

Introduction

Matrixology (Linear Algebra)—Episode 1/24 MATH 122, Fall, 2016

Prof. Peter Dodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center
Vermont Advanced Computing Core | University of Vermont



$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$



Licensed under the *Creative Commons Attribution-NonCommercial-ShareAlike 3.0 License*.



These slides are brought to you by:

Episode 1/24:
Introduction

Sealie & Lambie
Productions



Exciting Admin

Importance

Usages

Key problems

Three ways of
looking...

Colbert on
Equations

References

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

Outline

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

Episode 1/24:

Introduction

Exciting Admin

Importance

Usages


Key problems

Three ways of looking...

Colbert on Equations

References

$$\begin{bmatrix} I \heartsuit \\ N(A^T) \end{bmatrix}$$

- ▶ **Instructor:** Prof. Peter Dodds
- ▶ **Lecture room and meeting times:**
Perkins 107,
Tuesday and Thursday, 10:05 am to 11:20 am
- ▶ **Office:** Farrell Hall, second floor, Trinity Campus
- ▶ **E-mail:** peter.dodds@uvm.edu
- ▶ **Course website:**
<http://www.uvm.edu/~pdodds/teaching/courses/2016-08UVM-122> 
- ▶ **Textbook:** "Introduction to Linear Algebra" (3rd or 4th or 5th edition) by Gilbert Strang (published by Wellesley-Cambridge Press).

Exciting Admin

Importance

Usages

Key problems

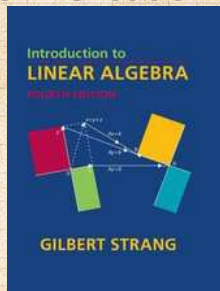
Three ways of looking...

Colbert on Equations

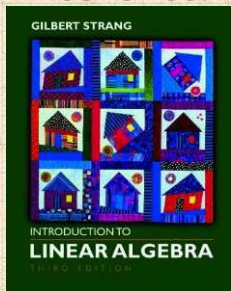
References

$$\begin{bmatrix} I & \heartsuit \\ & N(A^T) \end{bmatrix}$$

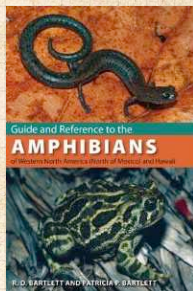
Our Textbook of Excellence:



4th Edition



3rd Edition



Unhelpful

Episode 1/24:
Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

▶ "Introduction to Linear Algebra"
by Gil Strang

▶ Textbook website:
<http://math.mit.edu/linearalgebra/>


▶ MIT Open Courseware site for 18.06
(=Linear Algebra):
<http://ocw.mit.edu/...linear-algebra-spring-2010/>

$$\begin{bmatrix} I \\ \heartsuit \\ N(A^T) \end{bmatrix}$$

Money quote from George Cobb's review of Strang's book:

Do you want a book written by a mathematician with a lifetime experience using linear algebra to understand important, authentic, applied problems, a former president of the Society for Industrial and Applied Mathematics, ...

or do you want a book shaped mainly by the [a]esthetics of pure mathematicians with only a weak, theoretical connection to how linear algebra is used in the natural and social sciences?

- ▶ George Cobb: Robert L. Rooke Professor of Mathematics and Statistics, Mount Holyoke College
- ▶ Full review [here](#)  [amazon]

[Exciting Admin](#)[Importance](#)[Usages](#)[Key problems](#)[Three ways of looking...](#)[Colbert on Equations](#)[References](#)

A hand-drawn logo consisting of the text "I ♥ N(A^T)" enclosed in large, hand-drawn square brackets. The heart symbol is simple, and the letters are in a slightly irregular, hand-drawn font.

Gil Strang, Exalted Friend of the Matrix:

Episode 1/24:
Introduction

- ▶ Professor of Mathematics at MIT since 1962.



These are 121 cupcakes with my favorite $\begin{bmatrix} -1 & 2 \\ -1 & -1 \end{bmatrix}$ matrix. It was the day before Thanksgiving and two days before my birthday. A happy surprise.

- ▶ Many awards including MAA Haimo Award [↗](#) for Distinguished College or University Teaching of Mathematics
- ▶ Rhodes Scholar.
- ▶ Legend.

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

- ▶ More on Laplacian matrices, graphs, and other madnesses here [↗](#).
- ▶ (Strang's Wikipedia page is here [↗](#)).

$$\begin{bmatrix} I \heartsuit \\ N(A^T) \end{bmatrix}$$



Admin:

Episode 1/24:

Introduction

Potential paper products:

1. Outline

Papers to read:

1. "The Fundamental Theorem of Linear Algebra" [2]
2. "Too Much Calculus" [3]

Office hours:

- ▶ 10:00 to 11:55 am Wednesdays,
Farrell Hall, second floor, Trinity Campus

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

Team Matrixology

Episode 1/24:

Introduction

We may try out Slack:

- ▶ Place for discussions about all things PoCS including assignments and projects.
- ▶ Once invited, please sign up here:
<http://team-matrixology.slack.com>
- ▶ Very good: Install Slack app on laptops, tablets, phone.
- ▶ Everyone will behave wonderfully.

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References



$$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$$



Grading breakdown:

Episode 1/24:

Introduction

1. Levels (40%)

- ▶ Ten one-week assignments.
- ▶ Lowest assignment score will be dropped.
- ▶ The last assignment cannot be dropped!
- ▶ Each assignment will have a random bonus point question which has nothing to do with linear algebra.

2. Challenge Levels (30%)

- ▶ Three 75 minutes tests distributed throughout the course, all of equal weighting.

3. Final Boss Level (20%)

- ▶ \leq Three hours of joyful celebration.
- ▶ Thursday, December 15, 1:30 pm to 4:15 pm, in Perkins 107.

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

$$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$$

Grading breakdown:

4. Mini-levels (10%)

- ▶ Most meeting times will end with a 10 to 15 minute mini-level.
- ▶ There will be around 20 mini-levels.

5. Homework (0%)—Problems assigned online from the textbook. Doing these exercises will be most beneficial and will increase happiness.

6. General existence—it is extremely desirable that students attend class, and class presence will be taken into account if a grade is borderline.

Episode 1/24:
Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

$$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$$

Questions are worth 3 points according to the following scale:

- ▶ 3 = correct or very nearly so.
- ▶ 2 = acceptable but needs some revisions.
- ▶ 1 = needs major revisions.
- ▶ 0 = way off.

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

Schedule: The course will mainly cover chapters 2 through 6 of the textbook. (You should know all about Chapter 1.)

Week # (dates)	Tuesday	Thursday
1 (8/30 and 9/01)	$\mathbf{A}\vec{x} = \vec{b}$	$\mathbf{A}\vec{x} = \vec{b}$ + Level 1
2 (9/06 and 9/08)	$\mathbf{A}\vec{x} = \vec{b}$	$\mathbf{A}\vec{x} = \vec{b}$ + Level 2
3 (9/13 and 9/15)	$\mathbf{A}\vec{x} = \vec{b}$	$\mathbf{A}\vec{x} = \vec{b}$ + Level 3
4 (9/20 and 9/22)	$\mathbf{A}\vec{x} = \vec{b}$ and review	<i>Challenge Level 1</i>
5 (9/27 and 9/29)	Big picture	Big picture + Level 4
6 (10/04 and 10/06)	Big picture	Big picture + Level 5
7 (10/11 and 10/13)	Big picture	Big picture + Level 6
8 (10/18 and 10/20)	Big picture	<i>Challenge Level 2</i>
9 (10/25 and 10/27)	Normal equation	Gram-Schmidt Process + Level 7
10 (11/01 and 11/03)	Eigenstuff	Eigenstuff + Level 8
11 (11/08 and 11/10)	Determinants	Determinants + Level 9
12 (11/15 and 11/17)	Eigenstuff	textitChallenge Level 3
13 (11/22 and 11/24)	Thanksgiving	Thanksgiving
14 (11/29 and 12/01)	Positive Definite Matrices + Level 10	SVD
15 (12/06)	SVD	—

Important dates:

1. Classes run from Tuesday, August 30 to Tuesday, December 6.
2. Add/Drop, Audit, Pass/No Pass deadline—Monday, September 12.
3. Last day to withdraw—Monday, October 31 (Sadness!).
4. Reading and Exam period—Saturday, December 10 to Friday, December 16.

More stuff:

Do check your zoo account for updates regarding the course.

Academic assistance: Anyone who requires assistance in any way (as per the ACCESS program or due to athletic endeavors), please see or contact me as soon as possible.

Episode 1/24:

Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$



More stuff:

Episode 1/24:

Introduction

Being good people:

1. In class there will be no electronic gadgetry, no cell phones, no beeping, no text messaging, etc. You really just need your brain, some paper, and a writing implement here (okay, and Matlab).
2. Second, I encourage you to email me questions, ideas, comments, etc., about the class but request that you please do so in a respectful fashion.
3. Finally, as in all UVM classes, **Academic honesty** will be expected and departures will be dealt with appropriately. See <http://www.uvm.edu/cses/> for guidelines.

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

$$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$$

Even more stuff:

Late policy: Unless in the case of an emergency (a real one) or if an absence has been predeclared and a make-up version sorted out, assignments that are not turned in on time or tests that are not attended will be given 0%.

Computing: Approximately 2 out of 10 questions per assignment will be Matlab based.

Note: for assignment problems, written details of calculations will be required.

[Exciting Admin](#)[Importance](#)[Usages](#)[Key problems](#)[Three ways of looking...](#)[Colbert on Equations](#)[References](#)

Why are we doing this?

Big deal: Linear Algebra is a body of mathematics that deals with **discrete problems**.

Many things are discrete:

- ▶ Information (0's & 1's, letters, words)
- ▶ People (sociology)
- ▶ Networks (the Web, people again, food webs, ...)
- ▶ Sounds (musical notes)

Even more:



If real data is continuous, we almost always discretize it (0's and 1's)

Episode 1/24:
Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

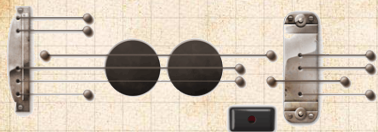
$$\begin{bmatrix} I \\ \heartsuit \\ N(A^T) \end{bmatrix}$$



Why are we doing this?

Linear Algebra is used in many fields to solve problems:

- ▶ Engineering
- ▶ Computer Science
- ▶ Physics
- ▶ Biology
- ▶ Ecology
- ▶ Economics
- ▶ Science of the Sociotechnocene



Big example:
[Google's Pagerank](#)

Some truth:

- ▶ Linear Algebra is as important as Calculus...
- ▶ Calculus \equiv the blue pill...

Episode 1/24:
Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

$$\begin{bmatrix} I \\ \heartsuit \\ N(A^T) \end{bmatrix}$$

Why are we doing this?

Episode 1/24:

Introduction

Exciting Admin

Importance

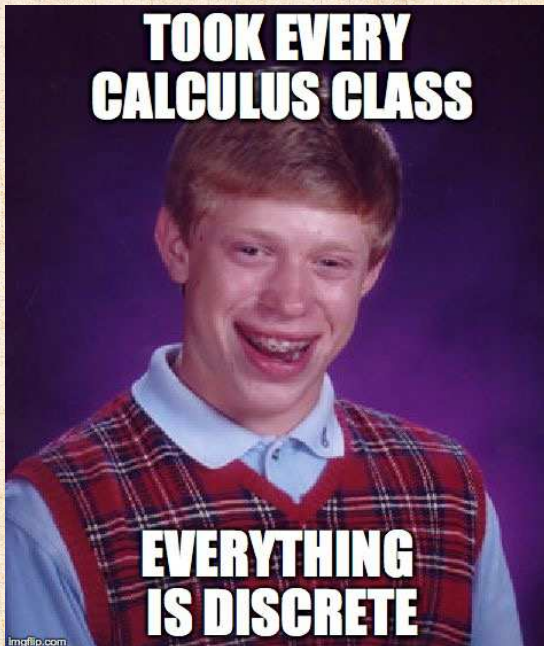
Usages

Key problems

Three ways of looking...

Colbert on Equations

References



$$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$$



You are now choosing the red pill:

Episode 1/24:

Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References



$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

The Truth:

Episode 1/24:

Introduction

Exciting Admin

Importance

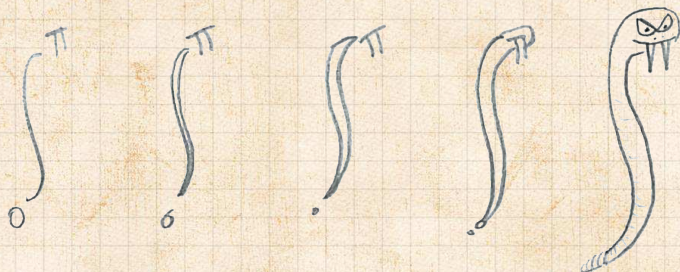
Usages

Key problems

Three ways of looking...

Colbert on Equations

References



► Calculus is the Serpent's Mathematics.

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

The Platypus of Truth:

Episode 1/24:

Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

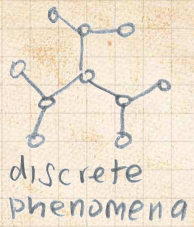
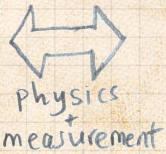


$$\begin{bmatrix} I & \heartsuit \\ N(A^T) \end{bmatrix}$$

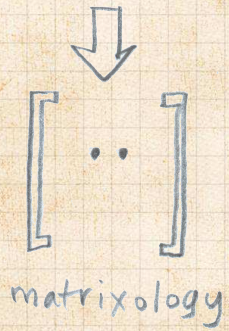
► Platypuses are masters of Linear Algebra.

The Actual Truth:

problem



tools



describe + explain
create + share

Matrices as gadgets:

Episode 1/24:
Introduction

A matrix A transforms a vector \vec{x} into a new vector \vec{x}' through matrix multiplication (whatever that is):

$$\vec{x}' = A \vec{x}$$

We can use matrices to:

- ▶ Grow vectors
- ▶ Shrink vectors
- ▶ Rotate vectors
- ▶ Flip vectors
- ▶ Do all these things in different directions
- ▶ Reveal the true ur-dystopian reality.

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References

A hand-drawn logo consisting of a square frame containing the text "I ♥ N(A^T)". The heart symbol is drawn with a simple outline, and the text is in a casual, slightly irregular font.

Digital photographs are matrices:

Episode 1/24:
Introduction



Exciting Admin

Importance

Usages


Key problems

Three ways of
looking...

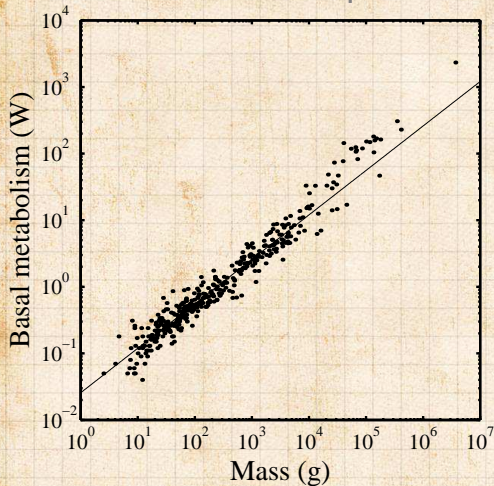
Colbert on
Equations

References

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

Usually three matrices: RGB color model .

Best fit line (least squares):



- ▶ Linear algebra does this beautifully;
- ▶ Calculus version is clunky. And evil.

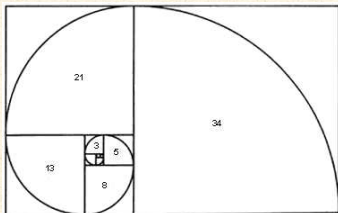
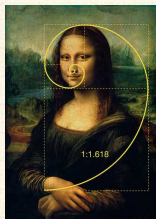
- ▶ From "Re-examination of the '3/4' law of metabolism"^[1]
Dodds, Rothman, and Weitz,
Journal of Theoretical Biology, 209, 9–27, 2001



The many delights of Eigenthings:

Episode 1/24:
Introduction

Using Linear Algebra we'll somehow connect:



- ▶ Fibonacci Numbers,
- ▶ Golden Ratio,
- ▶ Spirals,
- ▶ Sunflowers, pine cones, ...
- ▶ Harvard Square.

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

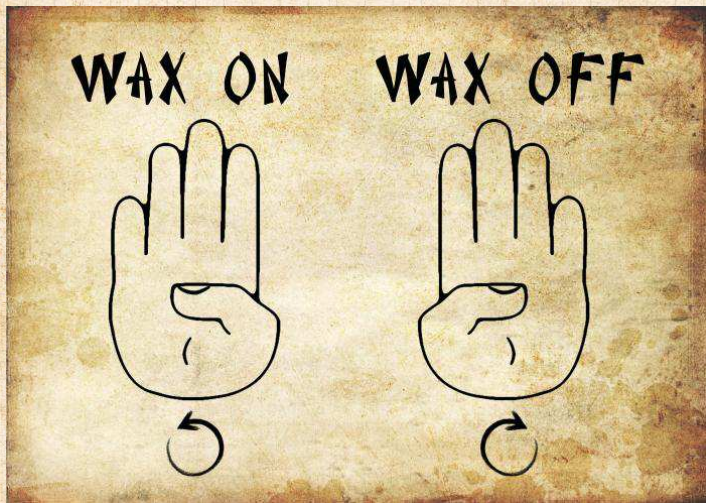
Colbert on Equations

References

$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$

This is a math course:

Episode 1/24:
Introduction



<http://www.pimpartworks.com/artwork/randomsteveo/Wax-On-Wax-Off>

► It's all connected. "More later."

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

References



Three key problems of Linear Algebra

Episode 1/24:
Introduction

1. Given a matrix A and a vector \vec{b} , find \vec{x} such that

$$A\vec{x} = \vec{b}.$$

2. Eigenvalue problem: Given A , find λ and \vec{v} such that

$$A\vec{v} = \lambda\vec{v}.$$

3. Coupled linear differential equations:

$$\frac{d}{dt}y(t) = Ay(t)$$

- ▶ Our focus will be largely on #1, partly on #2.

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

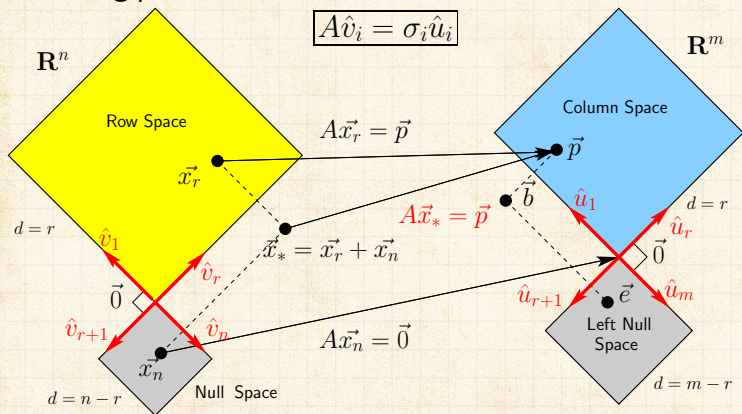
Colbert on Equations

References

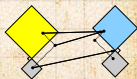


Major course objective:

To deeply understand the equation $A\vec{x} = \vec{b}$, the Fundamental Theorem of Linear Algebra, and the following picture:



What is going on here? We have 24 episodes to find out...



The fourfold ways of $A\vec{x} = \vec{b}$:

Episode 1/24:
Introduction

case	example R	big picture	# solutions
$m = r$ $n = r$	$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$		1 always
$m = r,$ $n > r$	$\begin{bmatrix} 1 & 0 & \text{☹}_1 \\ 0 & 1 & \text{☹}_2 \end{bmatrix}$		∞ always
$m > r,$ $n = r$	$\begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}$		0 or 1
$m > r,$ $n > r$	$\begin{bmatrix} 1 & 0 & \text{🚲}_1 \\ 0 & 1 & \text{🚲}_2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$		0 or ∞

Exciting Admin

Importance

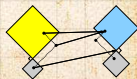
Usages

Key problems

Three ways of looking...

Colbert on Equations

References



Our new BFF: $A\vec{x} = \vec{b}$

Episode 1/24:
Introduction

Broadly speaking, $A\vec{x} = \vec{b}$ translates as follows:

- ▶ \vec{b} represents reality (e.g., music, structure)
- ▶ A contains building blocks (e.g., notes, shapes)
- ▶ \vec{x} specifies how we combine our building blocks to make \vec{b} (as best we can).

Exciting Admin

Importance

Usages

Key problems

Three ways of looking...

Colbert on Equations

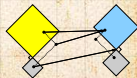
References

How can we disentangle an orchestra's sound?



- ▶ Radiolab's amazing piece: A 4-Track Mind

What about pictures, waves, signals, ...?



Is this your left nullspace?:

Episode 1/24:

Introduction

[Exciting Admin](#)

[Importance](#)

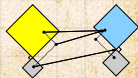
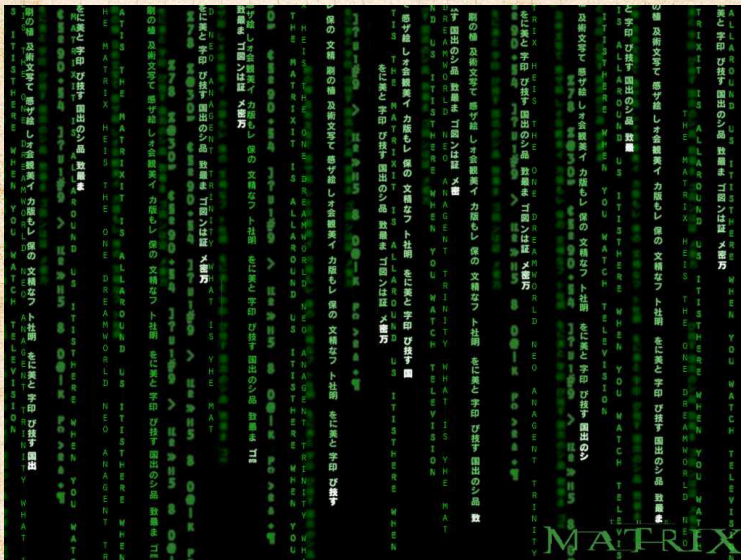
[Usages](#)

[Key problems](#)

[Three ways of looking...](#)

[Colbert on Equations](#)

[References](#)



Linear Algebra compliments/putdowns:

- ▶ Wow, you have such a tiny/huge [delete as applicable] left nullspace!



- ▶ See also: [The Dunning-Kruger effect.](#)

Episode 1/24:
Introduction

Exciting Admin

Importance

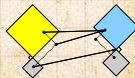
Usages

Key problems

Three ways of
looking...

Colbert on
Equations

References



Our friend $A\vec{x} = \vec{b}$

Episode 1/24:
Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of
looking...

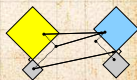
Colbert on
Equations

References

What does knowing \vec{x} give us?

If we can represent **reality** as a **superposition** (or combination or sum) of **simple elements**, we can do many things:

- ▶ Compress information
- ▶ See how we can alter information (filtering)
- ▶ Find a system's simplest representation
- ▶ Find a system's most important elements
- ▶ See how to adjust a system in a principled way



Three ways to understand $A\vec{x} = \vec{b}$:

- ▶ Way 1: The **Row** Picture
- ▶ Way 2: The **Column** Picture
- ▶ Way 3: The **Matrix** Picture

Example:

$$\begin{array}{rcl} -x_1 & + & x_2 = 1 \\ 2x_1 & + & x_2 = 4 \end{array}$$

- ▶ Call this a **2 by 2 system of equations**.
- ▶ 2 equations with 2 unknowns.
- ▶ Standard method of **simultaneous equations**: solve above by adding and subtracting multiples of equations to each other = **Row Picture**.

Episode 1/24:
Introduction

Exciting Admin

Importance

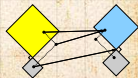
Usages

Key problems

Three ways of
looking...

Colbert on
Equations

References



Three ways to understand $A\vec{x} = \vec{b}$:

Episode 1/24:
Introduction

Row Picture—what we are doing:

- ▶ (a) Finding intersection of two lines
- ▶ (b) Finding the values of x_1 and x_2 for which both equations are satisfied (true/happy)
- ▶ A splendid and deep connection:
(a) Geometry \Leftrightarrow (b) Algebra

Exciting Admin

Importance

Usages

Key problems

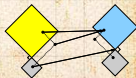
Three ways of
looking...

Colbert on
Equations

References

Three possible kinds of solution:

1. Lines intersect at one point — **One, unique solution**
2. Lines are parallel and disjoint — **No solutions**
3. Lines are the same — **Infinitely many solutions**



Three ways to understand $A\vec{x} = \vec{b}$:

Episode 1/24:
Introduction

The column picture:

See

$$\begin{aligned} -x_1 + x_2 &= 1 \\ 2x_1 + x_2 &= 4 \end{aligned}$$

as

$$x_1 \begin{bmatrix} -1 \\ 2 \end{bmatrix} + x_2 \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 4 \end{bmatrix}.$$

General problem

$$x_1 \vec{a}_1 + x_2 \vec{a}_2 = \vec{b}$$

- ▶ Column vectors are our **'building blocks'**
- ▶ **Key idea:** try to 'reach' \vec{b} by combining (summing) multiples of column vectors \vec{a}_1 and \vec{a}_2 .

Exciting Admin

Importance

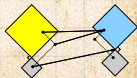
Usages

Key problems

Three ways of
looking...

Colbert on
Equations

References



Three ways to understand $A\vec{x} = \vec{b}$:

Episode 1/24:
Introduction

We love the column picture:

- ▶ Intuitive.
- ▶ Generalizes easily to many dimensions.

Exciting Admin

Importance

Usages

Key problems

Three ways of
looking...

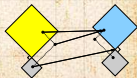
Colbert on
Equations

References

Three possible kinds of solution:

1. \vec{a}_1 not parallel \vec{a}_2 : 1 solution.
2. \vec{a}_1 parallel to \vec{a}_2 but not parallel to \vec{b} : No solutions.
3. \vec{a}_1 , \vec{a}_2 , and \vec{b} all parallel: infinitely many solutions.

(assuming neither \vec{a}_1 or \vec{a}_2 are $\vec{0}$)



Three ways to understand $A\vec{x} = \vec{b}$:

Episode 1/24:
Introduction

Exciting Admin

Importance

Usages

Key problems

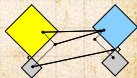
Three ways of
looking...

Colbert on
Equations

References

Difficulties:

- ▶ Do we give up if $A\vec{x} = \vec{b}$ has no solution?
- ▶ **No!** We can still find the \vec{x} that gets us as close to \vec{b} as possible.
- ▶ Method of approximation—very important!
- ▶ We may not have the right building blocks but we can do our best.



Three ways to understand $A\vec{x} = \vec{b}$:

Episode 1/24:
Introduction

The Matrix Picture:

Now see

$$x_1 \begin{bmatrix} -1 \\ 2 \end{bmatrix} + x_2 \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 4 \end{bmatrix}.$$

as

$$A\vec{x} = \vec{b} : \begin{bmatrix} -1 & 1 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 1 \\ 4 \end{bmatrix}$$

A is now an operator:

- ▶ A transforms \vec{x} into \vec{b} .
- ▶ Roughly speaking, A does two things to \vec{x} :
 1. Rotation/Flipping
 2. Dilation (stretching/contraction)

Exciting Admin

Importance

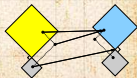
Usages

Key problems

Three ways of
looking...

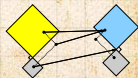
Colbert on
Equations

References



Key idea in linear algebra:

- ▶ Decomposition or factorization of matrices.
- ▶ Matrices can often be written as products or sums of simpler matrices
- ▶ $A = LU$, $A = QR$, $A = U\Sigma V^T$, $A = \sum_i \lambda_i \vec{v}\vec{v}^T$, ...



More Truth about Mathematics:

Episode 1/24:

Introduction

Exciting Admin

Importance

Usages

Key problems




Three ways of
looking...

Colbert on
Equations

References

[I ♥
N(A^T)]

References I

- [1] P. S. Dodds, D. H. Rothman, and J. S. Weitz.
Re-examination of the “3/4-law” of metabolism.
[Journal of Theoretical Biology](#), 209:9–27, 2001.
[pdf](#) 
- [2] G. Strang.
The fundamental theorem of linear algebra.
[The American Mathematical Monthly](#),
100(9):848–855, 1993. [pdf](#) 
- [3] G. Strang.
Too much calculus, 2002.
[SIAM Linear Algebra Activity Group Newsletter](#).
[pdf](#) 

Episode 1/24:

Introduction

Exciting Admin

Importance

Usages

Key problems

Three ways of
looking...

Colbert on
Equations

References

$$\left[\begin{array}{c} I \heartsuit \\ N(A^T) \end{array} \right]$$

