Small-world networks

Principles of Complex Systems | @pocsvox CSYS/MATH 300, Fall, 2017

Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont























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Nutshell

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Outline

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People thinking about people:

How are social networks structured?



How do we define and measure connections?



Methods/issues of self-report and remote sensing.

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How do we define and measure connections?

Methods/issues of self-report and remote sensing.

What about the dynamics of social networks?

How do social networks/movements begin & evolve?

How does collective problem solving work?

How does information move through social networks?

Which rules give the best 'game of society?'

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Sociotechnical phenomena and algorithms:

What can people and computers do together? (google)

Use Play + Crunch to solve problems. Which problems?

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Social Search

A small slice of the pie:



💫 Q. Can people pass messages between distant individuals using only their existing social connections?

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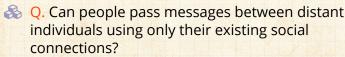


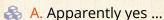




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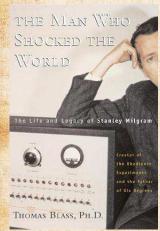






Milgram's social search experiment (1960s)

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Target person = Boston stockbroker.

296 senders from Boston and Omaha.

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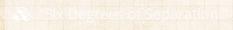
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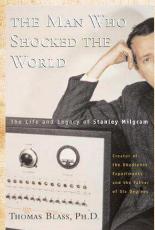


http://www.stanleymilgram.com



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- Target person = Boston stockbroker.
- 296 senders from Boston and Omaha.
- 20% of senders reached target.
- \Leftrightarrow chain length \simeq 6.5.

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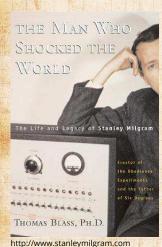






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Popular terms:

- The Small World Phenomenon;
- "Six Degrees of Separation."

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From Frigyes Karinthy's "Chain-links" Tin "Everything is Different", 1929:

'A fascinating game grew out of this discussion. One of us suggested performing the following experiment to prove that the population of the Earth is closer together now than they have ever been before. We should select any person from the 1.5 billion inhabitants of the Earth-anyone, anywhere at all. He bet us that, using no more than five individuals, one of whom is a personal acquaintance, he could contact the selected individual using nothing except the network of personal acquaintances. For example, "Look, you know Mr. X.Y., please ask him to contact his friend Mr. Q.Z., whom he knows, and so forth."

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Alt's a game ☑: "Kevin Bacon is the Center of the Universe"

♣ The Oracle of Bacon

Six Degrees of Paul Erdös:



Academic papers.

& Erdös Number Project 7

So naturally we must have the Endow Bacon number \mathbb{R}^n . One Story Lab alum has $\mathsf{EB\#} < \infty$.

Natalie Hershlag's (Portman's) $\mathsf{EB\#} = 5 + 2 = 7$.

The $\mathsf{EBS\#}$ is also a thing:

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The Oracle of Bacon

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🚓 Erdös Number 🗹

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& Erdös Number Project 2

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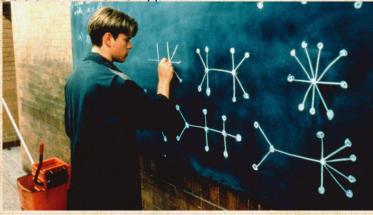
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Good Will Hunting:





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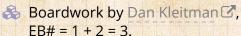
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See Kleitman's sidebar in Mark Saul's Movie Review (Notices of the AMS, Vol. 45, 1998.)





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You may already be a winner in NSA's "three-degrees" surveillance sweepstakes! NSA's probes could cover hundreds of millions of Americans. Thanks, Kevin Bacon.

by Sean Gallagher - July 18 2013, 4:00pm EDT





Aurich Lawson



A Many people are within three degrees from a random person ...

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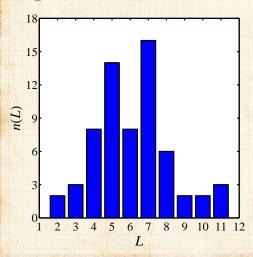
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Lengths of successful chains:



From Travers and Milgram (1969) in Sociometry: [12] "An Experimental Study of the Small World Problem." PoCS | @pocsvox
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Two features characterize a social 'Small World':

- 1. Short paths exist
 - and
- 2. People are good at finding them.

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Two features characterize a social 'Small World':

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piece)

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Two features characterize a social 'Small World':

- 1. Short paths exist, (= Geometric piece) and
- 2. People are good at finding them. (= Algorithmic piece)

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Social Search

Milgram's small world experiment with email:





"An Experimental study of Search in Global Social Networks" 🗹

Dodds, Muhamad, and Watts, Science, **301**, 827–829, 2003. [6]

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🚳 60,000+ participants in 166 countries







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60,000+ participants in 166 countries

Experiments

18 targets in 13 countries including

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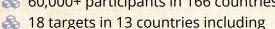


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60,000+ participants in 166 countries



a professor at an lvy League university,

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a policeman in Australia,







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Small-world networks

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24,000+ chains





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18 targets in 13 countries including

Generalized affiliation

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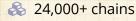
References

an archival inspector in Estonia,

a technology consultant in India,

a policeman in Australia, and

a veterinarian in the Norwegian army.



We were lucky and contagious (more later):

"Using E-Mail to Count Connections" , Sarah Milstein, New York Times, Circuits Section (December, 2001)







All targets:

Table S1

Target	City	Country	Occupation	Gender	N	N _c (%)	r (r ₀)	<l></l>
1	Novosibirsk	Russia	PhD student	F	8234	20(0.24)	64 (76)	4.05
2	New York	USA	Writer	F	6044	31 (0.51)	65 (73)	3.61
3	Bandung	Indonesia	Unemployed	M	8151	0	66 (76)	n/a
4	New York	USA	Journalist	F	5690	44 (0.77)	60 (72)	3.9
5	Ithaca	USA	Professor	M	5855	168 (2.87)	54 (71)	3.84
6	Melbourne	Australia	Travel Consultant	F	5597	20 (0.36)	60 (71)	5.2
7	Bardufoss	Norway	Army veterinarian	M	4343	16 (0.37)	63 (76)	4.25
8	Perth	Australia	Police Officer	M	4485	4 (0.09)	64 (75)	4.5
9	Omaha	USA	Life Insurance	F	4562	2 (0.04)	66 (79)	4.5
			Agent					
10	Welwyn Garden City	UK	Retired	M	6593	1 (0.02)	68 (74)	4
11	Paris	France	Librarian	F	4198	3 (0.07)	65 (75)	5
12	Tallinn	Estonia	Archival Inspector	M	4530	8 (0.18)	63(79)	4
13	Munich	Germany	Journalist	M	4350	32 (0.74)	62 (74)	4.66
14	Split	Croatia	Student	M	6629	0	63 (77)	n/a
15	Gurgaon	India	Technology	M	4510	12 (0.27)	67 (78)	3.67
			Consultant					
16	Managua	Nicaragua	Computer analyst	M	6547	2 (0.03)	68 (78)	5.5
17	Katikati	New Zealand	Potter	M	4091	12 (0.3)	62 (74)	4.33
18	Elderton	USA	Lutheran Pastor	M	4438	9 (0.21)	68 (76)	4.33
Totals					98,847	384 (0.4)	63 (75)	4.05

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Milgram's participation rate was roughly 75%







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Email version: Approximately 37% participation rate.

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Milgram's participation rate was roughly 75%

Email version: Approximately 37% participation rate.

Probability of a chain of length 10 getting through:

$$.37^{10} \simeq 5 \times 10^{-5}$$







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Milgram's participation rate was roughly 75%

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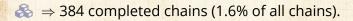
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Probability of a chain of length 10 getting through:

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Motivation/Incentives/Perception matter.

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Motivation/Incentives/Perception matter.

If target seems reachable ⇒ participation more likely.







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Motivation/Incentives/Perception matter.

If target seems reachable

⇒ participation more likely.

Small changes in attrition rates ⇒ large changes in completion rates







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Motivation/Incentives/Perception matter.

If target seems reachable
 ⇒ participation more likely.

🙈 Small changes in attrition rates

⇒ large changes in completion rates

e.g., \(\square 15\% \) in attrition rate⇒ \(\times 800\% \) in completion rate

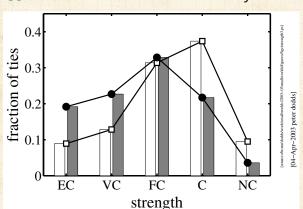






Comparing successful to unsuccessful chains:

Successful chains used relatively weaker ties:



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Successful chains disproportionately used:

Weak ties, Granovetter

Professional ties (34% vs. 13%)

Ties originating at work/college

Target's work (65% vs. 40%)

land disproportion thely avoided

fillibs (8% vs. 1%) (+ no evidence all funnels).

& family/friendship ties (60% vs. 83%

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Successful chains disproportionately used:



Meak ties, Granovetter [7]

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Successful chains disproportionately used:

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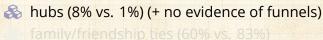
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Successful chains disproportionately used:

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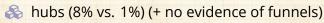
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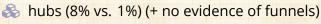
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🚓 family/friendship ties (60% vs. 83%)



Geography → Work





Senders of successful messages showed little absolute dependency on



age, gender

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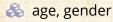
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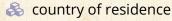
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Senders of successful messages showed little absolute dependency on

age, gender

country of residence

🙈 income

relationship to recipient

Range of completion rates for subpopulations:
30% to

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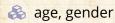
References

🚓 religion





Senders of successful messages showed little absolute dependency on



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Senders of successful messages showed little absolute dependency on

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🙈 age, gender

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country of residence

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🙈 income

🙈 religion

relationship to recipient

Range of completion rates for subpopulations: 30% to 40%







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Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."







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Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."

Why:



Specificity important

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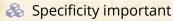


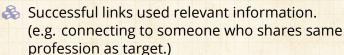
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Why:





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Basic results:



$\langle L \rangle = 4.05$ for all completed chains

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Basic results:



 $\langle L \rangle = 4.05$ for all completed chains



A L_* = Estimated 'true' median chain length (zero attrition)

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Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- A L_* = Estimated 'true' median chain length (zero attrition)
- A Intra-country chains: $L_* = 5$

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- A Inter-country chains: $L_* = 7$
- $All chains: L_* = 7$

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Small-world networks

Basic results:

- $\langle L \rangle = 4.05$ for all completed chains
- A L_* = Estimated 'true' median chain length (zero attrition)
- A Intra-country chains: $L_* = 5$
- A Inter-country chains: $L_* = 7$
- $All chains: L_* = 7$
- \clubsuit Milgram: $L_* \simeq 9$

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Harnessing social search:

- Can distributed social search be used for something big/good?
 - What about something evil? (Good idea to check.)
- What about socio-inspired algorithms for information search? (More later.)
- For real social search, we have an incentives problem.
- Which kind of influence mechanisms/algorithms would help propagate search?
- Fun, money, prestige, ...?
- Must be 'non-gameable.'

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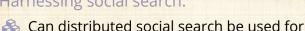
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Harnessing social search:



something big/good?

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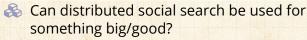
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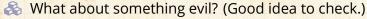
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A Grand Challenge:

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- Originally funded by DARPA who created a grand Newbook Challenge 2 for the 40th anniversary.
- Saturday December 5, 2009: DARPA puts 10 red weather balloons up during the day.
- Each 8 foot diameter balloon is anchored to the ground somewhere in the United States.
- Challenge: Find the latitude and longitude of each balloon.
- Prize: \$40,000

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A Grand Challenge:



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Where the balloons were:



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The winning team and strategy:



MIT's Media Lab won in less than 9 hours. [9]

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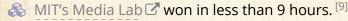
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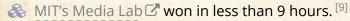
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Recursive incentive structure with exponentially decaying payout:

\$2000 for correctly reporting the coordinates of a balloon.

\$1000 for recruiting a person who finds a balloon \$500 for recruiting a person who recruits the balloon finder, ...

(Not a Ponzi scheme.)

True victory:

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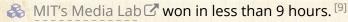
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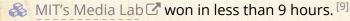
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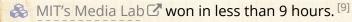
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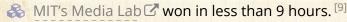
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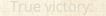
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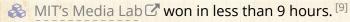
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🙈 True victory: Colbert interviews Riley Crane 🗹

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Clever scheme:



Max payout = \$4000 per balloon.

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Clever scheme:



Max payout = \$4000 per balloon.



A Individuals have clear incentives to both



2. find balloons (goal action).

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Clever scheme:



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Gameable?

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Limit to how much money a set of bad actors can extract.

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Extra notes:



MIT's brand helped greatly.

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Worthwhile looking at these competing strategies.

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A number of other teams did well .



Worthwhile looking at these competing strategies. [9]











Collective Detective:



Finding an errant panda

Once again, social media proved to be a powerful dragnet. Around 1:15 p.m., a Washingtonian posted a picture on Twitter of Rusty in a patch of weeds in the Adams Morgan district, not far from the 163-acre zoo, which was created in 1889 by an act of Congress. "Red panda in our neighborhood," wrote Ashley Foughty, who identified herself as a singer, actress and traveler. "Please come save him!"

Another neighbor posted a photograph of two zoo workers, one in safari shorts standing on a rooftop, one holding a giant butterfly net. Soon the zoo announced: "Rusty the red panda has been recovered, crated & is headed safely back to the National Zoo!"

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Nature News: "Crowdsourcing in manhunts can work: Despite mistakes over the Boston bombers, social media can help to find people quickly" by Philip Ball (April 26, 2013)

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Motherboard, Vice: One Degree of Separation in the Forever War dby Brian Castner (November 11, 2015)

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The social world appears to be small ...why?

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Theory: how do we understand the small world property?

Connected random networks have short average path lengths:

$$\langle d_{AB} \rangle \sim \log(N)$$

N = population size, d_{AB} = distance between nodes A and B.

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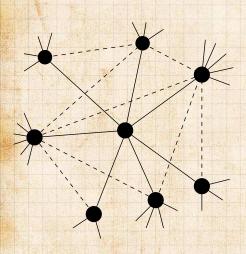
But: social networks aren't random ...







Simple socialness in a network:



Need "clustering" (your friends are likely to know each other):

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Small-world networks

Theory

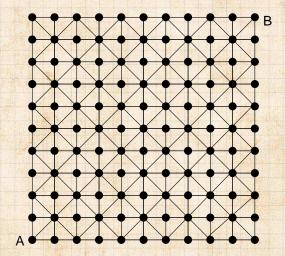
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Non-randomness gives clustering:



 $d_{AB} = 10 \rightarrow \text{too many long paths.}$

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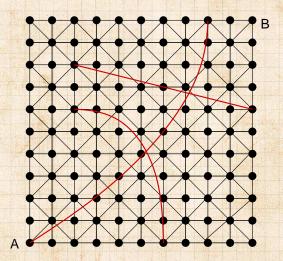






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Randomness + regularity



Now have $d_{AB}=3$

 $\langle d \rangle$ decreases overall

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Introduced by Watts and Strogatz (Nature, 1998) [14] "Collective dynamics of 'small-world' networks."

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Small-world networks were found everywhere:



neural network of C. elegans,

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- 🚳 food webs,

social networks of comic book characters, ...

čely weak jedicijements

local regularity + random short cuts

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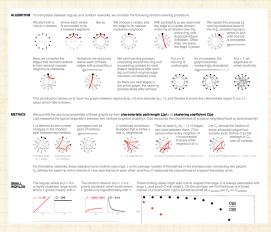
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Papers should be apps:



- Interactive figures and tables = windows into large data sets (empirical or simulated).

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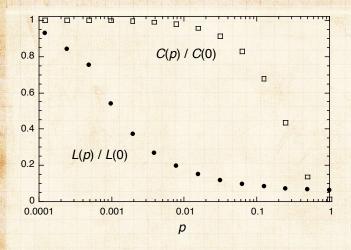
References





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The structural small-world property:



L(p) = average shortest path length as a function of p

Rrightarrow C(p) = average clustring as a function of p

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But are these short cuts findable?

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But are these short cuts findable?

Nope. [8]

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Nodes cannot find each other quickly with any local search method.

Need a more sophisticated model ...

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What can a local search method reasonably use?

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What can a local search method reasonably use?

How to find things without a map?

Experiments Generalized affiliation

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What can a local search method reasonably use?

networks Experiments

How to find things without a map?

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Small-world

Need some measure of distance between friends and the target.







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What can a local search method reasonably use?

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How to find things without a map?

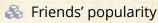
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Need some measure of distance between friends and the target.

References

Some possible knowledge:

Target's identity



Friends' identities

Where message has been







Jon Kleinberg (Nature, 2000) [8] "Navigation in a small world."

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Jon Kleinberg (Nature, 2000) [8] "Navigation in a small world."

Allowed to vary:

1. local search algorithm

2. network structure.

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Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice
- 2. Add local links so nodes know all nodes within a distance *q*.
- 3. Add m short cuts per node.
- 4. Connect i to j with probability

$$p_{ij} \propto x_{ij}^{-\alpha}$$

a = 0: random connections

diarge: reinforce local connections.

- connections grow logarithmically in space.

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Theoretical optimal search:



"Greedy" algorithm.

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Theoretical optimal search:

- "Greedy" algorithm.
- Number of connections grow logarithmically (slowly) in space: $\alpha = d$.

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Theoretical optimal search:

- "Greedy" algorithm.
- Number of connections grow logarithmically (slowly) in space: $\alpha = d$.
- Social golf.

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Theoretical optimal search:

- "Greedy" algorithm.
- Number of connections grow logarithmically (slowly) in space: $\alpha = d$.
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Search time grows slowly with system size (like $\log^2 N$).

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Theoretical optimal search:

- "Greedy" algorithm.
- Number of connections grow logarithmically (slowly) in space: $\alpha = d$.
- Social golf.

Search time grows slowly with system size (like $\log^2 N$).

But: social networks aren't lattices plus links.

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Advances for understanding Kleinberg's model:



"Kleinberg Navigation in Fractal Small World Networks"

Roberson and ben-Avraham, Phys. Rev. E, **74**, 017101, 2006. [10]



"Asymptotic behavior of the Kleinberg model"

Carmi et al., Phys. Rev. Lett., **102**, 238702, 2009. [4]



"Extended navigability of small world networks: Exact results and new insights"

Cartoza and De Los Rios, Phys. Rev. Lett., **2009**, 238703, 2009. [5] PoCS | @pocsvox Small-world networks

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If networks have hubs can also search well: Adamic et al. (2001)[1]

$$P(k_i) \propto k_i^{-\gamma}$$

where k = degree of node i (number of friends).

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Adamic et al. (2001)^[1]

$$P(k_i) \propto k_i^{-\gamma}$$

where k = degree of node i (number of friends).

Basic idea: get to hubs first (airline networks). PoCS | @pocsvox
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Adamic et al. (2001)[1]

$$P(k_i) \propto k_i^{-\gamma}$$

where k = degree of node i (number of friends).

& Basic idea: get to hubs first (airline networks).

& But: hubs in social networks are limited.

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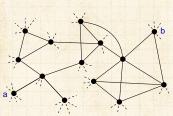






The problem

If there are no hubs and no underlying lattice, how can search be efficient?



Which friend of a is closest to the target b?

What does 'closest' mean?

What is 'social distance'?

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One approach: incorporate identity.

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One approach: incorporate identity.

Identity is formed from attributes such as:

Geographic location

Type of employment

Religious beliefs

Recreational activities.

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One approach: incorporate identity.

Identity is formed from attributes such as:

- Geographic location
- Type of employment
- Religious beliefs
- Recreational activities.

Groups are formed by people with at least one similar attribute.

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One approach: incorporate identity.

Identity is formed from attributes such as:

Geographic location

Type of employment

Religious beliefs

Recreational activities.

Groups are formed by people with at least one similar attribute.

Attributes ⇔ Contexts ⇔ Interactions ⇔ Networks.

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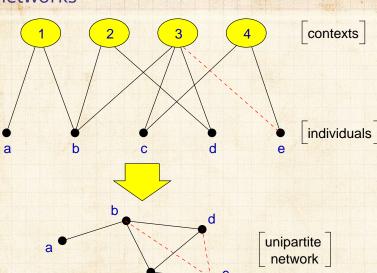
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Social distance—Bipartite affiliation networks



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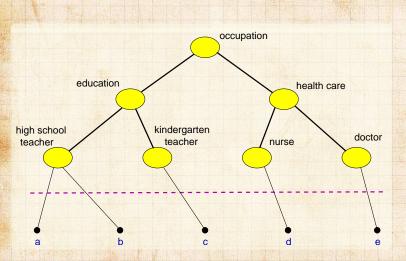




Bipartite affiliation networks: boards and



Social distance—Context distance



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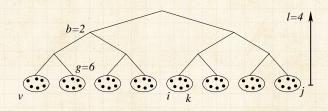
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Distance between two individuals x_{ij} is the height of lowest common ancestor.



$$x_{ij} = 3$$
, $x_{ik} = 1$, $x_{iv} = 4$.

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Individuals are more likely to know each other the closer they are within a hierarchy.

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Individuals are more likely to know each other the closer they are within a hierarchy.

Construct z connections for each node using

$$p_{ij} = c \exp\{-\alpha x_{ij}\}.$$

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Individuals are more likely to know each other the closer they are within a hierarchy.

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Construct z connections for each node using

networks

$$p_{ij} = c \exp\{-\alpha x_{ij}\}.$$

 $\alpha = 0$: random connections.







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Individuals are more likely to know each other the closer they are within a hierarchy.

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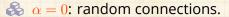
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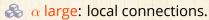
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$$p_{ij} = c \exp\{-\alpha x_{ij}\}.$$



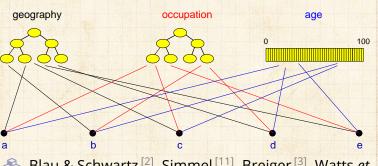






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Blau & Schwartz [2], Simmel [11], Breiger [3], Watts et al. [13]; see also Google+ Circles.

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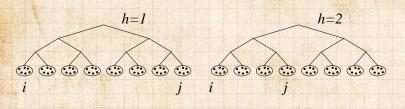
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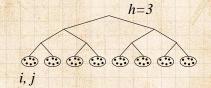
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$$\begin{split} \vec{v}_i &= [1\ 1\ 1]^T, \, \vec{v}_j = [8\ 4\ 1]^T \\ x^1_{ij} &= 4, \ x^2_{ij} = 3, \ x^3_{ij} = 1. \end{split}$$

Social distance: $y_{ij} = \min_{h} x_{ij}^{h}$.

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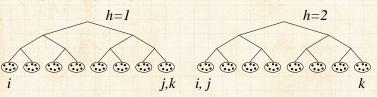






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Triangle inequality doesn't hold:



$$y_{ik} = 4 > y_{ij} + y_{jk} = 1 + 1 = 2.$$



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Individuals know the identity vectors of

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Individuals know the identity vectors of 1. themselves,

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends,

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends, and
- 3. the target.

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends, and
- 3. the target.

Individuals can estimate the social distance between their friends and the target.

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends, and
- 3. the target.
- Individuals can estimate the social distance between their friends and the target.
- Use a greedy algorithm + allow searches to fail randomly.

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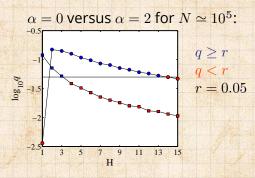
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The model-results—searchable networks



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q = probability an arbitrary message chain reaches atarget.

- A few dimensions help.
- Searchability decreases as population increases.

Precise form of hierarchy largely doesn't matter.



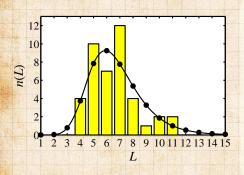




The model-results

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Milgram's Nebraska-Boston data:



Model parameters:



$$\gg z = 300, g = 100,$$

$$\alpha = 1, H = 2;$$

$$\langle L_{\rm model} \rangle \simeq 6.7$$

$$Alpha L_{\rm data} \simeq 6.5$$

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Social search—Data

Adamic and Adar (2003)

For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.

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Social search—Data

Adamic and Adar (2003)

- For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.
- Probability of connection as function of real distance $\propto 1/r$.

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Social Search—Real world uses

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Tags create identities for objects

Website tagging: bitly.com
 ✓

🙈 (e.g., Wikipedia)

Photo tagging: flickr.com

Dynamic creation of metadata plus links between information objects.

Folksonomy: collaborative creation of metadata







Social Search—Real world uses

Recommender systems:



Amazon uses people's actions to build effective connections between books.

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Social Search—Real world uses

Recommender systems:

- Amazon uses people's actions to build effective connections between books.
- Conflict between 'expert judgments' and tagging of the hoi polloi.

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Bare networks are typically unsearchable.

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Bare networks are typically unsearchable.



Paths are findable if nodes understand how network is formed.

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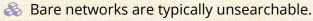
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Paths are findable if nodes understand how network is formed.

Importance of identity (interaction contexts).

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- Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- Importance of identity (interaction contexts).
- Improved social network models.

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- Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- Importance of identity (interaction contexts).
- Improved social network models.
- Construction of peer-to-peer networks.

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Nutshell







- Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- Importance of identity (interaction contexts).
- Improved social network models.
- Construction of peer-to-peer networks.
- Construction of searchable information databases.

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Neural reboot (NR):

Food-induced happiness

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