Small-world networks

Principles of Complex Systems | @pocsvox CSYS/MATH 300, Fall, 2016 | #FallPoCS2016

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Dept. of Mathematics & Statistics | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont























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Nutshell





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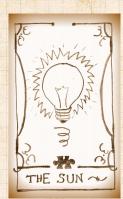
Nutshell

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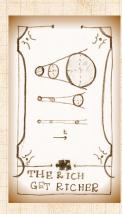
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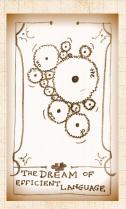
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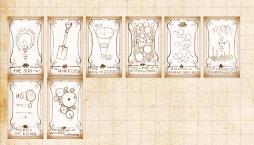
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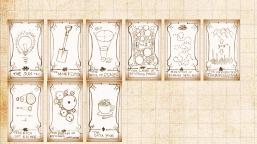
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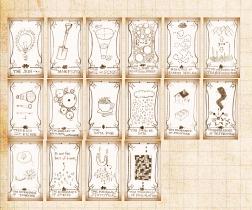
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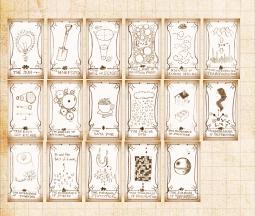
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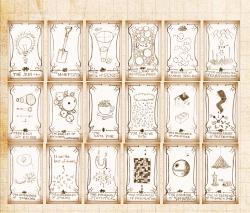
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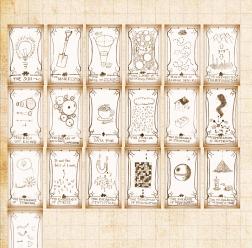
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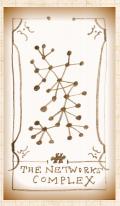
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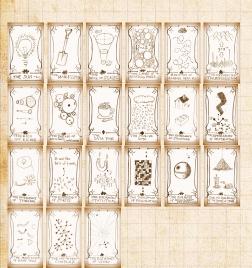
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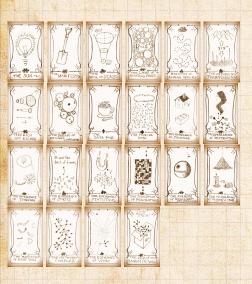
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People thinking about people:

How are social networks structured?



How do we define and measure connections?



Methods/issues of self-report and remote sensing.

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People thinking about people:

How are social networks structured?

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What about the dynamics of social networks?

- A How do social networks/movements begin & evolve?
- How does collective problem solving work?
- How does information move through social networks?
- Which rules give the best 'game of society?'

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Methods/issues of self-report and remote sensing.

What about the dynamics of social networks?

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How does collective problem solving work?

How does information move through social networks?

Which rules give the best 'game of society?'

Sociotechnical phenomena and algorithms:

What can people and computers do together? (google)

Use Play + Crunch to solve problems. Which problems?

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Social Search

A small slice of the pie:



Q. Can people pass messages between distant individuals using only their existing social connections?

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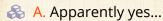




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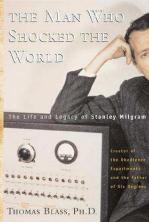
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Milgram's social search experiment (1960s)

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http://www.stanleymilgram.com

Target person = Boston stockbroker.

296 senders from Boston and Omaha.

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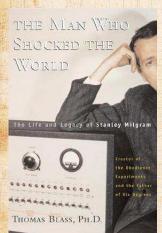






Milgram's social search experiment (1960s)

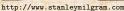
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- Target person = Boston stockbroker.
- 296 senders from Boston and Omaha.
- 20% of senders reached target.
- \Leftrightarrow chain length \simeq 6.5.

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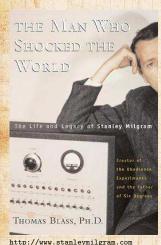






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Target person = Boston stockbroker.

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- 20% of senders reached target.
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Popular terms:

- The Small World Phenomenon;
- "Six Degrees of Separation."

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Six Degrees of Kevin Bacon:



Alt's a game ☑:
 "Kevin Bacon is the Center of the Universe"

♣ The Oracle of Bacon

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Six Degrees of Paul Erdös:

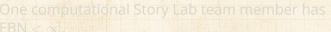


Academic papers.

🙈 Erdös Number 🗹

& Erdös Number Project 🗹

So naturally we must have the



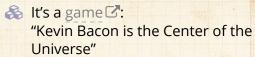




Natalie Hershlag's (Portman's) EBN# = 5 + 2 = 7

Six Degrees of Kevin Bacon:





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Six Degrees of Paul Erdös:



Academic papers.

🙈 Erdös Number 🗹

🙈 Erdös Number Project 🗹



So naturally we must have the Erdös-Bacon Number ...

One computational Story Lab team member has



Six Degrees of Kevin Bacon:



A The Oracle of Bacon 2

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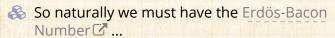
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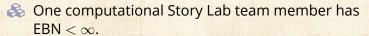


Academic papers.

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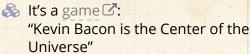






Six Degrees of Kevin Bacon:





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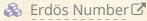
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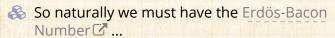
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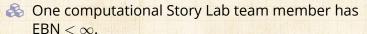


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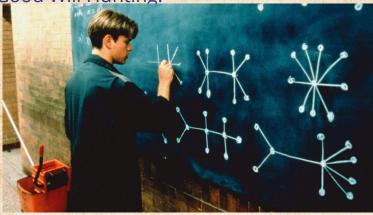






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Good Will Hunting:





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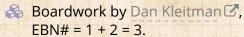
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See Kleitman's sidebar in Mark Saul's Movie Review C (Notices of the AMS, Vol. 45, 1998.)







You may already be a winner in NSA's "three-degrees" surveillance sweepstakes! NSA's probes could cover hundreds of millions of Americans. Thanks, Kevin Bacon.

by Sean Gallagher - July 18 2013, 4:00pm EDT





Aurich Lawson



A Many people are within three degrees from a random person ...

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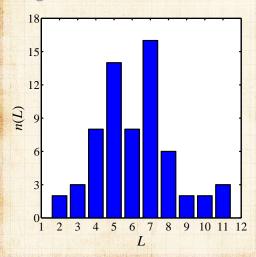
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Lengths of successful chains:



From Travers and Milgram (1969) in Sociometry: [12] "An Experimental Study of the Small World Problem."

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Two features characterize a social 'Small World':

- 1. Short paths exist
 - and
- 2. People are good at finding them.

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Two features characterize a social 'Small World':

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Two features characterize a social 'Small World':

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Two features characterize a social 'Small World':

- 1. Short paths exist, (= Geometric piece) and
- 2. People are good at finding them. (= Algorithmic piece)

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Social Search

Milgram's small world experiment with email:





"An Experimental study of Search in Global Social Networks"

**Total Control of Search Search in Global Social Networks

**Total Search Sea

Dodds, Muhamad, and Watts, Science, **301**, 827–829, 2003. [6]

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🚳 60,000+ participants in 166 countries







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60,000+ participants in 166 countries

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18 targets in 13 countries including

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18 targets in 13 countries including

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a professor at an lvy League university,





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🚳 60,000+ participants in 166 countries

18 targets in 13 countries including

a professor at an Ivy League university,

an archival inspector in Estonia,

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🚳 60,000+ participants in 166 countries

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18 targets in 13 countries including

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a professor at an lvy League university,

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an archival inspector in Estonia, a technology consultant in India,





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an archival inspector in Estonia,

a technology consultant in India,

a policeman in Australia,



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References

a technology consultant in India,

a policeman in Australia, and

a veterinarian in the Norwegian army.





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60,000+ participants in 166 countries

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3 18 targets in 13 countries including

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a professor at an lvy League university,

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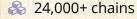
an archival inspector in Estonia, a technology consultant in India,

References

a policeman in Australia,

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THE SMALLINGS OF WORLDS

New York Times, Circuits Section (December, 2001)





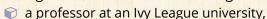
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🙈 60,000+ participants in 166 countries



18 targets in 13 countries including



an archival inspector in Estonia,

a technology consultant in India,

a policeman in Australia, and

a veterinarian in the Norwegian army.



24,000+ chains

We were lucky and contagious (more later):

"Using E-Mail to Count Connections" , Sarah Milstein, New York Times, Circuits Section (December, 2001)

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All targets:

Table S1

Target	City	Country	Occupation	Gender	N	N _c (%)	r (r ₀)	<l></l>
1	Novosibirsk	Russia	PhD student	F	8234	20(0.24)	64 (76)	4.05
2	New York	USA	Writer	F	6044	31 (0.51)	65 (73)	3.61
3	Bandung	Indonesia	Unemployed	M	8151	0	66 (76)	n/a
4	New York	USA	Journalist	F	5690	44 (0.77)	60 (72)	3.9
5	Ithaca	USA	Professor	M	5855	168 (2.87)	54 (71)	3.84
6	Melbourne	Australia	Travel Consultant	F	5597	20 (0.36)	60 (71)	5.2
7	Bardufoss	Norway	Army veterinarian	M	4343	16 (0.37)	63 (76)	4.25
8	Perth	Australia	Police Officer	M	4485	4 (0.09)	64 (75)	4.5
9	Omaha	USA	Life Insurance	F	4562	2 (0.04)	66 (79)	4.5
			Agent					
10	Welwyn Garden City	UK	Retired	M	6593	1 (0.02)	68 (74)	4
11	Paris	France	Librarian	F	4198	3 (0.07)	65 (75)	5
12	Tallinn	Estonia	Archival Inspector	M	4530	8 (0.18)	63(79)	4
13	Munich	Germany	Journalist	M	4350	32 (0.74)	62 (74)	4.66
14	Split	Croatia	Student	M	6629	0	63 (77)	n/a
15	Gurgaon	India	Technology	M	4510	12 (0.27)	67 (78)	3.67
			Consultant					
16	Managua	Nicaragua	Computer analyst	M	6547	2 (0.03)	68 (78)	5.5
17	Katikati	New Zealand	Potter	M	4091	12 (0.3)	62 (74)	4.33
18	Elderton	USA	Lutheran Pastor	M	4438	9 (0.21)	68 (76)	4.33
Totals				NA.	98,847	384 (0.4)	63 (75)	4.05

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Milgram's participation rate was roughly 75%







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Email version: Approximately 37% participation rate.

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Probability of a chain of length 10 getting through:

 $.37^{10} \simeq 5 \times 10^{-5}$







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Milgram's participation rate was roughly 75%

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Email version: Approximately 37% participation rate.

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Probability of a chain of length 10 getting through:

$$.37^{10} \simeq 5 \times 10^{-5}$$

 \Rightarrow 384 completed chains (1.6% of all chains).











Motivation/Incentives/Perception matter.

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Motivation/Incentives/Perception matter.



If target seems reachable ⇒ participation more likely.

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Motivation/Incentives/Perception matter.

If target seems reachable

 \Rightarrow participation more likely.

Small changes in attrition rates

 \Rightarrow large changes in completion rates

e.g., \ 15% in attrition rate ⇒ 7 800% in completion rat







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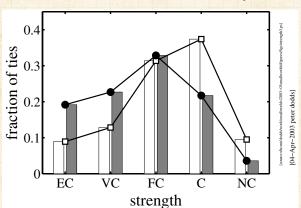
& e.g., \ 15% in attrition rate \Rightarrow \nearrow 800% in completion rate





Comparing successful to unsuccessful chains:

Successful chains used relatively weaker ties:



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Successful chains disproportionately used:

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Successful chains disproportionately used:



Weak ties, Granovetter [7]

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Successful chains disproportionately used:



Weak ties, Granovetter [7]



Professional ties (34% vs. 13%)

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Successful chains disproportionately used:

Weak ties, Granovetter [7]



Professional ties (34% vs. 13%)



Ties originating at work/college

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Successful chains disproportionately used:

- & Weak ties, Granovetter [7]
- Professional ties (34% vs. 13%)
- Ties originating at work/college
- Target's work (65% vs. 40%)

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Successful chains disproportionately used:

Weak ties, Granovetter [7]

Professional ties (34% vs. 13%)

Ties originating at work/college

Target's work (65% vs. 40%)

...and disproportionately avoided

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Successful chains disproportionately used:

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Weak ties, Granovetter [7]

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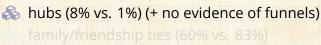
Professional ties (34% vs. 13%)

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Successful chains disproportionately used:

Weak ties, Granovetter [7]

Professional ties (34% vs. 13%)

Ties originating at work/college

Target's work (65% vs. 40%)

...and disproportionately avoided

A hubs (8% vs. 1%) (+ no evidence of funnels)

family/friendship ties (60% vs. 83%)

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Successful chains disproportionately used:

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& Weak ties, Granovetter [7]

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Professional ties (34% vs. 13%)

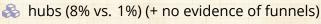
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Ties originating at work/college

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Target's work (65% vs. 40%)

...and disproportionately avoided



family/friendship ties (60% vs. 83%)



Geography → Work



Senders of successful messages showed little absolute dependency on



age, gender

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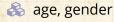
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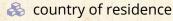
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References

Senders of successful messages showed little absolute dependency on











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Senders of successful messages showed little absolute dependency on

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age, gender

income

Generalized affiliation

country of residence





Senders of successful messages showed little absolute dependency on



age, gender



country of residence



income



🚓 religion

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Senders of successful messages showed little absolute dependency on

age, gender

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🚓 religion

relationship to recipient

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Senders of successful messages showed little absolute dependency on

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🙈 age, gender

Theory
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🙈 country of residence

References

🙈 income

🙈 religion

relationship to recipient

THE SHALL LINES OF VINSELDS

Range of completion rates for subpopulations:

30% to 40%



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Nutshell

References

Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."







Small-world networks

Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."

Why:



Specificity important

Small-world networks Experiments

Generalized affiliation







Small-world networks

Mildly bad for continuing chain:

choosing recipients because "they have lots of friends" or because they will "likely continue the chain."

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References

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Why:

Specificity important

Successful links used relevant information. (e.g. connecting to someone who shares same profession as target.)







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Basic results:



$\langle L \rangle = 4.05$ for all completed chains

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A L_* = Estimated 'true' median chain length (zero attrition)

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PoCS | @pocsvox Small-world networks

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- $\red{\$}$ Intra-country chains: $L_* = 5$
- $rac{1}{4}$ Inter-country chains: $L_*=7$

All chains: $L_* = 1$ Milgram: $L_* \simeq 9$ Small-world networks Experiments

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Harnessing social search:

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Harnessing social search:



Can distributed social search be used for something big/good?

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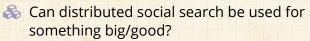




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What about something evil? (Good idea to check.)

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Can distributed social search be used for something big/good?

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What about socio-inspired algorithms for information search? (More later.)

References

For real social search, we have an incentives problem.



Which kind of influence mechanisms/algorithms would help propagate search?

Fun, money, prestige, ...?

Must be 'non-gameable.'



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A Grand Challenge:

- 1969: The Internet about 2 (the APANET 2—four nodes!).
- Originally funded by DARPA who created a grand Network Charlet P of for the 40th anniversary.
- Saturday December 5, 2009: DARPA puts 10 red weather balloons up during the day.
- Each 8 foot diameter balloon is anchored to the ground somewhere in the United States.
- Challenge: Find the latitude and longitude of each balloon.
- Prize: \$40,000.

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A Grand Challenge:



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A Grand Challenge:

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Nutshell

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A Grand Challenge:

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Nutshell References

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Where the balloons were:



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Finding red balloons:

The winning team and strategy:



MIT's Media Lab won in less than 9 hours. [9]

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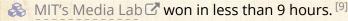
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Idea: Want people to both (1) find the balloons, and (2) involve more people.

Recursive incentive structure with exponentially decaying payout:

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\$2000 for correctly reporting the coordinates of a balloon.

\$1000 for recruiting a person who finds a balloon \$500 for recruiting a person who recruits the balloon finder, ...

(Not a Ponzi scheme.)

True victory:

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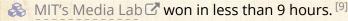
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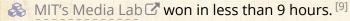
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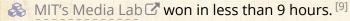
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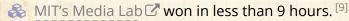
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🔉 True victory: Colbert interviews Riley Crane 🗹

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Clever scheme:



Max payout = \$4000 per balloon.

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Clever scheme:



Max payout = \$4000 per balloon.



A Individuals have clear incentives to both



1. involve/source more people (spread), and

2. find balloons (goal action).

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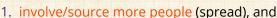
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Gameable?

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Limit to how much money a set of bad actors can extract.

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Extra notes:



MIT's brand helped greatly.

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- MIT group first heard about the competition a few days before. Ouch.
- - Worthwhile looking at these competing strategies.

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Clever scheme:



Max payout = \$4000 per balloon.

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Limit to how much money a set of bad actors can extract.

Extra notes:

MIT's brand helped greatly.

MIT group first heard about the competition a few days before. Ouch.

A number of other teams did well .

Worthwhile looking at these competing strategies. [9]

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Collective Detective:



Finding an errant panda

Once again, social media proved to be a powerful dragnet. Around 1:15 p.m., a Washingtonian posted a picture on Twitter of Rusty in a patch of weeds in the Adams Morgan district, not far from the 163-acre zoo, which was created in 1889 by an act of Congress. "Red panda in our neighborhood," wrote Ashley Foughty, who identified herself as a singer, actress and traveler. "Please come save him!"

Another neighbor posted a photograph of two zoo workers, one in safari shorts standing on a rooftop, one holding a giant butterfly net. Soon the zoo announced: "Rusty the red panda has been recovered, crated & is headed safely back to the National Zoo!"

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- Motherboard, Vice: One Degree of Separation in the Forever War 2 by Brian Castner (November 11, 2015)

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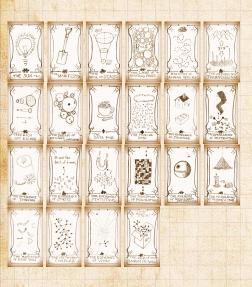
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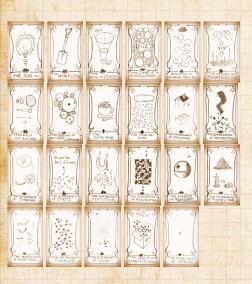
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The social world appears to be small... why?

Theory: how do we understand the small world property?

Connected random networks have short average path lengths:

$$\langle d_{AB} \rangle \sim \log(N)$$

N = population size, d_{AB} = distance between nodes A and B. PoCS | @pocsvox Small-world networks

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But: social networks aren't random...

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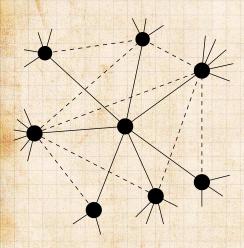
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Simple socialness in a network:



Need "clustering" (your friends are likely to know each other):

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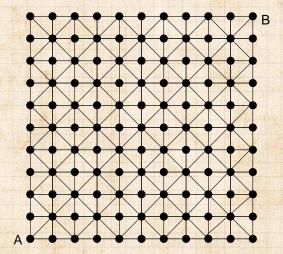
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Non-randomness gives clustering:



 $d_{AB}=10
ightarrow {
m too}$ many long paths.

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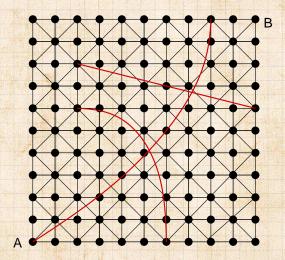
Generalized affiliation networks Nutshell







Randomness + regularity



Now have $d_{AB}=3$

 $\langle d \rangle$ decreases overall

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Introduced by Watts and Strogatz (Nature, 1998) [14] "Collective dynamics of 'small-world' networks."

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Introduced by Watts and Strogatz (Nature, 1998) [14] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:



neural network of C. elegans,

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- social networks of comic book characters,...

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networks

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- 🗞 social networks of comic book characters,...

Very weak requirements:

& local regularity + random short outs

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Small-world networks

Theory
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networks







Small-world networks

Introduced by Watts and Strogatz (Nature, 1998) [14] "Collective dynamics of 'small-world' networks."

Small-world networks were found everywhere:

- 🙈 neural network of C. elegans,
- 🙈 semantic networks of languages,
- actor collaboration graph,
- 🚓 food webs,
- 🗞 social networks of comic book characters,...

Very weak requirements:

& local regularity + random short cuts

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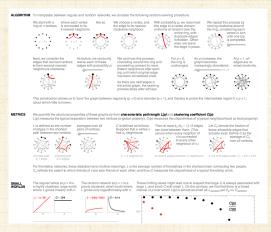
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Papers should be apps:



- Interactive figures and tables = windows into large data sets (empirical or simulated).

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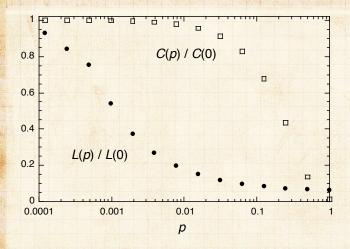
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The structural small-world property:



& L(p) = average shortest path length as a function of p

& C(p) = average clustring as a function of p

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Nutshell References







But are these short cuts findable?

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Nutshell







But are these short cuts findable?

Nope. [8]

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Nutshell







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Nope. [8]

Nodes cannot find each other quickly with any local search method.

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Nutshell







But are these short cuts findable?

Nope. [8]

Nodes cannot find each other quickly with any local search method.

Need a more sophisticated model...

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What can a local search method reasonably use?

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What can a local search method reasonably use?



How to find things without a map?

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What can a local search method reasonably use?



How to find things without a map?



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Need some measure of distance between friends and the target.









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What can a local search method reasonably use?

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How to find things without a map?

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Need some measure of distance between friends and the target.

References

Some possible knowledge:

Target's identity

Friends' popularity

Friends' identities

Where message has been





Jon Kleinberg (Nature, 2000) [8] "Navigation in a small world."

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Nutshell







Jon Kleinberg (Nature, 2000) [8] "Navigation in a small world."

Allowed to vary:

- 1. local search algorithm
 - and
- 2. network structure.

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Nutshell





Kleinberg's Network:

- 1. Start with regular d-dimensional cubic lattice
- 2. Add local links so nodes know all nodes within a distance *q*.
- 3. Add m short cuts per node
- 4. Connect i to j with probability

$$p_{ij} \propto x_{ij}^{-lpha}$$

0 = 0: random connections.

darge: reinforce local connections.

connections grow logarithmically in space.

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Theoretical optimal search:



"Greedy" algorithm.

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Theoretical optimal search:

- "Greedy" algorithm.
- Number of connections grow logarithmically (slowly) in space: $\alpha = d$.

Social golf.

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Nutshell







Theoretical optimal search:

- "Greedy" algorithm.
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Theoretical optimal search:

- "Greedy" algorithm.
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- Social golf.

Search time grows slowly with system size (like $\log^2 N$).

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Theoretical optimal search:

- "Greedy" algorithm.
- Number of connections grow logarithmically (slowly) in space: $\alpha = d$.
- Social golf.

Search time grows slowly with system size (like $\log^2 N$).

But: social networks aren't lattices plus links.

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Advances for understanding Kleinberg's model:



"Kleinberg Navigation in Fractal Small World Networks"

Roberson and ben-Avrahma, Phys. Rev. E, **74**, 017101, 2006. [10]



"Asymptotic behavior of the Kleinberg model"

Carmi et al., Phys. Rev. Lett., **102**, 238702, 2009. [4]



"Extended navigability of small world networks: Exact results and new insights"

Cartoza and De Los Rios, Phys. Rev. Lett., **2009**, 238703, 2009. [5] PoCS | @pocsvox Small-world networks

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If networks have hubs can also search well: Adamic et al. (2001)[1]

$$P(k_i) \propto k_i^{-\gamma}$$

where k = degree of node i (number of friends).

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Adamic et al. (2001)[1]

$$P(k_i) \propto k_i^{-\gamma}$$

where k = degree of node i (number of friends).

Basic idea: get to hubs first (airline networks). PoCS | @pocsvox Small-world networks

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Adamic et al. (2001)[1]

$$P(k_i) \propto k_i^{-\gamma}$$

where k = degree of node i (number of friends).

& Basic idea: get to hubs first (airline networks).

& But: hubs in social networks are limited.

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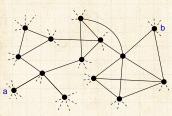






The problem

If there are no hubs and no underlying lattice, how can search be efficient?



Which friend of a is closest to the target b?

What does 'closest' mean?

What is 'social distance'?

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One approach: incorporate identity.

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One approach: incorporate identity.

Identity is formed from attributes such as:

Geographic location

Type of employment

Religious beliefs

Recreational activities.

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One approach: incorporate identity.

Identity is formed from attributes such as:

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Religious beliefs

Recreational activities.

Groups are formed by people with at least one similar attribute.

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Generalized affiliation networks Nutshell







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One approach: incorporate identity.

Identity is formed from attributes such as:

Geographic location

Type of employment

Religious beliefs

Recreational activities.

Groups are formed by people with at least one similar attribute.

Attributes ⇔ Contexts ⇔ Interactions ⇔ Networks.

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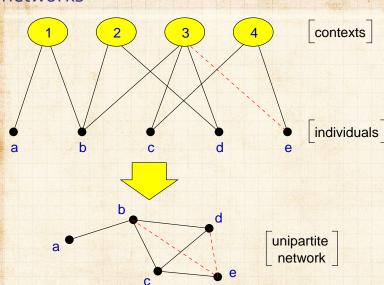
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Social distance—Bipartite affiliation networks



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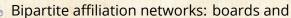
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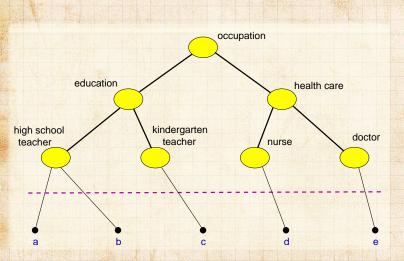








Social distance—Context distance



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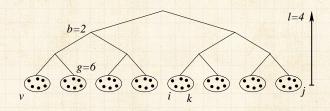
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Distance between two individuals $x_{i,j}$ is the height of lowest common ancestor.



$$x_{ij} = 3$$
, $x_{ik} = 1$, $x_{iv} = 4$.

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Individuals are more likely to know each other the closer they are within a hierarchy.

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- Individuals are more likely to know each other the closer they are within a hierarchy.

$$p_{ij} = c \exp\{-\alpha x_{ij}\}.$$

a = 0: random connections. a large: local connections. PoCS | @pocsvox Small-world networks

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netw

- Individuals are more likely to know each other the closer they are within a hierarchy.
- & Construct z connections for each node using

$$p_{ij} = c \exp\{-\alpha x_{ij}\}.$$

 $\alpha = 0$: random connections.

large: local connections.

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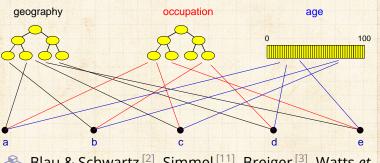






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Blau & Schwartz [2], Simmel [11], Breiger [3], Watts et al. [13]; see also Google+ Circles.

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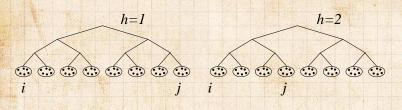
Experiments

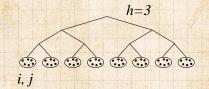
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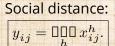








$$\begin{split} \vec{v}_i &= [1\ 1\ 1]^T, \, \vec{v}_j = [8\ 4\ 1]^T \\ x^1_{ij} &= 4, \ x^2_{ij} = 3, \ x^3_{ij} = 1. \end{split}$$



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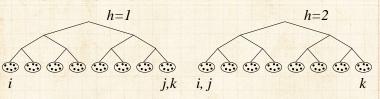






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Triangle inequality doesn't hold:



$$y_{ik} = 4 > y_{ij} + y_{jk} = 1 + 1 = 2.$$

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Individuals know the identity vectors of

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Individuals know the identity vectors of 1. themselves,

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends,

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends, and
- 3. the target.

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends, and
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Individuals can estimate the social distance between their friends and the target.

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Individuals know the identity vectors of

- 1. themselves,
- 2. their friends, and
- 3. the target.
- Individuals can estimate the social distance between their friends and the target.
- Use a greedy algorithm + allow searches to fail randomly.

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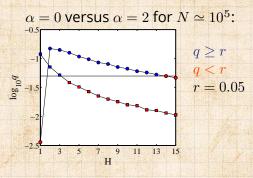
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The model-results—searchable networks



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q = probability an arbitrary message chain reaches atarget.



A few dimensions help.



Searchability decreases as population increases.



Precise form of hierarchy largely doesn't matter.



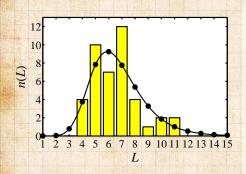




The model-results

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Milgram's Nebraska-Boston data:



Model parameters:



$$\approx z = 300, g = 100,$$

$$\& \alpha = 1, H = 2;$$

$$\langle L_{\rm model} \rangle \simeq 6.7$$

$$Alpha L_{\rm data} \simeq 6.5$$

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Social search—Data

Adamic and Adar (2003)

For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.

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Social search—Data

Adamic and Adar (2003)

- For HP Labs, found probability of connection as function of organization distance well fit by exponential distribution.
- Probability of connection as function of real distance $\propto 1/r$.

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Social Search—Real world uses

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- Tags create identities for objects
- Website tagging: bitly.com
 ✓
- 🖀 (e.g., Wikipedia)
- A Photo tagging: flickr.com
- Dynamic creation of metadata plus links between information objects.
- Folksonomy: collaborative creation of metadata







Social Search—Real world uses

Recommender systems:



Amazon uses people's actions to build effective connections between books.

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Social Search—Real world uses

Recommender systems:

- Amazon uses people's actions to build effective connections between books.
- Conflict between 'expert judgments' and tagging of the hoi polloi.

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Bare networks are typically unsearchable.

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Bare networks are typically unsearchable.

Paths are findable if nodes understand how network is formed.

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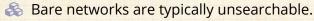
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Nutshell









Paths are findable if nodes understand how network is formed.

Importance of identity (interaction contexts).

Construction of peer-to-peer networks.

Construction of searchable information

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- Bare networks are typically unsearchable.
- Paths are findable if nodes understand how network is formed.
- Importance of identity (interaction contexts).
- Improved social network models.
 - Construction of peer-to-peer networks.

 Construction of searchable information databases.

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Neural reboot (NR):

Food-induced happiness

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