

Overview of Complex Networks

Last updated: 2018/03/23, 12:08:15

Complex Networks | @networksvox
CSYS/MATH 303, Spring, 2018

Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center
Vermont Advanced Computing Core | University of Vermont



- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References

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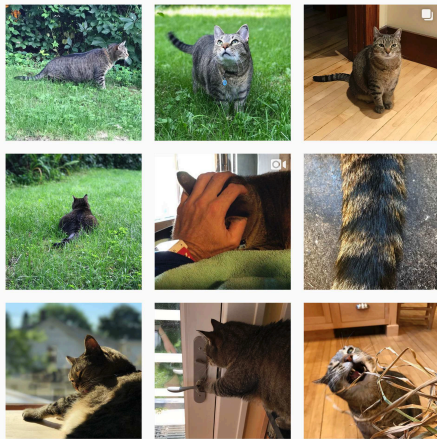
Orientation
Course Information
Projects
The rise of
networks
Models
Resources
Nutshell
References



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Orientation

Course Information

Projects



The rise of
networks

Models

Resources

Nutshell

References

 On Instagram at [pratchett_the_cat](https://www.instagram.com/pratchett_the_cat) 



Outline

Orientation

Course Information
Projects

The rise of networks

Models

Resources

Nutshell

References

COcoNuTS

Orientation

Course Information

Projects

The rise of
networks

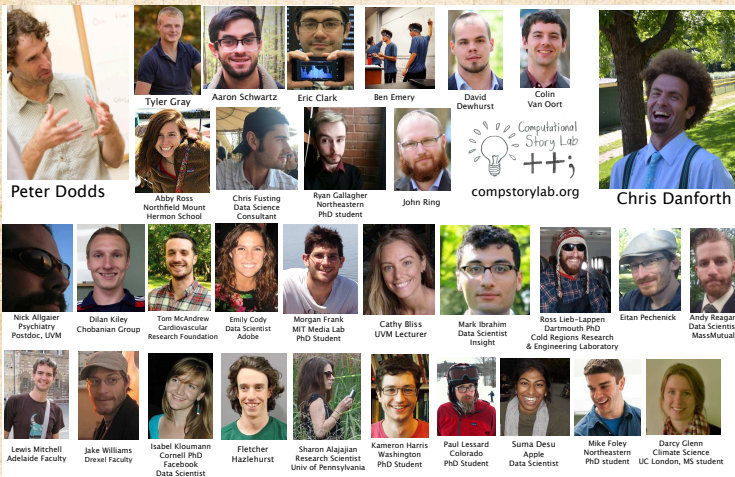
Models

Resources

Nutshell

References





Funding: NSF, NASA, MITRE.

Orientation
Course Information
Projects

The rise of
networks

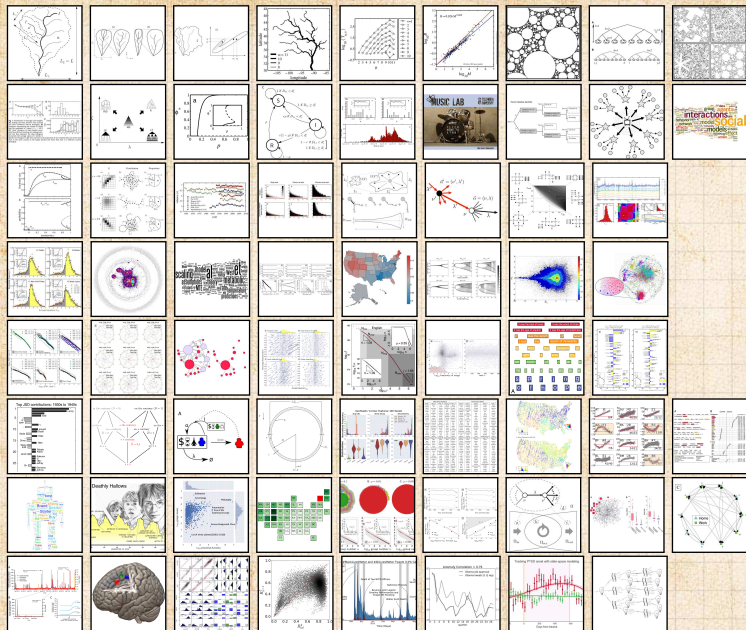
Models

Resources

Nutshell

References





Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



Outline

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

COcoNuTS

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References



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Basics:

COcoNuTS

-  Instructor: Prof. Peter Dodds
-  Lecture room and meeting times:
102 Perkins, Tuesday and Thursday, 8:30 am to 9:45 pm
-  Office: Farrell Hall, second floor, Trinity Campus
-  email: pdodds+coconuts@uvm.edu
-  Course Website:
<http://www.uvm.edu/pdodds/teaching/courses/2018-01UVM-303> 
-  Course Twitter handle: @networksvox
-  Course hashtag: #SpringCOcoNuTS2018

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References



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Potential paper products:

 [The Syllabus](#)  and a [Poster](#) .

Office hours:

 10:05 am to 12:00 pm, Tuesday and Thursday,
Farrell Hall, second floor, Trinity Campus

Graduate Certificate:

-  Principles of Complex Systems is one of two core requirements for UVM's five course [Certificate of Graduate Study in Complex Systems](#) .
-  Other required course: Prof. Maggie Eppstein's "Modelling Complex Systems" (CSYS/CS 302).
-  coCoNuTS: The Sequel to PoCS: "Complex Networks" (CSYS/MATH 303).

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Orientation

[Course Information](#)
Projects

The rise of
networks

Models

Resources

Nutshell

References




CoNKs

Complex Networks
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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



CoNKs

Complex Networks
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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References




CoNKs

Complex Networks
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 Some books will be linked to on amazon.

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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



CoNKs


Complex Networks
@networksvox

Everything is connected




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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



CoNKs

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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



CoNKs


Complex Networks
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Everything is connected




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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



CoNKs


Complex Networks
@networksvox

Everything is connected




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





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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Everything is connected



More super exciting details:

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Orientation

Course Information

Projects


The rise of
networks

Models


Resources


Nutshell

References

 We use Open Sans and make math look good:

```
\setmainfont[Ligatures=TeX]{Open Sans}
\setsansfont[Ligatures=TeX]{Open Sans}
\usefonttheme[onlymath]{serif}
```

 Working towards putting the course on Github.

 And writing a book. A few books.




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Yet more super exciting details:

 This is Season 8 of Complex Networks.

 Lectures will be called Episodes.

 All lectures are bottle  episodes .

 Other tropes  will be involved.

 Last coCoNuTs Episodes are here .









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Wonderful foundational support for PoCS and CoNKS has come from the NSF:

-  "CAREER: Explorations of Complex Social and Psychological Phenomena through Multiscale Online Sociological Experiments, Empirical Studies, and Theoretical Models." 2009–2015.
-  SES Division of Social and Economic Sciences
SBE Directorate for Social, Behavioral & Economic Sciences
-  Abstract is [here](#) .

-  Last season's Episodes are [here](#) .

Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References




CoNKS


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Team coCoNuTs

We'll be carrying on with the PoCS Slack:

 Place for discussions about all things PoCS/coCoNuTs including assignments and projects.

 Once invited, please sign up here:
<http://teampocs.slack.com>

 Very good: Install Slack app on laptops, tablets, phone.

 Everyone will behave wonderfully.



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Orientation

Course Information
Projects

The rise of networks

Models

Resources

Nutshell

References



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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Orientation

Course Information
Projects

The rise of networks

Models

Resources

Nutshell

References



CoNKs

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Orientation

Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References





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Grading breakdown:

 **Projects/talks (36%)**—Students will work on semester-long projects. Students will develop a proposal in the first few weeks of the course which will be discussed with the instructor for approval. Details: 12% for the first talk, 12% for the final talk, and 12% for the written project.





 **Assignments (60%)**—All assignments will be of equal weight and there will be 10 ± 1 of them.

 **General attendance/Class participation (4%)**



How grading works:

Questions are worth 3 points according to the following scale:

-  3 = correct or very nearly so.
-  2 = acceptable but needs some revisions.
-  1 = needs major revisions.
-  0 = way off.



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Important things:

1. Classes run from Tuesday, January 16 to Thursday, May 4.
2. Add/Drop, Audit, Pass/No Pass deadline—Monday, January 29.
3. Last day to withdraw—Monday, April 2 (Never!).
4. Reading and Exam period—Monday, May 7 to Friday, May 11.

Do check the course Twitter account, @networksvox, for updates regarding the course (part of the course site).

Academic assistance: Anyone who requires assistance in any way (as per the ACCESS program or due to athletic endeavors), please see or contact me as soon as possible.



Schedule in detail:

Week number (dates)	Tuesday	Thursday
1 (1/16 and 1/18)	overview, branching networks I	branching networks I and II
2 (1/23 and 1/25)	branching networks II	optimal supply networks I and II
3 (1/30 and 2/1)	optimal supply networks II	optimal supply networks II
4 (2/6 and 2/8)	optimal supply networks II	optimal supply networks III
5 (2/13 and 2/15)	optimal supply networks III, random networks	random networks
6 (2/20 and 2/22)	generating functions	random bipartite networks
7 (2/27 and 3/1)	Town meeting day	project presentations [†]
8 (3/6 and 3/8)	Spring Recess	Spring Recess
9 (3/13 and 3/15)	random networks	bipartite networks
10 (3/20 and 3/22)	contagion	contagion
11 (3/27 and 3/29)	contagion	chaotic contagion
12 (4/3 and 4/5)	multilayer networks	multilayer networks
13 (4/10 and 4/12)	assortativity	mixed random networks
14 (4/17 and 4/19)	centrality	structure detection
15 (4/24 and 4/26)	structure detection	structure detection
16 (5/1 and 5/3)	organizational networks	special topics

†: 3-4 minutes each + 1 or 2 questions;

Outline

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

COcoNuTS

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References



CoNKS

Complex Networks










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Projects

COcoNuTS

-  Semester-long projects, teams (maybe multiple)
-  Big themes: Stories, Narratives, and Language.
-  Big goal: Aim to submit to arXiv/journal by end of semester.
-  Continue from PoCS/Develop proposal in first few weeks
-  May range from novel research to investigation of an established area of complex systems.
-  Two talks + written piece + Project on Github Pages.
-  Usage of [the VACCE](#) is encouraged (ability to code well = super powers).
-  Massive data sets available, including Twitter.
-  Academic output (journal papers) resulting from Principles of Complex Systems and Complex Networks can be found [here](#). Add more!

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References



CoNKs

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Projects

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- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References



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- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References



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Projects

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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References



CoNKs






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Projects

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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References



CoNKs

Complex Networks

@networksvox

Everything is connected

Projects

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- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References




CoNKs

Complex Networks

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Everything is connected

Projects

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- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References



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- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References



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- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References





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The narrative hierarchy—Stories and Storytelling on all Scales: ↗





 1 to 3 word encapsulation = a soundbite = a buzzframe,


 1 sentence, title,


 few sentences, a haiku,

 a paragraph, abstract,

 short paper, essay,

 long paper,

 chapter,

 book,

 ...



Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References



CoNKs

Complex Networks
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Key Observation:



Many **complex systems** can be viewed as **complex networks** of physical or abstract interactions.



Opens door to mathematical and numerical analysis.



Dominant approach of last decade of a theoretical-physics/stat-mech flavor.








Mindboggling amount of work published on complex networks since 1998 ...



...due to your typical theoretical physicist:



Key Observation:

-  Many **complex systems** can be viewed as **complex networks** of physical or abstract interactions.
-  Opens door to mathematical and numerical analysis.
-  Dominant approach of last decade of a theoretical-physics/stat-mech-ish flavor.
-  Mindboggling amount of work published on complex networks since 1998 ...
-  ...due to your typical theoretical physicist!

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Orientation
Course Information
Projects
The rise of networks
Models
Resources
Nutshell
References



CoNKs

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Key Observation:

- Many **complex systems** can be viewed as **complex networks** of physical or abstract interactions.
- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a **theoretical-physics/stat-mechish** flavor.
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 *Piranha physicus*

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 Feast on new and interesting ideas
(see chaos, cellular automata, ...)



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Popularity (according to Google Scholar)

COcoNuTS

Orientation
Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References

“Collective dynamics of ‘small-world’ networks”^[10]

Duncan Watts and Steve Strogatz
Nature, 1998

Times cited: 35,226  (as of January 15, 2018)

“Emergence of scaling in random networks”^[3]

László Barabási and Réka Albert
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COcoNuTS

Orientation
Course Information
Projects

The rise of
networks

Models


Resources

Nutshell

References


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Complex Networks
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Everything is connected



Popularity (according to Google Scholar)

COcoNuTS

Orientation
Course Information
Projects

The rise of
networks

Models


Resources

Nutshell

References


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Some important models:

1. generalized random networks (touched on in PoCS)
2. scale-free networks  (partly covered in PoCS)
3. small world networks  (covered in PoCS)
4. statistical generative models (p^*)
5. generalized affiliation networks (covered in PoCS)





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Everything is connected

Orientation

Course Information

Projects

The rise of
networks

Models

Resources

Nutshell

References

1. generalized random networks:

- Arbitrary degree distribution P_k .
- Wire nodes together randomly.
- Create ensemble to test deviations from randomness.
- Interesting, applicable, rich mathematically.
- We will have fun with these things ...



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Everything is connected

Orientation

Course Information

Projects

The rise of
networks






Models

Resources

Nutshell

References

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CoNKs

Complex Networks
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Everything is connected

Orientation

Course Information

Projects

The rise of
networks


Models


Resources

Nutshell

References

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CoNKs

Complex Networks
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Everything is connected

Orientation

Course Information

Projects

The rise of
networks






Models

Resources

Nutshell

References

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CoNKs

Complex Networks
@networksvox

Everything is connected

Orientation

Course Information

Projects

The rise of
networks






Models

Resources

Nutshell

References

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CoNKs

Complex Networks
@networksvox

Everything is connected

Orientation

Course Information

Projects

The rise of
networks






Models

Resources

Nutshell

References

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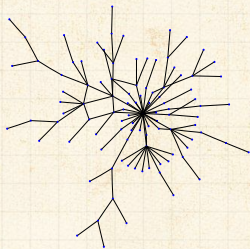


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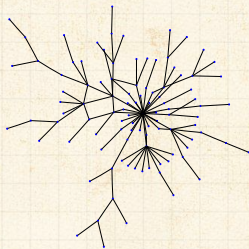
$$\gamma = 2.5, \langle k \rangle = 1.8, \\ N = 150$$

- Introduced by Barabasi and Albert [3]
- Generative model
- Preferential attachment model with growth:
 - $P[\text{attachment to node } i] \propto k_i^\alpha$.
 - Produces $P_k \sim k^{-\gamma}$ when $\alpha = 1$.
- Trickiness: other models generate skewed degree distributions.

[Orientation](#)[Course Information](#)[Projects](#)[The rise of networks](#)[Models](#)[Resources](#)[Nutshell](#)[References](#)**CoNKs**Complex Networks
@networksvox

Everything is connected

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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

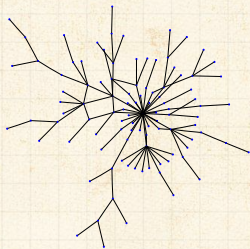


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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

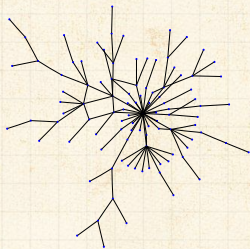


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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

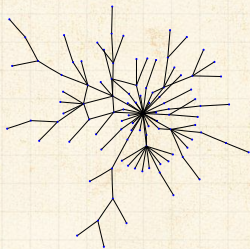


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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

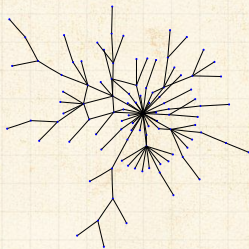


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Complex Networks
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References




CoNKs






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Everything is connected

3. small-world networks

 Introduced by Watts and Strogatz ^[10]

-  **local regularity** (an individual's friends know each other)
-  **global randomness** (shortcuts).
-  Shortcuts allow disease to jump
-  Number of infectives increases exponentially in time
-  Facilitates synchronization

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References




CoNKs

Complex Networks





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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References




CoNKs


Complex Networks
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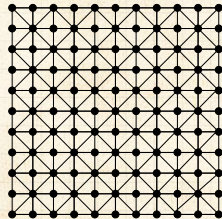
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References




CoNKs


Complex Networks
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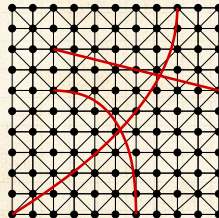
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References




CoNKs


Complex Networks
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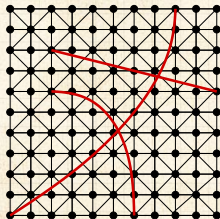
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References




CoNKs


Complex Networks
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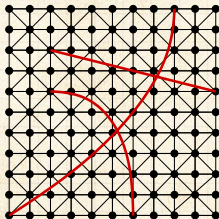
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References




CoNKs

Complex Networks


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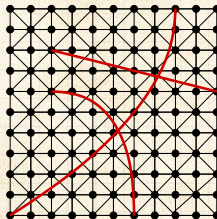
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References

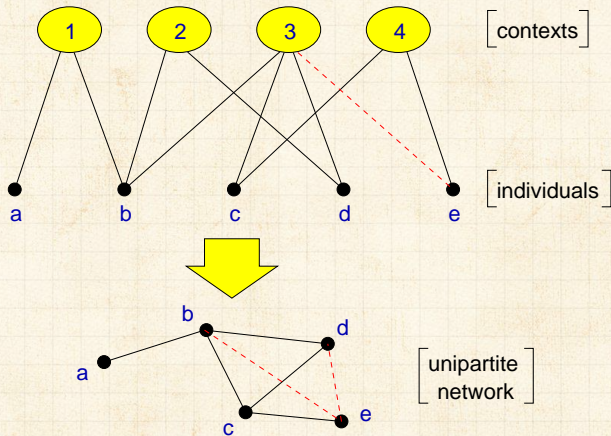


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5. generalized affiliation networks



Bipartite affiliation networks: boards and directors, movies and actors.

Orientation
Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References

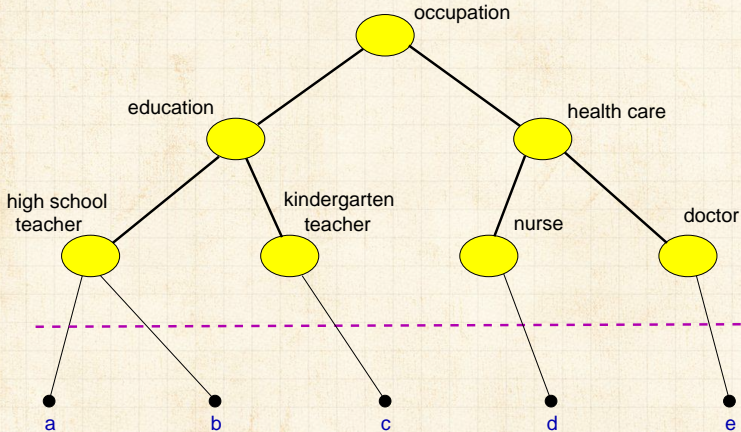


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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References



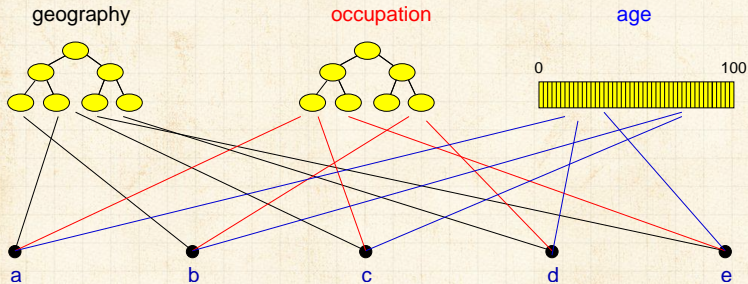
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5. generalized affiliation networks



Blau & Schwartz ^[4], Simmel ^[8], Breiger ^[6], Watts *et al.* ^[9]



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Bonus materials:

COcoNuTS

Orientation

Course Information

Projects

The rise of
networks

Models

Resources


Nutshell

References

Textbooks:



Mark Newman (Physics, Michigan)

"Networks: An Introduction" 



David Easley and Jon Kleinberg (Economics and
Computer Science, Cornell)

"Networks, Crowds, and Markets: Reasoning About a
Highly Connected World" 



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Bonus materials:

Review articles:

 S. Boccaletti et al.,
Physics Reports, 2006,
“Complex networks: structure and dynamics” [5]
Times cited: **7,897**  (as of January 15, 2018)

 M. Newman,
SIAM Review, 2003,
“The structure and function of complex
networks” [7]
Times cited: **16,768**  (as of January 15, 2018)

 R. Albert and A.-L. Barabási
Reviews of Modern Physics, 2002,
“Statistical mechanics of complex networks” [1]
Times cited: **20,656**  (as of January 15, 2018)

Orientation
Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References








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-  The field of complex networks came into existence in the late 1990s.
-  Explosion of papers and interest since 1998/99.
-  Hardened up much thinking about complex systems.
-  Specific focus on networks that are **large-scale**, sparse, **natural** or **man-made**, evolving and dynamic, and (crucially) **measurable**.
-  Three main (blurred) categories:
 1. **Physical** (e.g., river networks),
 2. **Interactional** (e.g., social networks),
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References








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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References








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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References








CoNKs

Complex Networks
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Everything is connected

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[Orientation](#)[Course Information](#)[Projects](#)[The rise of networks](#)[Models](#)[Resources](#)[Nutshell](#)[References](#)**CoNKs**

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[Orientation](#)[Course Information](#)[Projects](#)[The rise of networks](#)[Models](#)[Resources](#)[Nutshell](#)[References](#)**CoNKs**Complex Networks
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-  But focus on dynamics is more of a physics/stat-mech/comp-sci flavor.
-  Two main areas of focus:
 1. Description: Characterizing very large networks
 2. Explanation: Micro story \rightarrow Macro features
-  Some essential structural aspects are understood: degree distribution, clustering, assortativity, group structure, overall structure, ...
-  Still much work to be done, especially with respect to dynamics ...[exiting](#)...

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References








CoNKs

Complex Networks

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Everything is connected

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- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References








CoNKs

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Everything is connected

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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References








CoNKs

Complex Networks
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Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References








CoNKs

Complex Networks

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-  Still much work to be done, especially with respect to dynamics ...**exciting!**

Orientation

Course Information

Projects

The rise of networks

Models

Resources

Nutshell

References








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Overview Key Points (cont.):

-  Obvious connections with the vast extant field of graph theory.
-  But focus on dynamics is more of a physics/stat-mech/comp-sci flavor.
-  Two main areas of focus:
 1. **Description:** Characterizing very large networks
 2. **Explanation:** Micro story \Rightarrow Macro features
-  Some essential structural aspects are understood: degree distribution, clustering, assortativity, group structure, overall structure, ...
-  Still much work to be done, especially with respect to dynamics ...**exciting!**

- Orientation
- Course Information
- Projects
- The rise of networks
- Models
- Resources
- Nutshell
- References



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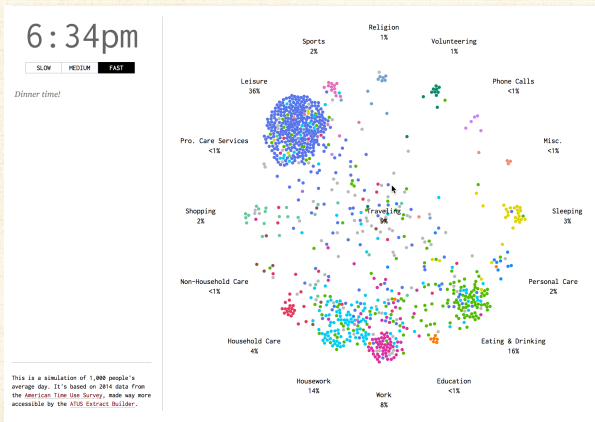
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Orientation
Course Information
Projects

The rise of
networks

Models

Resources

Nutshell

References



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Source: Flowing Data/Nathan Yau.



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Orientation
Course Information
Projects
The rise of
networks
Models
Resources
Nutshell
References



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