Overview of Complex Networks

Complex Networks | @networksvox CSYS/MATH 303, Spring, 2016

Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont























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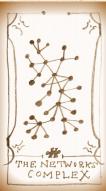


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Andy Reagan











Cathy Bliss























compstorylab.org















(Colorado)



(MIT)

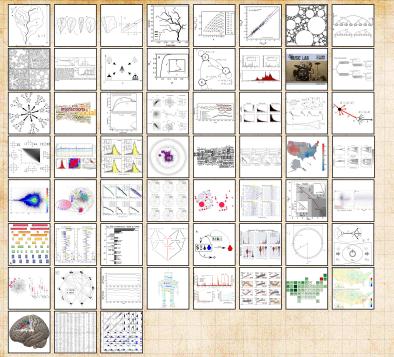


(Apple)

CocoNuTs Complex Networks @networksvox

Funding: NSF, NASA, MITRE.





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- ▶ Instructor: Prof. Peter Dodds
- Lecture room and meeting times:
 102 Perkins, Tuesday and Thursday, 1:15 pm to
 2:30 pm
- Office: Farrell Hall, second floor, Trinity Campus
- email: peter.dodds@uvm.edu
- ► Course Website:
 http://www.uvm.edu/ pdodds/teaching/courses/2016-01UVM-303 🗗
- ► Course Twitter handle: @networksvox
- ► Course hashtag: #SpringCOcoNuTS2016

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Potential paper products:

▶ The Syllabus 🗗 and a Poster 🗹.

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- Principles of Complex Systems is one of two core requirements for UVM's five course
- Other required course: Prof. Maggie Eppstein's "Modelling Complex Systems" (CSYS/CS 302).
- ► coCoNuTS: The Sequel to PoCS: "Complex Networks" (CSYS/MATH 303).







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Office hours:

2:30 pm to 3:15 pm, Tuesday and Thursday, Perkins 102; 11:00 am to 11:55 am, Wednesday, Farrell., Farrell Hall, second floor, Trinity Campus

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 - 1. Presentation,
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- Presentation versions are hyperly navigable:

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- ► Citations contain links to pdfs for papers (if available).
- ▶ Some books will be linked to on amazor
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#superpowers

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More super exciting details:

- ▶ This is Season 7 of Complex Networks.
- Lectures will be called Episodes.
- ▶ All lectures are bottle episodes .
- ▶ Other tropes will be involved.

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Wonderful foundational support for PoCS and CoNKS has come from the NSF:

- "CAREER: Explorations of Complex Social and Psychological Phenomena through Multiscale Online Sociological Experiments, Empirical Studies, and Theoretical Models." 2009–2015.
- ➤ SES Division of Social and Economic Sciences SBE Directorate for Social, Behavioral & Economic Sciences
- ▶ Abstract is here <a>C.

▶ Last season's Episodes are here ☑.

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We'll be carrying on with the PoCS Slack:

- Place for discussions about all things PoCS/coCoNuTs including assignments and projects.
- Once invited, please sign up here: http://teampocs.slack.com
- Very good: Install Slack app on laptops, tablets phone.
- Everyone will behave wonderfully.



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Grading breakdown:

▶ Projects/talks (36%)—Students will work on semester-long projects. Students will develop a proposal in the first few weeks of the course which will be discussed with the instructor for approval. Details: 12% for the first talk, 12% for the final talk, and 12% for the written project.

Assignments (60%)—All assignments will be of equal weight and there will be 10 ± 1 of them.

► General attendance/Class participation (4%)

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Questions are worth 3 points according to the following scale:

- ▶ 3 = correct or very nearly so.
- ▶ 2 = acceptable but needs some revisions.
- ▶ 1 = needs major revisions.
- ▶ 0 = way off.





1. Classes run from Tuesday, January 19 to Tuesday, May 4.

- 2. Add/Drop, Audit, Pass/No Pass deadline—Monday, February 1.
- 3. Last day to withdraw—Monday, April 4 (Never!).
- 4. Reading and Exam period—Thursday, May 6 to Friday, May 13.

Do check the course Twitter account, @networksvox, for updates regarding the course (part of the course site).

Academic assistance: Anyone who requires assistance in any way (as per the ACCESS program or due to athletic endeavors), please see or contact me as soon as possible.

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Schedule in detail:

Week number (dates)	Tuesday	Thursday
1 (1/18 and 1/20)	overview, branching networks I	branching networks I and II
2 (1/25 and 1/27)	branching networks II	optimal supply networks I and II
3 (2/2 and 2/4)	optimal supply networks II	optimal supply networks II
4 (2/9 and 2/11)	optimal supply networks II	optimal supply networks III
5 (2/16 and 2/18)	optimal supply networks III, random net- works	random networks
6 (2/23 and 2/25)	generating functions	random bipartite networks
7 (3/1 and 3/3)	Town meeting day	project presentations†
8 (3/8 and 3/10)	Spring Recess	Spring Recess
9 (3/15 and 3/17)	random networks	bipartite networks
10 (3/22 and 3/24)	contagion	contagion
11 (3/29 and 3/31)	contagion	chaotic contagion
12 (4/5 and 4/7)	multilayer networks	multilayer networks
13 (4/12 and 4/14)	assortativity	mixed random networks
14 (4/19 and 4/21)	centrality	structure detection
15 (4/26 and 4/28)	structure detection	structure detection
16 (4/3)	organizational networks	_

^{†: 3-4} minutes each + 1 or 2 questions;

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Semester-long projects.

- Possible theme: Stories, Narratives, and Language.
- Develop proposal in first few weeks.
- May range from novel research to investigation of an established area of complex systems.
- Two talks + written piece + Project on Github Pages.
- Usage of the VAC (2) is encouraged (ability to code well = super powers).
- Massive data sets available, including Twitter.
- We'll go through a list of possible projects soon.

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The narrative hierarchy—Stories and Storytelling on all Scales:







- ▶ 1 to 3 word encapsulation = a soundbite = a buzzframe,
- ▶ 1 sentence, title,
- ▶ few sentences, a haiku,
- a paragraph, abstract,
- short paper, essay,
- ▶ long paper,
- chapter,
- book,
- **...**

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Key Observation:

Many complex systems can be viewed as complex networks of physical or abstract interactions.

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Opens door to mathematical and numerical analysis.

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- Opens door to mathematical and numerical analysis.
- Dominant approach of last decade of a theoretical-physics/stat-mechish flavor.

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- Many complex systems

 can be viewed as complex networks
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- Mindboggling amount of work published on complex networks since 1998 ...

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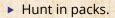
Piranha physicus

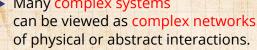




- Many complex systems can be viewed as complex networks
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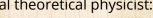
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- Piranha physicus
- Hunt in packs.
- Feast on new and interesting ideas (see chaos, cellular automata, ...)



Popularity (according to Google Scholar)

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"Collective dynamics of 'small-world' networks" [10]

Duncan Watts and Steve Strogatz Nature, 1998

Times cited: 28,017 (as of January 18, 2016)

"Emergence of scaling in random networks" [3]

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- 1. generalized random networks (touched on in 300
- 2. scale fr. a petworks (partly covered in 300)
- 3. shall mand record as 3 (covered in 300)
- 4. statistical generative models (p^*)
- 5. generalized affiliation networks (covered in 300)

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- \blacktriangleright Arbitrary degree distribution P_k .
- Wire nodes together randomly.
- Create ensemble to test deviations from randomness.
- Interesting, applicable, rich mathematically.
- ➤ We will have fun with these things.

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- We will have fun with these things

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- \blacktriangleright Arbitrary degree distribution P_k .
- ▶ Wire nodes together randomly.
- Create ensemble to test deviations from randomness.
- Interesting, applicable, rich mathematically.
- ▶ We will have fun with these things ...

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$$\gamma$$
 = 2.5, $\langle k \rangle$ = 1.8, $N = 150$

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$$\gamma$$
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- ► Introduced by Barabasi and Albert [3]
- Generative model
- Preferential attachment mode with growth:
- \blacktriangleright P[attachment to node $i] \propto k_i^{\alpha}$
- Produces $P_k \sim k$ when $\alpha = 1$.
 - Trickiness: other models generate skewed degree distributions

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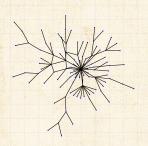
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▶ Introduced by Watts and Strogatz [10]

- Jocal regularity (an individual's friends know each other):
- ▶ global randomness (shortcuts).
- ➤ Shortcuts allow disease to jump
- Number of infectives increases exponentially in time
- Facilitates synchronization

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Two scales:

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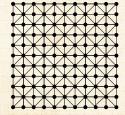




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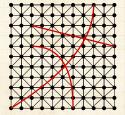




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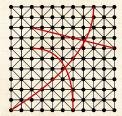




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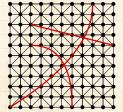




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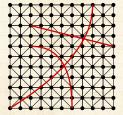




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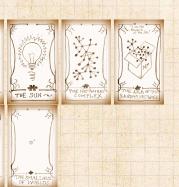
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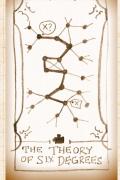
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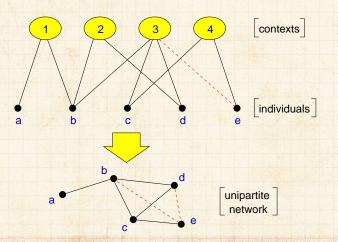








5. generalized affiliation networks



Bipartite affiliation networks: boards and directors, movies and actors.

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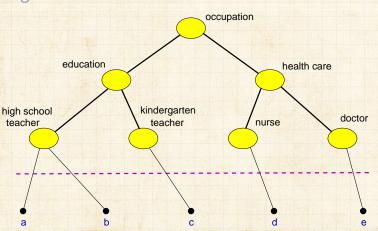
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5. generalized affiliation networks



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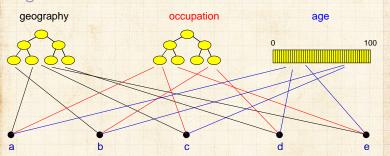
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5. generalized affiliation networks



▶ Blau & Schwartz [4], Simmel [8], Breiger [6], Watts et al. [9]

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- ► Mark Newman (Physics, Michigan) "Networks: An Introduction" ✓
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Overview Key Points:

- ► The field of complex networks came into existence in the late 1990s.
- Explosion of papers and interest since 1998/99.
- Hardened up much thinking about complex systems.
- ▶ Specific focus on networks that are large scale, sparse, natural or man-made, evolving and dynamic, and (crucially) measurable.
- ► Three main (blurred) categories:
 - 1. Physical (e.g., river networks),
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- Obvious connections with the vast extant field of graph theory.
- But focus on dynamics is more of a physics/stat-mech/comp-sci flavor.
- Two main areas of focus
 - Description: Characterizing very large networks
 Explanation: Micro story ⇒ Macro features
- ➤ Some essential structural aspects are understood: degree distribution, clustering, assortativity, group structure, overall structure, ...
- Still much work to be done, especially with respect to dynamics ...

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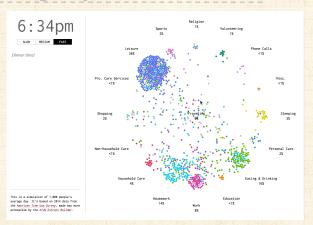
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Neural solace—Temporal social networks:

Visualizing a day in the life of Americans ☑



► Source: Flowing Data/Nathan Yau.

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