Voting, Success, and Superstars Principles of Complex Systems | @pocsvox

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Where do superstars come from?



"The economics of superstars" S. Rosen, Am. Econ. Rev., **71**, 845–858, 1981. [5] Winning: it's not for everyone Superstars

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Examples:

- \clubsuit Full-time Comedians (≈ 200)
- Soloists in Classical Music
- & Economic Textbooks (the usual myopic example)

Highly skewed distributions again...





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Outline

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Winning: it's not for everyone Rosen's theory:

- \mathfrak{S} Individual quality q maps to reward R(q).
- $\Re R(q)$ is 'convex' ($d^2R/dq^2 > 0$).
- Two reasons:
 - 1. Imperfect substitution:
 - A very good surgeon is worth many mediocre ones
 - 2. Technology:

Media spreads & technology reduces cost of reproduction of books, songs, etc.

- Joint consumption versus public good.
- No social element—success follows 'inherent quality'.











Superstars



'Stardom and Talent" 🗗 Moshe Adler, American Economic Review, 75, 208-212, 1985. ^[1]

- "Consumption capital": "Appreciation [of music] increases with knowledge. But how does one know about music? By listening to it, and discussing it with other persons who know about it."
- Assumes extreme case of equal 'inherent quality'
- Argues desire for coordination in knowledge and culture leads to differential success
- Success can be purely a social construction
- (How can we measure 'inherent quality'?)

Voting

Evidence from the web suggestions (Huberman et

- 1. Easy decisions (yes/no) lead to bandwagoning e.g. jyte.com
- 2. More costly evaluations lead to oppositional votes e.g. amazon.com
- Self-selection: Costly voting may lower incentives for those who agree with the current assessment and increase incentives for those who disagree.





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Score-based voting versus rank-based voting:



"A theory of measuring, electing, and ranking" Balinski and Laraki.

Proc. Natl. Acad. Sci., 104, 8720-8725, 2007. [2]

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"Aggregating partial, local evaluations to achieve global ranking"

Laureti, Moret, and Zhang, Physica A, **345**, 705–712, 2004. [4]

- underlying quality q
- Assume evaluation of object i is a random variable with mean q_i
- Choose objects based on votes:

$$p_i(t) \propto v_i(t)^\alpha \ {\rm or} \ p_i(t) \propto q_i v_i(t)^\alpha.$$

- If $\alpha < 1$, correct quality ordering is uncovered
- If $\alpha > 1$, some objects are never evaluated and mistakes are made...
- Related to Adler's approach

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Dominance hierarchies



"Individual differences versus social dynamics in the formation of animal dominance hierarchies"

Chase et al., Proc. Natl. Acad. Sci., **99**, 5744-5749, 2002. [3]

The aggressive female Metriaclima zebra:

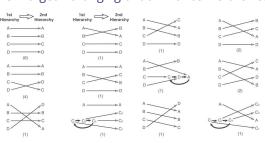




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Pecking orders for fish... Dominance hierarchies

Fish forget—changing of dominance hierarchies:



22 observations: about 3/4 of the time, hierarchy changed

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Dominance hierarchies

Methods of Forming Hierarchies

Group versus isolated interactions produce different hierarchies

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Music Lab Experiment

Music Lab Experiment

Experiments 2-4



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Music Lab Experiment



48 songs 30,000 participants



multiple 'worlds' Inter-world variability

- How probable is the world?
- Can we estimate variability?
- Superstars dominate but are unpredictable. Why?

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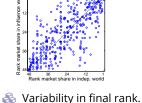
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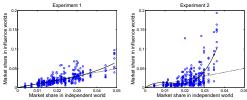


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Music Lab Experiment



Variability in final number of downloads.

Music Lab Experiment



"An experimental study of inequality and unpredictability in an artificial cultural

Salganik, Dodds, and Watts, Science, **311**, 854–856, 2006. [6]

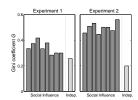






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Inequality as measured by Gini coefficient:

$$G = \frac{1}{(2N_{\rm S}-1)} \sum_{i=1}^{N_{\rm S}} \sum_{j=1}^{N_{\rm S}} |m_i - m_j|$$

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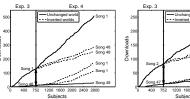
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Music Lab Experiment—Sneakiness [7]



Inversion of download count

The pretend rich get richer ...

🚵 ... but at a slower rate



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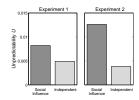
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Unpredictability

$$U = \frac{1}{N_{\mathrm{S}}\binom{N_{\mathrm{w}}}{2}} \sum_{i=1}^{N_{\mathrm{S}}} \sum_{j=1}^{N_{\mathrm{w}}} \sum_{k=j+1}^{N_{\mathrm{w}}} |m_{i,j} - m_{i,k}|$$





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> American Economic Review, pages 208-212, 1985. pdf 🛂

[2] M. Balinski and R. Laraki. A theory of measuring, electing, and ranking. Proc. Natl. Acad. Sci., 104(21):8720-8725, 2007.

[3] I. D. Chase, C. Tovey, D. Spangler-Martin, and M. Manfredonia.

Individual differences versus social dynamics in the formation of animal dominance hierarchies. Proc. Natl. Acad. Sci., 99(8):5744-5749, 2002. pdf





Music Lab Experiment

Sensible result:

Stronger social signal leads to greater following and greater inequality.

Peculiar result:

Stronger social signal leads to greater unpredictability.

Very peculiar observation:

- The most unequal distributions would suggest the greatest variation in underlying 'quality.'
- But success may be due to social construction through following. (so let's tell a story... [8, 9])

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[5] S. Rosen. The economics of superstars. Am. Econ. Rev., 71:845-858, 1981. pdf

[6] M. J. Salganik, P. S. Dodds, and D. J. Watts. An experimental study of inequality and unpredictability in an artificial cultural market. Science, 311:854-856, 2006. pdf



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Leading the herd astray: An experimental study of self-fulfilling prophecies in an artificial cultural market.

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Infotopia: How many minds produce knowledge. Oxford University Press, New York, 2006.

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