Overview of Complex Systems Principles of Complex Systems | @pocsvox CSYS/MATH 300, Fall, 2017

Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont













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References

PoCS

Outline

Orientation

Course Information **Topics** Narrative Arc Postcards from the Course **Tarot Cards Projects** Centers, Books, Resources

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References





9 9 € 4 of 63

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What's the John Dory?

Orientation

Course Information
Topics
Narrative Arc
Postcards from the Course
Tarot Cards Projects Centers, Books, Resources

References

References

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少 q (~ 1 of 63

Orientation Projects Centers, Books, Resource

References





•9 Q (№ 2 of 63







少 q (~ 5 of 63

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Orientation

References

These slides are also brought to you by:

Special Guest Executive Producer: Pratchett



On Instagram at pratchett_the_cat

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Orientation

References



Describe | Explain | Create | Share | Ethos: Play











少 q (~ 3 of 63

PoCS

vermontcomplexsystems.org



Vermont Complex Systems Center (2006-):

- Diverse research and teaching portfolio (> 400 papers in 2010-2015).
- Funding from many sources: NSF, NIH, DARPA, MITRE, Microsoft, foundations. In 2010–2015, \$70M tagged as Complex Systems.
- Regular global press coverage: NYT, BBC, NatGeo, ...
- 🗞 Conferences: "Big Data, Big Stories", "Big Scale, Big Fail", "Prediction: the Next Big Thing" and Flash Mob Research events.
- 🙈 Well developed Educational platform in Complex Systems and Data Science.
- Faculty hires of true Complex Systems scholars (+4 now).
- Numerous NSF CAREER awards (including PECASE).
- Connecting Graduate and Undergraduate Students across campus (SCRAPS) leading to real research output.

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References

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少 q (~ 7 of 63

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Orientation

References



Very happy to announce our awesome new partnership with Mass Mutual to support Complex Systems/Data Science:







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Dory?

References



•2 a 0 10 of 63

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Orientation

References

The Sequel to PoCS: "Complex Networks" (CSYS/MATH

303). Leveling up:

(STAT 287)

🙈 MS in Complex Systems and Data Science (Fall 2015) 🗹

Graduate Certificate in Complex Systems (and

Principles of Complex Systems is one of two core

requirements for UVM's five course teaching-

Other required course: Prof. Maggie Eppstein's

"Modelling Complex Systems" (CSYS/CS 302).

To be required: Prof. Jim Bagrow's "Data Science I"

learning/certificate-of-study-in-complex-systems/

Certificate of Graduate Study in Complex Systems .

Next: PhD in Complex Systems and Data Science in the Fall of 2018



Educational mission:

Data Science

Graduate

Undergrad.

Certificate in Complex

Systems. 🚓 Latest: MS in

Complex

Systems and

Data Science. Next: PhD in

> The Study of Interesting

Things.

Data Science):



Vermont Complex Systems Center—Misfit toys:



Peter Dodds, Math/Stats

Hugh

Garavan, Neu-

ro/Psychiatry

Paul Hines, EE



Josh Bongard,

Yves Dubief,

ME



Chris Danforth, Math/Stats



Maggie Eppstein, CS



Mads Almassalkhi,



lim Bagrow, Math/Stats



Brian Tivnan, MITRE



Laurent Hébert-Dufresne. CS



Puck Rombach. Math/Stats





少 Q (~ 8 of 63

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Orientation References

We're interested in many things:

Sociotechnical systems Social Contagion and Influence Happiness and Well-being Language and Stories Social unrest Conflict Robotics Artificial Intelligence

Data Science Complex Networks Climate Biology **Ecology** Geomorphology Space Complex Fluids (Smart) Power Grids Critical infrastructure

Defense Policy Health systems Food systems **Epidemiology Pandemics** Organizations Economics Wealth inequality **Financial** Systems





少 q (~ 9 of 63







•2 0 € 12 of 63



+ Brian Tivnan's MITRE team; Funding: NSF, NASA, MITRE, DARPA; [YOUR WONDERFUL **FUNDING AGENCY HERE]**

Systems (@pocsvox ☑)

(@networksvox ☑)

@svdthematrices (27) MATH 237: Numerical Analysis

(@MachEps237 **△**)

Adjacent: Strava Story Lab team

Courses:

Basics:

Instructor: Prof. Peter Dodds

& Lecture room and meeting times: 102 Perkins, Tuesday and Thursday, 11:40 am to

- Office: Farrell Hall, second floor, Trinity Campus
- & email: peter.dodds+pocs@uvm.edu
- Course Website: http://www.uvm.edu/pdodds/teaching/courses/2017-08UVM-300 2
- & Course Twitter handle: @pocsvox
- Course hashtag: #FallPoCS2017

Potential paper products:

Office hours:

pm Thursday,

1:15 pm to 2:30 pm on Tuesday, 1:15 pm to 4:45

Farrell Hall, second floor, Trinity Campus

Exciting details regarding these slides:

Three versions (all in pdf): 1. Presentation,

2. Flat Presentation,

available).



Course Information

References



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2 9 € 17 of 63

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Orientation Course Information

Projects Centers, Books, Resour References







少∢ペ 18 of 63

PoCS | @pocsvox What's the John Dory?

Orientation Course Information







ჟqॡ 19 of 63

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References

PoCS | @pocsvox

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少 q (~ 13 of 63

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Orientation Course Inform Topics Narrative Arc

Projects Centers, Books, Resour References

systems (@NonperiodicFlow ♂) MATH 330: Ordinary Differential Equations (@dallthethingsdt ☑)

🙈 MATH 266: Chaos, fractals & dynamical

CSYS/MATH 300: Principles of Complex

CSYS/MATH 303: Complex Networks

🙈 MATH 124/122: Matrixology (Linear

Algebra) (@matrixologyvox and

Courses act as research incubators and have helped generate many papers

(35+)





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Orientation

References

Some books will be linked to on Amazon.

3. Handout (3x2 slides per page). Presentation versions are hyperly navigable:

໑৭⊖≡ back + search + forward.

Brought to you by a frightening melange of X⊒MEX ☑, Beamer ☑, perl ☑, PerlTeX ☑, fevered command-line madness 2, and an almost fanatical devotion to the indomitable emacs. #evilsuperpowers

References in slides link to full citation at end. [1] & Citations contain links to pdfs for papers (if

. 1 1 **38** (8) all. 1 2 2 1 2 2 1 2 3 2 2 3 2 1 3 -÷ (6):

More super exciting details:

- We use Open Sans and make math look good: \setmainfont[Ligatures=TeX]{Open Sans} \setsansfont[Ligatures=TeX]{Open Sans} \usefonttheme[onlymath]{serif}
- Working towards putting the course on Github.

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Course Information
Topics
Narrative Arc
Postcards from the Courant Cards
Tarot Cards

References

Team PoCS

We'll continue to try out Slack:

- Place for discussions about all things PoCS including assignments and projects.
- Once invited, please sign up here: http://teampocs.slack.com
- Very good: Install Slack app on laptops, tablets, phone.

slack

Everyone will behave wonderfully.

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Course Information
Topics
Narrative Arc
Postcards from the C
Tarot Cards
Projects
Centers, Books, Resc

References





•23 of 63

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What's the John Dory?

Orientation

References

Course Information

Projects Centers, Books, Resource

Yet more super exciting details:

- This is Season 11 of Principles of Complex Systems.
- Lectures will be called Episodes.
- Other tropes will be involved.
- Last season's Episodes are here .

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w 8 少 q (~ 20 of 63

Orientation Course Information

References



少 q (~ 21 of 63

Orientation

References

Course Information

Grading breakdown:

- Projects/talks (36%)—Students will work on semester-long projects. Students will develop a proposal in the first few weeks of the course which will be discussed with the instructor for approval. Details: 12% for the first talk, 12% for the final talk, and 12% for the written project.
- Assignments (60%)—All assignments will be of equal weight and there will be 10 \pm 1 of them.
- General attendance/Class participation (4%)





•> q (~ 24 of 63

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What's the John Dory?

Orientation

References

Course Information

Wonderful foundational support for PoCS and CoNKS has come from the NSF:

- A "CAREER: Explorations of Complex Social and Psychological Phenomena through Multiscale Online Sociological Experiments, Empirical Studies, and Theoretical Models." 2009-2015.
- SES Division of Social and Economic Sciences SBE Directorate for Social, Behavioral & Economic Sciences
- Abstract is here .
- People have said nice things about PoCS

PoCS | @pocsvox How grading works: What's the John Dory?

Questions are worth 3 points according to the following scale:

- 3 = correct or very nearly so.
- 2 = acceptable but needs some revisions.
- 1 = needs major revisions.
- 3 0 = way off.





•9 q (~ 22 of 63





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Important things:

- 1. Classes run from Tuesday, August 29 to Friday, December 8.
- 2. Add/Drop, Audit, Pass/No Pass deadline—Monday, September 11.
- 3. Last day to withdraw—Monday, October 30 (Sadness!).
- 4. Reading and Exam period—Saturday, December 9 to Friday, December 15.

Do check the course Twitter account, @pocsvox, for updates regarding the course (part of the course site).

Academic assistance: Anyone who requires assistance in any way (as per the ACCESS program or due to athletic endeavors), please see or contact me as soon as possible.

The nature of PoCS:

Transitional from standard coursework to research-focused work. #alittlescary

Major themes:

- The Complexity Manifesto ☑;
- Complex Systems = Modern, Normal Science;
- Roles and limits of Data, Theory, and Experiment;
- Emergence;
- Universality and Accidents of History;
- Structure and Stories: Micro-to-macro Mechanisms;
- Elements: Scaling, Surprise, Networks, Robustness, Failure, and Spreading.
- The Theory of Anything: Why Complexify?
- It's all about stories.

Cryptolect:

Course mascot:



- What's the Story?
- What's the John Dory?
- What's the John Dory for Rhyming Slang ??
- \clubsuit Hemiteleia: beers \Rightarrow Edward Lears \Rightarrow Edwards.

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Course Information
Topics
Narrative Arc
Postcards from the
Tarot Cards

References





少 q (~ 26 of 63

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Orientation Topics

References





•> q (~ 28 of 63

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Orientation Topics

References





•9 q (~ 29 of 63

Topics:

Scaling phenomena:

- Allometry
- Scaling of social phenomena: crime, creativity, and consumption.
- Power law size distributions and non-Gaussian statistics
- Zipf's law

Topics:

Complex networks:

Structure and Dynamics

Statistical Mechanics A Phase transitions

Random Networks

Scale-free Networks

Multilayer networks

Small-world Networks

- & Key mechanisms for generating power law size distributions
- Scaling in biology (elephants and platypuses).
- & Law and Order—Theoricide Unit.
- Dimensional Analysis and Renormalization.

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Topics Narratio

References





•2 0 0 of 63

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Orientation

Topics Centers, Books, Res

References

Much more in Complex Networks next semester

Multiscale complex systems:

Integrity of complex systems:

Generic failure mechanisms

Network robustness

and fragility

Predictablity

- Hierarchies and Scaling
- Modularity

Topics:





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Orientation

Topics

References

Information and Language:

- Search in networked systems (e.g., the web, social systems)
- Search on scale-free networks
- Knowledge trees, metadata and tagging
- Evolution and structure of natural languages

A Highly Optimized Tolerance (HOT): Robustness





•9 q (~ 32 of 63

Topics:

Sociotechnical Systems:

- Biological and social spreading models
- & Schelling's model of segregation [13]
- S Granovetter's model of imitation [8]
- Collective behavior and Synchrony
- Global cooperation from bad actors
- Global conflicts from good actors
- Stories (Homo Narrativus)
- The Sociotechnocene

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Orientation
Course Information
Topics
Narrative Arc
Postcards from the Cours
Tarot Cards
Projects

References





◆) < (~ 33 of 63

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What's the John Dory?

Orientation

Topics

References

Schedule in detail:

Week # (dates)	Tuesday	Thursday
1 (8/29 and 8/31)	Overview; Fundamentals: The Complexity Manifesto	Scaling
2 (9/05 and 9/07)	Power-law size distributions	Zipf's law; Fundamentals: Data, Emer- gence, Limits to Understanding
3 (9/12 and 9/14)	Projects; Power-law mechanisms: Ran- domness	Power-law mechanisms: Variable Transformation
4 (9/19 and 9/21)	Power-law mechanisms: The Rich-Get-Richer	Power-law mechanisms: Optimization
5 (9/26 and 9/28)	Robustness and Fragility	Fundamentals: Statistical Mechanics Language evolution
6 (10/03 and 10/05)	Robustness vs. SOC	Complex networks: Introduction Basics and Examples networks Small-world networks
7 (10/10 and 10/12)	Complex networks: Key Properties Generalized random	Complex networks: Small-world networks
8 (10/17 and 10/19)	Complex networks: Scale-free networks	Project presentations†
9 (10/24 and 10/26)	Project presentations†	Complex networks: Scale-free networks
10 (10/31 and 11/02)	Complex networks: Scale-free networks	Contagion: Introduction
11 (11/07 and 11/09)	Contagion	Biological Contagion
12 (11/14 and 11/16)	Social Contagion	Social Contagion
13 (11/21 and 11/23)	Thanksgiving	Thanksgiving
14 (11/28 and 11/30)	Voting and Success	(Away: Quarterology)
15 (12/05 and 12/07)	Stories	The Big Story

†: 3-4 minutes each + 1 or 2 questions;

Topics:

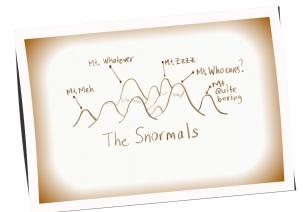
Large-scale social patterns:

- Movement of individuals
- Cities
- A Happiness
- Twitter

Collective decision making:

- Wisdom and madness of crowds
- Systems of voting
- The role of randomness and chance
- Success inequality: superstardom

Postcards from the Course:



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Orientation
Course Information

Narrative Arc Postcards from the Course Tarot Cards

Centers, Books, Resource

References





少 q (~ 40 of 63

Season's Narrative Arc (or Places We Will Go):

- Overview of Complex Systems with bonus Manifesto ☑.
- Thread of Understanding Sociotechnical Systems.
- Allometric scaling in complex systems.
- Size distributions of system elements:
 - Power-law size distributions.
 - Description and Mechanisms of Becoming.
- Robustness of Complex Systems.
- Complex networks—how system elements are connected:
 - Structure, Growth Mechanisms, Processes on Networks.
 - Social Contagion, Voting, Fame and Fate, Stories.
- Complexification: The Theory of Anything and the Rise of Algorithms

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Orientation
Course Information
Topics
Narrative Arc
Postcards from the Cours
Tarot Cards

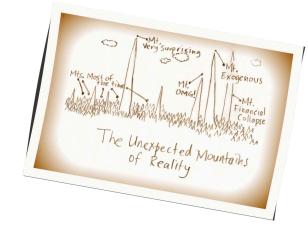
References





少 q (~ 37 of 63

Postcards from the Course:



PoCS | @pocsvox What's the John Dory?

Orientation

Topics
Narrative Arc
Postcards from the Course
Tarot Carrie

Tarot Cards Projects Centers, Books, Resourc

References





少 Q (~ 41 of 63

Postcards from the Course:



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Orientation
Course Information
Topics
Narrative Arc
Postcards from the Course

Tarot Cards
Projects
Centers, Books, Resources
References

Popular Science Books:

Historical artifact:



"Complexity: The Emerging Science at the Edge of Order and Chaos" (3 🗷 by M. Mitchell Waldrop (1993). [16]

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Orientation

Postcards from the Cours Tarot Cards Projects

Centers, Books, Resources

References



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Orientation

Projects

References

Shout-out: Dr. Andrew P. Morokoff , MBBS PhD FRACS D. Thau (Bug)





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少∢で 50 of 63

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Orientation

References

Postcards from the Cour Tarot Cards

Centers, Books, Resources

Projects

- Semester-long projects, teams.
- Develop proposal in first few weeks.
- May range from novel research to investigation of an established area of complex systems.
- Two talks + written piece.
- Substitute Substit
- Massive data sets available, including Twitter.
- Possible: Work with Twitter data and Story Lab on socially meaningful problems.
- Academic output (journal papers) resulting from Principles of Complex Systems and Complex Networks can be found here . Add more!
- We'll go through a list of possible projects soon.

Popular Science Books:



"Simply Complexity: A Clear Guide to Complexity Theory" **3** 7 by Neil F. Johnson (2009). [9]





"The Information: A History, A Theory, A Flood" (2) (2) by James Gleick (2011). [6]





◆9 **Q** ← 51 of 63

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Orientation

References

Centers, Books, Resources

The narrative hierarchy—Stories and Storytelling on all Scales:



- 1 to 3 word encapsulation = a soundbite = a buzzframe,
- <page-header> 1 sentence, title,
- 🚷 few sentences, a haiku,
- 🙈 a paragraph, abstract,
- 🚓 short paper, essay,
- 🙈 long paper,
- 🚓 chapter,
- ቆ book,
- ♣ ...

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少 q (~ 47 of 63

Orientation
Course Information
Topics
Narrative Arc
Postcards from the Course
Tarot Cards
Projects
Centers, Books, Resources

References

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"Human Behaviour and the Principle of Least-Effort" **a**. (27) by G. K. Zipf (1949). [17]

On complex sociotechnical systems:



"Micromotives and Macrobehavior" **3**. by Thomas C. Schelling (1978). [14]



"Critical Mass: How One Thing Leads to Another" (3.07) by Philip Ball (2004). [2]





少 q (~ 52 of 63





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It's all about algorithms (stories):

"The Engine of Complexity: Evolution as Computation" 3. 2

by John E. Mayfield (2013). [10]



"On the Origin of Stories: Evolution, Cognition, and Fiction" **3**, 🖸 by Brian Boyd (2010). [5]



"The Storytelling Animal: How Stories Make Us Human" 3, 12

by Jonathan Gottschall (2013). [7]

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Relevant online courses:

Melanie Mitchell (Santa Fe Institute): Introduction to Complexity 🗗

& Lada Adamic (Facebook): Social Network Analysis

Principles of Complex Systems and Complex Networks 🗹

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Centers, Books, Resources

References





2 9 0 € 56 of 63

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Orientation

References

Postcards from the Course Tarot Cards

Centers, Books, Resources

A few textbooky books:



"Complex Adaptive Systems: An introduction to computational models of social life" a, 🖸

by John H. Miller and Scott E. Page and John H. Miller and Scott E. Page (2007). [11]



"Critical Phenomena in Natural Sciences" 3, 🗷 by Didier Sornette (2003). [15]



"Modeling Complex Systems" 🚨 🗹 by Nino Boccara (2004). [4]

Eventually: "Principles of Complex Systems"

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•9 q (> 53 of 63

w 8

Orientation Postcards from the Course Tarot Cards

Centers, Books, Resources References





少 q (~ 54 of 63

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Centers, Books, Resources

References

Orientation

Centers:

- Santa Fe Institute (SFI)
- New England Complex Systems Institute (NECSI)
- Michigan's Center for the Study of Complex Systems (CSCS ☑)
- Northwestern Institute on Complex Systems (NICO ☑)
- Also: Indiana, Davis, Brandeis, University of Illinois, Duke, Warsaw, Melbourne, ...,
- Vermont Complex Systems Center







•> q (~ 57 of 63

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Orientation

Centers, Books, Resources

References



Complexity Digest: http://www.comdig.org ☑ https://twitter.com/@cxdig ☑

Other inputs:

Nautilus Magazine:

Aeon: http://aeon.co/

Books on scaling:



"Scaling, self-similarity, and intermediate asymptotics" **3** 🖸

by G. I. Barenblatt (1996). [3]



少 q (~ 55 of 63





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References I

[1] P. W. Anderson. More is different. <u>Science</u>, 177(4047):393–396, 1972. pdf

[2] P. Ball.

Critical Mass: How One Thing Leads to Another. Farra, Straus, and Giroux, New York, 2004.

[3] G. I. Barenblatt.

Scaling, self-similarity, and intermediate asymptotics, volume 14 of Cambridge Texts in Applied Mathematics.

Cambridge University Press, 1996.

[4] N. Boccara.

Modeling Complex Systems.

Springer-Verlag, New York, 2nd edition, 2004.

References II

[5] B. Boyd.

 On the Origin of Stories: Evolution, Cognition, and Fiction.
 Belknap Press, 2010.

[6] J. Gleick.

The Information: A History, A Theory, A Flood. Pantheon, 2011.

[7] J. Gottschall.

The Storytelling Animal: How Stories Make Us Human.

Mariner Books, 2013.

[8] M. Granovetter.

Threshold models of collective behavior. Am. J. Sociol., 83(6):1420–1443, 1978. pdf 🗗

References III

[9] N. F. Johnson.
Simply Complexity: A Clear Guide to Complexity
Theory.
Oneworld Publications, London, UK, 2009. pdf

[10] J. E. Mayfield.

The Engine of Complexity: Evolution as Computation.

Columbia University Press, New York, 2013.

[11] J. H. Miller and S. E. Page.

Complex Adaptive Systems: An introduction to computational models of social life.

Princeton University Press, Princeton, NJ, 2007.

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Orientation Course Information Topics Narrative Arc

Centers, Books, N

References





少 Q (~ 59 of 63

PoCS | @pocsvox What's the John Dory?

Orientation
Course Information
Topics
Narrative Arc
Postcards from the Course
Tarot Cards
Projects
Centers, Books, Resources

References



少 q (~ 60 of 63

PoCS | @pocsvox What's the John Dory?

Orientation
Course Information
Topics
Narrative Arc
Postcards from the Course
Tarot Cards
Projects

References





少 q (~ 61 of 63

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[12] M. Mitchell.

Complexity: A Guided Tour.

Oxford University Press, New York, NY, 2009. pdf ☑

[13] T. C. Schelling.

[14] T. C. Schelling.

Micromotives and Macrobehavior. Norton, New York, 1978.

[15] D. Sornette.

References V

[16] M. M. Waldrop.

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Critical Phenomena in Natural Sciences.
Springer-Verlag, Berlin, 2nd edition, 2003.



References

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少 q (~ 62 of 63

PoCS | @pocsvox What's the John Dory?

Orientation
Course Information
Topics
Narrative Arc
Postcards from the Course
Tarot Cards
Projects
Centers, Books, Resources

References

Simon & Schuster, New York, NY, 1993. [17] G. K. Zipf.

<u>Human Behaviour and the Principle of</u> <u>Least-Effort.</u>

Complexity: The Emerging Science at the Edge of

Addison-Wesley, Cambridge, MA, 1949.





୬९℃ 63 of 63