

# Biological Contagion

Principles of Complex Systems | @pocsvox  
CSYS/MATH 300, Fall, 2017

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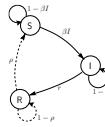


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## Outline

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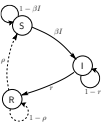
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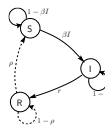


Sealie & Lambie Productions

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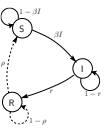
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An awful recording: Wikipedia's list of epidemics from 430 BC on.

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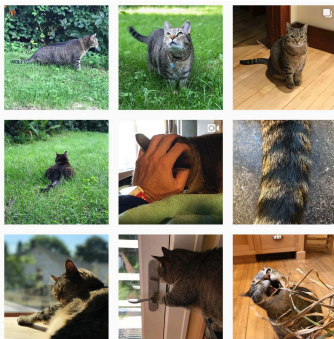
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These slides are also brought to you by:

Special Guest Executive Producer: Pratchett

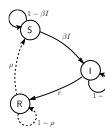


On Instagram at pratchett\_the\_cat

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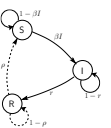
A confusion of contagions:

- Is Harry Potter some kind of virus?
- What about the Da Vinci Code?
- Did Sudoku spread like a disease?
- Language? The alphabet?
- Religion?
- Democracy...?

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# Contagion

## Naturomorphisms

- “The feeling was contagious.”
- “The news spread like wildfire.”
- “Freedom is the most contagious virus known to man.”  
—Hubert H. Humphrey, Johnson’s vice president
- “Nothing is so contagious as enthusiasm.”  
—Samuel Taylor Coleridge

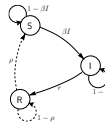
## Optimism according to Ambrose Bierce:

The doctrine that everything is beautiful, including what is ugly, everything good, especially the bad, and everything right that is wrong. ... It is hereditary, but fortunately not contagious.

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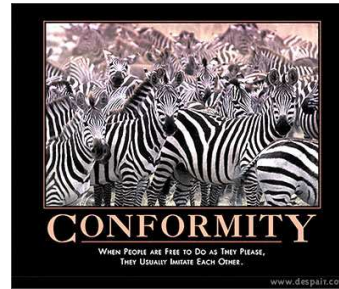
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# Imitation



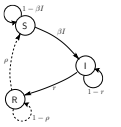
despair.com

“When people are free to do as they please, they usually imitate each other.”  
 —Eric Hoffer  
 “The Passionate State of Mind” [12]

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# Social contagion

## Eric Hoffer, 1902–1983

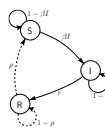
There is a grandeur in the uniformity of the mass. When a fashion, a dance, a song, a slogan or a joke sweeps like wildfire from one end of the continent to the other, and a hundred million people roar with laughter, sway their bodies in unison, hum one song or break forth in anger and denunciation, there is the overpowering feeling that in this country we have come nearer the brotherhood of man than ever before.

Hoffer was an interesting fellow...

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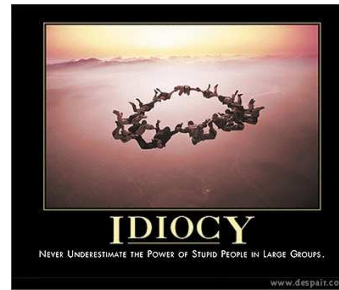
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# The collective...



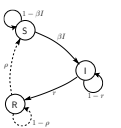
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“Never Underestimate the Power of Stupid People in Large Groups.”

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# The spread of fanaticism

Hoffer’s most famous work: “The True Believer: Thoughts On The Nature Of Mass Movements” (1951) [11]

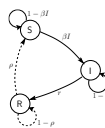
## Aphorisms-aplenty:

- “We can be absolutely certain only about things we do not understand.”
- “Mass movements can rise and spread without belief in a God, but never without belief in a devil.”
- “Where freedom is real, equality is the passion of the masses. Where equality is real, freedom is the passion of a small minority.”

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# Examples of non-disease spreading:

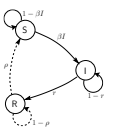
## Interesting infections:

- Spreading of certain buildings in the US:
- 2008 Viral get-out-the-vote video.

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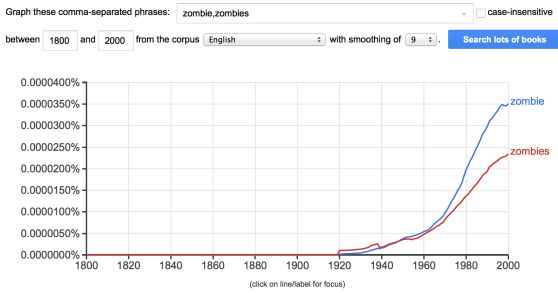
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# The most terrifying contagious outbreak?

## Google books Ngram Viewer



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## Two main classes of contagion

- Infectious diseases:** tuberculosis, HIV, ebola, SARS, influenza, zombification, ...
- Social contagion:** fashion, word usage, rumors, uprisings, religion, stories about zombies, ...

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## The standard SIR model<sup>[17]</sup>

- ⊞ = basic model of disease contagion
- ⊞ Three states:
  - S = Susceptible
  - I = Infective/Infectious
  - R = Recovered or Removed or Refractory
- ⊞  $S(t) + I(t) + R(t) = 1$
- ⊞ Presumes random interactions (mass-action principle)
- ⊞ Interactions are independent (no memory)
- ⊞ Discrete and continuous time versions

# Contagion

## Definitions

- ⊞ (1) The spreading of a quality or quantity between individuals in a population.
- ⊞ (2) A disease itself: the plague, a blight, the dreaded lurgi, ...
- ⊞ from Latin: *con* = 'together with' + *tangere* 'to touch.'
- ⊞ Contagion has unpleasant overtones...
- ⊞ Just **Spreading** might be a more neutral word
- ⊞ But contagion is kind of exciting...

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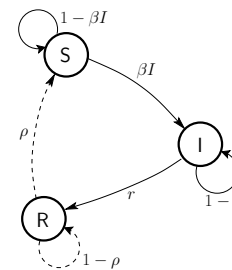
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## Discrete time automata example:



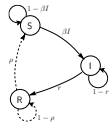
## Transition Probabilities:

- $\beta$  for being infected given contact with infected
- $r$  for recovery
- $\rho$  for loss of immunity

# Mathematical Epidemiology

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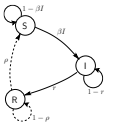
## Original models attributed to

- 1920's: Reed and Frost
- 1920's/1930's: Kermack and McKendrick [13, 15, 14]
- Coupled differential equations with a mass-action principle

# Reproduction Number $R_0$

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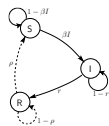
## Discrete version:

- Set up: One Infective in a randomly mixing population of Susceptibles
- At time  $t = 0$ , single infective random bumps into a Susceptible
- Probability of transmission =  $\beta$
- At time  $t = 1$ , single Infective remains infected with probability  $1 - r$
- At time  $t = k$ , single Infective remains infected with probability  $(1 - r)^k$

# Independent Interaction models

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## Differential equations for continuous model

$$\frac{d}{dt}S = -\beta IS + \rho R$$

$$\frac{d}{dt}I = \beta IS - rI$$

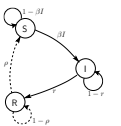
$$\frac{d}{dt}R = rI - \rho R$$

$\beta, r,$  and  $\rho$  are now **rates**.

# Reproduction Number $R_0$

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## Discrete version:

- Expected number infected by original infective:

$$R_0 = \beta + (1 - r)\beta + (1 - r)^2\beta + (1 - r)^3\beta + \dots$$

$$= \beta(1 + (1 - r) + (1 - r)^2 + (1 - r)^3 + \dots)$$

$$= \beta \frac{1}{1 - (1 - r)} = \beta/r$$

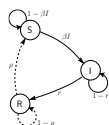
For  $S(0) \approx 1$  initial susceptibles  
 $(1 - S(0)) = R(0) =$  fraction initially immune):

$$R_0 = S(0)\beta/r$$

# Reproduction Number $R_0$

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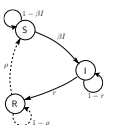
## Reproduction Number $R_0$

- $R_0 =$  expected number of infected individuals resulting from a single initial infective
- Epidemic threshold: If  $R_0 > 1$ , 'epidemic' occurs.
- Exponential take off:  $R_0^n$  where  $n$  is the number of generations.
- Fantastically awful notation convention:  $R_0$  and the  $R$  in  $SIR$ .

# Independent Interaction models

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## For the continuous version

- Second equation:

$$\frac{d}{dt}I = \beta SI - rI$$

$$\frac{d}{dt}I = (\beta S - r)I$$

- Number of infectives grows initially if

$$\beta S(0) - r > 0 \Rightarrow \beta S(0) > r \Rightarrow \beta S(0)/r > 1$$

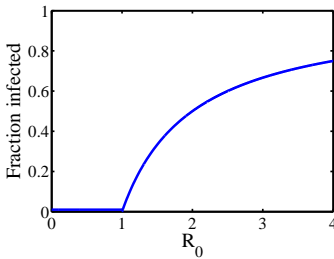
where  $S(0) \approx 1$ .

- Same story as for discrete model.



## Independent Interaction models

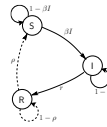
Example of epidemic threshold:



- Continuous phase transition.
- Fine idea from a simple model.

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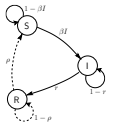
Save the world yourself: [🔗](#)



- And you can be the virus. [🔗](#)
- Also contagious?: Cooperative games ...

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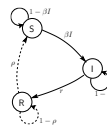
## Independent Interaction models

Many variants of the SIR model:

- SIS: susceptible-infective-susceptible
- SIRS: susceptible-infective-recovered-susceptible
- compartment models (age or gender partitions)
- more categories such as 'exposed' (SEIRS)
- recruitment (migration, birth)

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Neural reboot—Save another pretend world with Vax: [🔗](#)

Lesson 4: Quarantine

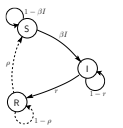
Vaccines take time to 'kick in' so they're ineffective if an infection has already begun to spread.

Start >

VAX! Networks Epidemics Vaccines Quarantine

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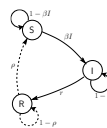
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Watch someone else pretend to save the world:



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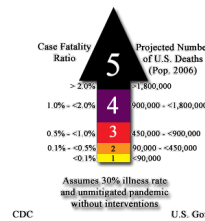
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Pandemic severity index (PSI) [🔗](#)

Classification during/post pandemic:



- Category based.
- 1-5 scale.
- Modeled on the Saffir-Simpson hurricane scale. [🔗](#)

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For novel diseases:

1. Can we predict the size of an epidemic?
2. How important is the reproduction number  $R_0$ ?

$R_0$  approximately same for all of the following:

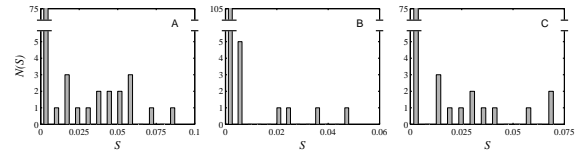
- 1918-19 "Spanish Flu" ~ 75,000,000 world-wide, 500,000 deaths in US.
- 1957-58 "Asian Flu" ~ 2,000,000 world-wide, 70,000 deaths in US.
- 1968-69 "Hong Kong Flu" ~ 1,000,000 world-wide, 34,000 deaths in US.
- 2003 "SARS Epidemic" ~ 800 deaths world-wide.

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## Really not so good at all in Iceland

Epidemic size distributions  $N(S)$  for Measles, Rubella, and Whooping Cough.



Spike near  $S = 0$ , relatively flat otherwise.

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## Size distributions

Size distributions are important elsewhere:

- earthquakes (Gutenberg-Richter law)
- city sizes, forest fires, war fatalities
- wealth distributions
- 'popularity' (books, music, websites, ideas)
- Epidemics?**

Power laws distributions are common but not obligatory...

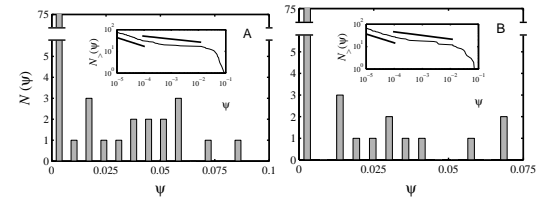
Really, what about epidemics?

- Simply hasn't attracted much attention.
- Data not as clean as for other phenomena.

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## Measles & Pertussis



Insert plots:  
Complementary cumulative frequency distributions:

$$N(\Psi' > \Psi) \propto \Psi^{-\gamma+1}$$

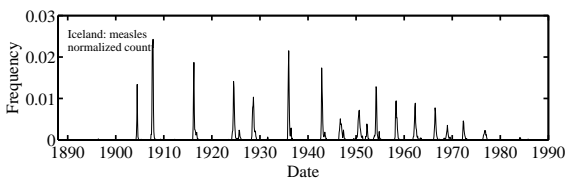
Limited scaling with a possible break.

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## Feeling Ill in Iceland

Caseload recorded monthly for range of diseases in Iceland, 1888-1990



- Treat outbreaks separated in time as 'novel' diseases.

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## Power law distributions

Measured values of  $\gamma$ :

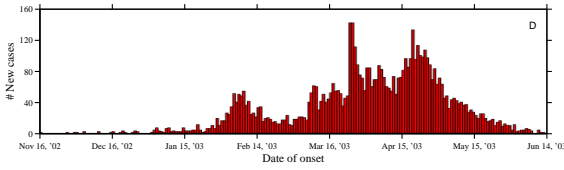
- measles: 1.40 (low  $\Psi$ ) and 1.13 (high  $\Psi$ )
- pertussis: 1.39 (low  $\Psi$ ) and 1.16 (high  $\Psi$ )

- Expect  $2 \leq \gamma < 3$  (finite mean, infinite variance)
- When  $\gamma < 1$ , can't normalize
- Distribution is quite flat.

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# Resurgence—example of SARS



- Epidemic slows... then an infective moves to a new context.
- Epidemic discovers new 'pools' of susceptibles: **Resurgence.**
- Importance of rare, stochastic events.

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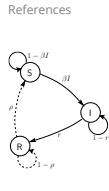
# The challenge

So... can a simple model produce

1. broad epidemic distributions and
2. resurgence ?

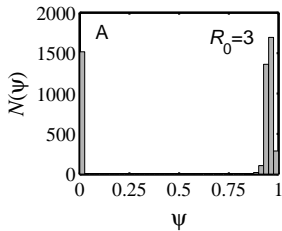
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# Size distributions

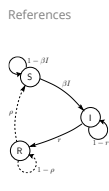


Simple models typically produce **bimodal** or **unimodal** size distributions.

- This includes network models: random, small-world, scale-free, ...
- Exceptions:
  1. Forest fire models
  2. Sophisticated metapopulation models

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# Burning through the population

Forest fire models: [18]

- Rhodes & Anderson, 1996
- The physicist's approach: **"if it works for magnets, it'll work for people..."**

A bit of a stretch:

1. Epidemics ≡ forest fires spreading on 3-d and 5-d lattices.
2. Claim Iceland and Faroe Islands exhibit power law distributions for outbreaks.
3. Original forest fire model not completely understood.

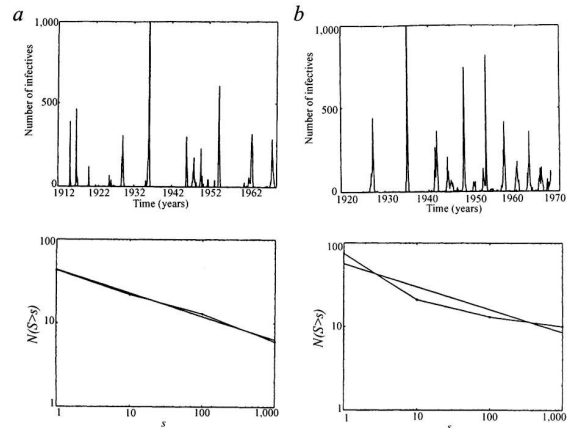
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# Size distributions



From Rhodes and Anderson, 1996.

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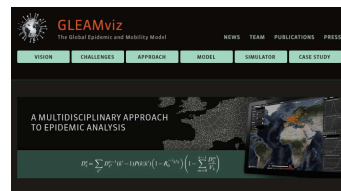
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# Sophisticated metapopulation models:

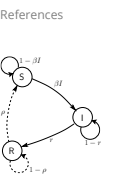
- Multiscale models suggested earlier by others but not formalized (Bailey [1], Cliff and Haggett [5], Ferguson et al.)
- Community based mixing (two scales)—Longini. [16]
- Eubank et al.'s EpiSims/TRANSIMS—city simulations. [8]
- Spreading through countries—Airlines: Germann et al., Colizza et al. [6]



GLEAM: Global pandemic simulations by Vespignani et al.

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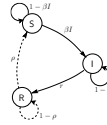
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## Size distributions

- Vital work but perhaps hard to generalize from...
- ⇒ Create a simple model involving multiscale travel
- Very big question: **What is  $N$ ?**
- Should we model SARS in Hong Kong as spreading in a neighborhood, in Hong Kong, Asia, or the world?
- For simple models, we need to know the final size beforehand...

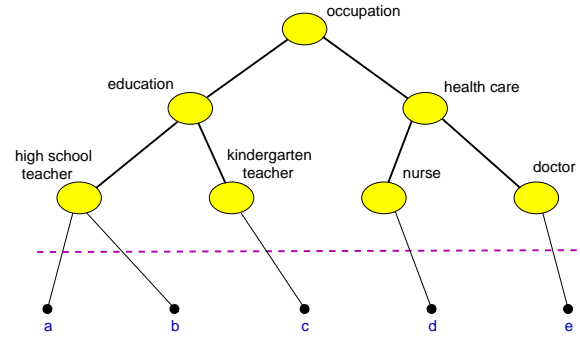
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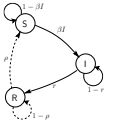
## Infer interactions/network from identities



Distance makes sense in identity/context space.

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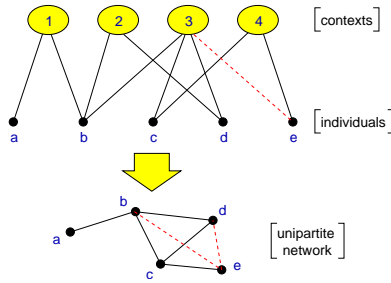
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## Improving simple models

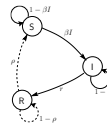
### Contexts and Identities—Bipartite networks



- boards of directors
- movies
- transportation modes (subway)

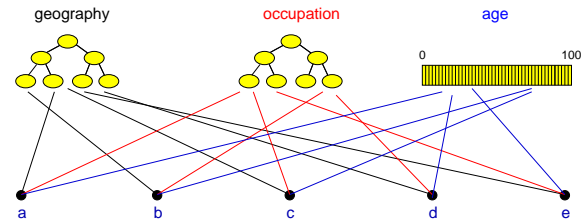
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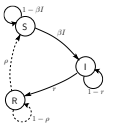
## Generalized context space



(Blau & Schwartz<sup>[3]</sup>, Simmel<sup>[19]</sup>, Breiger<sup>[4]</sup>)

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## Improving simple models

### Idea for social networks: incorporate identity

#### Identity is formed from attributes such as:

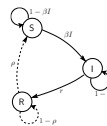
- Geographic location
- Type of employment
- Age
- Recreational activities

#### Groups are crucial...

- formed by people with at least one similar attribute
- Attributes ⇔ Contexts ⇔ Interactions ⇔ Networks.<sup>[22]</sup>

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## A toy agent-based model:



"Multiscale, resurgent epidemics in a hierarchical metapopulation model"

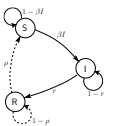
Watts et al.,  
Proc. Natl. Acad. Sci., **102**, 11157-11162, 2005.<sup>[23]</sup>

### Geography: allow people to move between contexts

- Locally: standard SIR model with random mixing
- discrete time simulation
- $\beta$  = infection probability
- $\gamma$  = recovery probability
- $P$  = probability of travel
- Movement distance:**  $\Pr(d) \propto \exp(-d/\xi)$
- $\xi$  = typical travel distance

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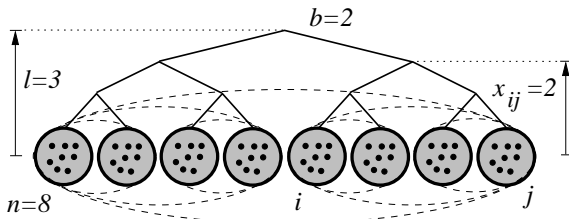
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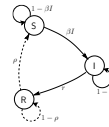
# A toy agent-based model

Schematic:



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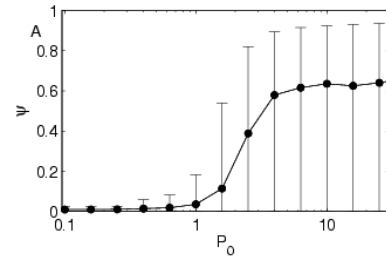
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# Model output

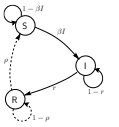
Varying  $P_0$ :



- Transition in expected final size based on typical number of infectives leaving first group (also sensible)
- Travel advisories:  $\xi$  has larger effect than  $P_0$ .

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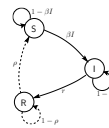
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# Model output

- Define  $P_0$  = Expected number of infected individuals leaving initially infected context.
- Need  $P_0 > 1$  for disease to spread (independent of  $R_0$ ).
- Limit epidemic size by restricting frequency of travel and/or range

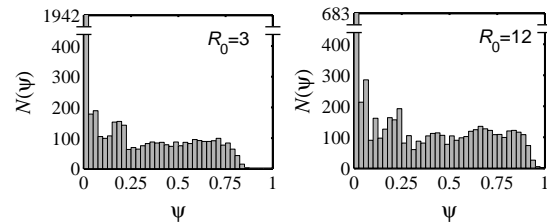
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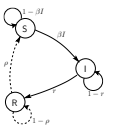
# Example model output: size distributions



- Flat distributions are possible for certain  $\xi$  and  $P$ .
- Different  $R_0$ 's may produce similar distributions
- Same epidemic sizes may arise from different  $R_0$ 's

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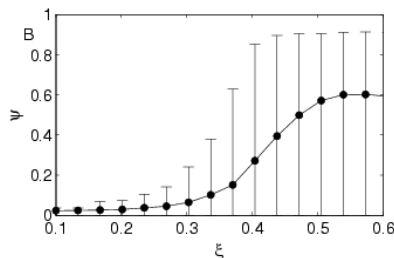
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# Model output

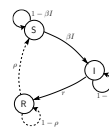
Varying  $\xi$ :



- Transition in expected final size based on typical movement distance (sensible)

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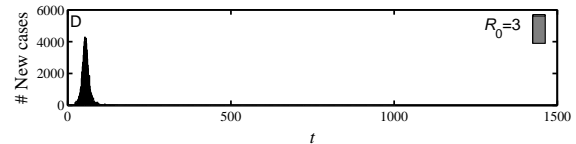
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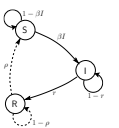
# Model output—resurgence

Standard model:



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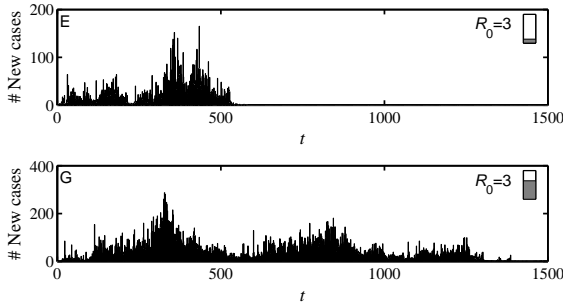


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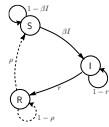
# Model output—resurgence

## Standard model with transport:



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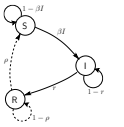
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# Conclusions

- 🧠 Disease's spread is highly sensitive to population structure.
- 🧠 Rare events may matter enormously: e.g., an infected individual taking an international flight.
- 🧠 More support for controlling population movement: e.g., travel advisories, quarantine

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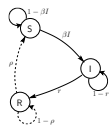
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# The upshot

Simple multiscale population structure  
+  
stochasticity  
leads to  
resurgence  
+  
broad epidemic size distributions

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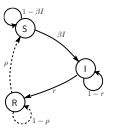
# Nutshelling

- What to do:
- 🧠 Need to separate movement from disease
  - 🧠  $R_0$  needs a friend or two.
  - 🧠 Need  $R_0 > 1$  and  $P_0 > 1$  and  $\xi$  sufficiently large for disease to have a chance of spreading
  - 🧠 And in general: keep building up the kitchen sink models.

- More wondering:
- 🧠 Exactly how important are rare events in disease spreading?
  - 🧠 Again, what is  $N$ ?

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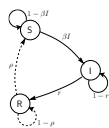
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# Nutshelling

- 🧠 For the hierarchical movement model, epidemic size is highly unpredictable
- 🧠 Model is more complicated than SIR but still simple.
- 🧠 We haven't even included normal social responses such as travel bans and self-quarantine.
- 🧠 The reproduction number  $R_0$  is not terribly useful.
- 🧠  $R_0$ , however measured, is not informative about
  1. how likely the observed epidemic size was,
  2. and how likely future epidemics will be.
- 🧠 Problem:  $R_0$  summarises one epidemic after the fact and enfold movement, the price of bananas, everything.

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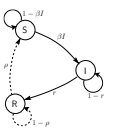
# Krugman, 1998: "Why most economists' predictions are wrong."



"The growth of the Internet will slow drastically, as the flaw in "Metcalfe's law"—which states that the number of potential connections in a network is proportional to the square of the number of participants—becomes apparent: most people have nothing to say to each other! By 2005 or so, it will become clear that the Internet's impact on the economy has been no greater than the fax machine's."<sup>1</sup>

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<sup>1</sup><http://www.redherring.com/mag/issue55/economics.html>

## Economics, Schmeconomics

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Alan Greenspan (September 18, 2007):

"I've been dealing with these big mathematical models of forecasting the economy ...

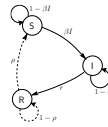
If I could figure out a way to determine whether or not people are more fearful or changing to more euphoric, I don't need any of this other stuff.

I could forecast the economy better than any way I know."



http://wikipedia.org

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## Economics, Schmeconomics

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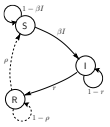
James K. Galbraith:

NYT But there are at least 15,000 professional economists in this country, and you're saying only two or three of them foresaw the mortgage crisis? [JKG] Ten or 12 would be closer than two or three.

NYT What does that say about the field of economics, which claims to be a science? [JKG] It's an enormous blot on the reputation of the profession. There are thousands of economists. Most of them teach. And most of them teach a theoretical framework that has been shown to be fundamentally useless.

From the New York Times, 11/02/2008

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## Economics, Schmeconomics

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Greenspan continues:

"The trouble is that we can't figure that out. I've been in the forecasting business for 50 years. I'm no better than I ever was, and nobody else is. Forecasting 50 years ago was as good or as bad as it is today. And the reason is that human nature hasn't changed. We can't improve ourselves."

Jon Stewart:

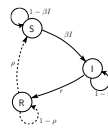
"You just bummed the @\*!# out of me."



wildbluffmedia.com

From the Daily Show (September 18, 2007)  
The full interview is here.

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Other attempts to use SIR and co. elsewhere:

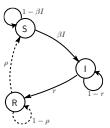
- Adoption of ideas/beliefs (Goffman & Newell, 1964)<sup>[10]</sup>
- Spread of rumors (Daley & Kendall, 1965)<sup>[7]</sup>
- Diffusion of innovations (Bass, 1969)<sup>[2]</sup>
- Spread of fanatical behavior (Castillo-Chávez & Song, 2003)
- Spread of Feynmann diagrams (Bettencourt et al., 2006)

Social contagion:

- SIR may apply sometimes ...
- But we need new fundamental models.
- Next up: Thresholds.

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## Predicting social catastrophe isn't easy...

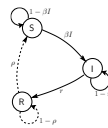
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"Greenspan Concedes Error on Regulation"

- ...humbled Mr. Greenspan admitted that he had put too much faith in the self-correcting power of free markets ...
- "Those of us who have looked to the self-interest of lending institutions to protect shareholders' equity, myself included, are in a state of shocked disbelief"
- Rep. Henry A. Waxman: "Do you feel that your ideology pushed you to make decisions that you wish you had not made?"
- Mr. Greenspan conceded: "Yes, I've found a flaw. I don't know how significant or permanent it is. But I've been very distressed by that fact."

New York Times, October 23, 2008

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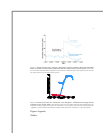
## We really should know social contagion is different but ...

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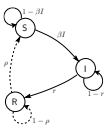
"It's contagious: Rethinking a metaphor dialogically"  
Warren and Power, Culture & Psychology, 21, 359-379, 2015.<sup>[21]</sup>

"Facebook will lose 80% of users by 2017, say Princeton researchers" (Guardian, 2014)



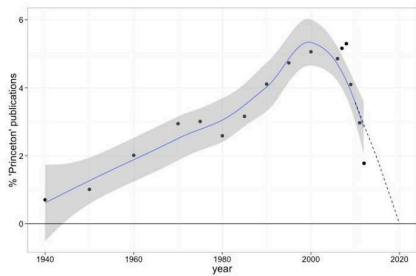
"Epidemiological modeling of online social network dynamics"  
Spechler and Cannarella, Available online at <http://arxiv.org/abs/1401.4208>, 2014.<sup>[20]</sup>

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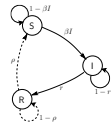
The Facebook Data Science team's [response](#)



Mike Develin, Lada Adamic, and Sean Taylor.

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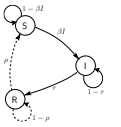
85 of 93

References III

- [8] S. Eubank, H. Guclu, V. S. A. Kumar, M. V. Marathe, A. Srinivasan, Z. Toroczkai, and N. Wang. Modelling disease outbreaks in realistic urban social networks. [Nature](#), 429:180–184, 2004. [pdf](#)
- [9] J. Gleick. [The Information: A History, A Theory, A Flood](#). Pantheon, 2011.
- [10] W. Goffman and V. A. Newell. Generalization of epidemic theory: An application to the transmission of ideas. [Nature](#), 204:225–228, 1964. [pdf](#)

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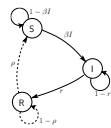
88 of 93

References I

- [1] N. T. J. Bailey. [The Mathematical Theory of Infectious Diseases and Its Applications](#). Griffin, London, Second edition, 1975.
- [2] F. Bass. A new product growth model for consumer durables. [Manage. Sci.](#), 15:215–227, 1969. [pdf](#)
- [3] P. M. Blau and J. E. Schwartz. [Crosscutting Social Circles](#). Academic Press, Orlando, FL, 1984.
- [4] R. L. Breiger. The duality of persons and groups. [Social Forces](#), 53(2):181–190, 1974. [pdf](#)

PoCS | @pocsvox  
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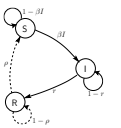
86 of 93

References IV

- [11] E. Hoffer. [The True Believer: On The Nature Of Mass Movements](#). Harper and Row, New York, 1951.
- [12] E. Hoffer. [The Passionate State of Mind: And Other Aphorisms](#). Buccaneer Books, 1954.
- [13] W. O. Kermack and A. G. McKendrick. A contribution to the mathematical theory of epidemics. [Proc. R. Soc. Lond. A](#), 115:700–721, 1927. [pdf](#)

PoCS | @pocsvox  
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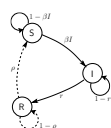
89 of 93

References II

- [5] A. D. Cliff, P. Haggett, J. K. Ord, and G. R. Versey. [Spatial diffusion: an historical geography of epidemics in an island community](#). Cambridge University Press, Cambridge, UK, 1981.
- [6] V. Colizza, A. Barrat, M. Barthelme, A.-J. Valleron, and A. Vespignani. Modeling the worldwide spread of pandemic influenza: Baseline case and containment interventions. [PLoS Med.](#), 4:e13, 2007. [pdf](#)
- [7] D. J. Daley and D. G. Kendall. Stochastic rumours. [J. Inst. Math. Appl.](#), 1:42–55, 1965.

PoCS | @pocsvox  
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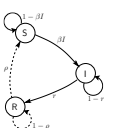
87 of 93

References V

- [14] W. O. Kermack and A. G. McKendrick. A contribution to the mathematical theory of epidemics. III. Further studies of the problem of endemicity. [Proc. R. Soc. Lond. A](#), 141(843):94–122, 1927. [pdf](#)
- [15] W. O. Kermack and A. G. McKendrick. Contributions to the mathematical theory of epidemics. II. The problem of endemicity. [Proc. R. Soc. Lond. A](#), 138(834):55–83, 1927. [pdf](#)
- [16] I. M. Longini. A mathematical model for predicting the geographic spread of new infectious agents. [Math. Biosci.](#), 90:367–383, 1988.

PoCS | @pocsvox  
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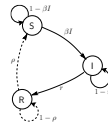
## References VI

- [17] J. D. Murray.  
Mathematical Biology.  
Springer, New York, Third edition, 2002.
- [18] C. J. Rhodes and R. M. Anderson.  
Power laws governing epidemics in isolated populations.  
Nature, 381:600–602, 1996. [pdf](#)
- [19] G. Simmel.  
The number of members as determining the sociological form of the group. I.  
American Journal of Sociology, 8:1–46, 1902.

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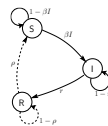
## References VII

- [20] J. A. Spechler and J. Cannarella.  
Epidemiological modeling of online social network dynamics.  
Available online at <http://arxiv.org/abs/1401.4208>, 2014. [pdf](#)
- [21] Z. J. Warren and S. A. Power.  
It's contagious: Rethinking a metaphor dialogically.  
Culture & Psychology, 21:359–379, 2015. [pdf](#)
- [22] D. J. Watts, P. S. Dodds, and M. E. J. Newman.  
Identity and search in social networks.  
Science, 296:1302–1305, 2002. [pdf](#)

PoCS | @pocsvox  
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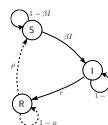
## References VIII

- [23] D. J. Watts, R. Muhamad, D. Medina, and P. S. Dodds.  
Multiscale, resurgent epidemics in a hierarchical metapopulation model.  
Proc. Natl. Acad. Sci., 102(32):11157–11162, 2005. [pdf](#)

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