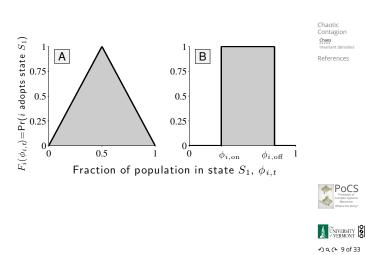






Take r = 2 case:



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Definition of the tent map:

$$F(x) = \begin{cases} rx \text{ for } 0 \le x \le \frac{1}{2}, \\ r(1-x) \text{ for } \frac{1}{2} \le x \le 1. \end{cases}$$

 \clubsuit The usual business: look at how *F* iteratively maps the unit interval [0, 1].





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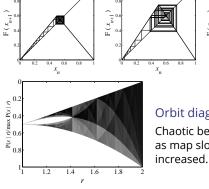
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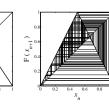
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References

The tent map

Effect of increasing r from 1 to 2.





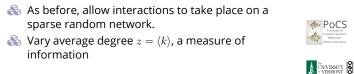






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What happens if nodes have limited information?

Two population examples:

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 $\begin{array}{c} \widehat{\prod}_{i=1}^{l} \begin{bmatrix} A & & & \\ 0.5 & \\ 0.5 & 0.6 \\ 0.2 & \\ 0 &$

- \clubsuit Randomly select $(\phi_{i,1},\phi_{i,2})$ from gray regions shown in plots B and C.
- Insets show composite response function averaged over population.
- 🗞 We'll consider plot C's example: the tent map.

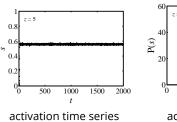


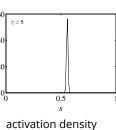
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Invariant densities—stochastic response functions

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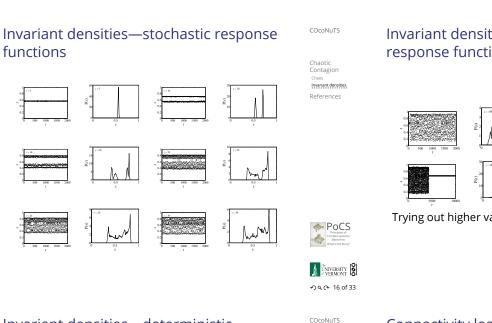




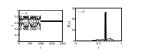


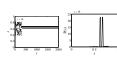


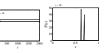
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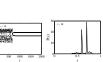


Invariant densities—deterministic response functions for one specific network with $\langle k \rangle = 18$









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Complex Syste (Ppocsvox) What's the Str

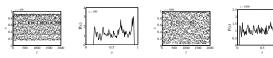
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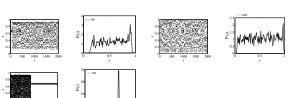


Trying out higher values of $\langle k \rangle$...





Invariant densities References



Trying out higher values of $\langle k \rangle$...

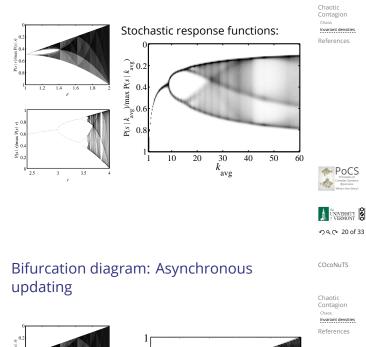


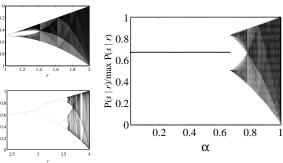
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Connectivity leads to chaos:

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Bifurcation diagram: Asynchronous updating

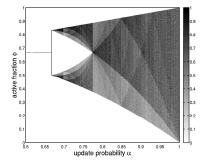


FIG. 3. Bifurcation diagram for the dense map $\Phi(\phi;\alpha)$, Eqn. (18). This was generated by iterating the map at 1000 α values between 0 and 1. The iteration was carried out with 3 random initial conditions for 10000 time steps each, discarding the first 1000. The ϕ -axis contains 1000 bins and the invariant density, shown by the grayscale value, is normalized by the maximum for each α . With $\alpha < 2/3$, all trajectories go to the fixed point at $\phi = 2/3$.

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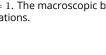
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https://www.youtube.com/watch?v=3bo4fzp4Snw?rel=0 LIC dynamics on a fixed graph with a shared stochastic (tent map) response function. Average degree = 6, update synchronicity parameter α = 1. The macroscopic behavior is period-1, plus noisy fluctuations.



https://www.youtube.com/watch?v=7UCula_ktmw?rel=0 \square LIC dynamics on a fixed graph with a shared stochastic (tent map) response function. Average degree = 11, update synchronicity parameter $\alpha = 1$. The macroscopic behavior is period-2, plus noisy fluctuations.





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https://www.youtube.com/watch?v=oWKt8Zj1Ccw?rel=0 LIC dynamics on a fixed graph with a shared stochastic (tent map) response function. $\langle k \rangle = 30$, update synchronicity parameter $\alpha = 1$. The macroscopic behavior is chaotic.





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https://www.youtube.com/watch?v=7JHrZyyq870?rel=0 How the bifurcation diagram changes with increasing average degree $\langle k \rangle$ as a function of the synchronicity parameter α for the stochastic response (tent map) case.





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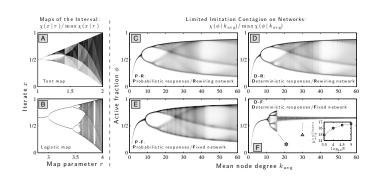
https://www.youtube.com/watch?v=_zwK6polBvc?rel=0 \square How the bifurcation diagram changes with increasing α , the synchronicity parameter as a function of average degree $\langle k \rangle$ for the stochastic response (tent map) case.



Deriversity Solution

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LIC dynamics on a fixed graph with fixed, deterministic response functions. Average degree = 30, update synchronicity parameter $\alpha = 1$. The dynamics exhibit transient chaotic behavior before collapsing to a fixed point.

https://www.youtube.com/watch?v=AfhUlkIOiOU?rel=0 LIC dynamics on a fixed graph with fixed, deterministic response functions. Average degree = 30, update

synchronicity parameter α = 1. Shown are nodes which

behavior has "collapsed."

continue changing (703/1000) after the transient chaotic

https://www.youtube.com/watch?v=ZwY0hTstJ2M?rel=0

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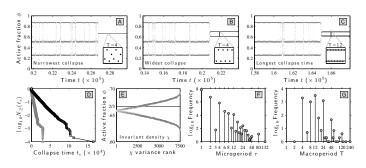
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https://www.youtube.com/watch?v=YDhjmFyBSn4?rel=0 LIC dynamics on a fixed graph with fixed, deterministic response functions. Average degree = 17, update synchronicity parameter α = 1. The dynamics exhibit transient chaotic behavior before collapsing to a period-4 orbit.



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References I

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Contagion References

- [1] P. S. Dodds, K. D. Harris, and C. M. Danforth. Limited Imitation Contagion on random networks: Chaos, universality, and unpredictability. Phys. Rev. Lett., 110:158701, 2013. pdf
- [2] K. D. Harris, C. M. Danforth, and P. S. Dodds. Dynamical influence processes on networks: General theory and applications to social contagion.

Phys. Rev. E, 88:022816, 2013. pdf 🖸



