

Semester projects

Principles of Complex Systems | @pocsvox
CSYS/MATH 300, Fall, 2016 | #FallPoCS2016

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Suggestions for
Projects
Archive
References

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Vermont Advanced Computing Core | University of Vermont



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Suggestions for
Projects

Archive

References



Outline

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The Plan

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Suggestions for
Projects

Archive

References

Suggestions for Projects

Archive



References



Requirements:

1. 2 minute introduction to project (n th week).
2. 4 minute final presentation.
3. Report: ≥ 4 pages (single space), journal-style

Goals:

-  Understand, critique, and communicate published work.
-  Seed research papers or help papers along.

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Projects


Archive


References





The narrative hierarchy—Stories and Storytelling on all Scales: ↗





 1 to 3 word encapsulation = a
soundbite = a buzzframe,


 1 sentence, title,


 few sentences, a haiku,

 a paragraph, abstract,

 short paper, essay,

 long paper,

 chapter,

 book,

 ...



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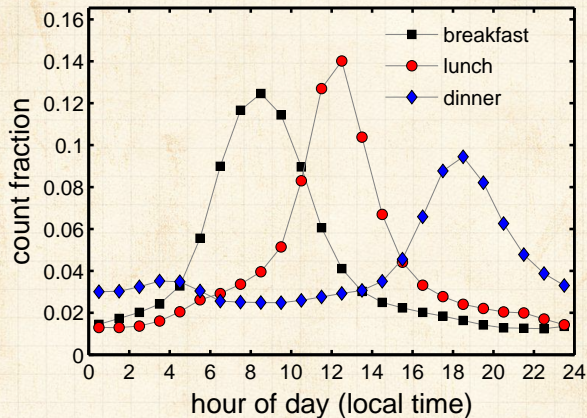
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Twitter—living in the now:



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Projects

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References



Research opportunity: be involved in our socio-info-algorithmo-econo-geo-technico-physical systems research group studying Twitter and other wordful large data sets.



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Archive

References

Rummage round in the papers  we've covered in our weekly Complex Systems Reading Group at UVM.







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Archive

References

-  Explore the Sociotechnocene.
-  Develop and elaborate an **online experiment** to study some aspect of **sociotechnical phenomena**
-  e.g., collective search, cooperation, cheating, influence, creation, decision-making, language, belief, stories, etc.
-  Part of the PLAY project.



The Sixipedia!



SIXIPEDIA

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Archive

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Sociotechnical phenomena—Foldit:

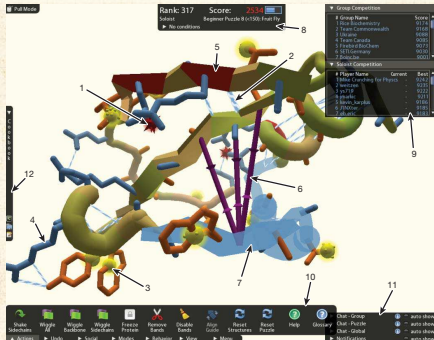



Figure 1 | Foldit screenshot illustrating tools and visualizations. The visualizations include a clash representing atoms that are too close (arrow 1); a hydrogen bond (arrow 2); a hydrophobic side chain with a yellow blob because it is exposed (arrow 3); a hydrophilic side chain (arrow 4); and a segment of the backbone that is red due to high residue energy (arrow 5). The players can make modifications including 'rubber bands' (arrow 6), which add constraints to guide automated tools, and freezing (arrow 7), which

prevents degrees of freedom from changing. The user interface includes information about the player's current status, including score (arrow 8); a leaderboard (arrow 9), which shows the scores of other players and groups; toolbars for accessing tools and options (arrow 10); chat for interacting with other players (arrow 11); and a 'cookbook' for making new automated tools or 'recipes' (arrow 12).

 **"Predicting protein structures with a multiplayer online game."** Cooper et al., Nature, 2010. ^[14]

 Also: [zooniverse](#), [ESP game](#), [captchas](#).

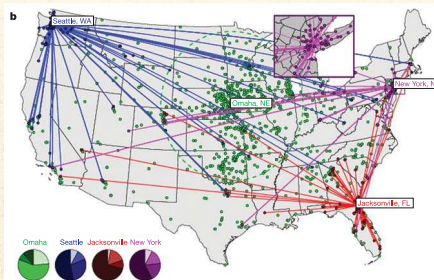
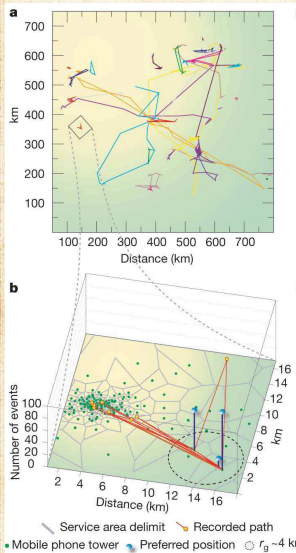
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Projects

Archive

References





- Study movement and interactions of people.
- Brockmann *et al.* [6] "Where's George" study.
- Barabasi's group: tracking movement via cell phones [23].



The madness of modern geography:

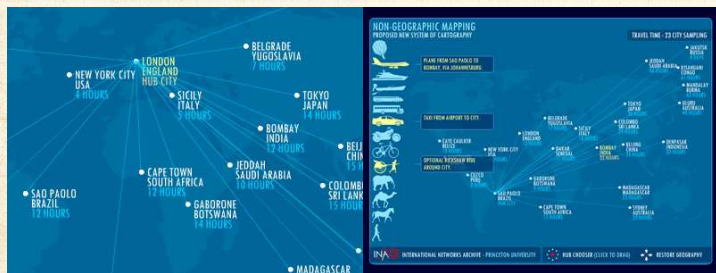
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Projects

Archive

References




 Explore distances between points on the Earth as travel times.

 See Jonathan Harris's work [here](#) and [here](#).






"A universal model for mobility and migration patterns" 

Simini et al.,

Nature, **484**, 96–100, 2012. ^[37]



"The hidden geometry of complex, network-driven contagion phenomena" 

Brockmann and Helbing,

Science, **342**, 1337–1342, 2013. ^[5]



Multilayer networks:

Explore “Catastrophic cascade of failures in interdependent networks” [7]. Buldyrev et al., Nature 2010.

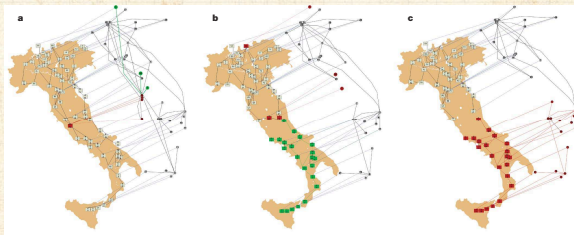


Figure 1 | Modelling a blackout in Italy. Illustration of an iterative process of a cascade of failures using real-world data from a power network (located on the map of Italy) and an Internet network (shifted above the map) that were implicated in an electrical blackout that occurred in Italy in September 2003³⁹. The networks are drawn using the real geographical locations and every Internet server is connected to the geographically nearest power station. **a.** One power station is removed (red node on map) from the power network and as a result the Internet nodes depending on it are removed from the Internet network (red nodes above the map). The nodes that will be disconnected from the giant cluster (a cluster that spans the entire network)

at the next step are marked in green. **b.** Additional nodes that were disconnected from the Internet communication network giant component are removed (red nodes above map). As a result the power stations depending on them are removed from the power network (red nodes on map). Again, the nodes that will be disconnected from the giant cluster at the next step are marked in green. **c.** Additional nodes that were disconnected from the giant component of the power network are removed (red nodes on map) as well as the nodes in the Internet network that depend on them (red nodes above map).



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Projects

Archive








References




"The "Robust yet Fragile" nature of the
Internet" 




Doyle et al.,
Proc. Natl. Acad. Sci., **2005**, 14497–14502,
2005. ^[19]



-  Read and critique "Historical Dynamics: Why States Rise and Fall" by Peter Turchin. ^[41]
-  Can history be explained by differential equations?: Clyodynamics 
-  Construct a working version of Psychohistory 
-  "Big History" 



"The life-spans of Empires" 
Samuel Arbesman,
Historical Methods: A Journal of
Quantitative and Interdisciplinary History,
44, 127–129, 2011. ^[1]

- 
-  Also see "Secular Cycles" 

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References



- Explore general theories on **system robustness**.
- Are there **universal signatures** that presage system failure?
- See “Early-warning signals for critical transitions” Scheffer et al., Nature 2009. ^[36]
- “Although predicting such critical points before they are reached is extremely difficult, work in different scientific fields is now suggesting the existence of generic early-warning signals that may indicate for a wide class of systems if a critical threshold is approaching.”
- Robust-yet-fragile systems, HOT theory.

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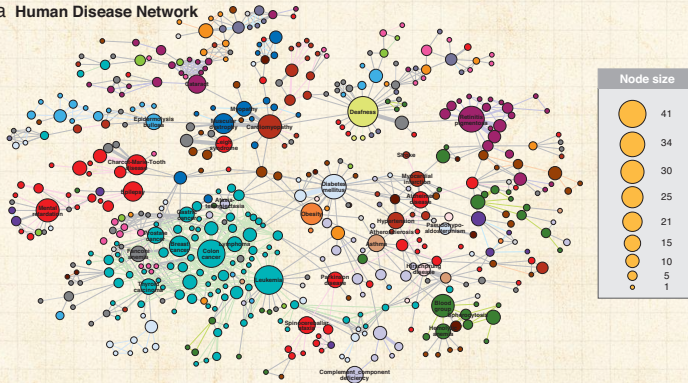
References





Study the human disease and disease gene networks (Goh *et al.*, 2007):

a Human Disease Network



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topics:

Explore and critique Fowler and Christakis et al. work on social contagion of:

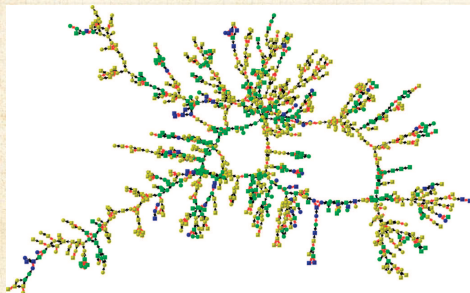






Figure 1. Loneliness clusters in the Framingham Social Network. This graph shows the largest component of friends, spouses, and siblings at Exam 7 (centered on the year 2000). There are 1,019 individuals shown. Each node represents a participant, and its shape denotes gender (circles are female, squares are male). Lines between nodes indicate relationship (red for siblings, black for friends and spouses). Node color denotes the mean number of days the focal participant and all directly connected (Distance 1) linked participants felt lonely in the past week, with yellow being 0–1 days, green being 2 days, and blue being greater than 3 days or more. The graph suggests clustering in loneliness and a relationship between being peripheral and feeling lonely, both of which are confirmed by statistical models discussed in the main text.

-  Obesity [10]
-  Smoking cessation [11]
-  Happiness [21]
-  Loneliness [8]

One of many questions:

How does the (very) sparse sampling of a real social network affect their findings?

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Archive

References



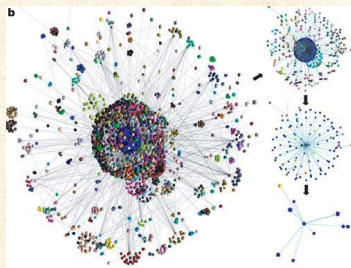
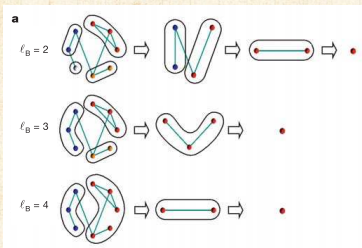
- Explore “self-similarity of complex networks” [38, 39]
First work by Song *et al.*, Nature, 2005.
- See accompanying comment by Strogatz [40]
- See also “Coarse-graining and self-dissimilarity of complex networks” by Itzkovitz *et al.* [?]

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References



Related papers:

-  "Origins of fractality in the growth of complex networks"
Song et al. (2006a) [39]
-  "Skeleton and Fractal Scaling in Complex Networks"
Go et al. (2006a) [22]
-  "Complex Networks Renormalization: Flows and Fixed Points"
Radicchi et al. (2008a) [35]

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Archive

References





Explore patterns, designed and undesigned, of cities and suburbs.



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[Suggestions for
Projects](#)

[Archive](#)

[References](#)







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Projects

Archive

References

-  Study collective creativity arising out of social interactions
-  Productivity, wealth, creativity, disease, etc. appear to increase superlinearly with population
-  Start with Bettencourt et al.'s (2007) "Growth, innovation, scaling, and the pace of life in cities" [3]
-  Dig into Bettencourt (2013) "The Origins of Scaling in Cities" [3]



Study networks and creativity:

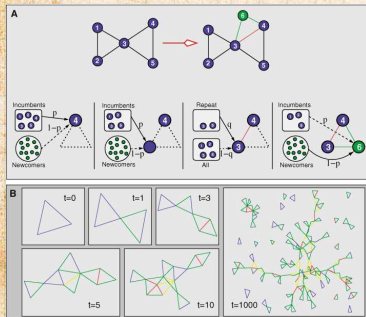


Fig. 2. Modeling the emergence of collaboration networks in creative enterprises. (A) Creation of a team with $m = 3$ agents. Consider, at time zero, a collaboration network comprising five agents, all incumbents (blue circles). Along with the incumbents, there is a large pool of newcomers (green circles) available to participate in new teams. Each agent in a team has a probability p of being drawn from the pool of incumbents and a probability $1 - p$ of being drawn from the pool of newcomers. For the second and subsequent agents selected from the incumbents' pool: (i) with probability q , the new agent is randomly selected from among the set of collaborators of a randomly selected incumbent already in the team; (ii) otherwise, he or she is selected at random among all incumbents in the network. For concreteness, let us assume that incumbent 4 is selected as the first agent in the new team (leftmost box). Let us also assume that the second agent is an incumbent, too (center-left box). In this example, the second agent is a past collaborator of agent 4, specifically agent 3 (center-right box). Lastly, the third agent is selected from the pool of newcomers; this agent becomes incumbent 6 (rightmost box). In these boxes and in the following panels and figures, blue lines indicate newcomer-newcomer collaborations, green lines indicate newcomer-incumbent collaborations, yellow lines indicate new incumbent-incumbent collaborations, and red lines indicate repeat collaborations. (B) Time evolution of the network of collaborations according to the model for $p = 0.5$, $q = 0.5$, and $m = 3$.



Guimerà et al., Science 2005: [24] "Team Assembly Mechanisms Determine Collaboration Network Structure and Team Performance"



Broadway musical industry



Scientific collaboration in Social Psychology, Economics, Ecology, and Astronomy.

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Vague/Large:

- Study Yelp: is there Accounting for Taste?
- Study Metacritic: the success of stories.
- Study amazon's recommender networks.

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References

Customers Who Bought This Item Also Bought










Item	Author	Rating	Price
Harry Potter Schoolbooks: Fantastic Beasts and...	J.K. Rowling	★★★★☆ (465)	\$10.19
The Tales of Beedle the Bard, Collector's E...	J. K. Rowling	★★★★☆ (153)	
Harry, A History: The True Story of a Boy Wizard...	Melissa Anelli	★★★★☆ (52)	\$10.88
Inkdeath (Inkheart)	Cornelia Funke	★★★★☆ (41)	\$16.49

See work by Sornette *et al.*

- Study Netflix's open data (movies and people form a bipartite graph).



More Vague/Large:

-  How do countries depend on each other for water, energy, people (immigration), investments?
-  How is the media connected? Who copies whom?
-  (Problem: Need to be able to measure interactions.)
-  Investigate memetics, the 'science' of memes.
-  <http://memetracker.org/> 
-  Work on the evolution of proverbs and sayings.

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Archive

References







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Projects

Archive

References

More Vague/Large:

-  How does **advertising** work collectively?
-  Does one car manufacturers' ads indirectly help other car manufacturers?
-  Ads for junk food versus fruits and vegetables.
-  Ads for cars versus bikes versus walking.



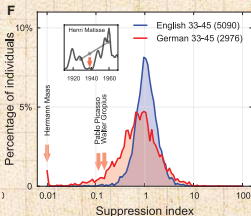
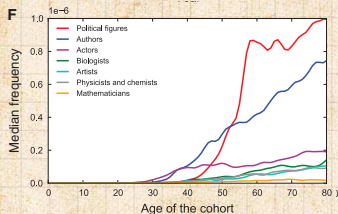
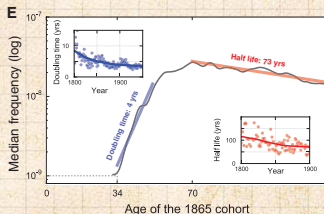
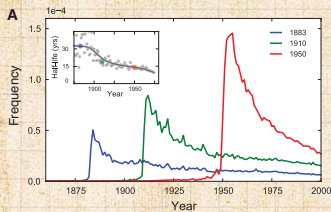
“Quantitative analysis of culture using millions of digitized books” by Michel et al., Science, 2011 [33]

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Projects

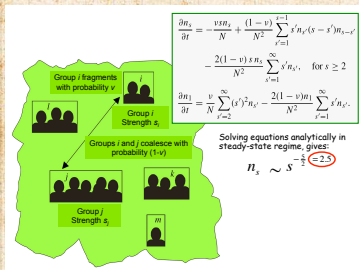
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References





<http://www.culturomics.org/>
Google Books ngram viewer





 **Physics/Society—Wars:**
Study work that started with Lewis Richardson’s “Variation of the frequency of fatal quarrels with magnitude” in 1949.

 Specifically explore Clauset et al. and Johnson et al.’s work [13, 28, 4] on terrorist attacks and civil wars

 Richardson bonus: Britain’s coastline, turbulence, weather prediction, ...

- The Plan
- Suggestions for Projects
- Archive
- References



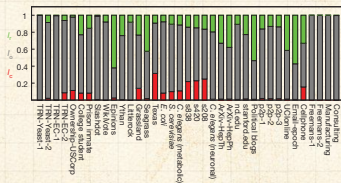
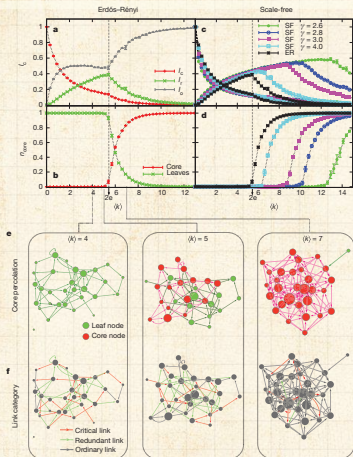






Figure 4 | Link categories for robust control. The fractions of critical (red, L_c), redundant (green, L_r) and ordinary (grey, L_o) links for the real networks named in Table 1. To make controllability robust to link failures, it is sufficient to double only the critical links, formally making each of these links redundant and therefore ensuring that there are no critical links in the system.

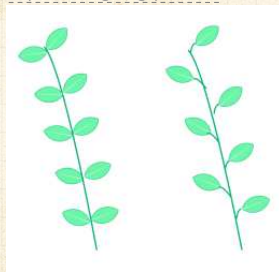
“Controllability of complex networks”^[32] Liu et al., Nature 2011.



-  Study phyllotaxis , how plants grow new buds and branches.
-  Some delightful mathematics appears involving the Fibonacci series.
-  Excellent work to start with: "Phyllotaxis as a Dynamical Self Organizing Process: Parts I, II, and III" by Douady and Couder ^[16, 17, 18]



<http://andbug.blogspot.com/> 



[Wikipedia](#) 

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Suggestions for
Projects
Archive
References



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Suggestions for
Projects

Archive

References

The problem of missing data in networks:



Clauset et al. (2008)

“Hierarchical structure and the prediction of missing links in networks” [12]




Kossinets (2006)


“Effects of missing data in social networks” [30]




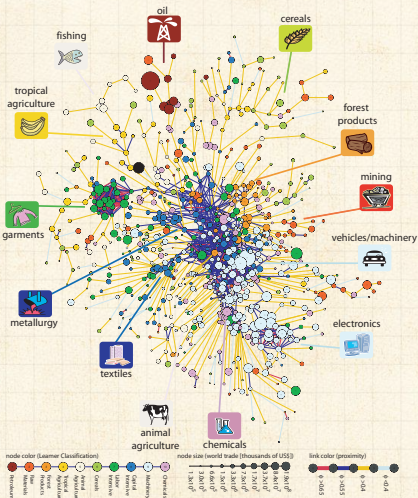
Much more ...



 Study Hidalgo et al.'s "The Product Space Conditions the Development of Nations" [25]

 How do products depend on each other, and how does this network evolve?

 How do countries depend on each other for water, energy, people (immigration), investments?



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Archive

References










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Projects

Archive

References

-  Explore Dunbar's number 
-  See here  and here  for some food for thought regarding large-scale online games and Dunbar's number. [<http://www.lifewithalacrity.com> 
-  Recent work: "Network scaling reveals consistent fractal pattern in hierarchical mammalian societies" Hill et al. (2008) ^[26].







topics:

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Suggestions for
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Archive

References

-  Study scientific collaboration networks.
-  Mounds of data + good models.
-  See seminal work by De Solla Price^[15].
plus modern work by Redner, Newman, *et al.*
-  We will study some of this in class...






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Projects

Archive

References

-  Study Kearns et al.'s experimental studies of people solving classical graph theory problems [29]
-  "An Experimental Study of the Coloring Problem on Human Subject Networks"
-  (Possibly) Run some of these experiments for our class.






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Suggestions for
Projects

Archive

References

-  Study **collective tagging** (or folksonomy)
-  e.g., del.icio.us, flickr
-  See work by Bernardo Huberman et al. at HP labs.






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Projects

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References

-  Study games (as in game theory) on networks.
-  For cooperation: Review Martin Nowak's piece in Science, "Five rules for the evolution of cooperation." [34] and related works.
-  Much work to explore: voter models, contagion-type models, etc.



-  **Semantic networks:** explore word-word connection networks generated by linking semantically related words.
-  Also: Networks based on morphological or phonetic similarity.
-  More general: Explore **language evolution**
-  One paper to start with: “The small world of human language” by Ferrer i Cancho and Solé [20]
-  Study spreading of neologisms.
-  Examine new words relative to existing words—is there a pattern? Phonetic and morphological similarities.
-  **Crazy:** Can new words be predicted?
-  Use Google Books n-grams as a data source.

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Projects

Archive

References



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Suggestions for
Projects

Archive

References



Explore work by Doyle, Alderson, et al. as well as Pastor-Satorras et al. on the structure of the Internet(s).





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Projects






Archive

References

-  Review: Study Castronova's and others' work on massive multiplayer online games. How do social networks form in these games? ^[9]
-  See work by Johnson et al. on gang formation in the real world and in World of Warcraft (really!).



Social networks:

-  Study social networks as revealed by email patterns, Facebook connections, tweets, etc.
-  "Empirical analysis of evolving social networks" Kossinets and Watts, Science, Vol 311, 88-90, 2006. ^[31]
-  "Inferring friendship network structure by using mobile phone data" Eagle, et al., PNAS, 2009.
-  "Community Structure in Online Collegiate Social Networks"
Traud et al., 2008.
<http://arxiv.org/abs/0809.0690> 

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Suggestions for
Projects

Archive

References



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Suggestions for
Projects

Archive

References

Score-based voting versus rank-based voting:



Balinski and Laraki^[2]

“A theory of measuring, electing, and ranking”
Proc. Natl. Acad. Sci., pp. 8720–8725 (2007)






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Suggestions for
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Archive

References

More Vague/Large:

-  Study spreading of anything where influence can be measured (very hard).
-  Study any interesting micro-macro story to do with evolution, biology, ethics, religion, history, food, international relations, ...
-  Data is key.




topics:

Vague/Large:



Study how the Wikipedia's content is interconnected.



“Connecting every bit of knowledge: The structure of Wikipedia’s First Link Network” 

Ibrahim, Danforth, and Dodds,
Available online at

<https://arxiv.org/abs/1605.00309>, 2016. [27]



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Projects

Archive




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The life-spans of empires.
[Historical Methods: A Journal of Quantitative and Interdisciplinary History, 44:127–129, 2011. pdf](#) ↗
- [2] M. Balinski and R. Laraki.
A theory of measuring, electing, and ranking.
[Proc. Natl. Acad. Sci., 104\(21\):8720–8725, 2007. pdf](#) ↗
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Growth, innovation, scaling, and the pace of life in cities.
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References



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The hidden geometry of complex, network-driven contagion phenomena.
[Science](#), 342:1337–1342, 2013. [pdf](#) 
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The scaling laws of human travel.
[Nature](#), pages 462–465, 2006. [pdf](#) 

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Suggestions for
Projects

Archive

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Catastrophic cascade of failures in interdependent networks.

[Nature](#), 464:1025–1028, 2010. pdf ↗

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Alone in the crowd: The structure and spread of loneliness in a large social network.

[Journal of Personality and Social Psychology](#), 97:977–991, 2009. pdf ↗

- [9] E. Castronova.

Synthetic Worlds: The Business and Culture of Online Games.

University of Chicago Press, Chicago, IL, 2005.




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Archive

References



- [10] N. A. Christakis and J. H. Fowler.
The spread of obesity in a large social network
over 32 years.
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- [11] N. A. Christakis and J. H. Fowler.
The collective dynamics of smoking in a large
social network.
[New England Journal of Medicine](#), 358:2249–2258,
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Projects

Archive

References



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On the Frequency of Severe Terrorist Events.
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M. Beenen, A. Leaver-Fay, D. Baker, Z. Popović,
and F. players.
Predicting protein structures with a multiplayer
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[Nature](#), 466:756–760, 466. [pdf](#) 
- [15] D. J. de Solla Price.
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Suggestions for
Projects


Archive


References



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Phyllotaxis as a dynamical self organizing process
Part I: The spiral modes resulting from
time-periodic iterations.
[J. Theor. Biol., 178:255–274, 1996. pdf](#) 

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Phyllotaxis as a dynamical self organizing process
Part II: The spontaneous formation of a
periodicity and the coexistence of spiral and
whorled patterns.
[J. Theor. Biol., 178:275–294, 1996. pdf](#) 

- [18] S. Douady and Y. Couder.
Phyllotaxis as a dynamical self organizing process
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Archive


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The “Robust yet Fragile” nature of the Internet.
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