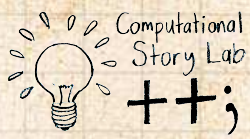
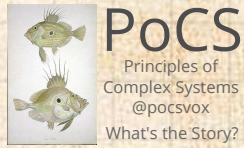
Fundamentals

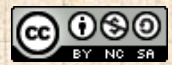
Principles of Complex Systems | @pocsvox
CSYS/MATH 300, Fall, 2017

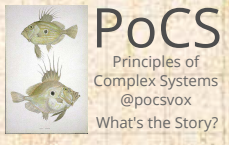
Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center
Vermont Advanced Computing Core | University of Vermont









These slides are brought to you by:

PoCS
Principles of Complex Systems
@pocsvox
What's the Story?

These slides are also brought to you by:

Special Guest Executive Producer: Pratchett

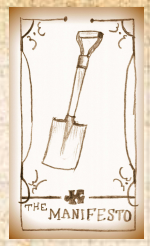
On Instagram at pratchett_the_cat

Outline

PoCS
Principles of Complex Systems
@pocsvox
What's the Story?


THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

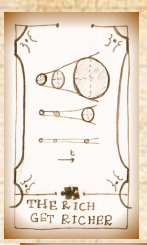

THE MANIFESTO

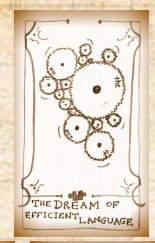

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST

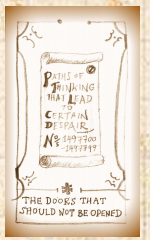

THE MANY TALES OF MANY TAILS


THE DATA POOR


THE POURING DATA


THE CHARMS OF THE MANY WRONG PATHS


THE KNOWLEDGE OF DEAD MONKS

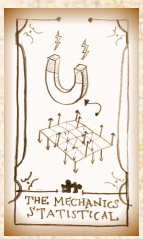

PATHS OF THINKING THAT LEAD TO CERTAIN DESPAIR
THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION


THE NETWORKS COMPLEX

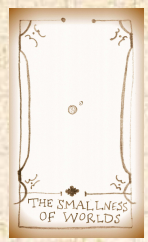

THE ELEMENTS OF WEBS


"I am the Monarch of the Sea."
THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS

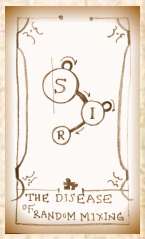

THE SMALLNESS OF WORLDS

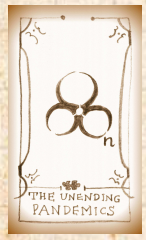

THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED PHOENIX BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

?
THE UNKNOWN MECHANISM

THE JOHN DORY

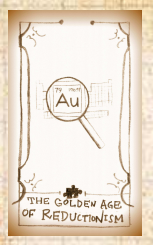
THE STORYTELLERS

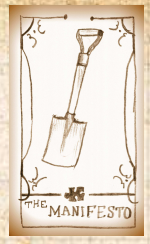
THE ADJACENT NARRATIVES

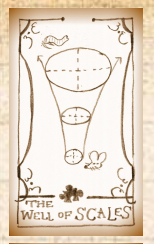
7
THE END

THE MEASURING


THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

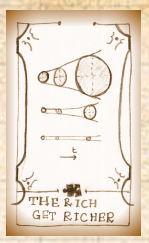

THE MANIFESTO

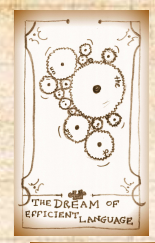

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING BORNE YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST

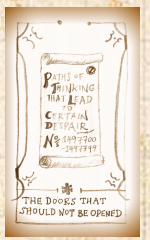

THE MANY TALES OF MANY TAILS


THE MEASURING


THE POURING DATA


THE CHARMS OF THE MANY WRONG PATHS


THE KNOWLEDGE OF DEAD MONKS


PATHS OF THINKING THAT LEAD TO CERTAIN DESPAIR
THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION

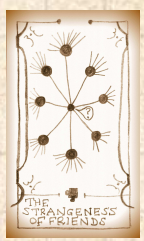

THE NETWORKS COMPLEX

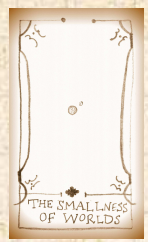

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

?
THE UNKNOWN MECHANISM

THE JOHN DORY

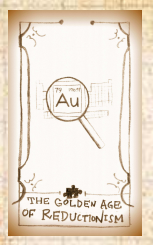
THE STORYTELLERS

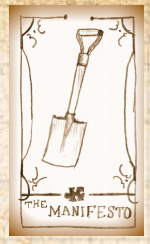
THE ADJACENT NARRATIVES

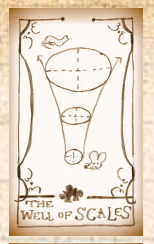
7
THE END

THE DATA POOR


THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

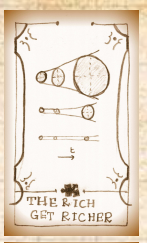

THE MANIFESTO

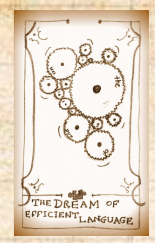

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST

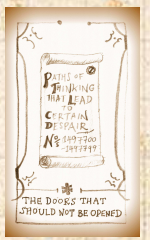

THE MANY TALES OF MANY TAILS


THE MEASURING


THE DATA POOR


THE CHARMS OF THE MANY WRONG PATHS


THE KNOWLEDGE OF DEAD MONKS

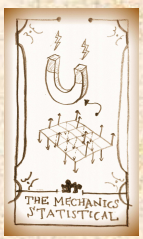

PATHS OF THINKING THAT LEAD TO CERTAIN DESPAIR
THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION


THE NETWORKS COMPLEX

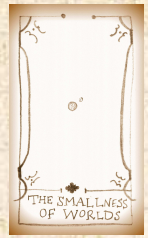

THE ELEMENTS OF WEBS


"I am the Monarch of the Sea."
THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS

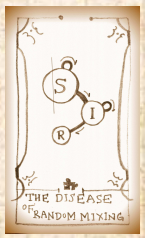

THE SMALLNESS OF WORLDS

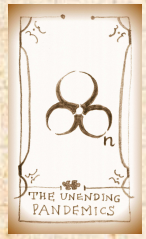

THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

?
THE UNKNOWN MECHANISM

THE JOHN DORY

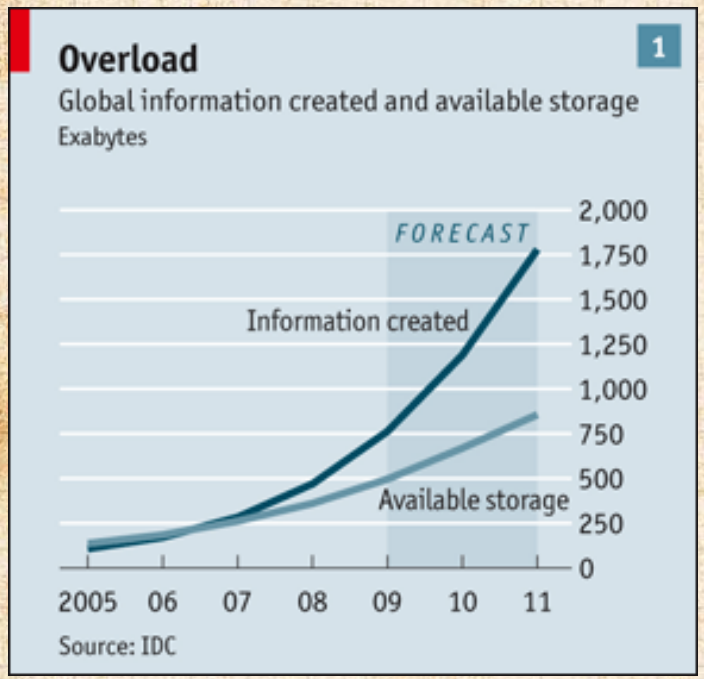
THE STORYTELLERS

THE ADJACENT NARRATIVES

7
THE END

THE POURING DATA

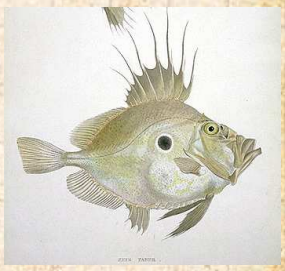
Data, Data, Everywhere—the Economist, Feb 25, 2010



- Exponential growth: $\sim$ 60% per year.

Big Data Science:

- 2013: year traffic on Internet estimate to reach 2/3 Zettabytes (1ZB = 10^3EB = 10^6PB = 10^9TB)
- Large Hadron Collider: 40 TB/second.
- 2016—Large Synoptic Survey Telescope: 140 TB every 5 days.
- Facebook: $\sim$ 250 billion photos (mid 2013)
- Twitter: $\sim$ 500 billion tweets (mid 2013)



No really, that's a lot of data

Data inflation

2

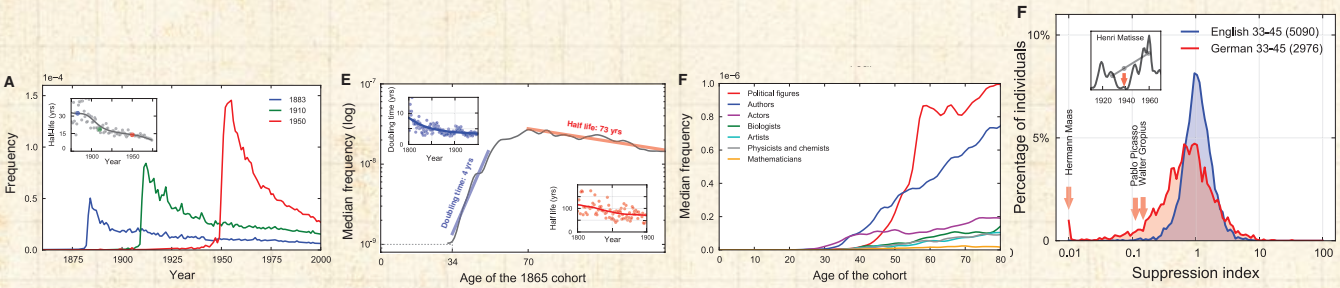
Unit	Size	What it means
Bit (b)	1 or 0	Short for "binary digit", after the binary code (1 or 0) computers use to store and process data
Byte (B)	8 bits	Enough information to create an English letter or number in computer code. It is the basic unit of computing
Kilobyte (KB)	1,000, or 2^{10}, bytes	From "thousand" in Greek. One page of typed text is 2KB
Megabyte (MB)	1,000KB; 2^{20} bytes	From "large" in Greek. The complete works of Shakespeare total 5MB. A typical pop song is about 4MB
Gigabyte (GB)	1,000MB; 2^{30} bytes	From "giant" in Greek. A two-hour film can be compressed into 1-2GB
Terabyte (TB)	1,000GB; 2^{40} bytes	From "monster" in Greek. All the catalogued books in America's Library of Congress total 15TB
Petabyte (PB)	1,000TB; 2^{50} bytes	All letters delivered by America's postal service this year will amount to around 5PB. Google processes around 1PB every hour
Exabyte (EB)	1,000PB; 2^{60} bytes	Equivalent to 10 billion copies of *The Economist*
Zettabyte (ZB)	1,000EB; 2^{70} bytes	The total amount of information in existence this year is forecast to be around 1.2ZB
Yottabyte (YB)	1,000ZB; 2^{80} bytes	Currently too big to imagine

The prefixes are set by an intergovernmental group, the International Bureau of Weights and Measures. Yotta and Zetta were added in 1991; terms for larger amounts have yet to be established.

Source: *The Economist*

Big Data—Culturomics:

"Quantitative analysis of culture using millions of digitized books" by Michel et al., Science, 2011 [6]

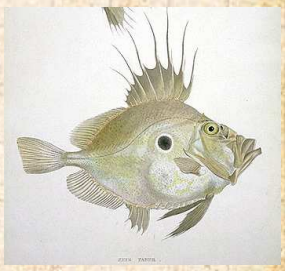


http://www.culturomics.org/ and Google Books ngram viewer

Barney Rubble:

"Characterizing the Google Books corpus: Strong limits to inferences of socio-cultural and linguistic evolution"

Pechenick, Danforth, and Dodds, PLoS ONE, **10**, e0137041, 2015. [7]



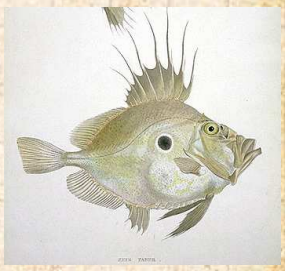
Basic Science ≃ Describe + Explain:

Lord Kelvin (possibly):

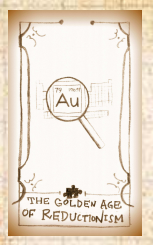
- “To measure is to know.”
- “If you cannot measure it, you cannot improve it.”

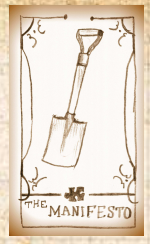
Bonus:

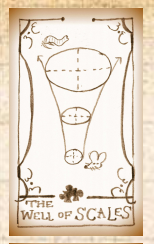
- “X-rays will prove to be a hoax.”
- “There is nothing new to be discovered in physics now, All that remains is more and more precise measurement.”




THE SUN


THE GOLDEN AGE OF REDUCTIONISM

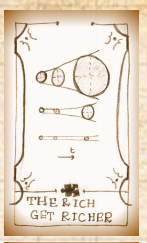

THE MANIFESTO

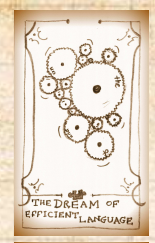

THE WELL OF SCALES


THE LAWS OF DECAYING POWER

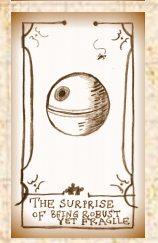

MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS


THE MEASURING


THE DATA POOR


THE POURING DATA

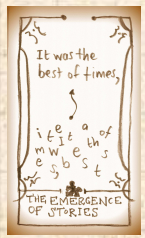

THE KNOWLEDGE OF DEAD MONKS

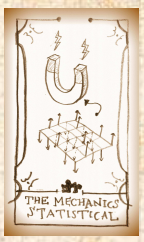

THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION

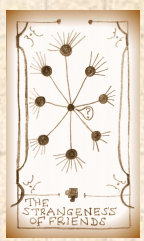

THE NETWORKS COMPLEX

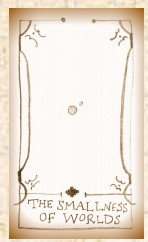

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

THE UNKNOWN MECHANISM

THE JOHN DORY

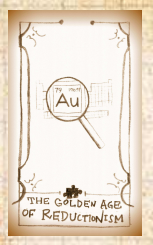
THE STORYTELLERS

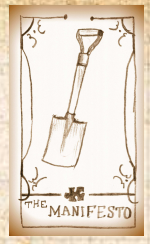
THE ADJACENT NARRATIVES

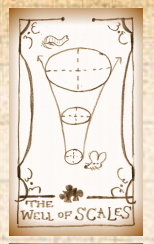
THE END

THE CHARMS OF THE MANY WRONG PATHS


THE SUN


THE GOLDEN AGE OF REDUCTIONISM

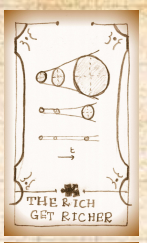

THE MANIFESTO

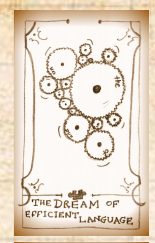

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET ERASABLE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS


THE MEASURING


THE DATA POOR


THE POURING DATA

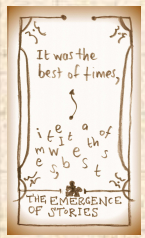

THE CHARMS OF THE MANY WRONG PATHS

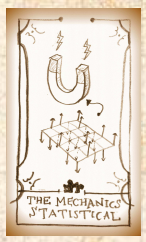

THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION

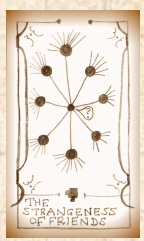

THE NETWORKS COMPLEX

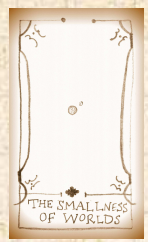

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

THE UNKNOWN MECHANISM

THE JOHN DORY

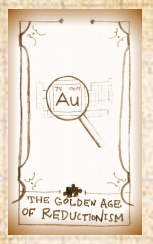
THE STORYTELLERS

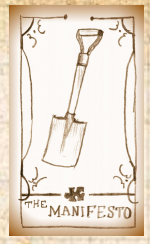
THE ADJACENT NARRATIVES

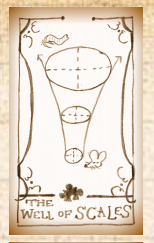
THE END

Gravity Books
Making Money
Alchemy
THE KNOWLEDGE OF DEAD MONKS


THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

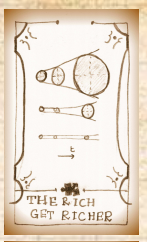

THE MANIFESTO

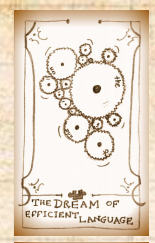

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS


THE MEASURING


THE DATA POOR


THE POURING DATA

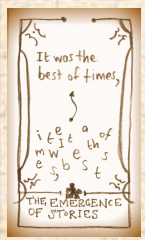

THE CHARMS OF THE MANY WRONG PATHS

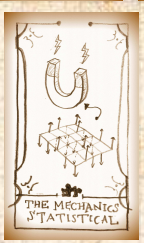

THE KNOWLEDGE OF DEAD MONKS


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION

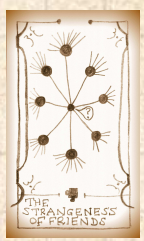

THE NETWORKS COMPLEX

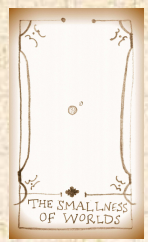

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

?
THE UNKNOWN MECHANISM

THE JOHN DORY

THE STORYTELLERS

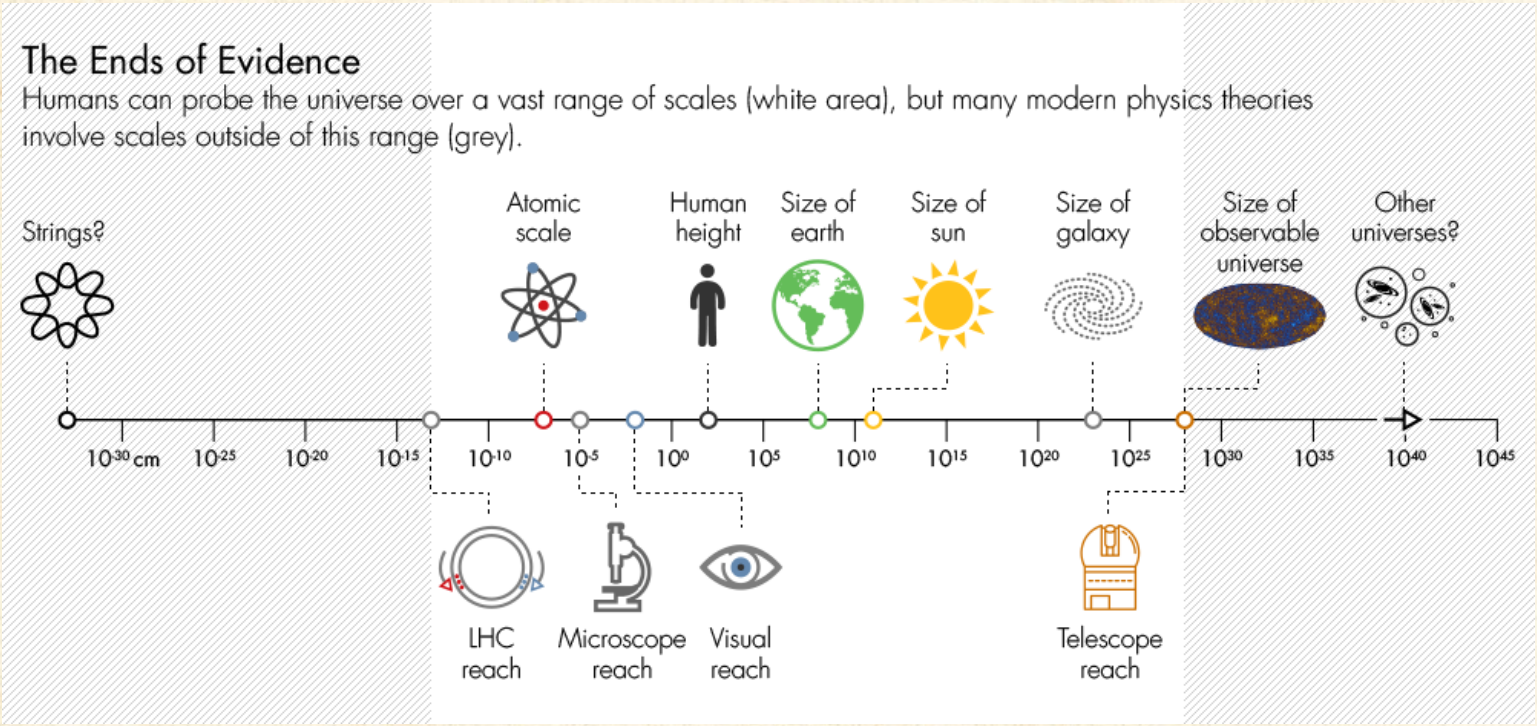
THE ADJACENT NARRATIVES

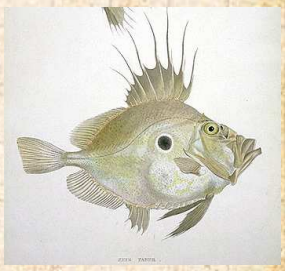
7
THE END

PATHS OF THINKING THAT LEAD TO CERTAIN DESPAIR
Nos 1497700 - 1497799
THE DOORS THAT SHOULD NOT BE OPENED

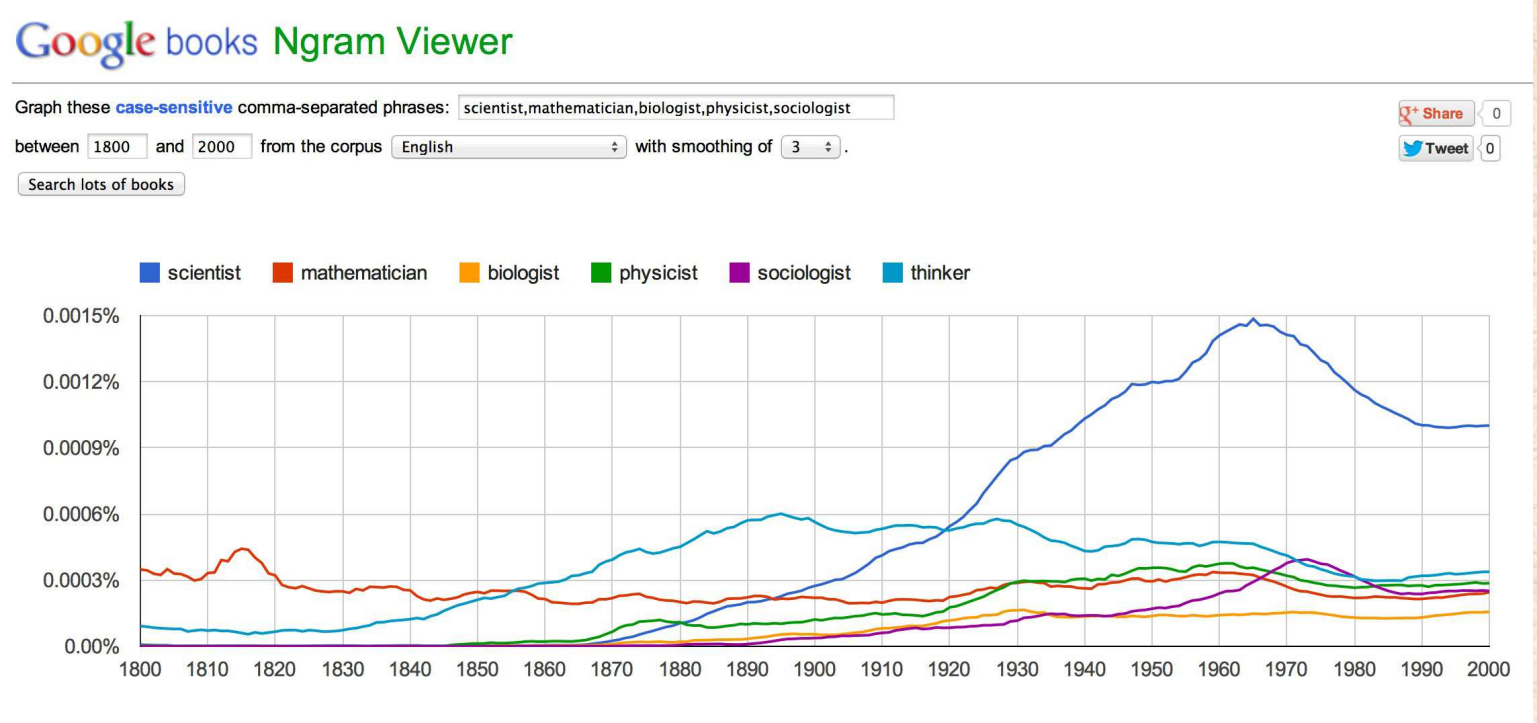
Limits of testability and happiness in Science:

From A Fight for the soul of Science in Quanta Magazine (2016/02):

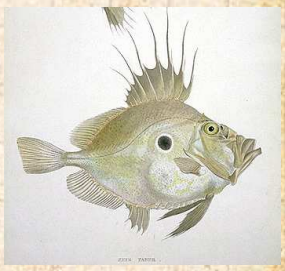




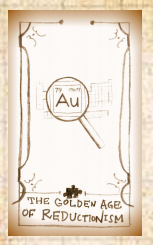
The Newness of being a Scientist (1833 on):

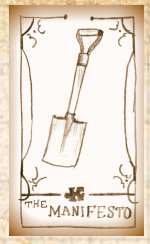


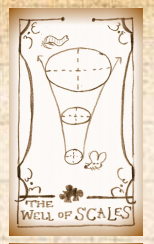
- Etymology here.
- "Scientists are the people who ask a question about a phenomenon and proceed to systematically go about answering the question themselves. They are by nature curious, creative and well organized."




THE SUN


THE GOLDEN AGE OF REDUCTIONISM

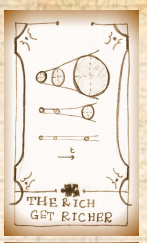

THE MANIFESTO

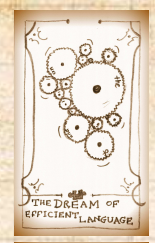

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS

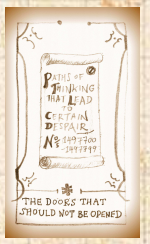

THE MEASURING


THE DATA POOR


THE POURING DATA

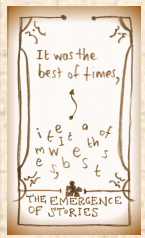

THE CHARMS OF THE MANY WRONG PATHS

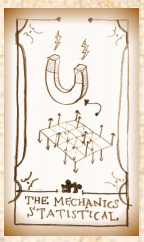

THE KNOWLEDGE OF DEAD MONKS


THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION


THE NETWORKS COMPLEX

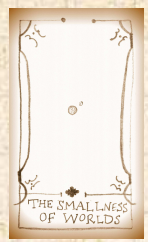

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

THE UNKNOWN MECHANISM

THE JOHN DORY

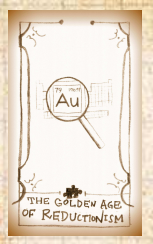
THE STORYTELLERS

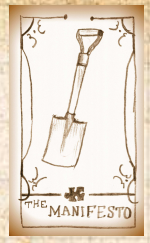
THE ADJACENT NARRATIVES

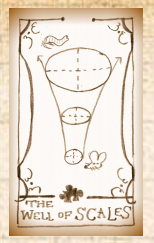
THE END

THE EMERGENCE OF STRUCTURE


THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

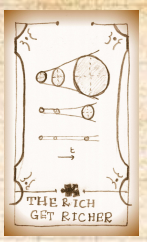

THE MANIFESTO

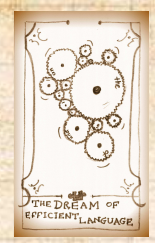

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS

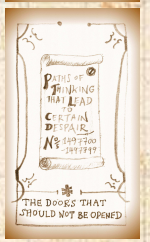

THE MEASURING


THE DATA POOR


THE POURING DATA


THE CHARMS OF THE MANY WRONG PATHS

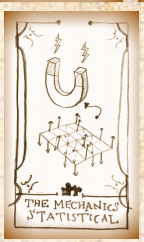

THE KNOWLEDGE OF DEAD MONKS


THE BOOKS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION


THE NETWORKS COMPLEX

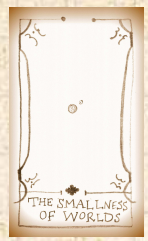

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED PHOENIX BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUBLES OF BIFURCATING REALITIES

?
THE UNKNOWN MECHANISM

THE JOHN DORY

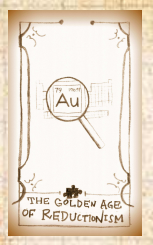
THE STORYTELLERS

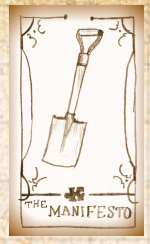
THE ADJACENT NARRATIVES

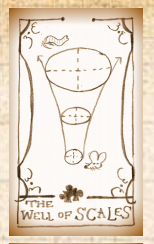
THE END

H
H
O2
THE EMERGENCE OF DESTRUCTION


THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

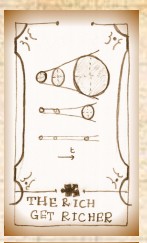

THE MANIFESTO

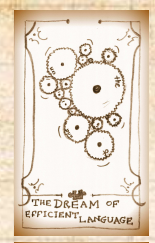

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS

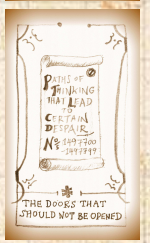

THE MEASURING


THE DATA POOR


THE POURING DATA

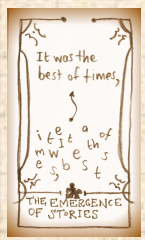

THE CHARMS OF THE MANY WRONG PATHS

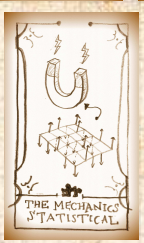

THE KNOWLEDGE OF DEAD MONKS


THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION

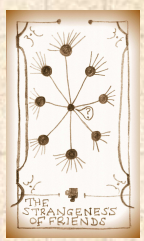

THE NETWORKS COMPLEX

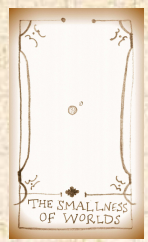

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

?
THE UNKNOWN MECHANISM

THE JOHN DORY

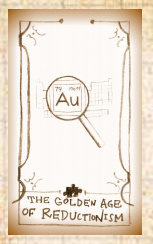
THE STORYTELLERS

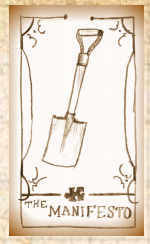
THE ADJACENT NARRATIVES

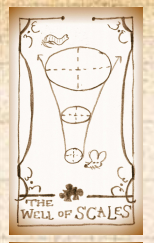
7
THE END

THE EMERGENCE OF THINKING


THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

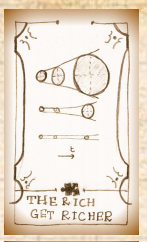

THE MANIFESTO

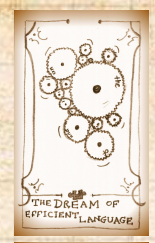

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS

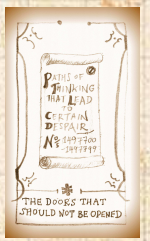

THE MEASURING


THE DATA POOR


THE POURING DATA


THE CHARMS OF THE MANY WRONG PATHS

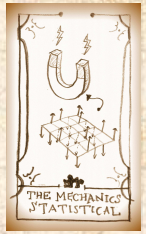

THE KNOWLEDGE OF DEAD MONKS

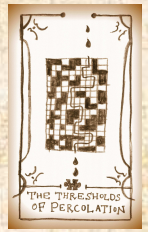

PATHS OF THINKING THAT LEAD TO CERTAIN DESPAIR
THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION


THE NETWORKS COMPLEX

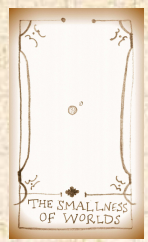

THE ELEMENTS OF WEBS


THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

?
THE UNKNOWN MECHANISM

THE JOHN DORY

THE STORYTELLERS

THE ADJACENT NARRATIVES

7
THE END

It was the best of times,
THE EMERGENCE OF STORIES

Emergence:

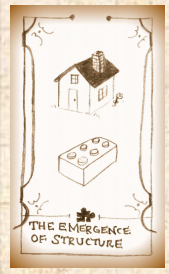
The Wikipedia on Emergence (2006):

"In philosophy, systems theory and the sciences, emergence refers to the way complex systems and patterns arise out of a multiplicity of relatively simple interactions. ... emergence is central to the physics of complex systems and yet very controversial."

Wikipedia, 2016:

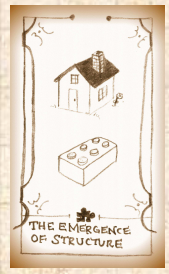
In philosophy, systems theory, science, and art, emergence is a process whereby larger entities arise through interactions among smaller or simpler entities such that the larger entities exhibit properties the smaller/simpler entities do not exhibit.

The philosopher G. H. Lewes first used the word explicity in 1875.



Fireflies ⇒ Synchronized Flashes:

Film: Sir David Attenborough, BBC.
Voiceover: Steve Strogatz on Radiolab's Emergence, S1E3.

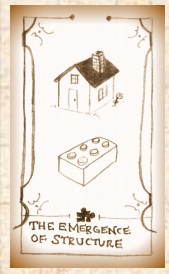


Emergence:

Tornadoes, financial collapses, human emotion aren't found in water molecules, dollar bills, or carbon atoms.

Examples:

- Fundamental particles ⇒ Life, the Universe, and Everything
- Genes ⇒ Organisms
- Neurons etc. ⇒ Brain ⇒ Thoughts
- People ⇒ Religion, Collective behaviour
- People ⇒ The Web
- People ⇒ Language, and rules of language
- ? ⇒ time; ? ⇒ gravity; ? ⇒ reality.

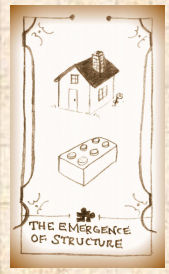


"The whole is more than the sum of its parts" –Aristotle

Emergence:

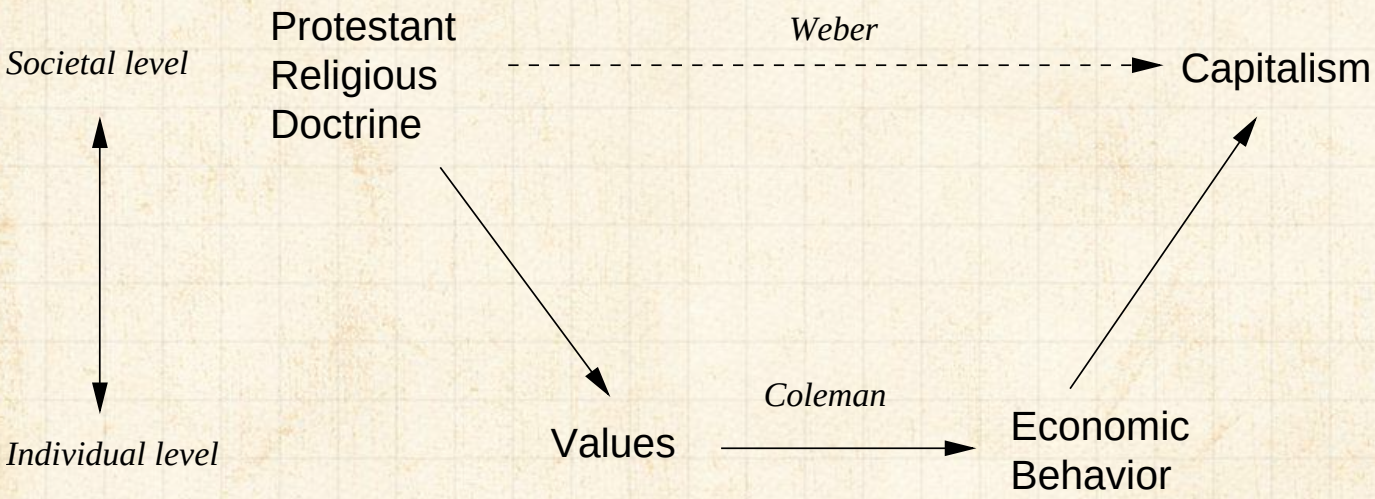
Friedrich Hayek (Economist/Philospher/Nobelist):

- Markets, legal systems, political systems are emergent and not designed.
- 'Taxis' = made order (by God, Sovereign, Government, ...)
- 'Cosmos' = grown order
- Archetypal limits of hierarchical and decentralized structures.
- Hierarchies arise once problems are solved. [4]
- Decentralized structures help solve problems.
- Dewey Decimal System versus tagging.

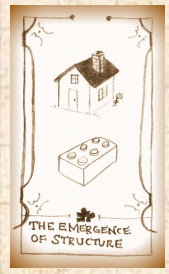


Emergence:

James Coleman in *Foundations of Social Theory*:



- Understand macrophenomena arises from microbehavior which in turn depends on macrophenomena. [3]
- More on Coleman here.

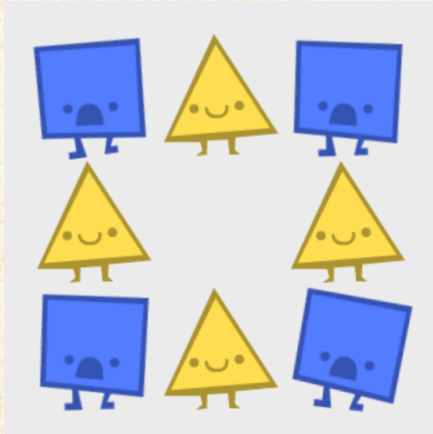


Emergence:

Thomas Schelling (Economist/Nobelist):

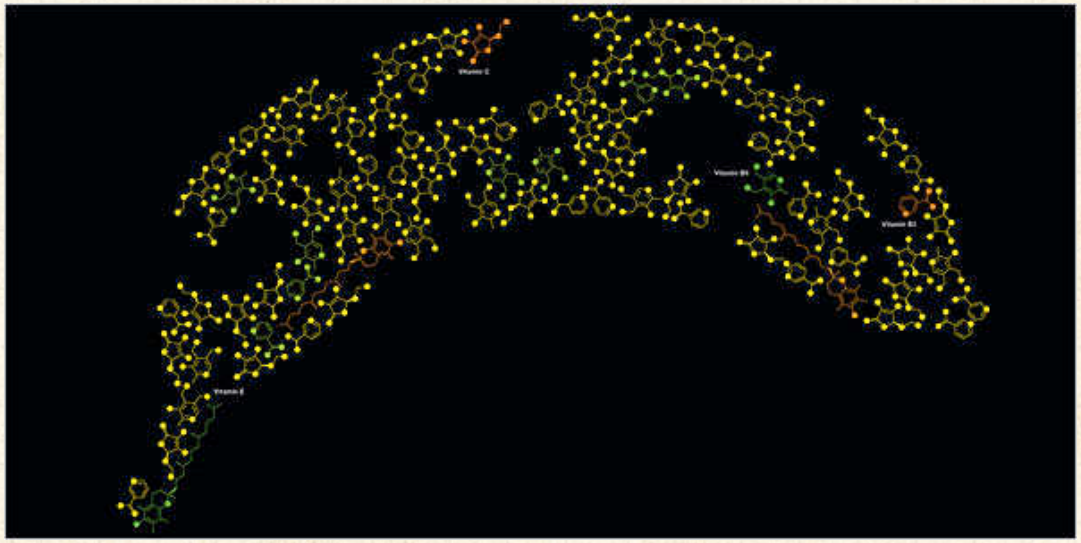
- "Micromotives and Macrobehavior" [10]
  - Segregation [8, 11]
  - Wearing hockey helmets [9]
  - Seating choices

Vi Hart and Nicky Case's Polygon-themed visualization:



The emergence of taste:

- Molecules ⇒ Ingredients ⇒ Taste
- See Michael Pollan's article on nutritionism in the New York Times, January 28, 2007.

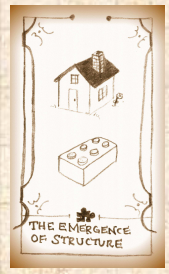


nytimes.com

Reductionism

Reductionism and food:

- Pollan: “even the simplest food is a hopelessly complex thing to study, a virtual wilderness of chemical compounds, many of which exist in complex and dynamic relation to one another…”
- “So … break the thing down into its component parts and study those one by one, even if that means ignoring complex interactions and contexts, as well as the fact that the whole may be more than, or just different from, the sum of its parts. This is what we mean by reductionist science.”



Reductionism

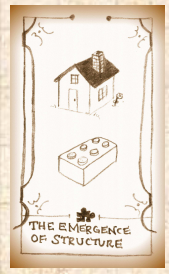
- “people don’t eat nutrients, they eat foods, and foods can behave very differently than the nutrients they contain.”
- Studies suggest diets high in fruits and vegetables help prevent cancer.
- So… find the nutrients responsible and eat more of them
- But “in the case of beta carotene ingested as a supplement, scientists have discovered that it actually increases the risk of certain cancers. Oops.”

Reductionism

Thyme's known antioxidants:

4-Terpineol, alanine, anethole, apigenin, ascorbic acid, beta carotene, caffeic acid, camphene, carvacrol, chlorogenic acid, chrysoeriol, eriodictyol, eugenol, ferulic acid, gallic acid, gamma-terpinene isochlorogenic acid, isoeugenol, isothymonin, kaempferol, labiatic acid, lauric acid, linalyl acetate, luteolin, methionine, myrcene, myristic acid, naringenin, oleanolic acid, p-coumoric acid, p-hydroxy-benzoic acid, palmitic acid, rosmarinic acid, selenium, tannin, thymol, tryptophan, ursolic acid, vanillic acid.

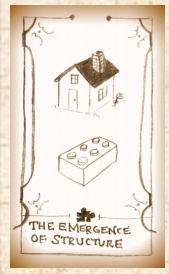
[cnn.com]



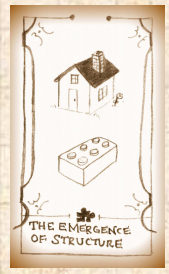
Reductionism

"It would be great to know how this all works, but in the meantime we can enjoy thyme in the knowledge that it probably doesn't do any harm (since people have been eating it forever) and that it may actually do some good (since people have been eating it forever) and that even if it does nothing, we like the way it tastes."

Gulf between theory and practice (see baseball and bumblebees).



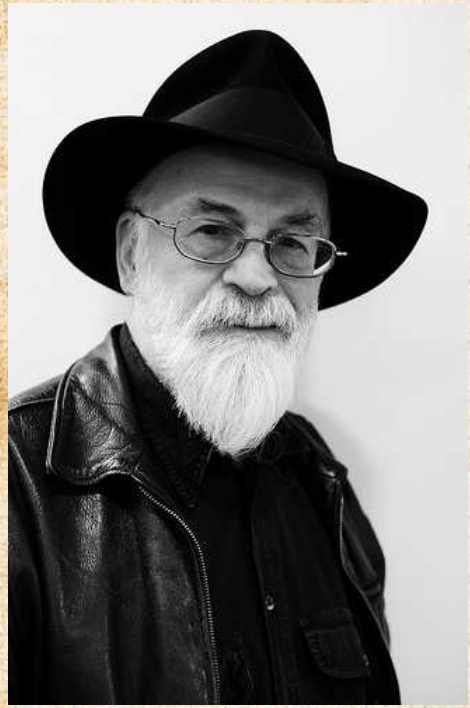
This is a Collateralized Debt Obligation:



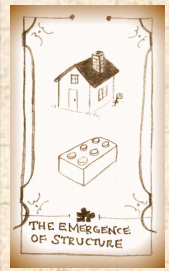
- “The Universe is made of stories, not of atoms.”

- From “The Speed of Darkness” (1968) by Muriel Rukeyser
- Quoted by Metatron in Supernatural, Meta Fiction, S9E18.

(Sir Terry) Pratchett's Narrativium:



- "The most common element on the disc, although not included in the list of the standard five: earth, fire, air, water and surprise. It ensures that everything runs properly as a story."
- "A little narrativium goes a long way: the simpler the story, the better you understand it. Storytelling is the opposite of reductionism: 26 letters and some rules of grammar are no story at all."



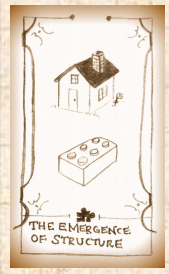
Emergence:

Higher complexity:

- Many system scales (or levels) that interact with each other.
- Potentially much harder to explain/understand.

Even mathematics: [5]

Gödel's Theorem: we can't prove every theorem that's true ...



- Suggests a strong form of emergence: Some phenomena cannot be analytically deduced from elementary aspects of a system.

Emergence:

Roughly speaking, there are two types of emergence:

I. Weak emergence:

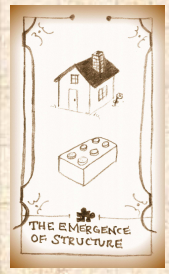
System-level phenomena is different from that of its constituent parts yet can be connected theoretically.

II. Strong emergence:

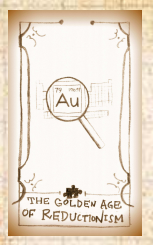
System-level phenomena fundamentally cannot be deduced from how parts interact.

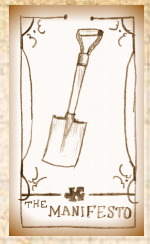
Emergence:

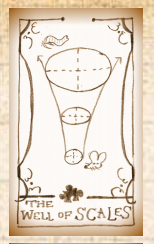
- Reductionist techniques can explain weak emergence.
- Magic explains strong emergence. [2]
- But: maybe magic should be interpreted as an inscrutable yet real mechanism that cannot ever be simply described.
- Gulp.




THE SUN


Au
THE GOLDEN AGE OF REDUCTIONISM

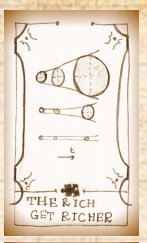

THE MANIFESTO

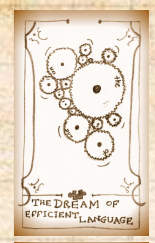

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING BORN TO THE FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS

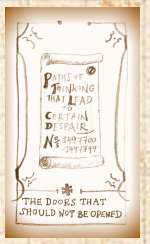

THE MEASURING


THE DATA POOR


THE POURING DATA


THE CHARMS OF THE MANY WRONG PATHS


THE KNOWLEDGE OF DEAD MONKS


PATHS OF THINKING THAT LEAD TO CERTAIN DESPAIR
THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE THRESHOLDS OF PERCOLATION

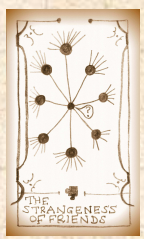

THE NETWORKS COMPLEX

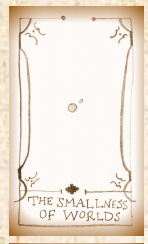

THE ELEMENTS OF WEBS


"I am the Monarch of the Sea."
THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS

THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

THE JOHN DORY

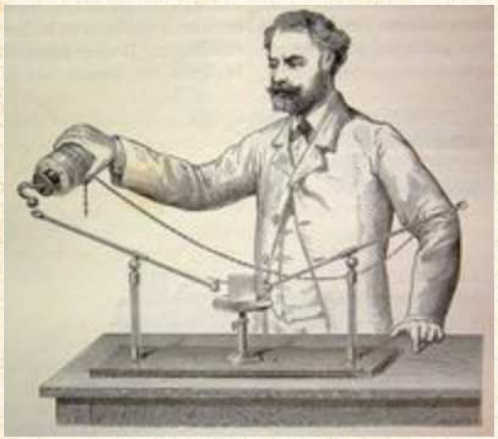
THE STORYTELLERS

THE ADJACENT NARRATIVES

THE END

?
THE UNKNOWN MECHANISM

Listen to Steve Strogatz, Hod Lipson, and Michael Schmidt (Cornell) in the last piece (11:16) on Radiolab's show 'Limits' (April 5, 2010).

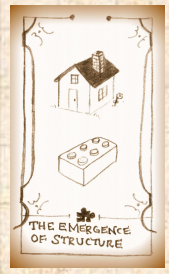


(El Bibliomata/flickr)

Dr. Steve Strogatz wonders if we've reached the limits of human scientific understanding, and should soon turn the reins of research over to robots. Cold, calculating robots. Then, Dr. Hod Lipson and Michael Schmidt walk us through the workings of a revolutionary computer program that they developed--a program that can deduce mathematical relationships in nature, through simple observation. The catch? As Dr. Gurol Suel explains, the program gives answers to complex biological questions that we humans have yet to ask, or even to understand.

TAGS: mind bending

Pair with some slow tv
Bonus: Mike Schmidt's talk on Eureqa at UVM's 2011 TEDx event "Big Data, Big Stories."



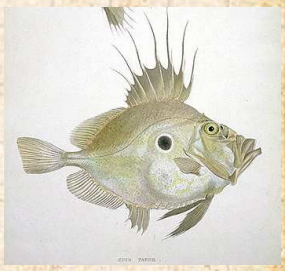
Definitions

"Self-organization is a process in which the internal organization of a system, normally an open system, increases in complexity without being guided or managed by an outside source." (also: Self-assembly)

Examples:

- Molecules/Atoms liking each other → Gases, liquids, and solids.
- Spin alignment → Magnetization.
- Protein folding.
- Imitation → Herding, flocking, mobs, ...

Fundamental question: how likely is 'complexification'?

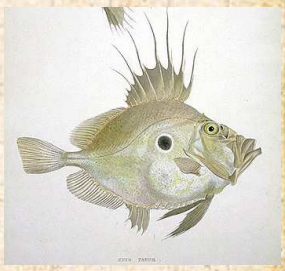


Tools and techniques:

- Differential equations, difference equations, linear algebra, stochastic models.
- Statistical techniques for comparisons and descriptions.
- Methods from statistical mechanics and computer science.
- Machine learning (but beware the black box).
- Computer modeling, everything from
  - Artisanal toy models
  - to kitchen sink models.

Key advance (more soon):

- Representation of complex interaction patterns as complex networks.
- The driver: Massive amounts of Data

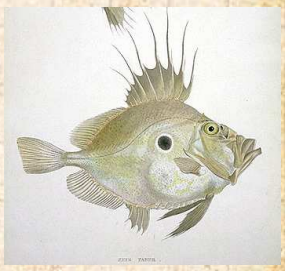


Rather silly but great example of real science:

"How Cats Lap: Water Uptake by *Felis catus*"

Reis et al., *Science*, 2010.

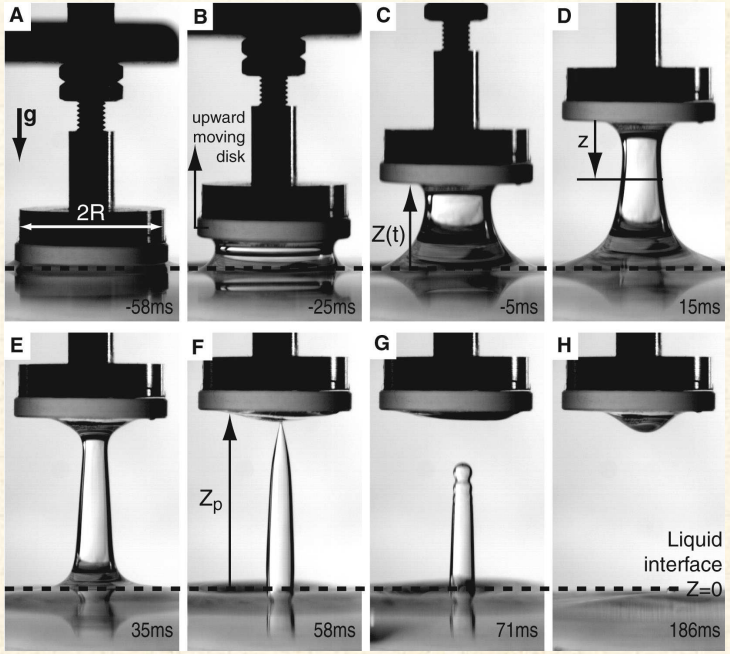
Amusing interview here

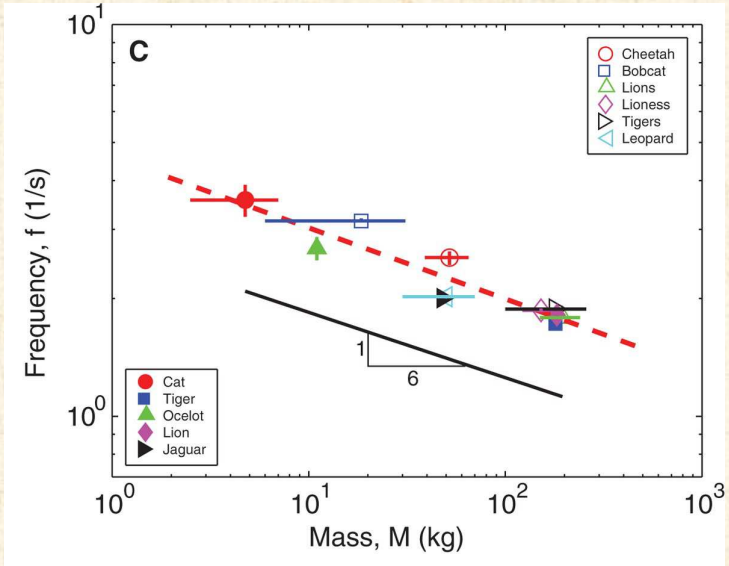


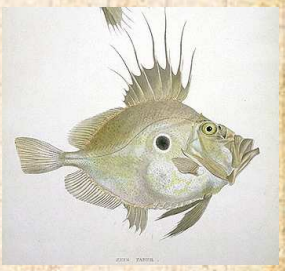
Another great, great moment in scaling:

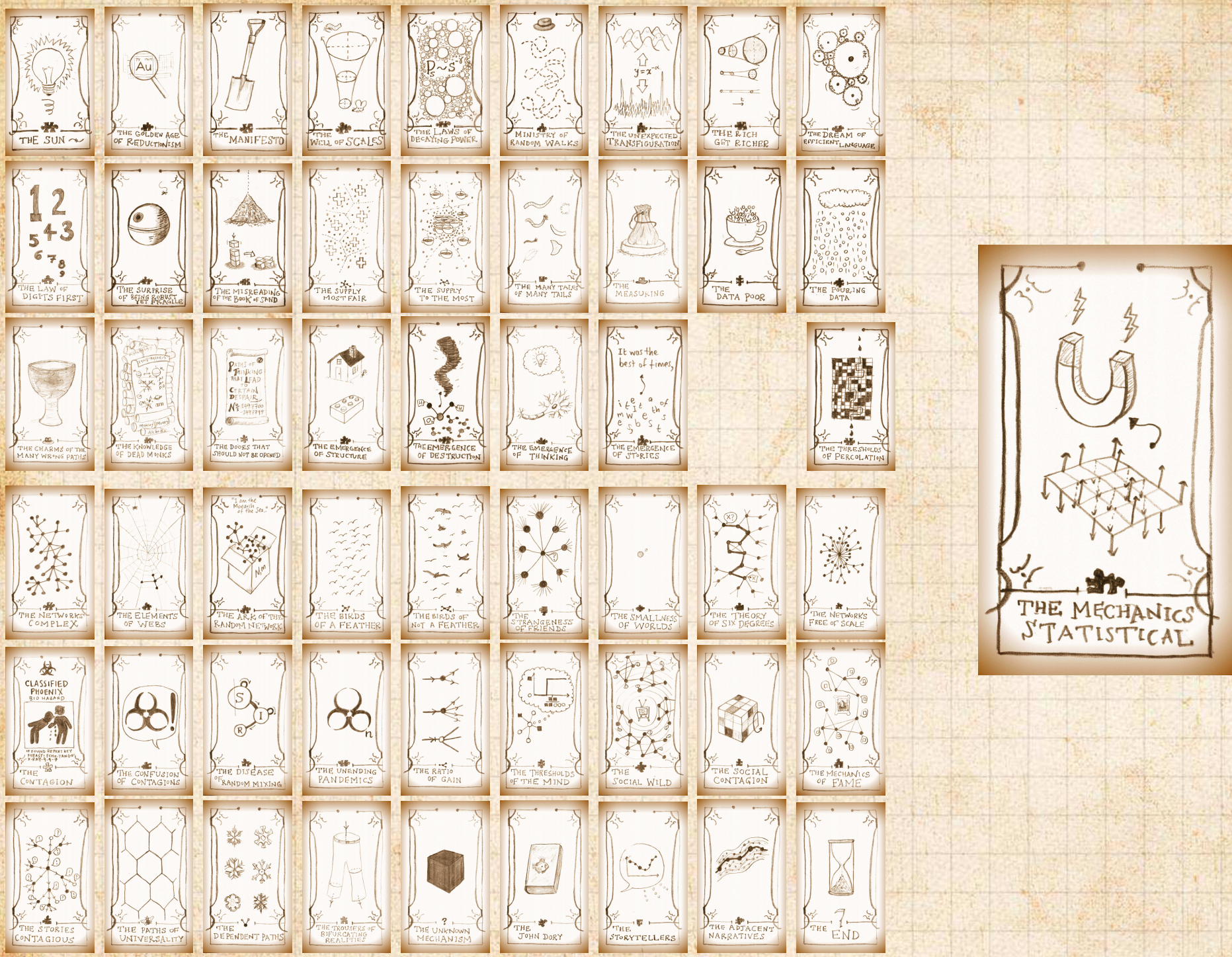
$$f \sim M^{-1/6}$$

The balance of inertia and gravity yields a prediction for the lapping frequency of other felines. Assuming isometry within the Felidae family (i.e., that lapping height H scales linearly with tongue width R and animal mass M scales as R^3), the finding that Fr* is of order one translates to the prediction $f \sim R^{-1/2} \sim M^{-1/6}$. Isometry or marginally positive allometry among the Felidae has been demonstrated for skull (*20*, *21*) and limb bones (*22*). Although variability by function can lead to departures from isometry in interspecific scalings (*23*), reported variations within the Felidae (*23*, *24*) only minimally affect the predicted scaling $f \sim M^{-1/6}$. We tested this –1/6 power-law dependence by measuring the lapping frequency for eight species of felines, from videos acquired at the Zoo New England or available on YouTube (*16*). The lapping frequency was observed to decrease with animal mass as $f = 4.6\ M^{-0.181 \pm 0.024}$ (f in s^{-1}, M in kg) (Fig. 4C), close to the predicted $M^{-1/6}$. This close agreement suggests that the domestic cat's inertia- and gravity-controlled lapping mechanism is conserved among felines.

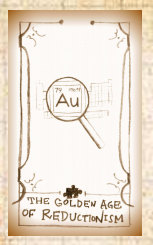


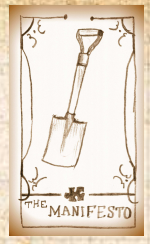


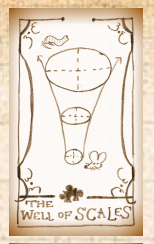



THE SUN
THE GOLDEN AGE OF REDUCTIONISM
THE MANIFESTO
THE WELL OF SCALES
THE LAWS OF DECAYING POWER
MINISTRY OF RANDOM WALKS
THE UNEXPECTED TRANSFIGURATION
THE RICH GET RICHER
THE DREAM OF EFFICIENT LANGUAGE
THE LAW OF DIGITS FIRST
THE SURPRISE OF BEING ROBUST YET FRAGILE
THE MISREADING OF THE BOOK OF SAND
THE SUPPLY MOST FAIR
THE SUPPLY TO THE MOST
THE MANY TALES OF MANY TAILS
THE MEASURING
THE DATA POOR
THE POURING DATA
THE CHARMS OF THE MANY WRONG PATHS
THE KNOWLEDGE OF DEAD MONKS
THE DOORS THAT SHOULD NOT BE OPENED
THE EMERGENCE OF STRUCTURE
THE EMERGENCE OF DESTRUCTION
THE EMERGENCE OF THINKING
It was the best of times,
THE EMERGENCE OF STORIES
THE THRESHOLDS OF PERCOLATION
THE NETWORKS COMPLEX
THE ELEMENTS OF WEBS
THE ARK OF THE RANDOM NETWORK
THE BIRDS OF A FEATHER
THE BIRDS OF NOT A FEATHER
THE STRANGENESS OF FRIENDS
THE SMALLNESS OF WORLDS
THE THEORY OF SIX DEGREES
THE NETWORKS FREE OF SCALE
CLASSIFIED PHOENIX BIO HAZARD
THE CONTAGION
THE CONFUSION OF CONTAGIONS
THE DISEASE OF RANDOM MIXING
THE UNENDING PANDEMICS
THE RATIO OF GAIN
THE THRESHOLDS OF THE MIND
THE SOCIAL WILD
THE SOCIAL CONTAGION
THE MECHANICS OF FAME
THE STORIES CONTAGIOUS
THE PATHS OF UNIVERSALITY
THE DEPENDENT PATHS
THE TROUSERS OF BIFURCATING REALITIES
THE UNKNOWN MECHANISM
THE JOHN DORY
THE STORYTELLERS
THE ADJACENT NARRATIVES
THE END
THE MECHANICS STATISTICAL


THE SUN


THE GOLDEN AGE OF REDUCTIONISM

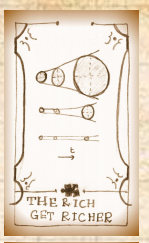

THE MANIFESTO

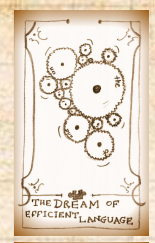

THE WELL OF SCALES


THE LAWS OF DECAYING POWER


MINISTRY OF RANDOM WALKS


THE UNEXPECTED TRANSFIGURATION


THE RICH GET RICHER


THE DREAM OF EFFICIENT LANGUAGE


THE LAW OF DIGITS FIRST


THE SURPRISE OF BEING ROBUST YET FRAGILE


THE MISREADING OF THE BOOK OF SAND


THE SUPPLY MOST FAIR


THE SUPPLY TO THE MOST


THE MANY TALES OF MANY TAILS

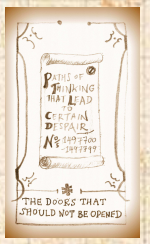

THE MEASURING


THE DATA POOR


THE POURING DATA


THE CHARMS OF THE MANY WRONG PATHS

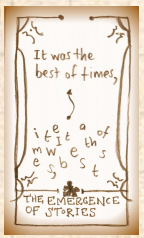

THE KNOWLEDGE OF DEAD MONKS

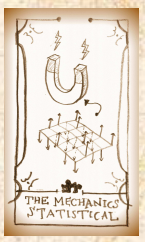

THE DOORS THAT SHOULD NOT BE OPENED


THE EMERGENCE OF STRUCTURE


THE EMERGENCE OF DESTRUCTION


THE EMERGENCE OF THINKING


It was the best of times,
THE EMERGENCE OF STORIES


THE MECHANICS STATISTICAL


THE NETWORKS COMPLEX


THE ELEMENTS OF WEBS

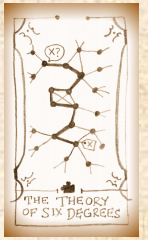

THE ARK OF THE RANDOM NETWORK


THE BIRDS OF A FEATHER


THE BIRDS OF NOT A FEATHER


THE STRANGENESS OF FRIENDS


THE SMALLNESS OF WORLDS


THE THEORY OF SIX DEGREES


THE NETWORKS FREE OF SCALE


CLASSIFIED
PHOENIX
BIO HAZARD
THE CONTAGION


THE CONFUSION OF CONTAGIONS


THE DISEASE OF RANDOM MIXING


THE UNENDING PANDEMICS


THE RATIO OF GAIN

THE THRESHOLDS OF THE MIND

THE SOCIAL WILD

THE SOCIAL CONTAGION

THE MECHANICS OF FAME

THE STORIES CONTAGIOUS

THE PATHS OF UNIVERSALITY

THE DEPENDENT PATHS

THE TROUSERS OF BIFURCATING REALITIES

THE UNKNOWN MECHANISM

THE JOHN DORY

THE STORYTELLERS

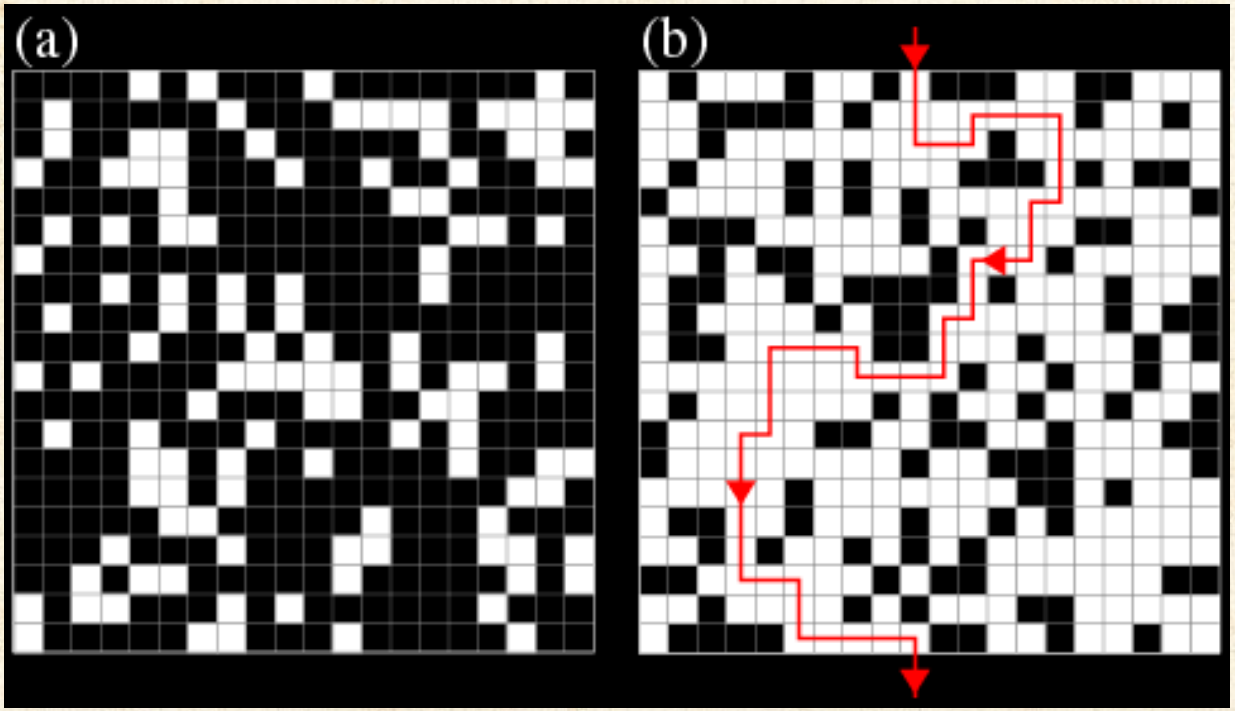
THE ADJACENT NARRATIVES

THE END

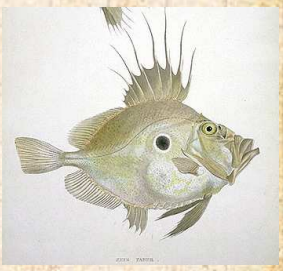
THE THRESHOLDS OF PERCOLATION

- Statistical Mechanics is “a science of collective behavior.”
- Simple rules give rise to collective phenomena.

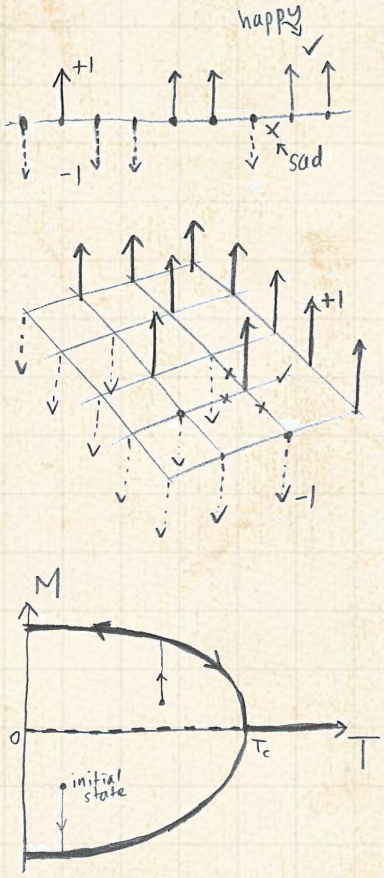
Percolation:



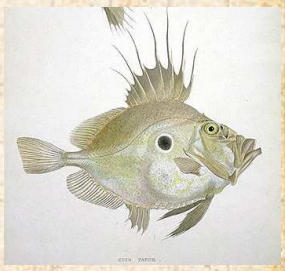
Snared from Michael Gastner’s page on percolation [no longer online]



The Ising Model of a ferromagnet:



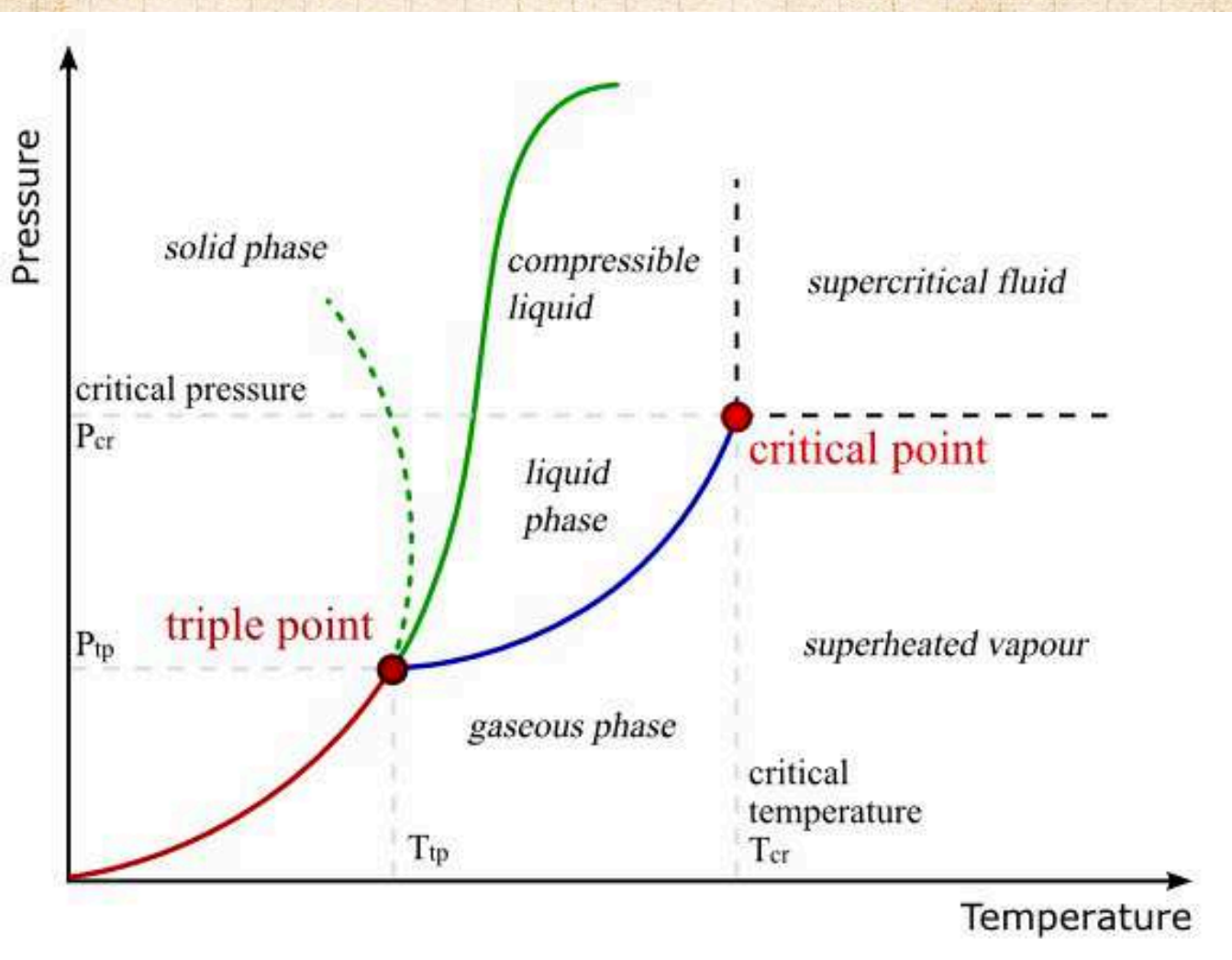
- Each atom is assumed to have a local spin that can be up or down: $S_i = \pm 1$.
- Spins are assumed to be arranged on a lattice.
- In isolation, spins like to align with each other.
- Increasing temperature breaks these alignments.
- The drosophila of statistical mechanics.
- Criticality: Power-law distributions at critical points.

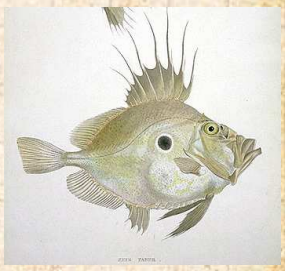


Example 2-d Ising model simulation:

http://dtjohnson.net/projects/ising

Phase diagrams

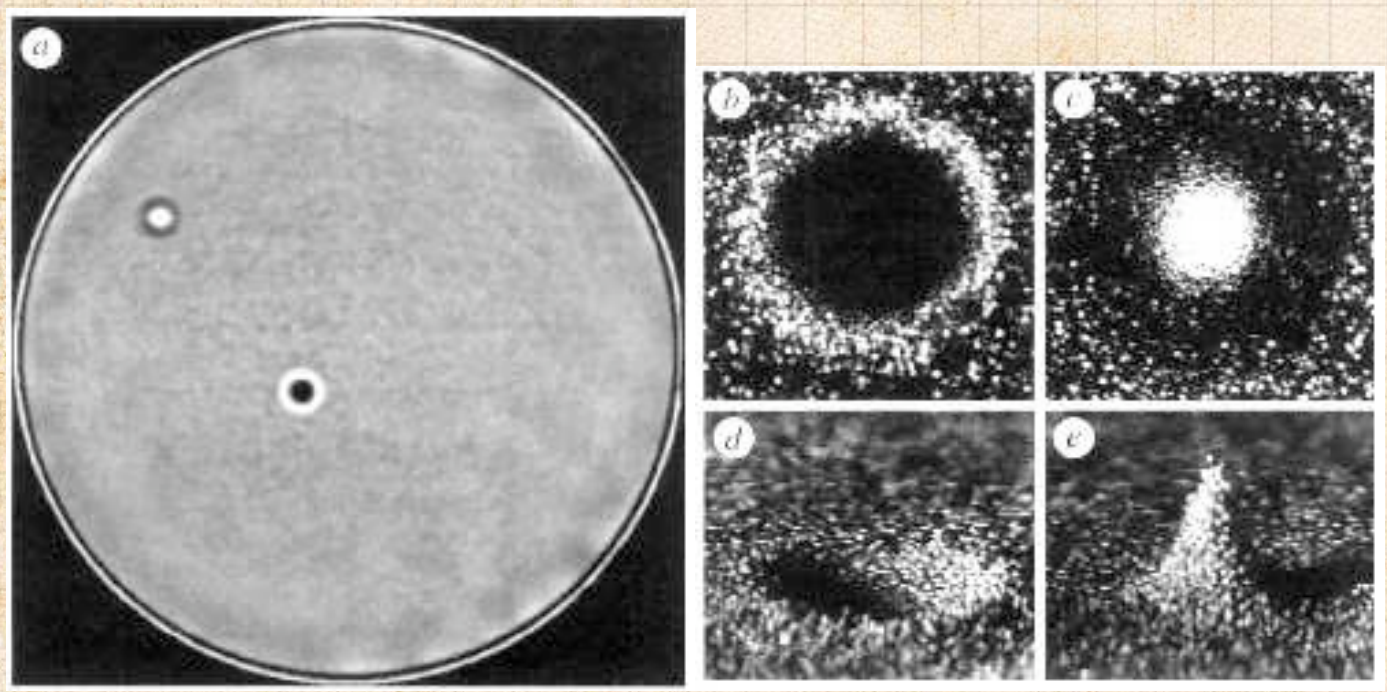




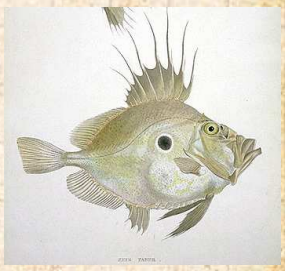
Qualitatively distinct macro states.

Phase diagrams

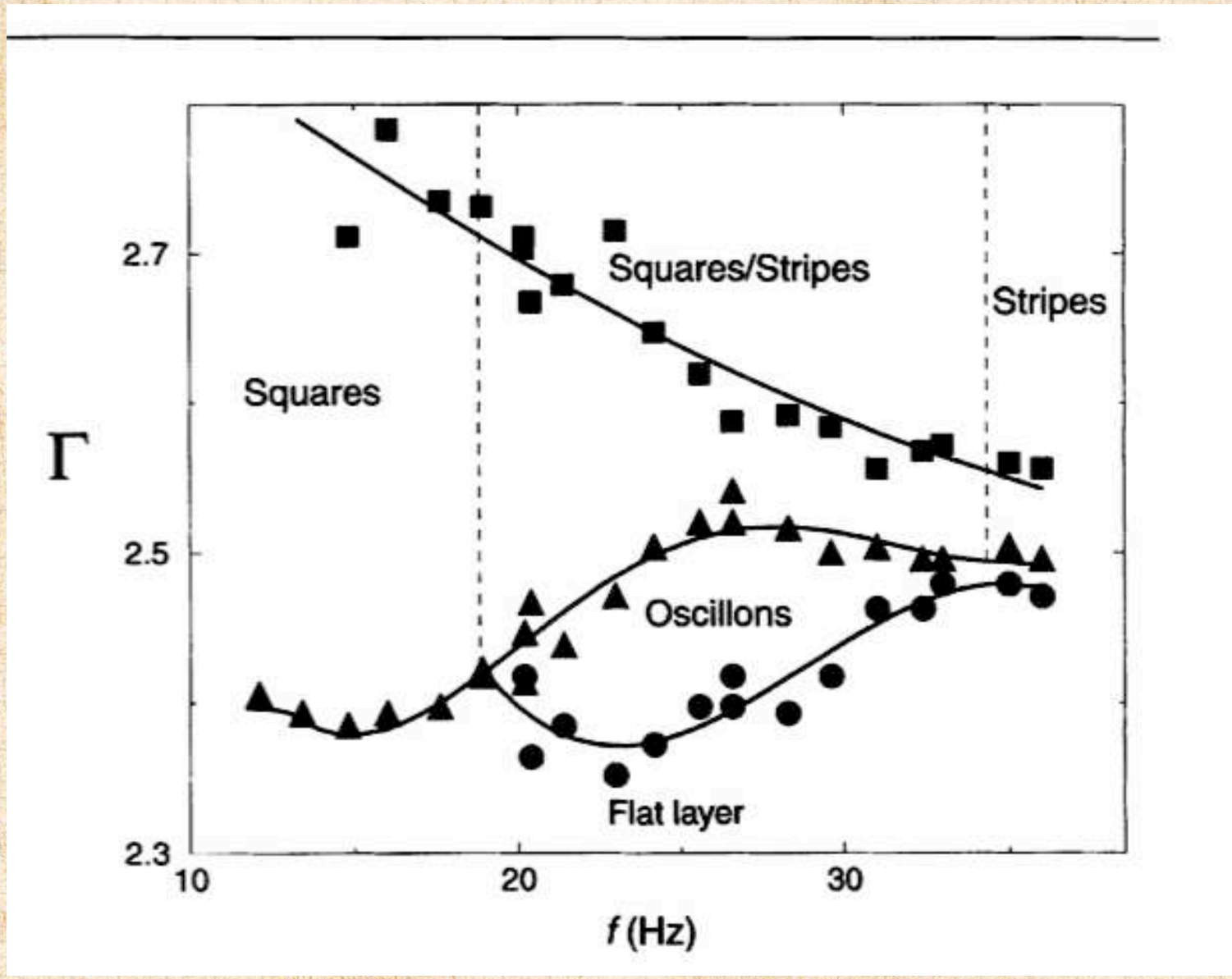
Oscillons, bacteria, traffic, snowflakes, ...

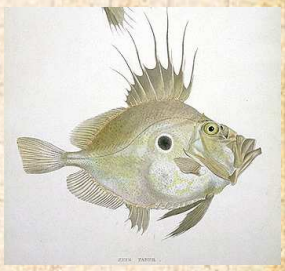


Umbanhowar et al., *Nature*, 1996 [12]

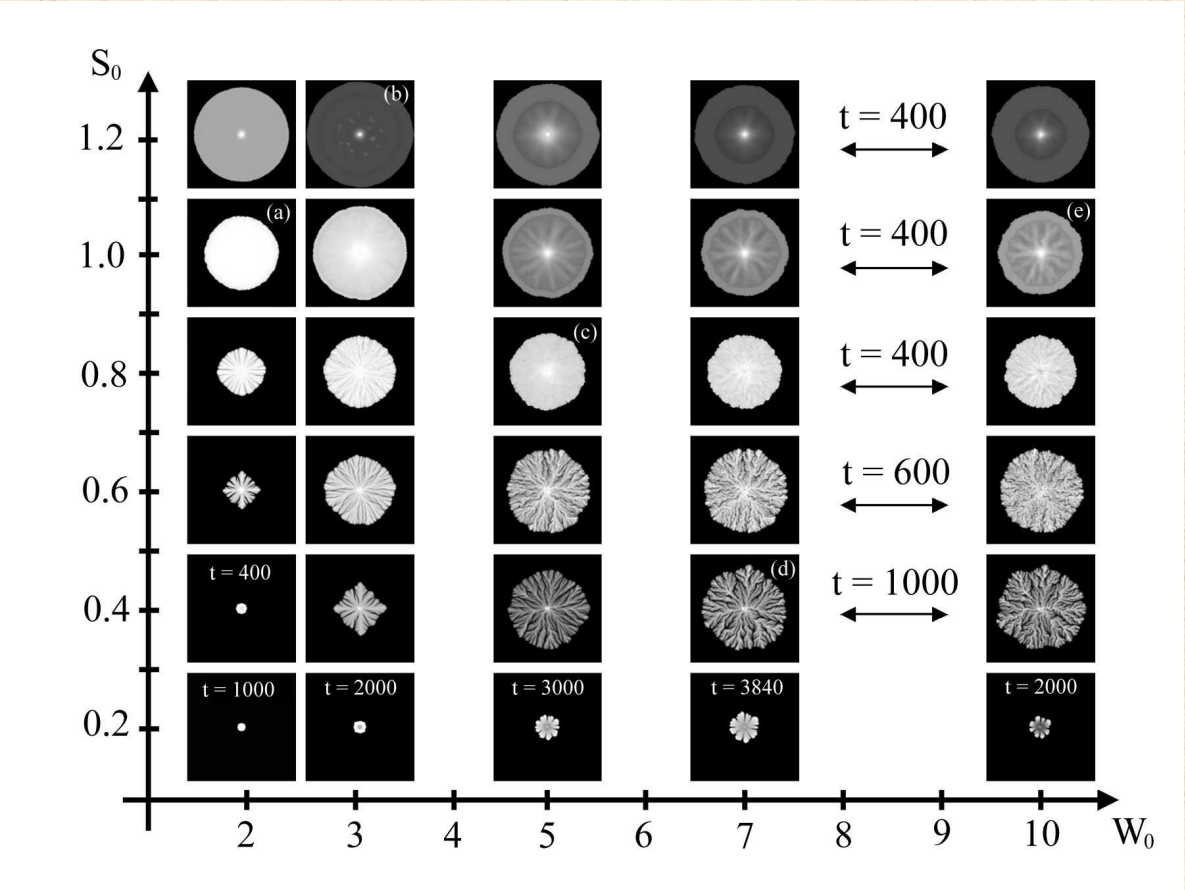


Phase diagrams

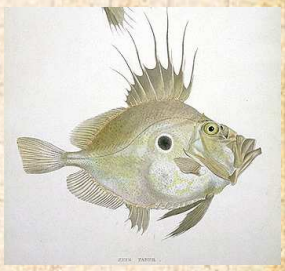




Phase diagrams



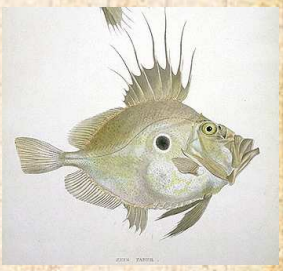
W_0 = initial wetness, S_0 = initial nutrient supply
http://math.arizona.edu/~lega/HydroBact.html



Ising model

Analytic issues:

- 1-d: simple (Ising & Lenz, 1925)
- 2-d: hard (Onsager, 1944)
- 3-d: extremely hard...
- 4-d and up: simple.



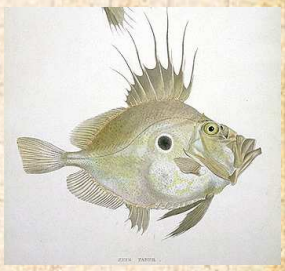
Statistics

Historical surprise:

- Origins of Statistical Mechanics are in the studies of people... (Maxwell and co.)
- Now physicists are using their techniques to study everything else including people...
- See Philip Ball's "Critical Mass" [1]

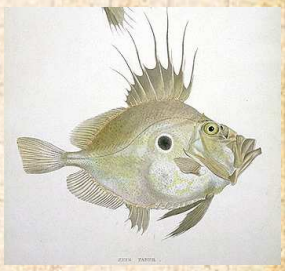
Beyond Statistical Mechanics:

- Analytic approaches have their limits, especially in evolutionary, algorithm-rich systems.
- Algorithmic methods and simulation techniques will continue to rise in importance.



Nutshell

- The central concepts Complexity and Emergence are reasonably well defined.
- There is no general theory of Complex Systems.
- But the problems exist...
  Complex (Adaptive) Systems abound...
- And the observation of Universality of dynamical systems, statistical mechanics, and other quantitative areas means not everything is special and different.
- Framing from the Manifesto: Science's focus is moving to Complex Systems because it finally can.
- We use whatever tools we need.
- Science $\simeq$ Describe + Explain.

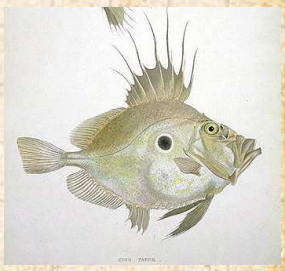


References I

[1] P. Ball.
Critical Mass: How One Thing Leads to Another.
Farra, Straus, and Giroux, New York, 2004.

[2] M. A. Bedau.
Weak emergence.
In J. Tomberlin, editor, Philosophical Perspectives: Mind, Causation, and World, volume 11, pages 375–399. Blackwell, Malden, MA, 1997. pdf

[3] J. S. Coleman.
Foundations of Social Theory.
Belknap Press, Cambridge, MA, 1994.

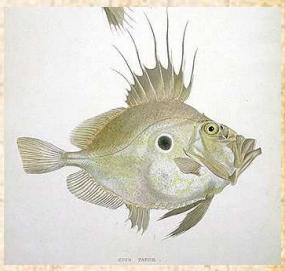


References II

[4] P. S. Dodds, D. J. Watts, and C. F. Sabel.
Information exchange and the robustness of organizational networks.
Proc. Natl. Acad. Sci., 100(21):12516–12521, 2003. pdf

[5] R. Foote.
Mathematics and complex systems.
Science, 318:410–412, 2007. pdf

[6] J.-B. Michel, Y. K. Shen, A. P. Aiden, A. Veres, M. K. Gray, The Google Books Team, J. P. Pickett, D. Hoiberg, D. Clancy, P. Norvig, J. Orwant, S. Pinker, M. A. Nowak, and E. A. Lieberman.
Quantitative analysis of culture using millions of digitized books.
Science Magazine, 331:176–182, 2011. pdf

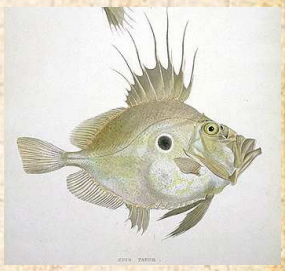


References III

[7] E. A. Pechenick, C. M. Danforth, and P. S. Dodds.
Characterizing the google books corpus: Strong limits to inferences of socio-cultural and linguistic evolution.
PLoS ONE, 10:e0137041, 2015. pdf

[8] T. C. Schelling.
Dynamic models of segregation.
J. Math. Sociol., 1:143–186, 1971. pdf

[9] T. C. Schelling.
Hockey helmets, concealed weapons, and daylight saving: A study of binary choices with externalities.
J. Conflict Resolut., 17:381–428, 1973. pdf



References IV

[10] T. C. Schelling.
Micromotives and Macrobehavior.
Norton, New York, 1978.

[11] T. C. Schelling.
Some fun, thirty-five years ago.
In L. Tesfatsion and K. L. Judd, editors, Handbook of Computational Economics, volume 2, pages 1639–1644. Elsevier, 2006. pdf

[12] P. B. Umbanhowar, F. Melo, and H. L. Swinney.
Localized excitations in a vertically vibrated granular layer.
Nature, 382:793–6, 1996. pdf