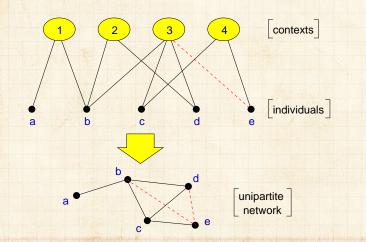
References



うへ @ 33 of 45







COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models Resources Nutshell

References

Complex Networks ©networksvox Everything is connected

Bipartite affiliation networks: boards and directors, movies and actors.

2 0 0 35 of 45

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

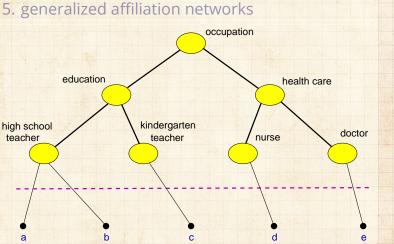
The rise of networks

Models Resources Nutshell

References



2 9 9 36 of 45



geography

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

100

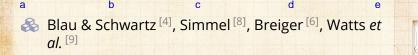
age

0

Resources

Nutshell

References



occupation

5. generalized affiliation networks

CoNKs

Complex Network

Bonus materials:

Textbooks:

- Mark Newman (Physics, Michigan) "Networks: An Introduction"
- David Easley and Jon Kleinberg (Economics and Computer Science, Cornell) "Networks, Crowds, and Markets: Reasoning About a Highly Connected World" ^C

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



na @ 38 of 45

Bonus materials:

Review articles:

😤 S. Boccaletti et al., Physics Reports, 2006, "Complex networks: structure and dynamics"^[5] Times cited: 7,897 C (as of January 15, 2018) 🖂 M. Newman, SIAM Review, 2003, "The structure and function of complex networks"^[7] Times cited: 16,768 C (as of January 15, 2018) 🖧 R. Albert and A.-L. Barabási Reviews of Modern Physics, 2002, "Statistical mechanics of complex networks"^[1]

Times cited: 20,656 C (as of January 15, 2018)

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



うへで 39 of 45

Nutshell:

Overview Key Points:

- The field of complex networks came into existence in the late 1990s.
 - 🗞 Explosion of papers and interest since 1998/99.
- Hardened up much thinking about complex systems.
- Specific focus on networks that are large-scale, sparse, natural or man-made, evolving and dynamic, and (crucially) measurable.
- 🚳 Three main (blurred) categories:
 - 1. Physical (e.g., river networks),
 - 2. Interactional (e.g., social networks),
 - 3. Abstract (e.g., thesauri).

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell References



UVN S

29 C 40 of 45

Nutshell:

Overview Key Points (cont.):

- Obvious connections with the vast extant field of graph theory.
- But focus on dynamics is more of a physics/stat-mech/comp-sci flavor.
- 🚓 Two main areas of focus:
 - 1. Description: Characterizing very large networks
 - 2. Explanation: Micro story \Rightarrow Macro features
- Some essential structural aspects are understood: degree distribution, clustering, assortativity, group structure, overall structure, ...
- Still much work to be done, especially with respect to dynamics ...exciting!

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

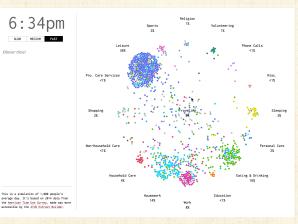
Resources

Nutshell References



Neural solace—Temporal social networks:

Visualizing a day in the life of Americans 🗹



🚳 Source: Flowing Data/Nathan Yau.

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References





2 0 42 of 45

References I

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References

- R. Albert and A.-L. Barabási.
 Statistical mechanics of complex networks.
 Rev. Mod. Phys., 74:47–97, 2002. pdf
- P. W. Anderson.
 More is different.
 Science, 177(4047):393–396, 1972. pdf
- [3] A.-L. Barabási and R. Albert. Emergence of scaling in random networks. Science, 286:509–511, 1999. pdf 2
- P. M. Blau and J. E. Schwartz.
 <u>Crosscutting Social Circles</u>.
 Academic Press, Orlando, FL, 1984.



29 C 43 of 45

WN OS

References II

- [5] S. Boccaletti, V. Latora, Y. Moreno, M. Chavez, and D.-U. Hwang.
 Complex networks: Structure and dynamics. Physics Reports, 424:175–308, 2006. pdf
- [6] R. L. Breiger. The duality of persons and groups. Social Forces, 53(2):181–190, 1974. pdf C
- [7] M. E. J. Newman. The structure and function of complex networks. SIAM Rev., 45(2):167–256, 2003. pdf 2
- [8] G. Simmel. The number of members as determining the sociological form of the group. I. American Journal of Sociology, 8:1–46, 1902.

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References



WN OS

References III

COcoNuTS @networksvox

Overview

Orientation Course Information Projects

The rise of networks

Models

Resources

Nutshell

References

[9] D. J. Watts, P. S. Dodds, and M. E. J. Newman. Identity and search in social networks. <u>Science</u>, 296:1302–1305, 2002. pdf

[10] D. J. Watts and S. J. Strogatz. Collective dynamics of 'small-world' networks. Nature, 393:440–442, 1998. pdf 2



20 A 45 of 45