Semester projects

Principles of Complex Systems | @pocsvox CSYS/MATH 300, Fall, 2016 | #FallPoCS2016

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Dept. of Mathematics & Statistics | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont













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Requirements:

- 1. 2 minute introduction to project (nth week).
- 2. 4 minute final presentation.
- 3. Report: \geq 4 pages (single space), journal-style

Goals:

- 💫 Understand, critique, and communicate published work.
- Seed research papers or help papers along.



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The narrative hierarchy—Stories and Storytelling on all Scales: 🗗



1 to 3 word encapsulation = a soundbite = a buzzframe,

breakfast

dinner

- lunch

- 1 sentence, title,
- 🚳 few sentences, a haiku,
- 🙈 a paragraph, abstract,
- 🙈 short paper, essay,
- 🙈 long paper,
- 🚓 chapter,
- 备 book,
- **&** ...

Twitter—living in the now:







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Outline

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0.14

0.12

0.1 0.08

0.06

0.02

count fraction

Research opportunity: be involved in our socioinfo-algorithmo-econo-geo-technico-physical systems research group studying Twitter and other wordful large data sets.

6 8 10 12 14 16 18 20 22 24 hour of day (local time)





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Rummage round in the papers we've covered in our weekly Complex Systems Reading Group at UVM.



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Sociotechnical phenomena—Foldit:





"Predicting protein structures with a multiplayer online game." Cooper et al., Nature, 2010. [14]





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topics:

- Explore the Sociotechnocene.
- Develop and elaborate an online experiment to study some aspect of sociotechnical phenomena
- 🚓 e.g., collective search, cooperation, cheating, influence, creation, decision-making, language, belief, stories, etc.
- Part of the PLAY project.



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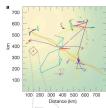
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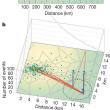
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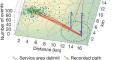
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- Study movement and interactions of people.
- Brockmann et al. [6] "Where's George" study.
- Barabasi's group: tracking movement via cell phones [23].







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Explore distances between points on the Earth as travel times.

The madness of modern geography:

& See Jonathan Harris's work here \Box and here \Box .





The Sixipedia!







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"A universal model for mobility and migration patterns" Simini et al., Nature, **484**, 96–100, 2012. [37]



"The hidden geometry of complex, network-driven contagion phenomena" Brockmann and Helbing, Science, **342**, 1337–1342, 2013. [5]

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topics:

- Read and critique "Historical Dynamics: Why States Rise and Fall" by Peter Turchin. [41]
- & Can history be explained by differential equations?: Clyodynamics 🗷,
- Construct a working version of Psychohistory .
- "Big History"



"The life-spans of Empires" Samuel Arbesman, Historical Methods: A Journal of Quantitative and Interdisciplinary History, **44**, 127–129, 2011. [1]



Also see "Secular Cycles" .



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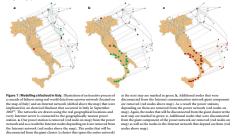
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Multilayer networks:

Explore "Catastrophic cascade of failures in interdependent networks" [7]. Buldyrev et al., Nature 2010.



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topics:

topics:

- Explore general theories on system robustness.
- Are there universal signatures that presage system failure?
- See "Early-warning signals for critical transitions" Scheffer et al., Nature 2009. [36]
- "Although predicting such critical points before they are reached is extremely difficult, work in different scientific fields is now suggesting the existence of generic early-warning signals that may indicate for a wide class of systems if a critical threshold is approaching."
- Robust-yet-fragile systems, HOT theory.

Study the human disease and disease gene

networks (Goh et al., 2007):







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HOT networks:

*001

"The "Robust yet Fragile" nature of the Internet"

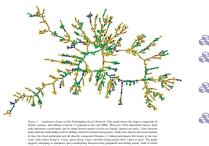
Doyle et al., Proc. Natl. Acad. Sci., 2005, 14497-14502, 2005. [19]





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Explore and critique Fowler and Christakis et al. work on social contagion of:



Obesity [10]

Smoking cessation [11]

Happiness [21]

& Loneliness [8]

One of many questions:

How does the (very) sparse sampling of a real social network affect their findings?

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topics:

Explore patterns, designed and undesigned, of cities and suburbs.



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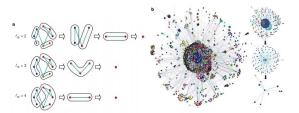


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topics:

- Explore "self-similarity of complex networks" [38, 39] First work by Song et al., Nature, 2005.
- See accompanying comment by Strogatz [40]
- See also "Coarse-graining and self-dissimilarity of complex networks" by Itzkovitz et al. [?]



topics:

- Study collective creativity arising out of social interactions
- Productivity, wealth, creativity, disease, etc. appear to increase superlinearly with population
- Start with Bettencourt et al.'s (2007) "Growth, innovation, scaling, and the pace of life in cities" [3]
- Dig into Bettencourt (2013) "The Origins of Scaling" in Cities" [3]

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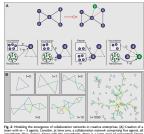
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topics:

Related papers:

- "Origins of fractality in the growth of complex networks" Song et al. (2006a) [39]
- "Skeleton and Fractal Scaling in Complex Networks" Go et al. (2006a) [22]
- "Complex Networks Renormalization: Flows and Fixed Points" Radicchi et al. (2008a) [35]

Study networks and creativity:



- Guimerà et al., Science 2005: [24] "Team Assembly Mechanisms Determine Collaboration Network Structure and Team Performance"
- Broadway musical industry
- Scientific collaboration in Social Psychology, Economics, Ecology, and Astronomy.











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Vague/Large:

- Study Yelp: is there Accounting for Taste?
- Study Metacritic: the success of stories.
- Study amazon's recommender networks.









See work by Sornette et al..

Wague/Large: Study Netflix's open data (movies and people form a bipartite graph).



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http://www.culturomics.org/

Google Books ngram viewer

Culturomics:

"Quantitative analysis of culture using millions of digitized

books" by Michel et al., Science, 2011

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topics:

More Vague/Large:

- How do countries depend on each other for water, energy, people (immigration), investments?
- A How is the media connected? Who copies whom?
- (Problem: Need to be able to measure interactions.)
- Investigate memetics, the 'science' of memes.
- A http://memetracker.org/
- Work on the evolution of proverbs and sayings.

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Physics/Society—Wars: Study work that started with Lewis Richardson's "Variation of the frequency of fatal quarrels with magnitude" in 1949.

Specifically explore Clauset et al. and Johnson et al.'s work [13, 28, 4] on terrorist attacks and civil wars

Richardson bonus: Britain's coastline, turbulence, weather prediction, ...

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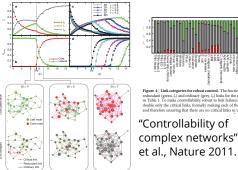
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topics:

More Vague/Large:

- How does advertising work collectively?
- Does one car manufacturers' ads indirectly help other car manufacturers?
- Ads for junk food versus fruits and vegetables.
- Ads for cars versus bikes versus walking.

topics:



"Controllability of complex networks" [32] Liu





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- Study phyllotaxis Z, how plants grow new buds and branches.
- Some delightful mathematics appears involving the Fibonacci series.
- Excellent work to start with: "Phyllotaxis as a Dynamical Self Organizing Process: Parts I, II, and III" by Douady and Couder [16, 17,



http://andbug.blogspot.com/



Wikipedia 🗹

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- regarding large-scale online games and Dunbar's number. [http://www.lifewithalacrity.com ☑]
- Recent work: "Network scaling reveals consistent fractal pattern in hierarchical mammalian societies" Hill et al. (2008) [26].

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topics:

The problem of missing data in networks:

- Clauset et al. (2008) "Hierarchical structure and the prediction of missing links in networks" [12]
- & Kossinets (2006) "Effects of missing data in social networks" [30]
- Much more ...

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topics:

topics:

- Study scientific collaboration networks.
- Mounds of data + good models.
- See seminal work by De Solla Price [15]. plus modern work by Redner, Newman, et al.
- We will study some of this in class...



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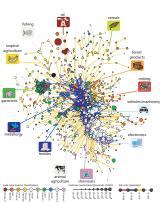
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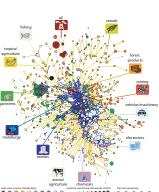
Archive References

- Study Kearns et al.'s experimental studies of people solving classical graph theory problems [29]
- "An Experimental Study of the Coloring Problem on Human Subject Networks"
- (Possibly) Run some of these experiments for our class.

topics:

- Study Hidalgo et al.'s "The Product **Space Conditions** the Development of Nations" [25]
- How do products depend on each other, and how does this network evolve?
- How do countries depend on each other for water, energy, people (immigration), investments?









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Study collective tagging (or folksonomy)

🗞 e.g., del.icio.us, flickr

See work by Bernardo Huberman et al. at HP labs.

Explore work by Doyle, Alderson, et al. as well as Pastor-Satorras et al. on the structure of the

Internet(s).

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Study games (as in game theory) on networks.

A For cooperation: Review Martin Nowak's piece in Science, "Five rules for the evolution of cooperation." [34] and related works.

Much work to explore: voter models, contagion-type models, etc.



networks form in these games? [9] See work by Johnson et al. on gang formation in the real world and in World of Warcraft (really!).







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topics:

- Semantic networks: explore word-word connection networks generated by linking semantically related words.
- Also: Networks based on morphological or phonetic similarity.
- More general: Explore language evolution
- One paper to start with: "The small world of human language" by Ferrer i Cancho and Solé [20]
- Study spreading of neologisms.
- Examine new words relative to existing words—is there a pattern? Phonetic and morphological similarities.
- Crazy: Can new words be predicted?
- Use Google Books n-grams as a data source.

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Social networks:

- Study social networks as revealed by email patterns, Facebook connections, tweets, etc.
- "Empirical analysis of evolving social networks" Kossinets and Watts, Science, Vol 311, 88-90, 2006. [31]
- "Inferring friendship network structure by using mobile phone data" Eagle, et al., PNAS, 2009.
- "Community Structure in Online Collegiate Social Networks" Traud et al., 2008.

http://arxiv.org/abs/0809.0690









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Voting

Score-based voting versus rank-based voting:

🙈 Balinski and Laraki [2] "A theory of measuring, electing, and ranking" Proc. Natl. Acad. Sci., pp. 8720–8725 (2007)

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topics:

More Vague/Large:

- Study spreading of anything where influence can be measured (very hard).
- Study any interesting micro-macro story to do with evolution, biology, ethics, religion, history, food, international relations, ...
- Data is key.

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topics:

Vague/Large:

Study how the Wikipedia's content is interconnected.



"Connecting every bit of knowledge: The structure of Wikipedia's First Link Network"

Ibrahim, Danforth, and Dodds, Available online at https://arxiv.org/abs/1605.00309, 2016. [27]

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