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People thinking about people:

How are social networks structured?

- How do we define and measure connections?
- Methods/issues of self-report and remote sensing.

What about the dynamics of social networks?

- How do social networks/movements begin & evolve?
- How does collective problem solving work?
- How does information move through social networks?
- Which rules give the best 'game of society?'

Sociotechnical phenomena and algorithms:

What can people and computers do together? (google) Use Play + Crunch to solve problems. Which problems?

Social Search

A small slice of the pie:

- 🗞 Q. Can people pass messages between distant individuals using only their existing social connections?
- 🗞 A. Apparently yes ...



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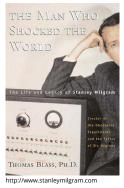


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Milgram's social search experiment (1960s)



- 🗞 Target person = Boston stockbroker.
- 🙈 296 senders from Boston and Omaha.
- 20% of senders reached target.
- & chain length \simeq 6.5.

Popular terms:

- 🗞 The Small World Phenomenon;
- Six Degrees of Separation."

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From Frigyes Karinthy's "Chain-links" I in "Everything is Different", 1929:

'A fascinating game grew out of this discussion. One of us suggested performing the following experiment to prove that the population of the Earth is closer together now than they have ever been before. We should select any person from the 1.5 billion inhabitants of the Earth-anyone, anywhere at all. He bet us that, using no more than five individuals, one of whom is a personal acquaintance, he could contact the selected individual using nothing except the network of personal acquaintances. For example, "Look, you know Mr. X.Y., please ask him to contact his friend Mr. Q.Z., whom he knows, and so forth."

Six Degrees of Kevin Bacon:



- 🗞 It's a game 🗷: "Kevin Bacon is the Center of the Universe"
- 🚳 The Oracle of Bacon 🗹

Six Degrees of Paul Erdös:



\lambda Academic papers.

- 🚳 Erdös Number 🗹 🚳 Erdös Number Project 🗹
- 🗞 So naturally we must have the Erdös-Bacon Number 🗹.
- & One Story Lab alum has EB# $< \infty$.
- 🗞 Natalie Hershlag's (Portman's) EB# = 5 + 2 = 7.
- 🗞 The EBS# is also a thing: erdosbaconsabbath.com 🗹.

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Good Will Hunting:



1998.)

You may already be a winner in NSA's

"three-degrees" surveillance sweepstakes!



🚳 Boardwork by Dan Kleitman 🗹, EB# = 1 + 2 = 3. 🗞 See Kleitman's sidebar in Mark Saul's Movie Review (Notices of the AMS, Vol. 45,

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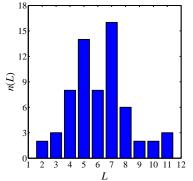
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🗞 Many people 🗹 are within three degrees from a random person ...

The problem

Lengths of successful chains:



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From Travers and Milgram (1969) in Sociometry:^[12] "An Experimental Study of the Small World Problem."



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The problem

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All targets:

Table S1

Two features characterize a social 'Small World':

- 1. Short paths exist, (= Geometric piece) and
- 2. People are good at finding them. (= Algorithmic piece)

	1	Novosibirsk	R
	2	New York	U
on	3	Bandung	In
	4	New York	U
	5	Ithaca	U
	6	Melbourne	A
	7	Bardufoss	N
	8	Perth	A
	9	Omaha	U
	10	Welwyn Garden City	U
	11	Paris	Fr
	12	Tallinn	E

Target	City	Country	Occupation	Gender	N	N_{c} (%)	$r(r_0)$	<l></l>
1	Novosibirsk	Russia	PhD student	F	8234	20(0.24)	64 (76)	4.05
2	New York	USA	Writer	F	6044	31 (0.51)	65 (73)	3.61
3	Bandung	Indonesia	Unemployed	М	8151	0	66 (76)	n/a
4	New York	USA	Journalist	F	5690	44 (0.77)	60 (72)	3.9
5	Ithaca	USA	Professor	М	5855	168 (2.87)	54 (71)	3.84
6	Melbourne	Australia	Travel Consultant	F	5597	20 (0.36)	60 (71)	5.2
7	Bardufoss	Norway	Army veterinarian	М	4343	16 (0.37)	63 (76)	4.25
8	Perth	Australia	Police Officer	м	4485	4 (0.09)	64 (75)	4.5
9	Omaha	USA	Life Insurance	F	4562	2 (0.04)	66 (79)	4.5
			Agent					
10	Welwyn Garden City	UK	Retired	м	6593	1 (0.02)	68 (74)	4
11	Paris	France	Librarian	F	4198	3 (0.07)	65 (75)	5
12	Tallinn	Estonia	Archival Inspector	м	4530	8 (0.18)	63(79)	4
13	Munich	Germany	Journalist	м	4350	32 (0.74)	62 (74)	4.66
14	Split	Croatia	Student	м	6629	0	63 (77)	n/a
15	Gurgaon	India	Technology	М	4510	12 (0.27)	67 (78)	3.67
			Consultant					
16	Managua	Nicaragua	Computer analyst	м	6547	2 (0.03)	68 (78)	5.5
17	Katikati	New Zealand	Potter	м	4091	12 (0.3)	62 (74)	4.33
18	Elderton	USA	Lutheran Pastor	м	4438	9 (0.21)	68 (76)	4.33
Totals					98,847	384 (0.4)	63 (75)	4.05



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Social Search

Milgram's small world experiment with email:



"An Experimental study of Search in Global Social Networks" Dodds, Muhamad, and Watts, Science, **301**, 827–829, 2003. ^[6]

Social search—the Columbia experiment

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- 18 targets in 13 countries including
 - a professor at an Ivy League university,
 - an archival inspector in Estonia,
 - a technology consultant in India,
 - 📦 a policeman in Australia, and
 - a veterinarian in the Norwegian army.
- 🗞 24,000+ chains

We were lucky and contagious (more later):

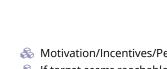
"Using E-Mail to Count Connections" C, Sarah Milstein, New York Times, Circuits Section (December, 2001)

References

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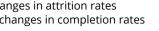
(W) [8]



- Small changes in attrition rates \Rightarrow large changes in completion rates
- 🚳 e.g., 🔪 15% in attrition rate $\Rightarrow \nearrow$ 800% in completion rate



- 🗞 Motivation/Incentives/Perception matter. lf target seems reachable \Rightarrow participation more likely.





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Social search—the Columbia experiment

Milgram's participation rate was roughly 75%

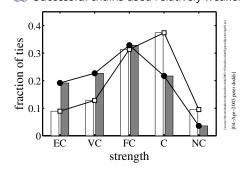
- Email version: Approximately 37% participation rate.
- Probability of a chain of length 10 getting through:

 \Rightarrow 384 completed chains (1.6% of all chains).

 $.37^{10}\simeq 5\times 10^{-5}$

Social search—the Columbia experiment

Comparing successful to unsuccessful chains: Successful chains used relatively weaker ties:



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Social search—the Columbia experiment

Successful chains disproportionately used:

- 🚳 Weak ties, Granovetter 🖓
- Professional ties (34% vs. 13%)
- Ties originating at work/college
- Target's work (65% vs. 40%)

...and disproportionately avoided

- hubs (8% vs. 1%) (+ no evidence of funnels)
- line family/friendship ties (60% vs. 83%)

Geography \rightarrow Work

Social search—the Columbia experiment

Senders of successful messages showed little absolute dependency on

- \delta age, gender
- 🗞 country of residence
- 🚳 income
- 🗞 religion
- 🗞 relationship to recipient

Range of completion rates for subpopulations: 30% to 40%



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Social search—the Columbia experiment

Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."

Why:

- Specificity important
- links used relevant information. (e.g. connecting to someone who shares same profession as target.)



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Social search—the Columbia experiment

🗞 L, = Estimated 'true' median chain length (zero

 $\langle L \rangle = 4.05$ for all completed chains

 \clubsuit Intra-country chains: $L_* = 5$

 \clubsuit Inter-country chains: $L_* = 7$

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- All chains: $L_* = 7$ 3 Milgram: $L_* \simeq 9$

Basic results:

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Usefulness:

Harnessing social search:

- 🚳 Can distributed social search be used for something big/good?
- 🚳 What about something evil? (Good idea to check.)
- 🗞 What about socio-inspired algorithms for information search? (More later.)
- For real social search, we have an incentives problem.
- Which kind of influence mechanisms/algorithms would help propagate search?
- 🚳 Fun, money, prestige, ...?
- 🚳 Must be 'non-gameable.'





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Red balloons:

A Grand Challenge:

- 🚳 1969: The Internet is born 🗹 (the ARPANET C -- four nodes!).
- Originally funded by DARPA who created a grand Network Challenge 🕝 for the 40th anniversary.
- 🗞 Saturday December 5, 2009: DARPA puts 10 red weather balloons up during the day.
- 🗞 Each 8 foot diameter balloon is anchored to the ground somewhere in the United States.
- 🗞 Challenge: Find the latitude and longitude of each balloon.
- A Prize: \$40,000.

Where the balloons were:

*DARPA = Defense Advanced Research Projects Agency



Finding red balloons:

The winning team and strategy:

- 🗞 MIT's Media Lab 🗹 won in less than 9 hours. [9]
- Pickard et al. "Time-Critical Social Mobilization," [9] Science Magazine, 2011.
- People were virally recruited online to help out.
- ldea: Want people to both (1) find the balloons, and (2) involve more people.
- Recursive incentive structure with exponentially decaying payout:
 - \$2000 for correctly reporting the coordinates of a balloon.
 - \$1000 for recruiting a person who finds a balloon. \$500 for recruiting a person who recruits the
 - 📦 (Not a Ponzi scheme.)

balloon finder, ...

🗞 True victory: Colbert interviews Riley Crane 🗹

Finding balloons:

Clever scheme:

- 🚳 Max payout = \$4000 per balloon.
- 🗞 Individuals have clear incentives to both 1. involve/source more people (spread), and 2. find balloons (goal action).
- 🚳 Gameable?
- limit to how much money a set of bad actors can extract.

Extra notes:

- MIT's brand helped greatly.
- MIT group first heard about the competition a few days before. Ouch.
- & A number of other teams did well \square .
- Worthwhile looking at these competing strategies.^[9]

Collective Detective:



- langle Section 2017 Nature News: "Crowdsourcing in manhunts can work: Despite mistakes over the Boston bombers, social media can help to find people quickly" 🗷 by Philip Ball (April 26, 2013)
- Motherboard, Vice: One Degree of Separation in the Forever War 🗷 by Brian Castner (November 11, 2015)



The social world appears to be small ...why?

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Theory

Theory: how do we understand the small world property?

Connected random networks have short average path lengths:

$$\langle d_{AB}\rangle \sim \log(N$$

N = population size,

 d_{AB} = distance between nodes A and B. 🚳 But: social networks aren't random ...





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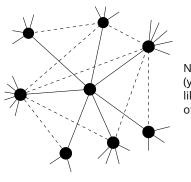


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Simple socialness in a network:



Need "clustering" (your friends are likely to know each other):



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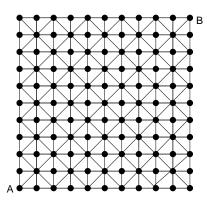
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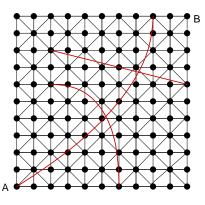
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 $d_{AB}=10 \rightarrow$ too many long paths.

Randomness + regularity



Now have $d_{AB} = 3$

 $\langle d
angle$ decreases overall



Small-world networks

Introduced by Watts and Strogatz (Nature, 1998)^[14] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

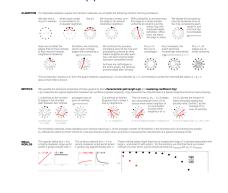
- A neural network of C. elegans,
- 🗞 semantic networks of languages,
- actor collaboration graph,
- 🚳 food webs,
- 🗞 social networks of comic book characters, ...

Very weak requirements:

local regularity + random short cuts



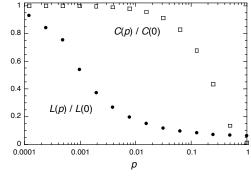
Papers should be apps:



Bret Victor's Scientific Communication As Sequential Art

Interactive figures and tables = windows into large data sets (empirical or simulated).





 $\label{eq:L} \bigotimes \ L(p) \mbox{=} \mbox{average shortest path length as a function of } p$ $\mbox{\&} \ C(p) \mbox{=} \mbox{average clustring as a function of } p$

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Previous work—finding short paths

But are these short cuts findable?

Nodes cannot find each other quickly

Need a more sophisticated model ...

with any local search method.

Nope. [8]

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Theory

Previous work—finding short paths

Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice.
- 2. Add local links so nodes know all nodes within a distance q.
- 3. Add *m* short cuts per node.

 $\alpha = 0$: random connections.

Theoretical optimal search:

(slowly) in space: $\alpha = d$.

🚳 "Greedy" algorithm.

\delta Social golf.

 α large: reinforce local connections.

Previous work—finding short paths

Number of connections grow logarithmically

Search time grows slowly with system size (like $\log^2 N$).

But: social networks aren't lattices plus links.

4. Connect i to j with probability

 $p_{ij} \propto x_{ij}^{-\alpha}.$

 $\alpha = d$: connections grow logarithmically in space.



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Previous work—finding short paths

- What can a local search method reasonably use?
- How to find things without a map?
- Need some measure of distance between friends and the target.

Some possible knowledge:

- 🗞 Target's identity
- 🗞 Friends' popularity
- 🗞 Friends' identities
- 🚳 Where message has been



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Jon Kleinberg (Nature, 2000)^[8] "Navigation in a small world."

Allowed to vary:

- 1. local search algorithm and
- 2. network structure.







Theory References





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"Kleinberg Navigation in Fractal Small World Networks" Roberson and ben-Avraham,

Advances for understanding Kleinberg's model:

"Asymptotic behavior of the Kleinberg



insights" 🖸

Phys. Rev. E, 74, 017101, 2006.^[10]

model"

Phys. Rev. Lett., 102, 238702, 2009. [4]

"Extended navigability of small world networks: Exact results and new Cartoza and De Los Rios,

Phys. Rev. Lett., 2009, 238703, 2009.^[5]



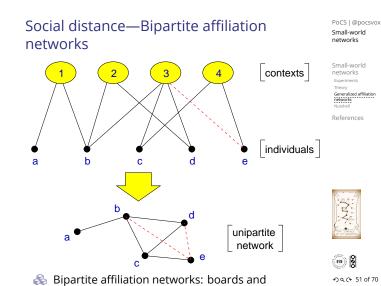
Previous work—finding short paths

If networks have hubs can also search well: Adamic et al. (2001)^[1]

 $P(k_i) \propto k_i^{-\gamma}$

where k = degree of node i (number of friends). & Basic idea: get to hubs first

- (airline networks).
- 🚳 But: hubs in social networks are limited.



Bipartite affiliation networks: boards and directors, movies and actors.

Social distance—Context distance

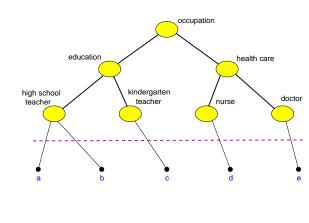


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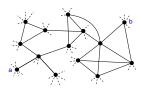




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The problem

If there are no hubs and no underlying lattice, how can search be efficient?



Which friend of a is closest to the target b?

What does 'closest' mean?

What is 'social distance'?



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Models

One approach: incorporate identity.

Identity is formed from attributes such as:

- 🚳 Geographic location
- 🗞 Type of employment
- 🗞 Religious beliefs
- 🚳 Recreational activities.

Groups are formed by people with at least one similar attribute.

 $\mathsf{Attributes} \Leftrightarrow \mathsf{Contexts} \Leftrightarrow \mathsf{Interactions} \Leftrightarrow \mathsf{Networks}.$

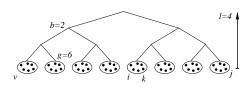


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Models

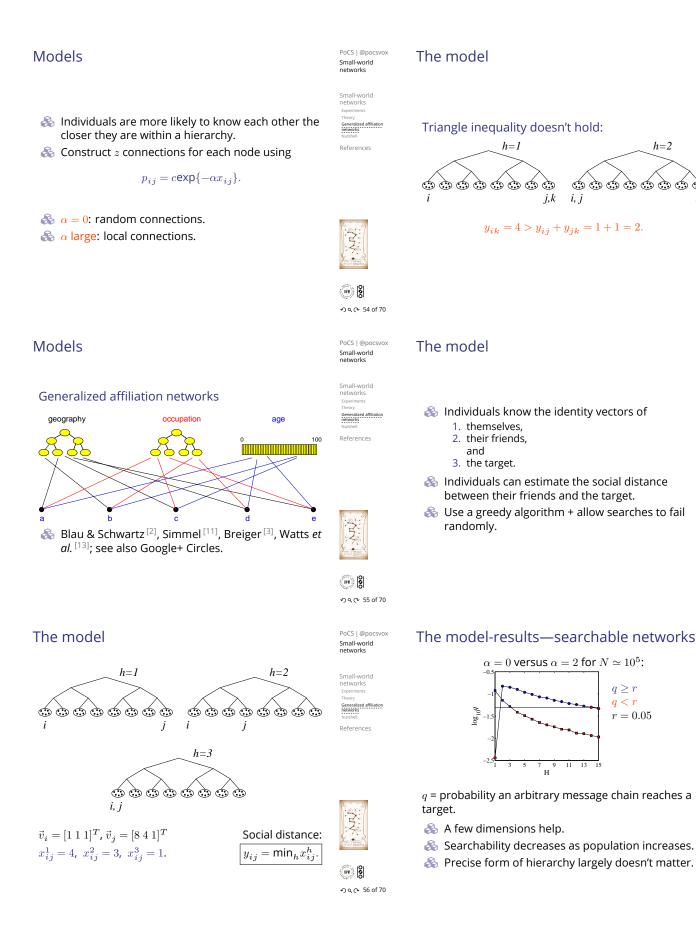
Distance between two individuals x_{ij} is the height of lowest common ancestor.



 $x_{ij} = 3$, $x_{ik} = 1$, $x_{iv} = 4$.

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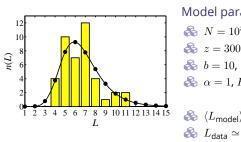
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The model-results

Milgram's Nebraska-Boston data:



del parameters:
$N = 10^{8}$,
z = 300, $g = 100$,
b = 10,
$\alpha = 1$, $H = 2$;
$\langle L_{\rm model}\rangle\simeq 6.7$
$L_{\rm data}\simeq 6.5$



Social search—Data

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Adamic and Adar (2003)

- For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.
- Probability of connection as function of real distance $\propto 1/r$.





Social Search—Real world uses

Tags create identities for objects

- 🗞 Website tagging: bitly.com 🗹
- 🗞 (e.g., Wikipedia)
- 🗞 Photo tagging: flickr.com 🗹
- A Dynamic creation of metadata plus links between information objects.
- 🗞 Folksonomy: collaborative creation of metadata





References I

[1] L. Adamic, R. Lukose, A. Puniyani, and B. Huberman. Search in power-law networks. Phys. Rev. E, 64:046135, 2001. pdf

Social Search—Real world uses

connections between books.

Nutshell for Small-World Networks:

lmproved social network models.

Construction of peer-to-peer networks.

Construction of searchable information

network is formed.

databases.

🚳 Bare networks are typically unsearchable.

Paths are findable if nodes understand how

lmportance of identity (interaction contexts).

tagging of the hoi polloi.

Conflict between 'expert judgments' and

Amazon uses people's actions to build effective

Recommender systems:

- [2] P. M. Blau and J. E. Schwartz. Crosscutting Social Circles. Academic Press, Orlando, FL, 1984.
- [3] R. L. Breiger. The duality of persons and groups. Social Forces, 53(2):181–190, 1974. pdf
- [4] S. Carmi, S. Carter, J. Sun, and D. ben Avrahim. Asymptotic behavior of the Kleinberg model. Phys. Rev. Lett., 102:238702, 2009. pdf

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