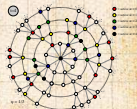


# Social Contagion

Principles of Complex Systems | @pocsvox  
 CSYS/MATH 300, Fall, 2015 | #FallPoCS2015

Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center  
 Vermont Advanced Computing Core | University of Vermont



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- Background
- Granovetter's model
- Network version
- Final size
- Spreading success
- Groups

References

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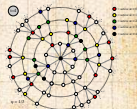
## Sealie & Lambie Productions



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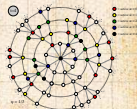
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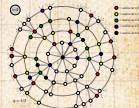
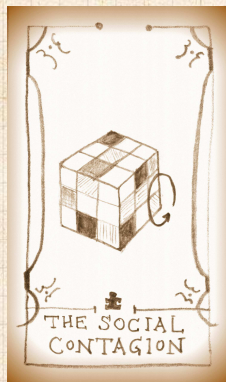
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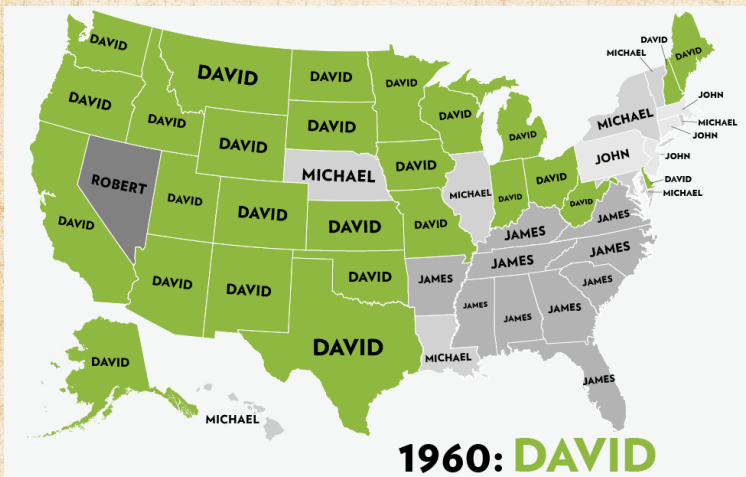


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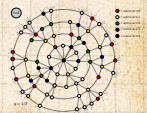


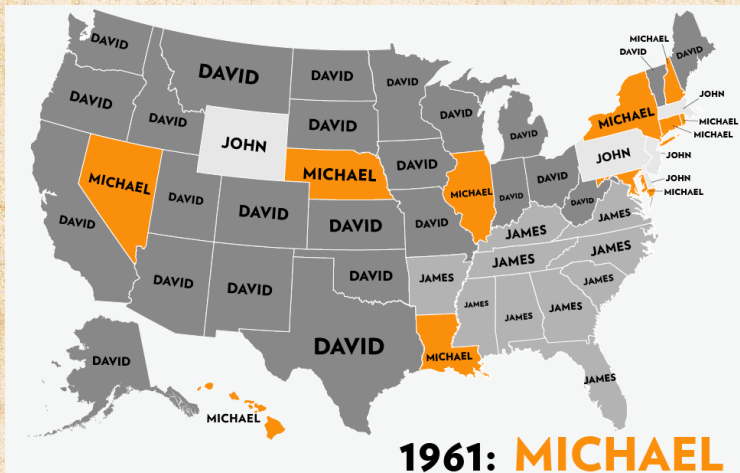
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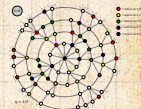


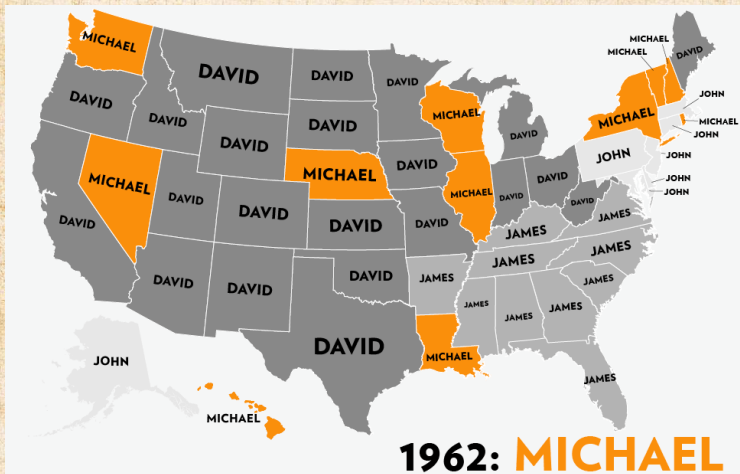
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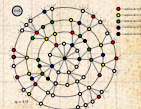


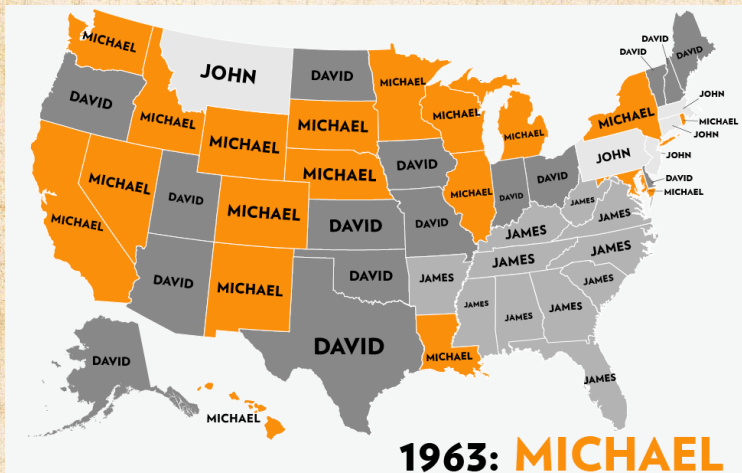
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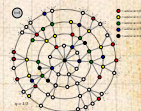




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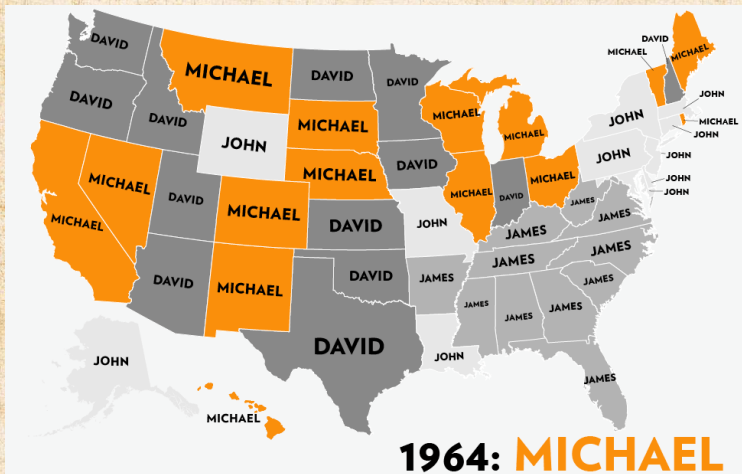
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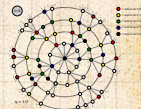


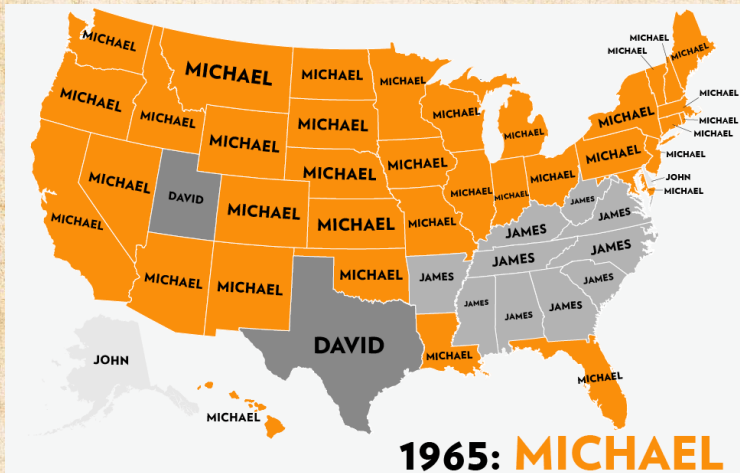
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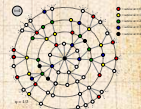


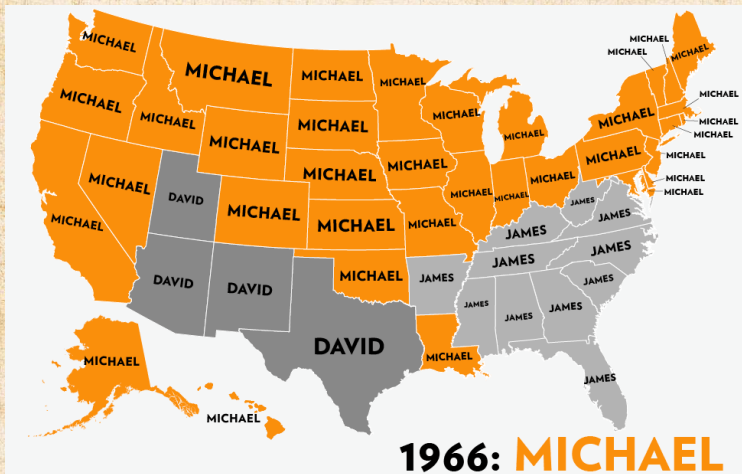
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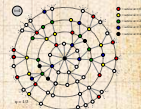


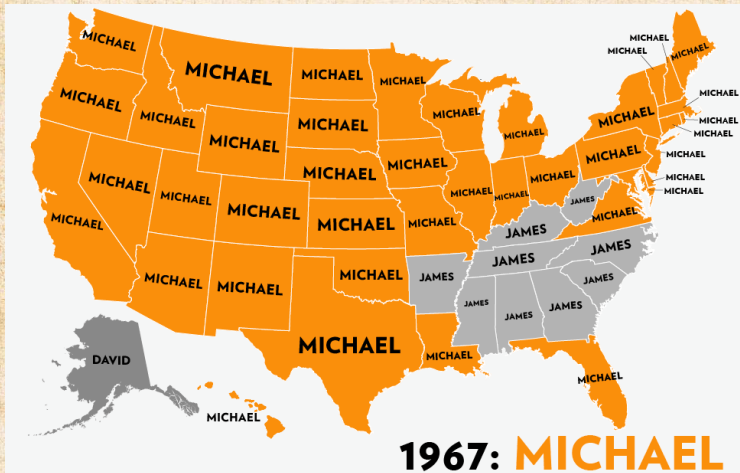
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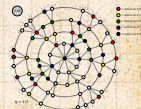


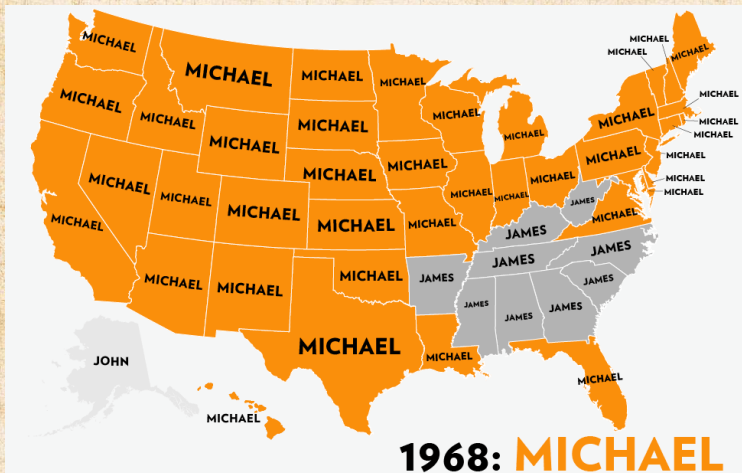
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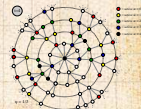


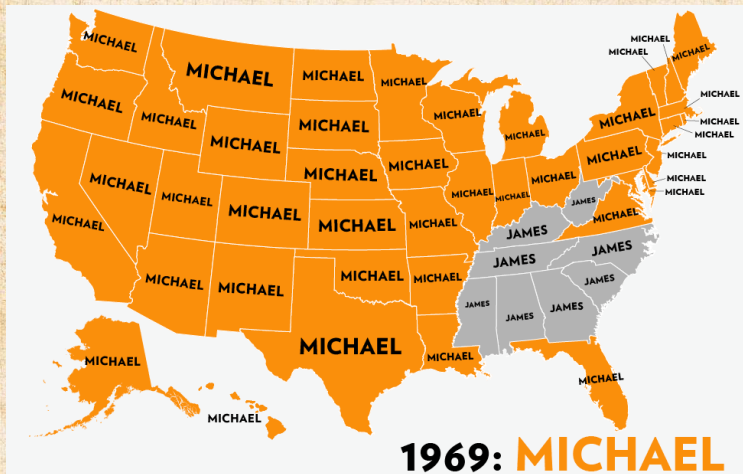
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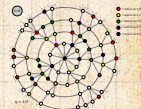


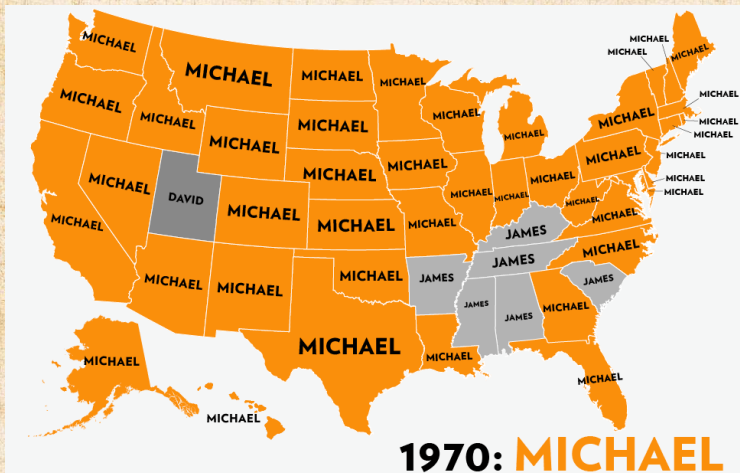
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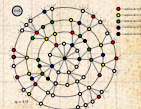


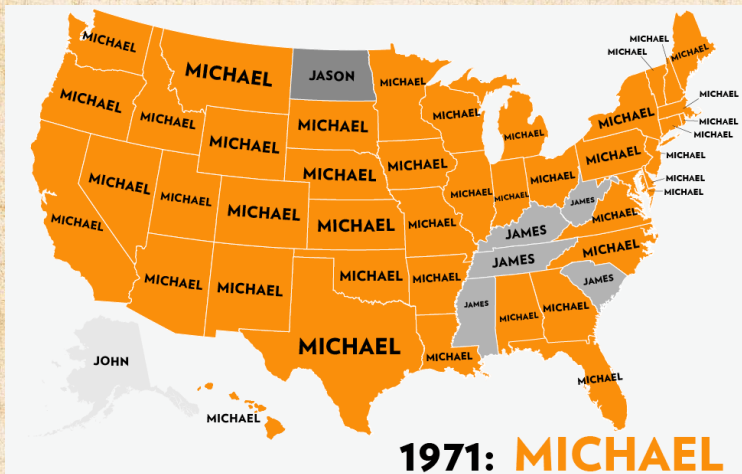
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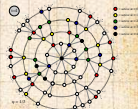


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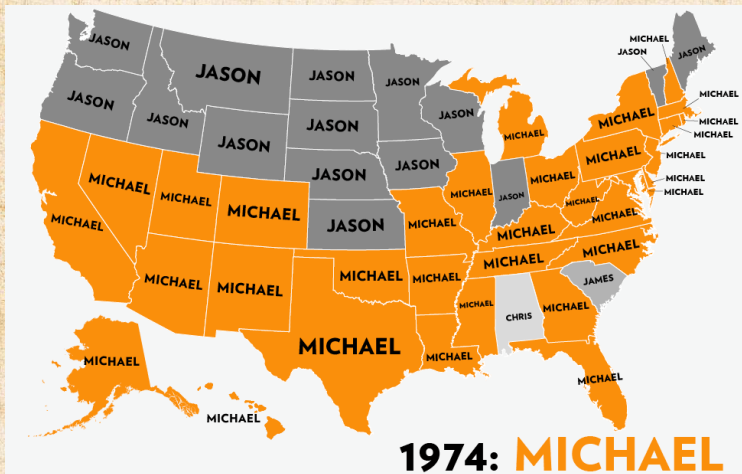
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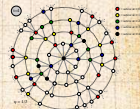


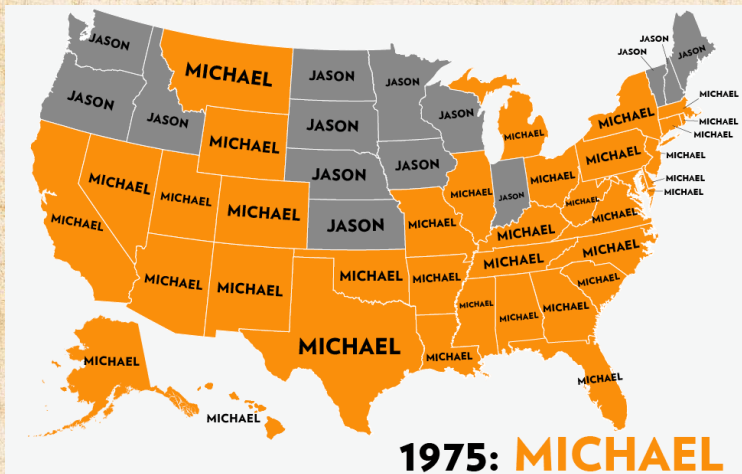
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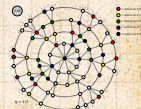


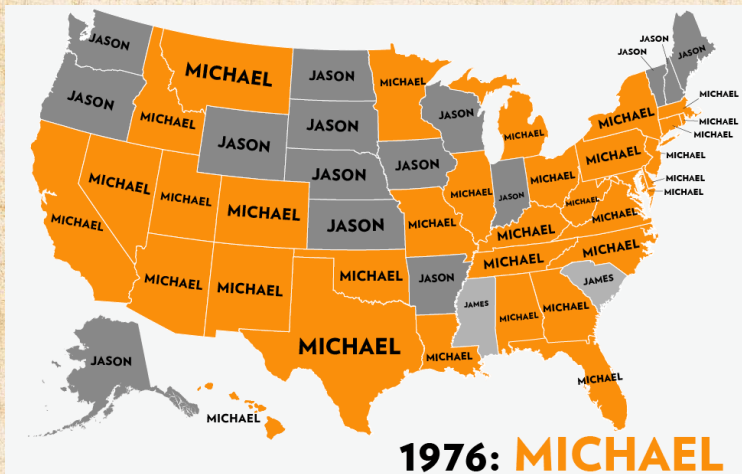
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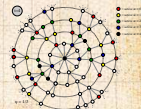


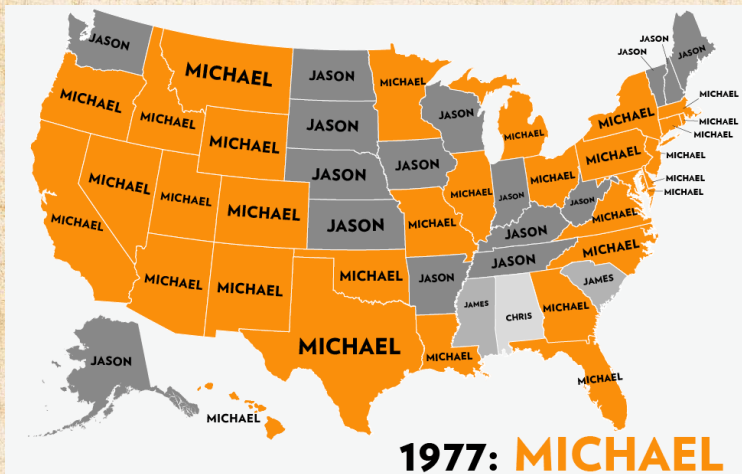
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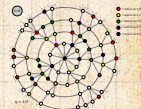


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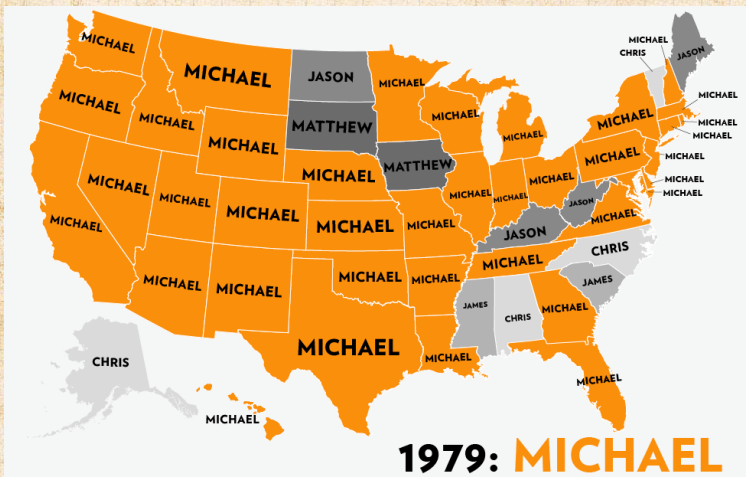
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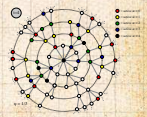


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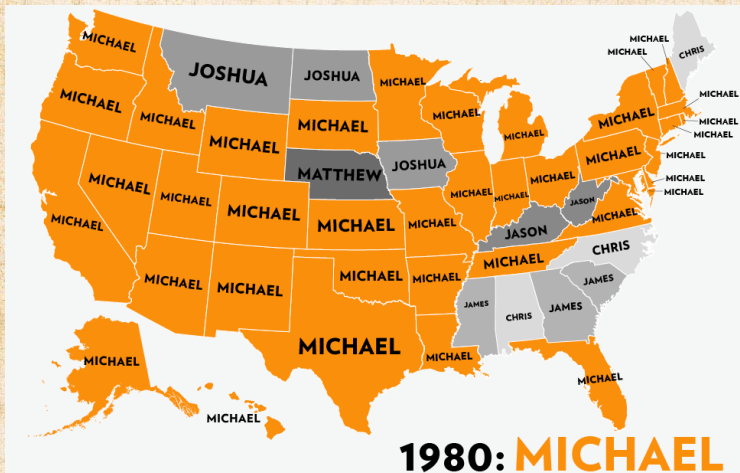
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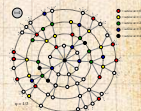




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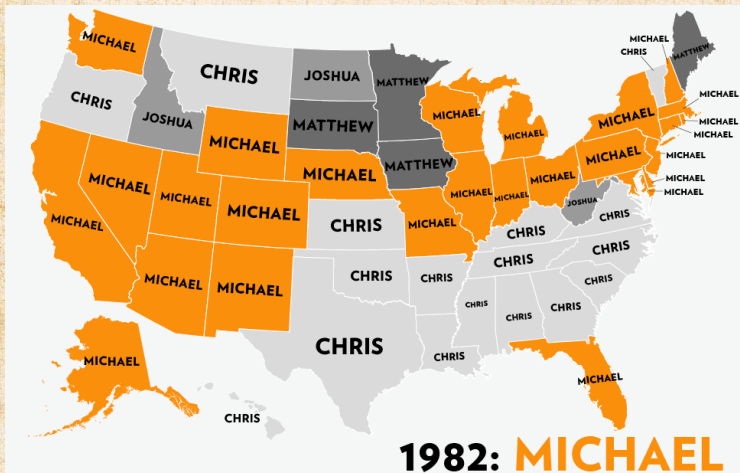
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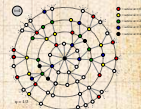


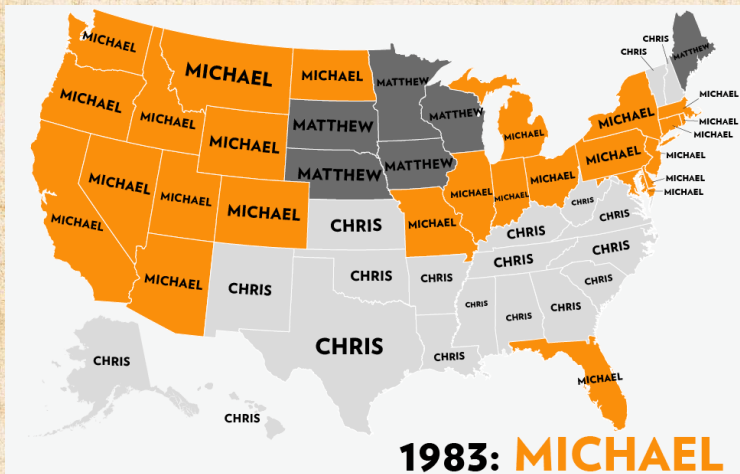
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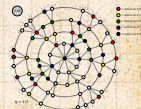


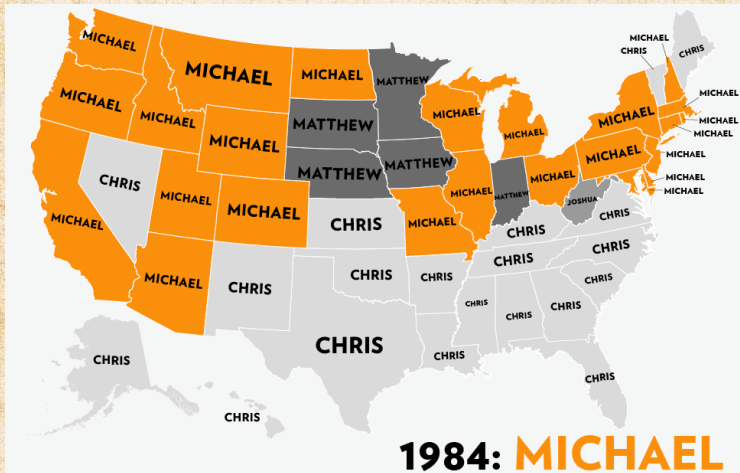
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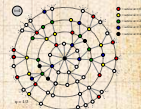


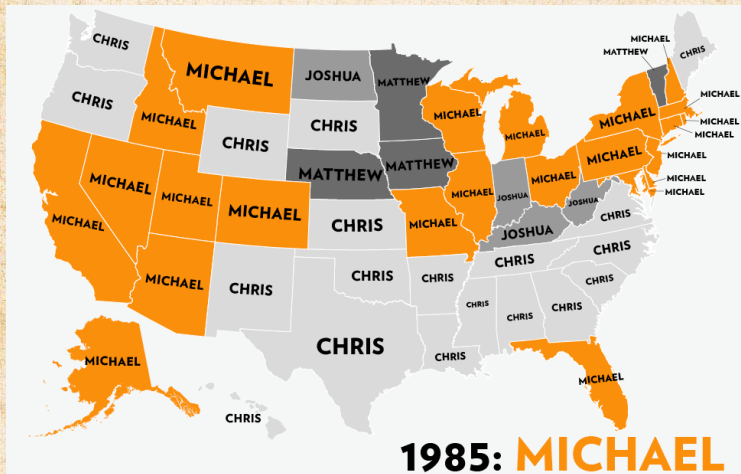
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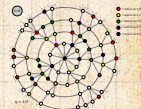


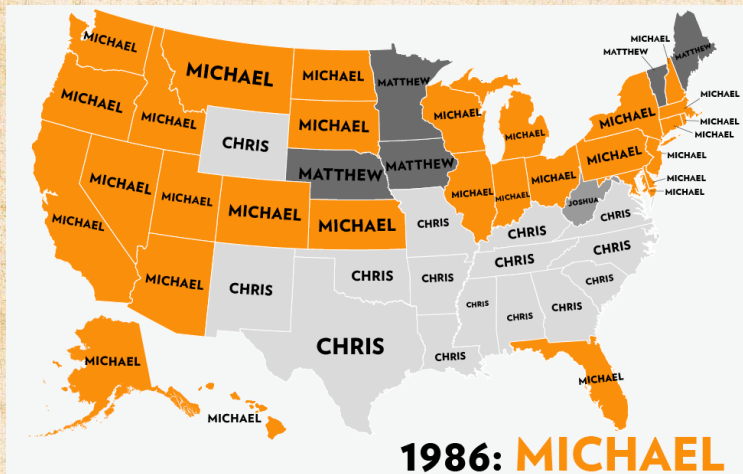
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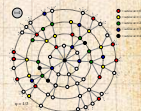


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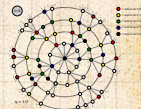


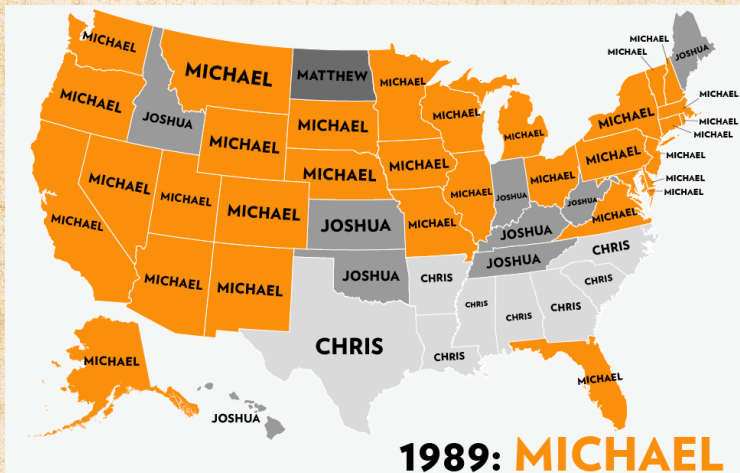
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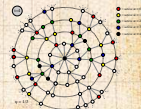


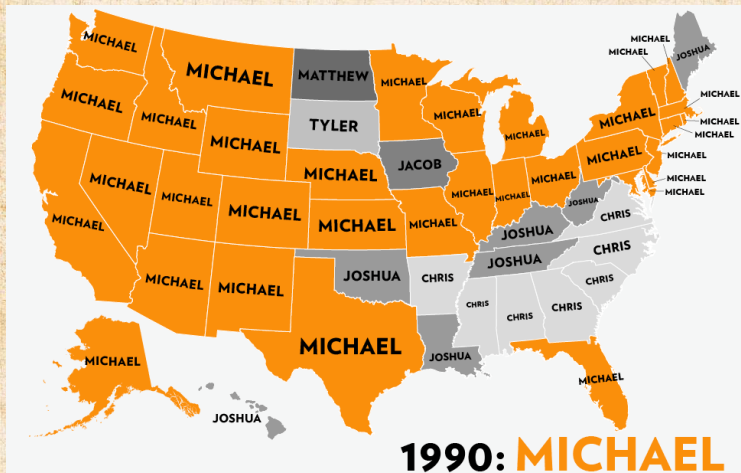
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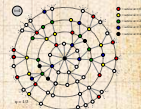


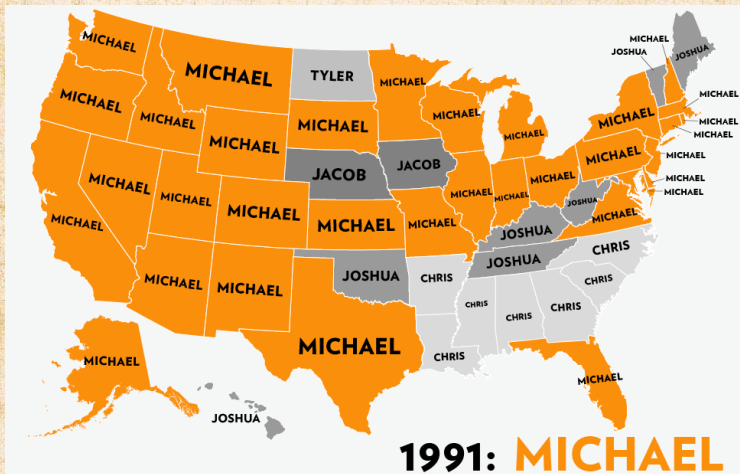
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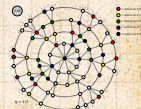


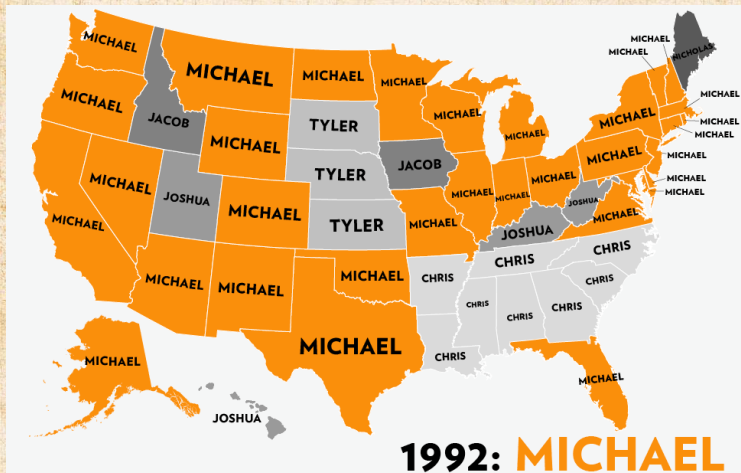
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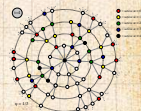


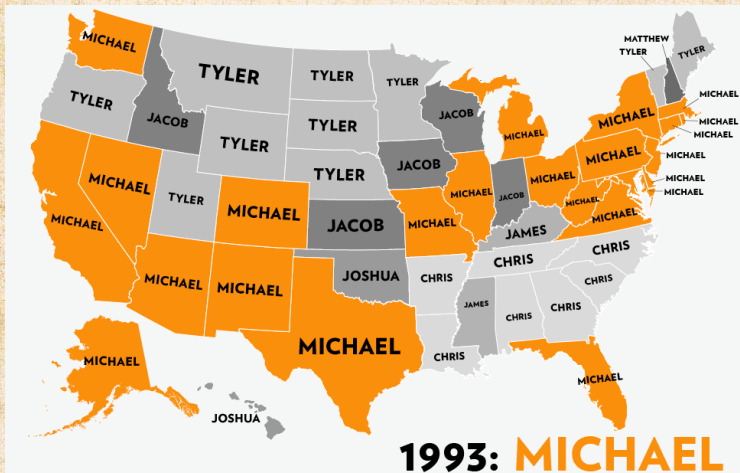
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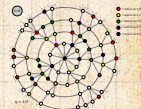


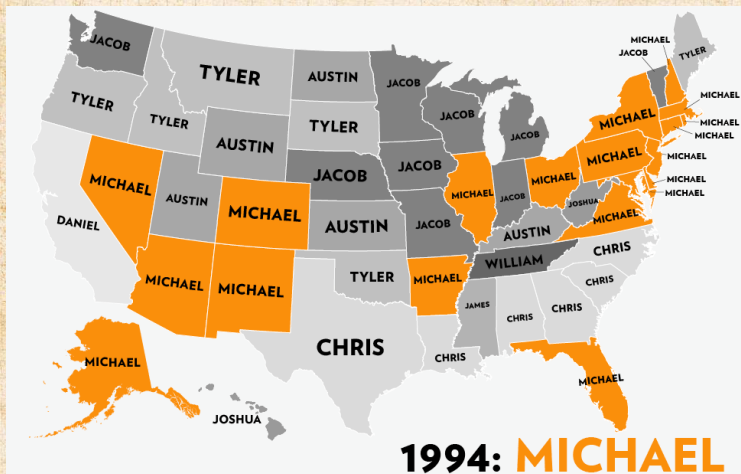
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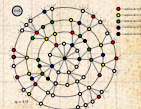


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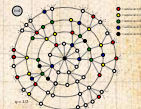


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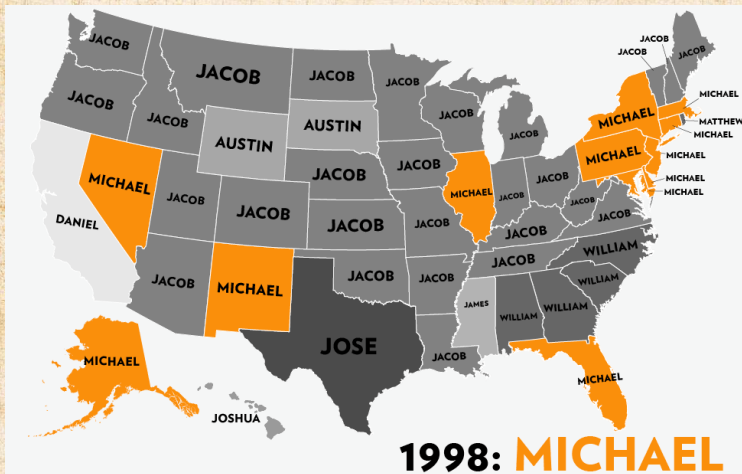
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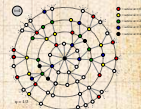


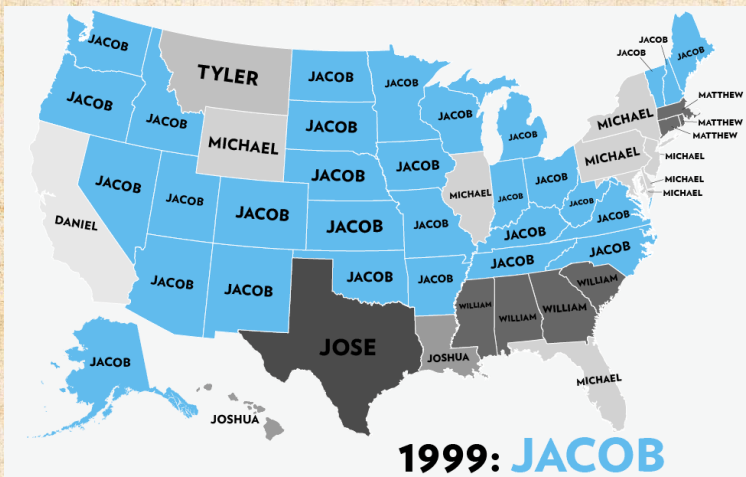
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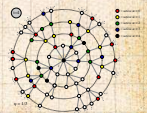




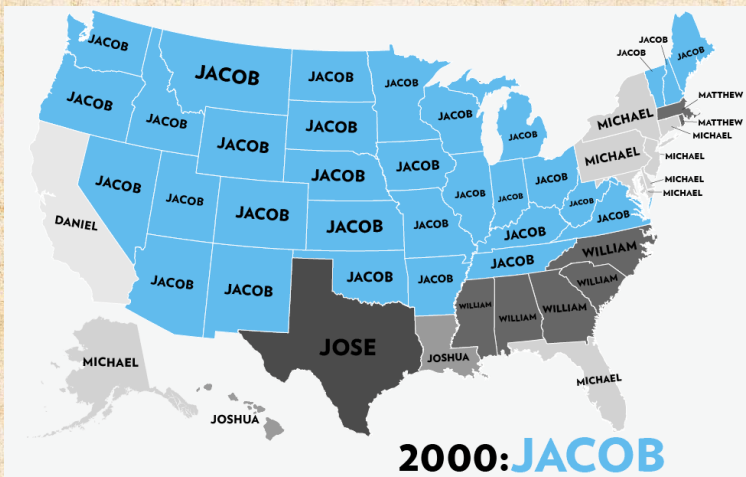
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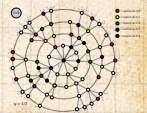


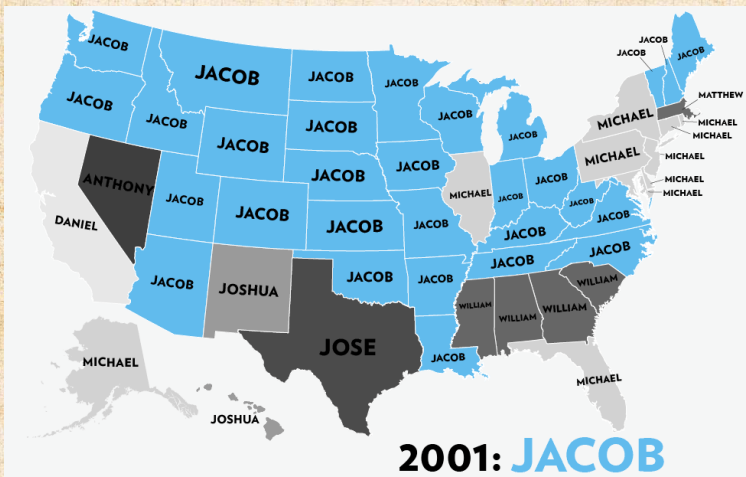
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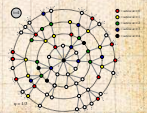




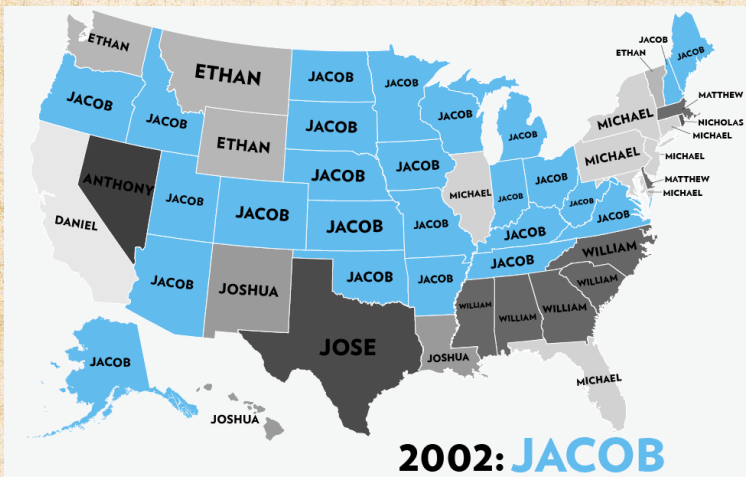
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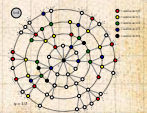
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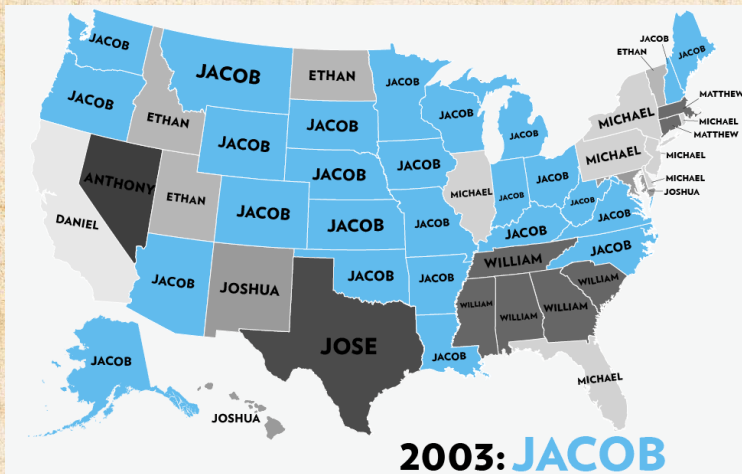
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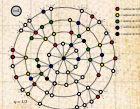


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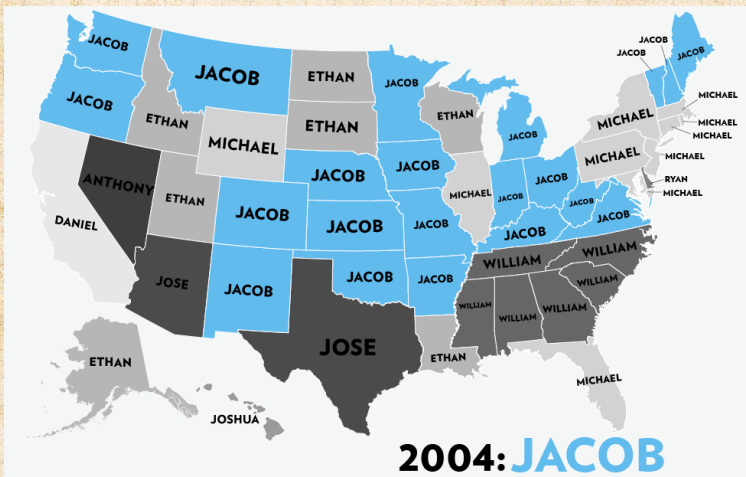
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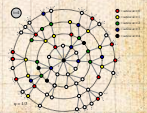




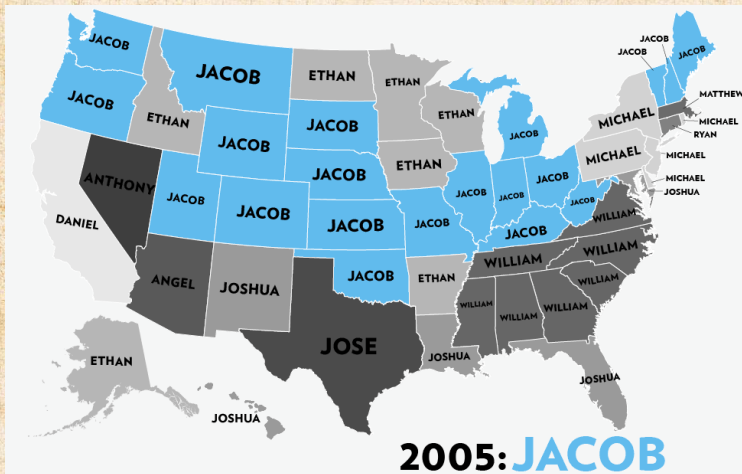
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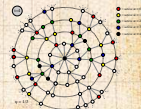


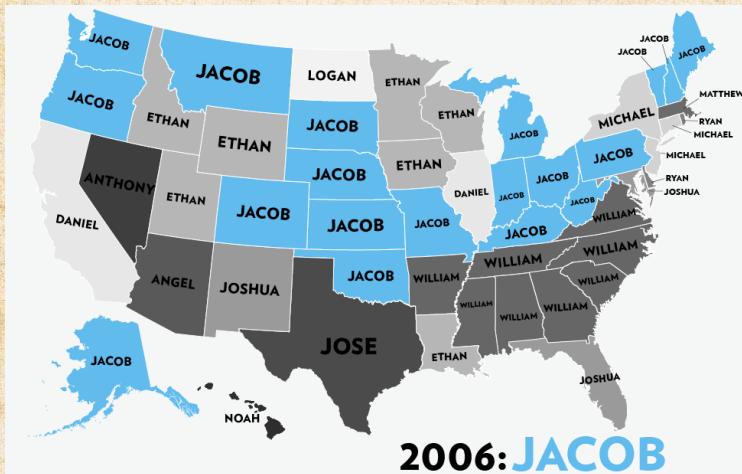
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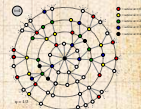


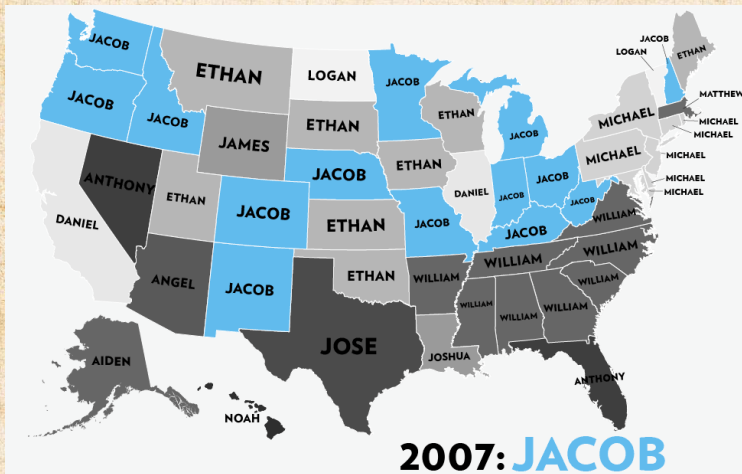
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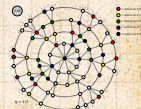


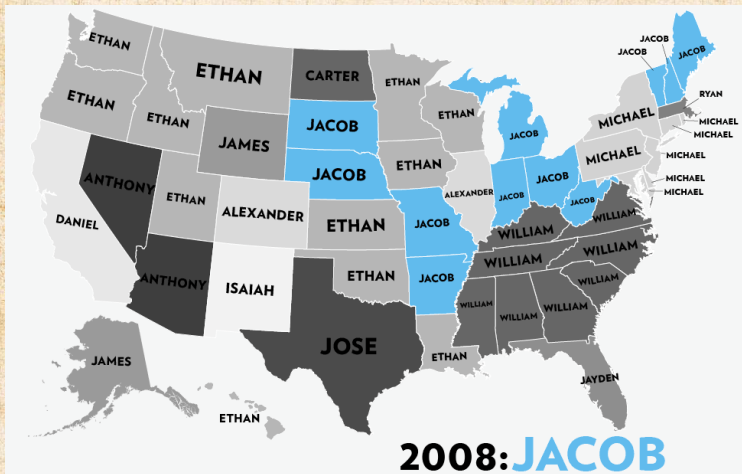
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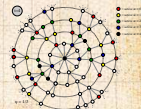


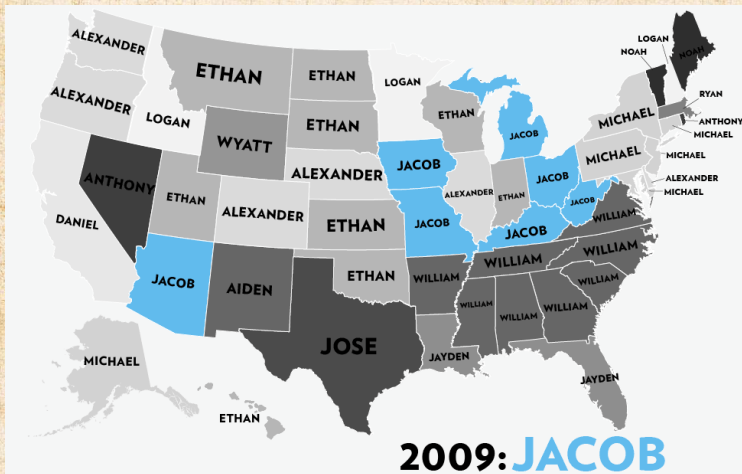
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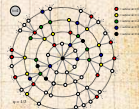


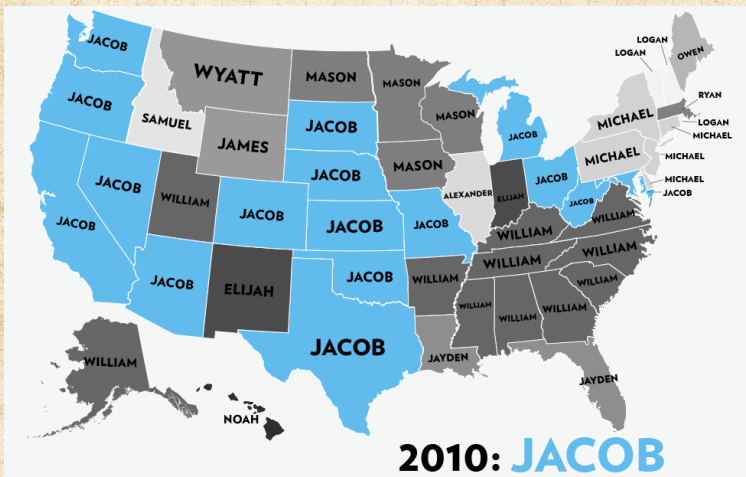
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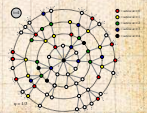


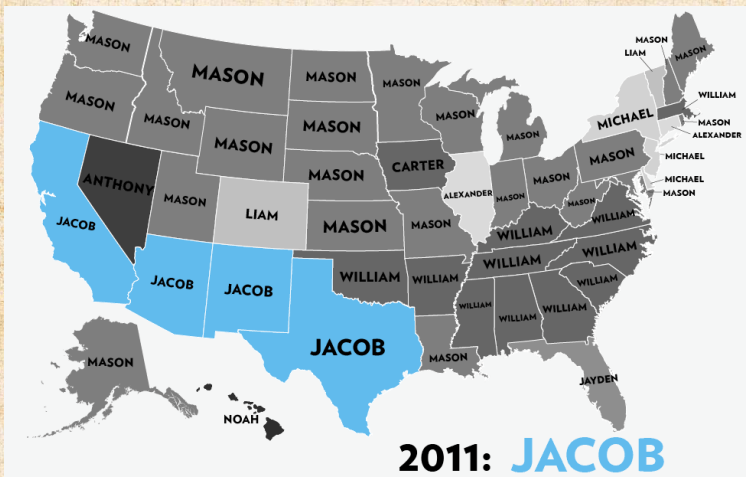
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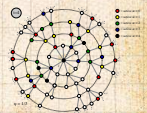


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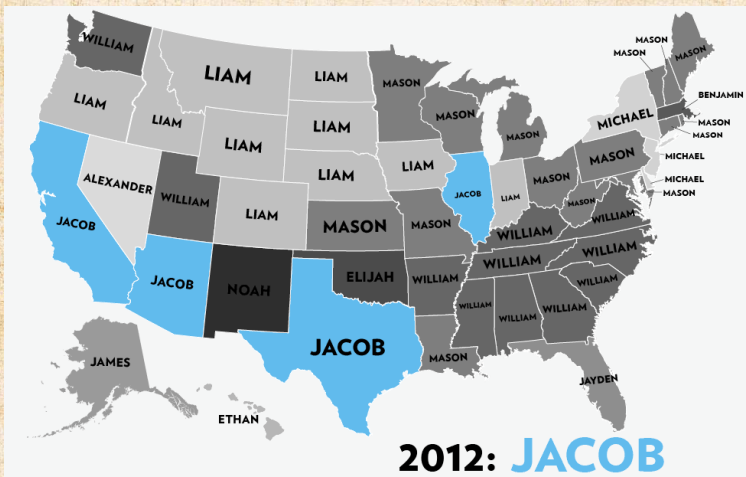
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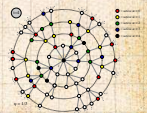


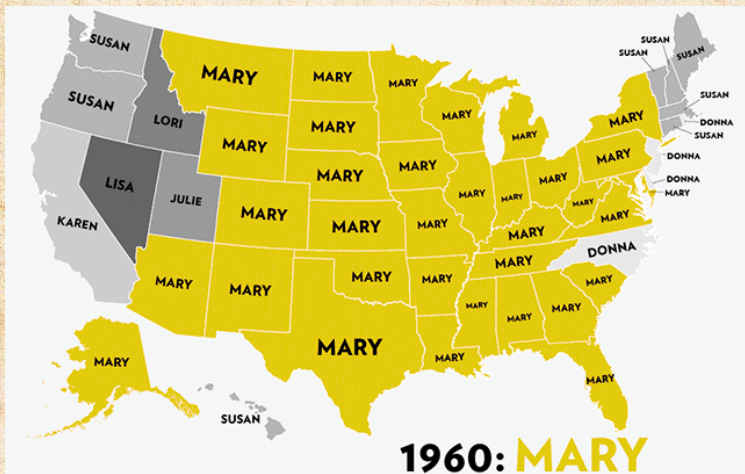
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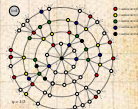


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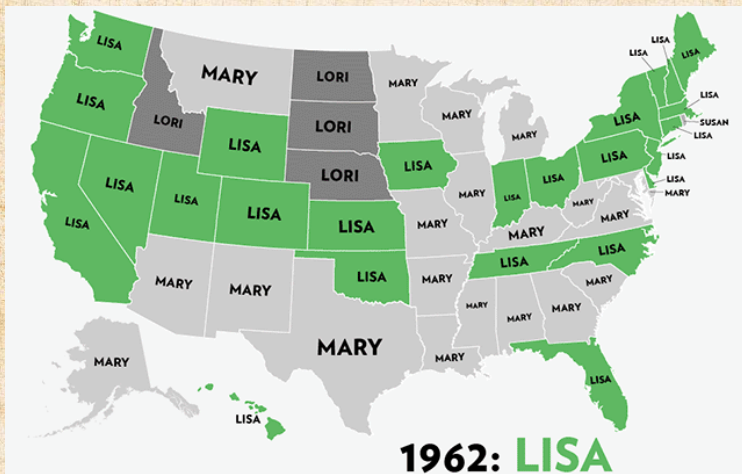
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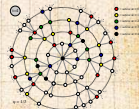


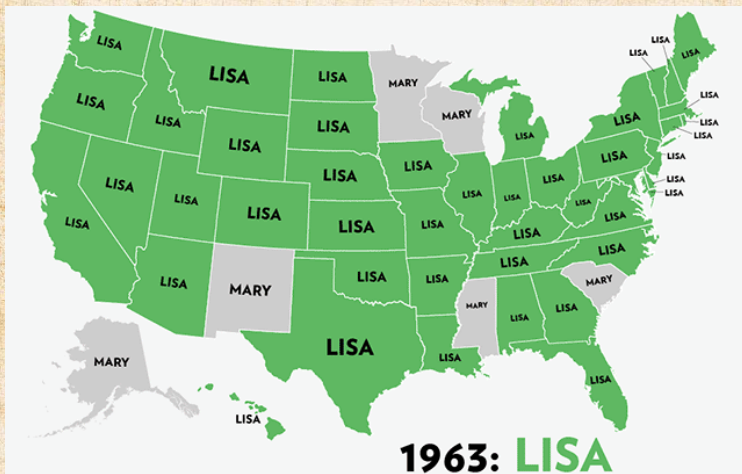
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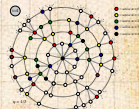


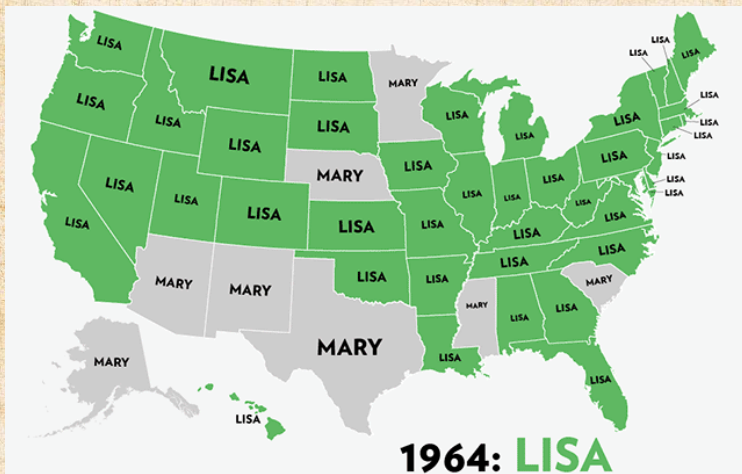
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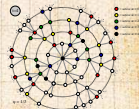


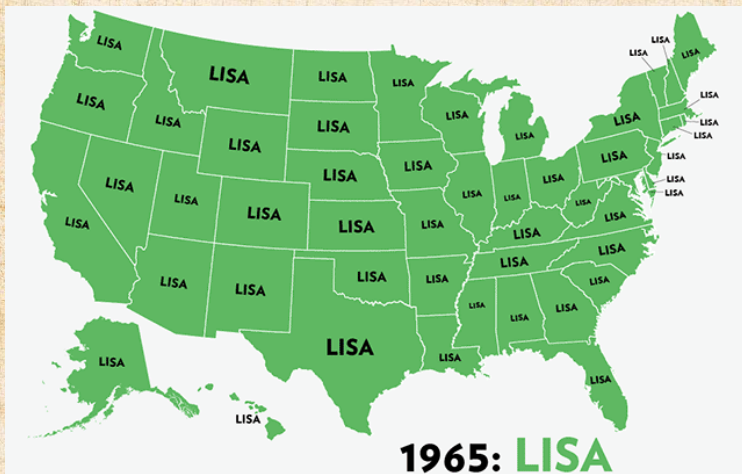
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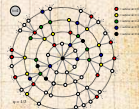


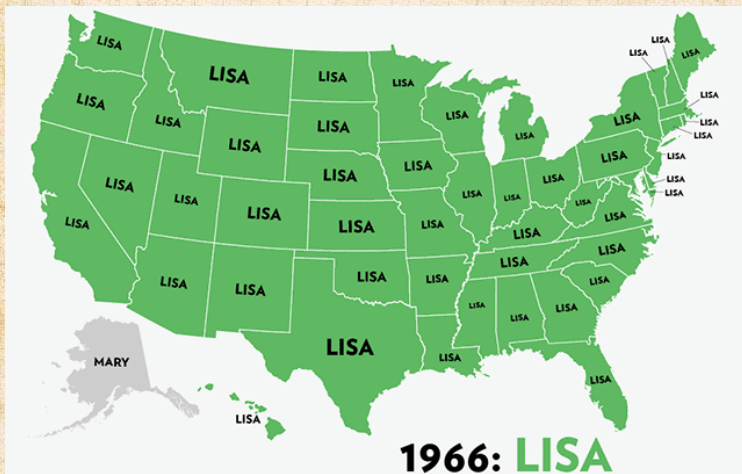
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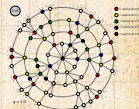


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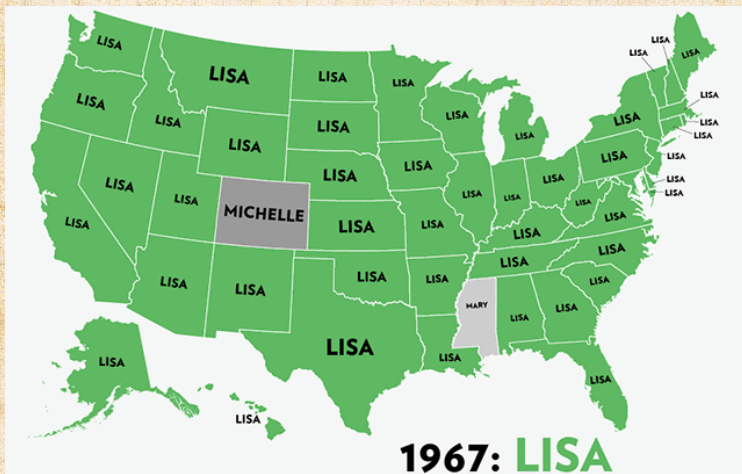
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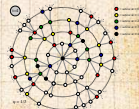


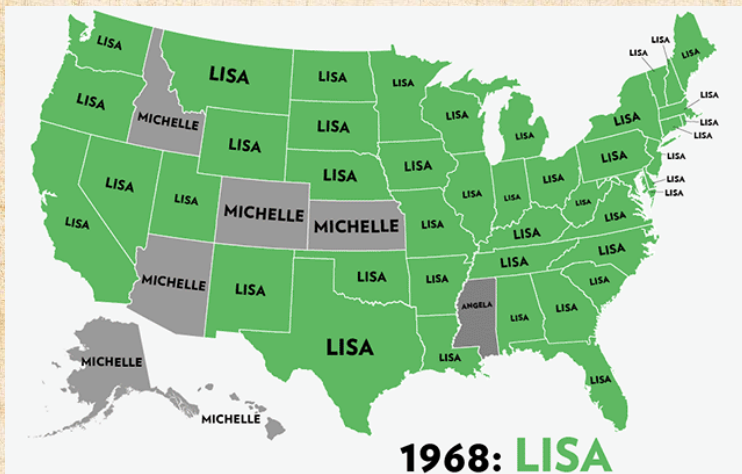
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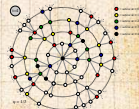


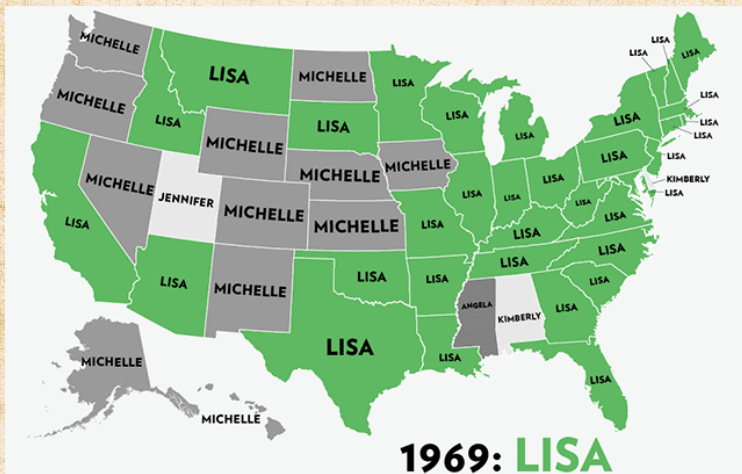
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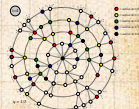


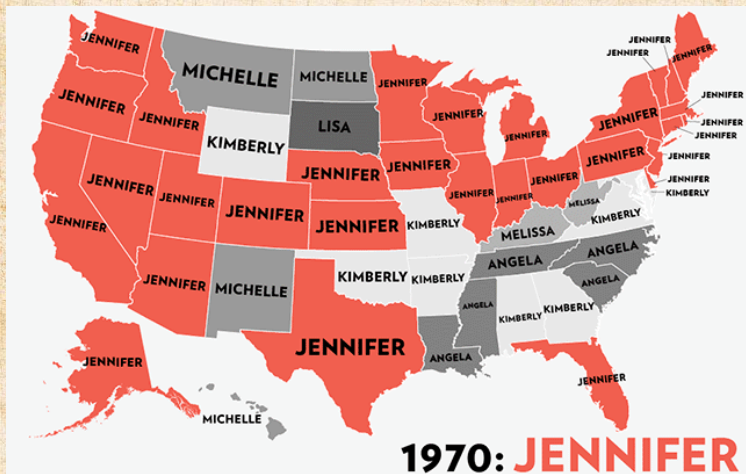
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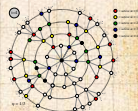


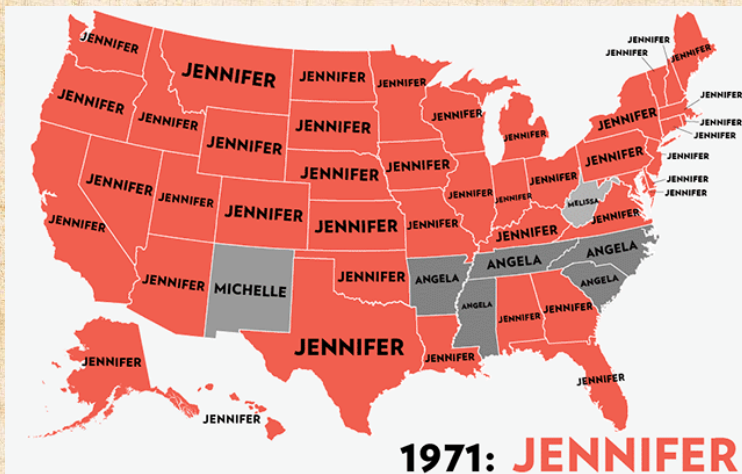
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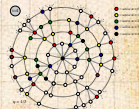


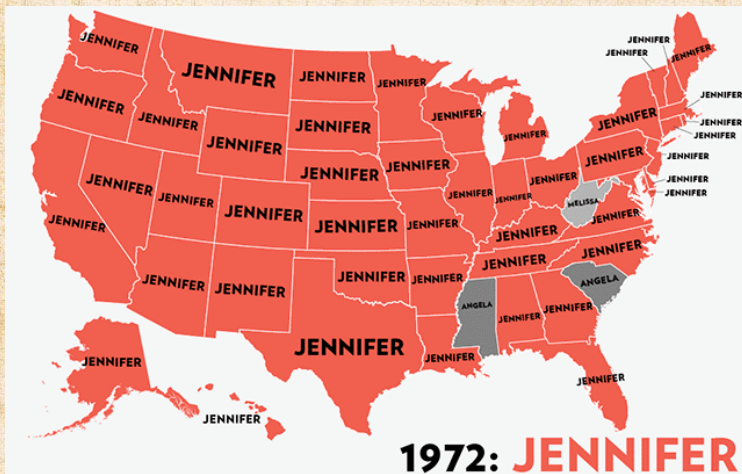
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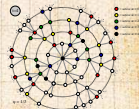


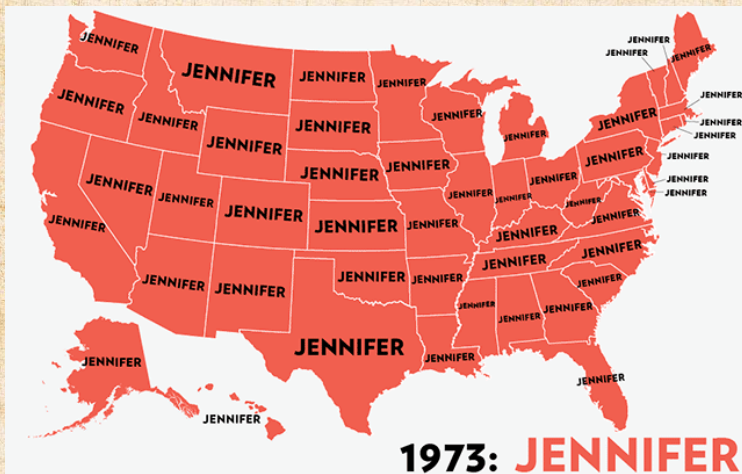
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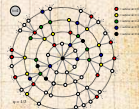


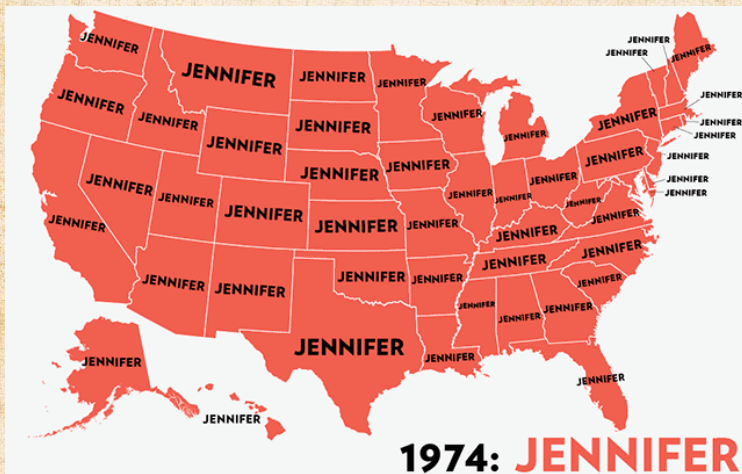
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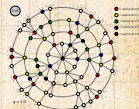


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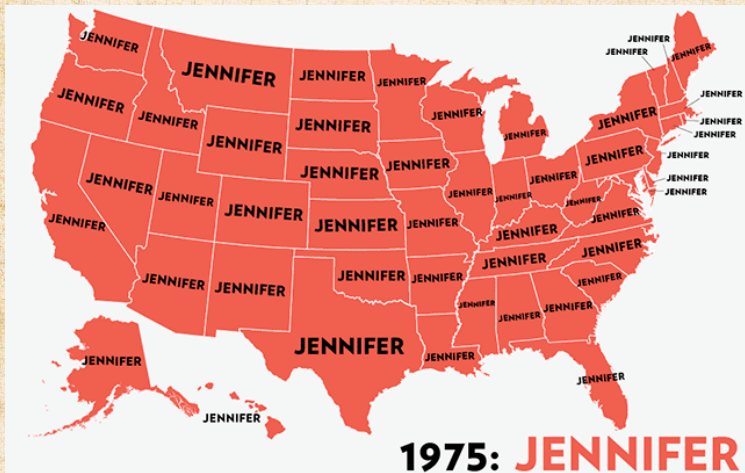
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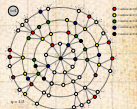


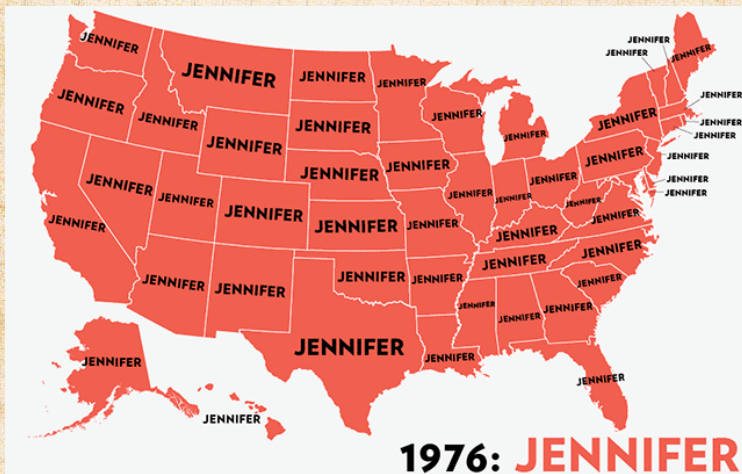
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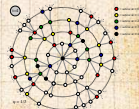


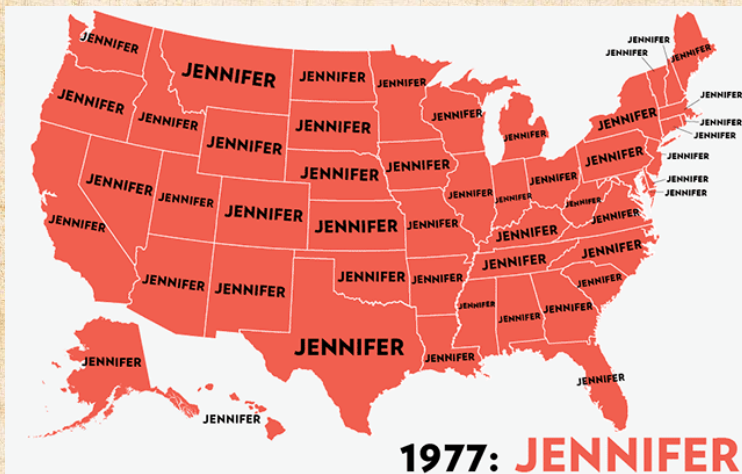
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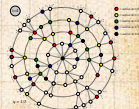


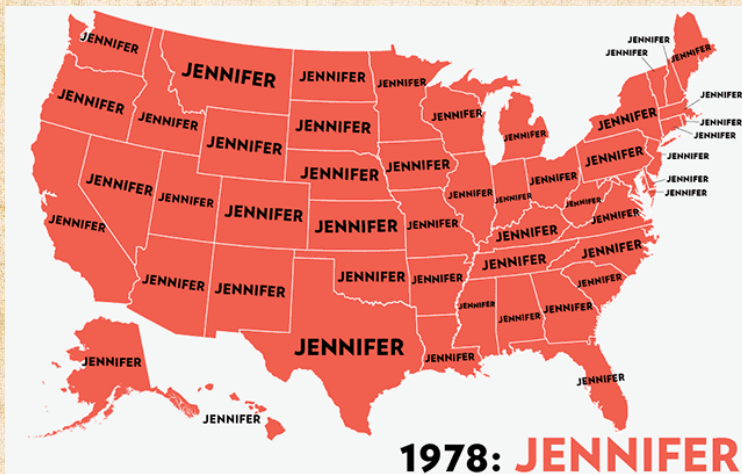
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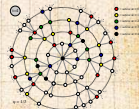


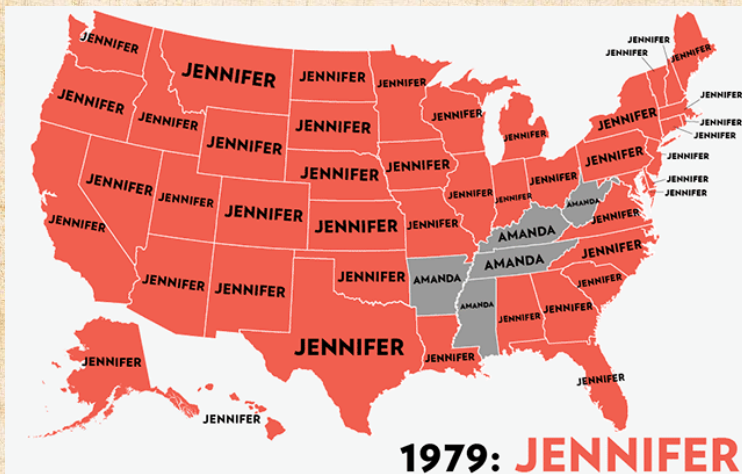
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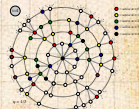


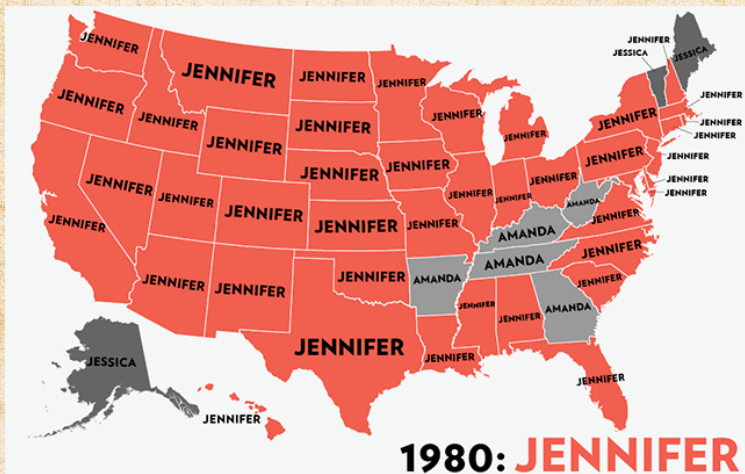
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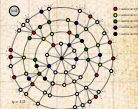


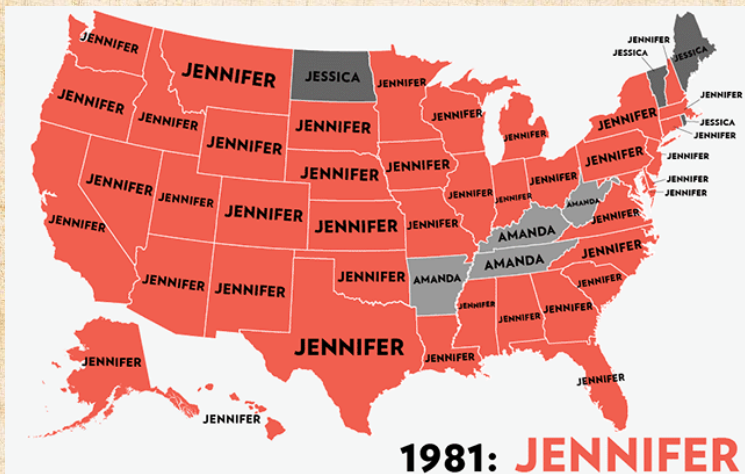
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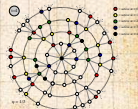


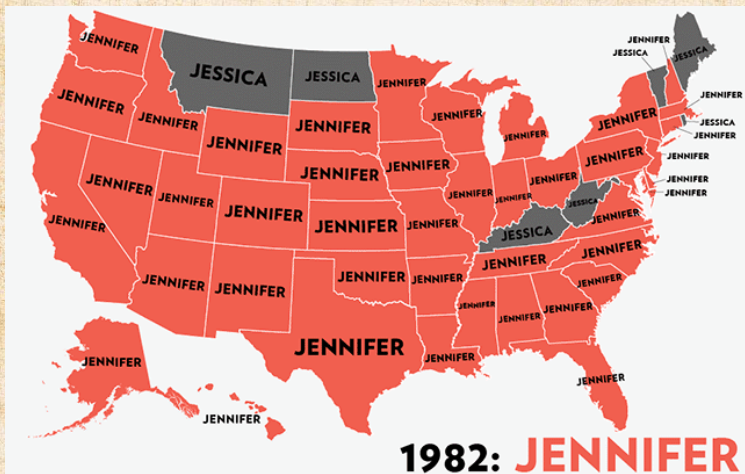
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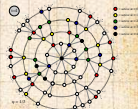


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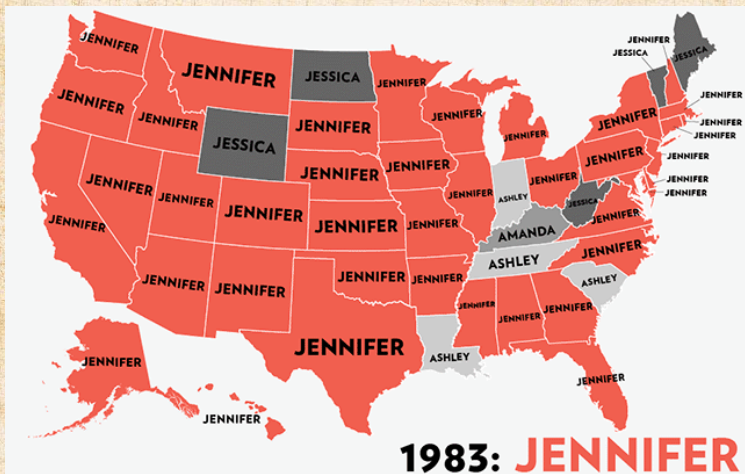
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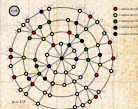


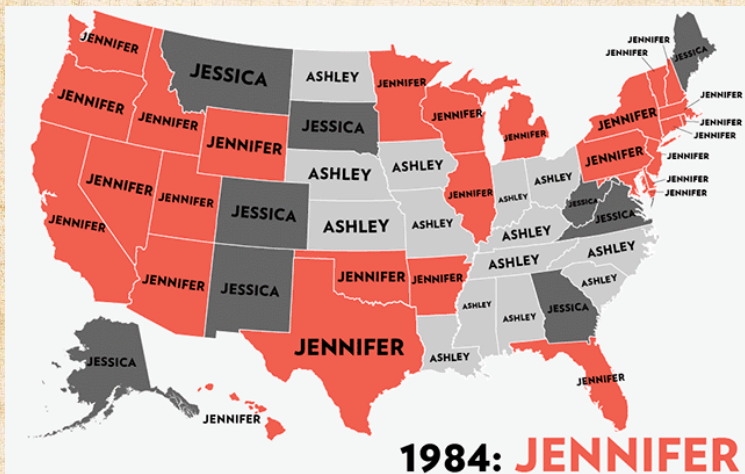
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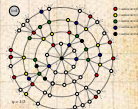


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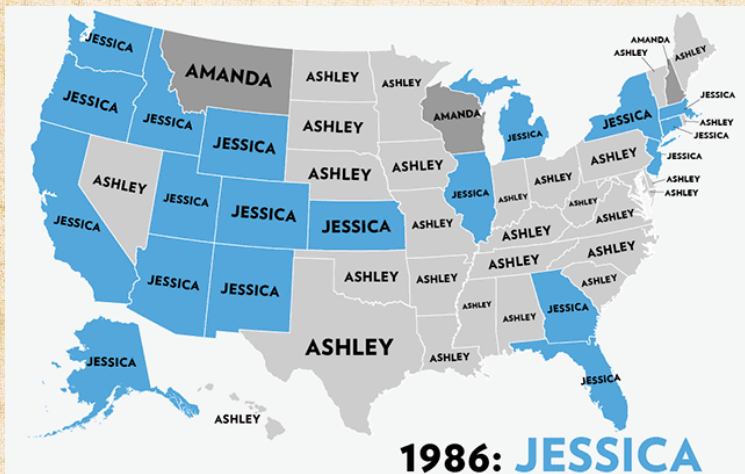
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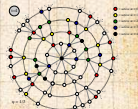


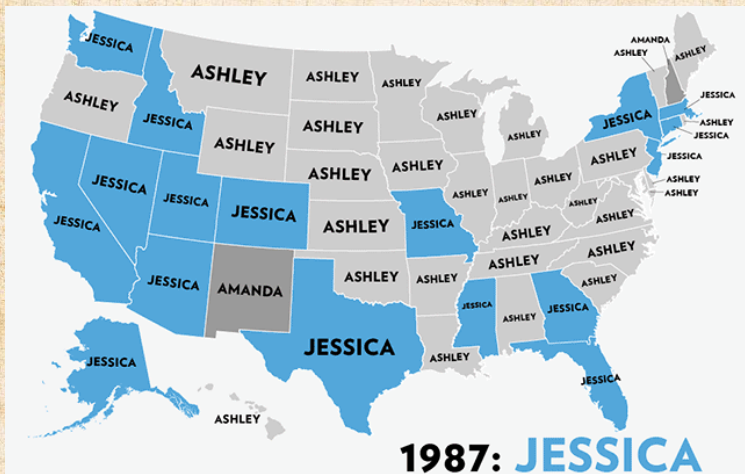
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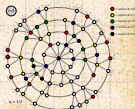


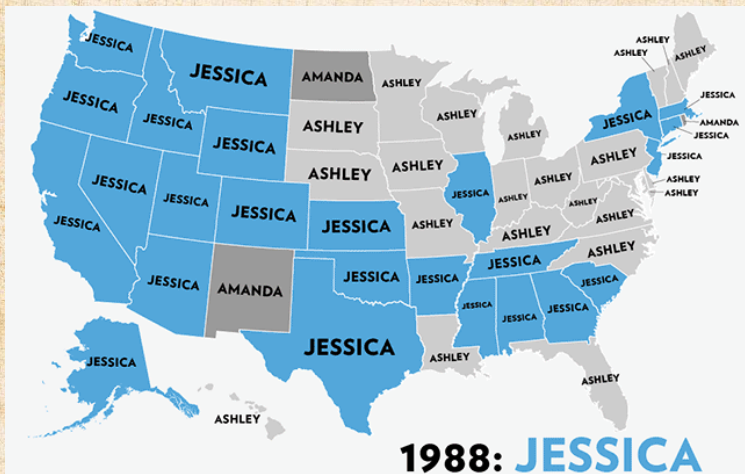
From the Atlantic 

## Social Contagion Models

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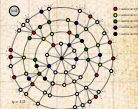


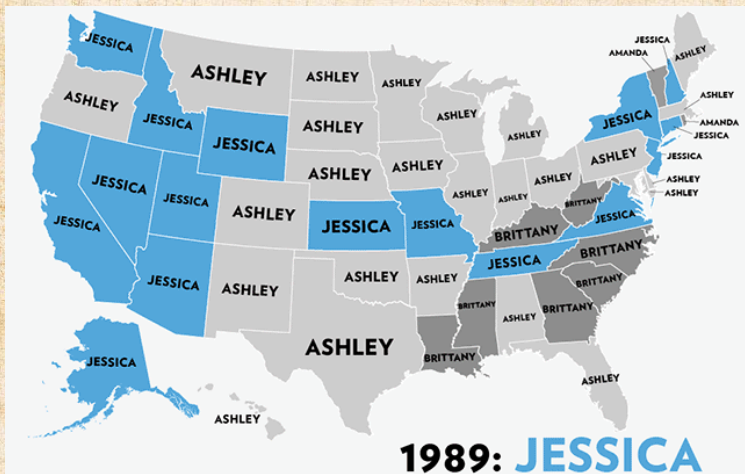
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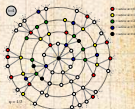


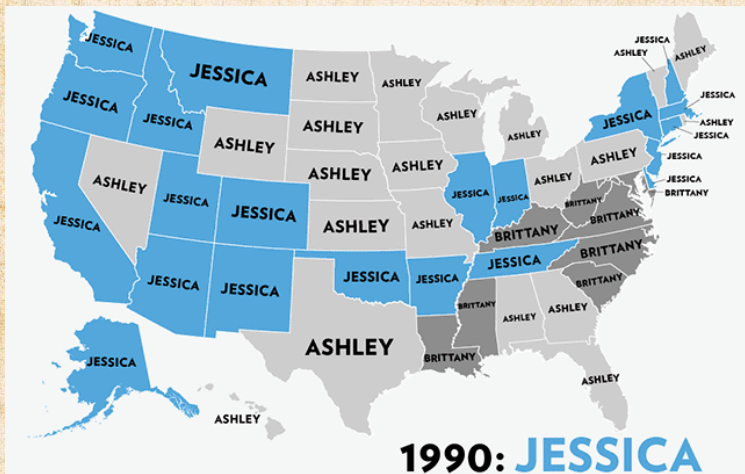
From the Atlantic ↗

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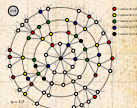


From the Atlantic 

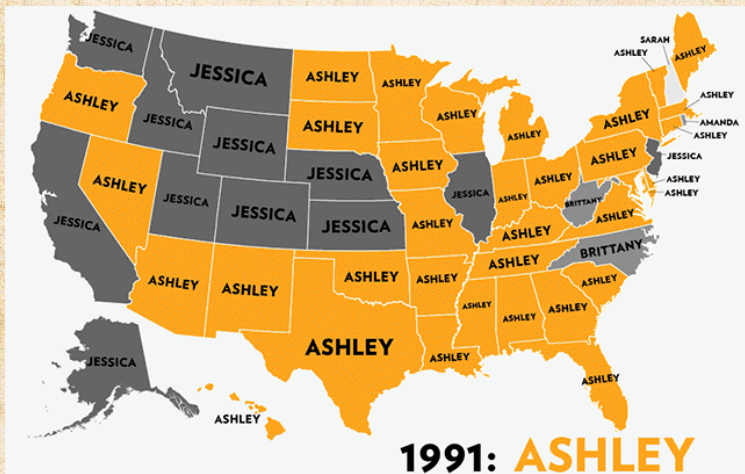
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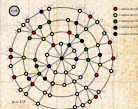


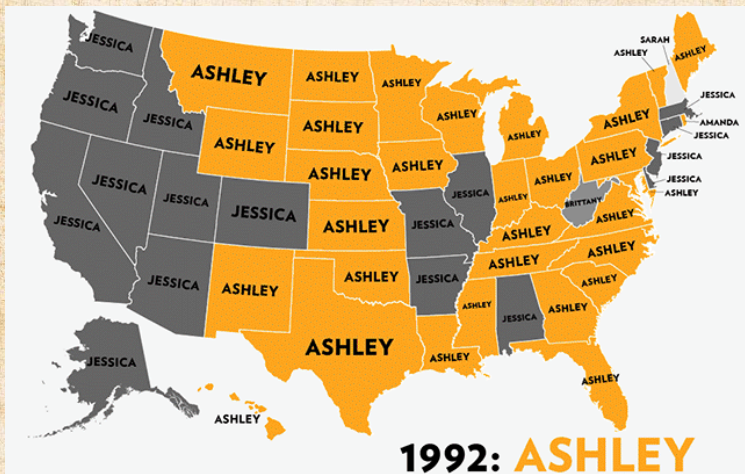
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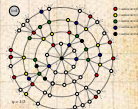


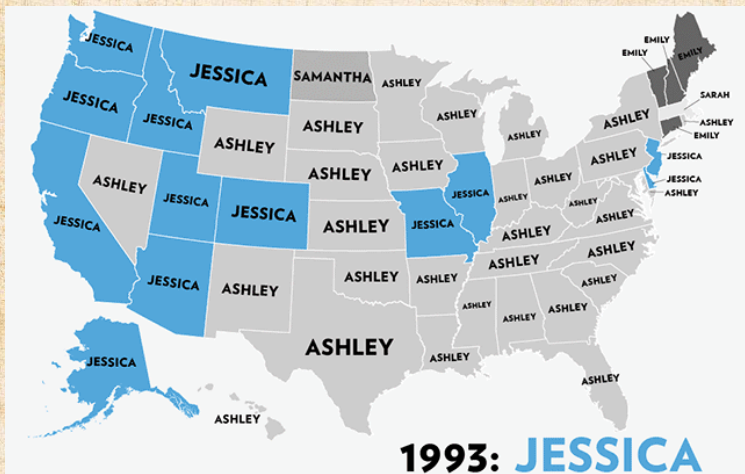
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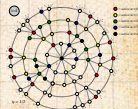


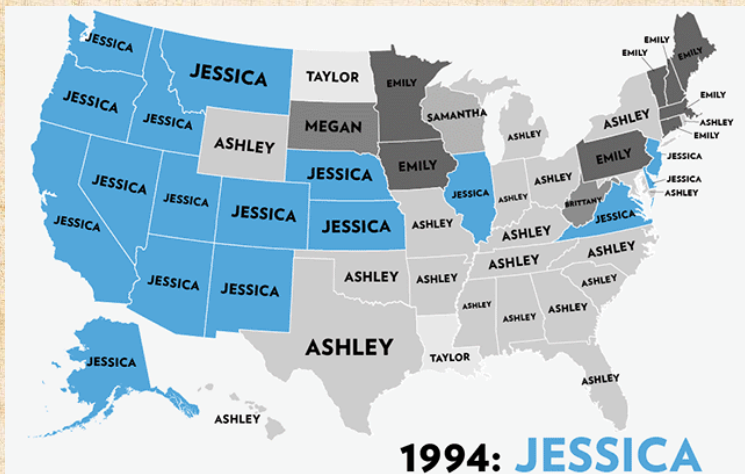
From the Atlantic 

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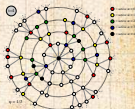


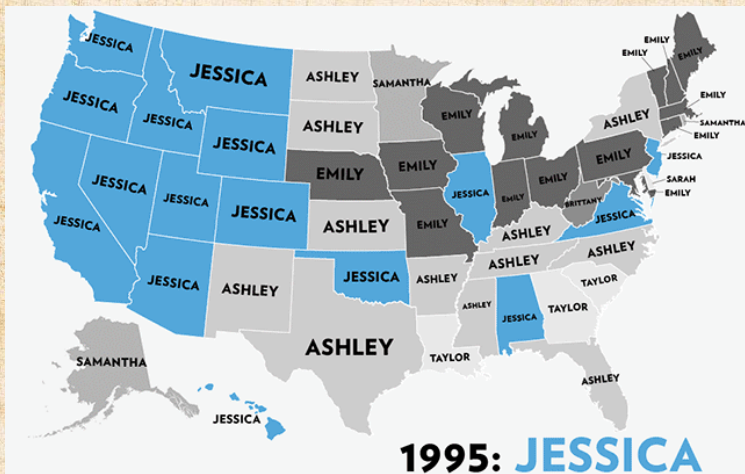
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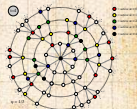


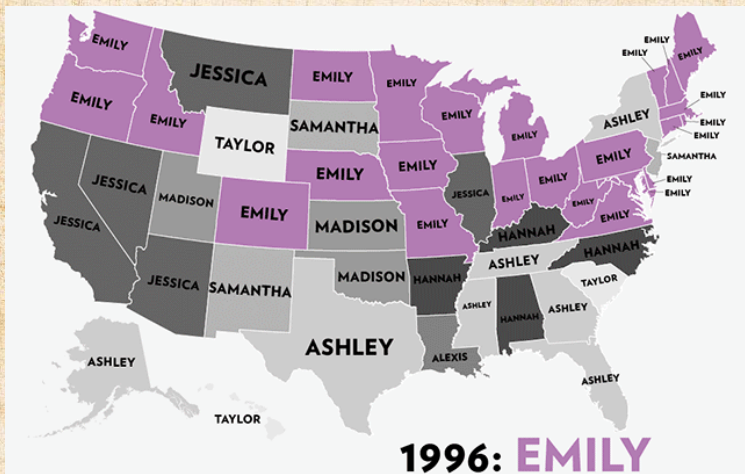
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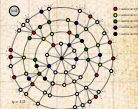


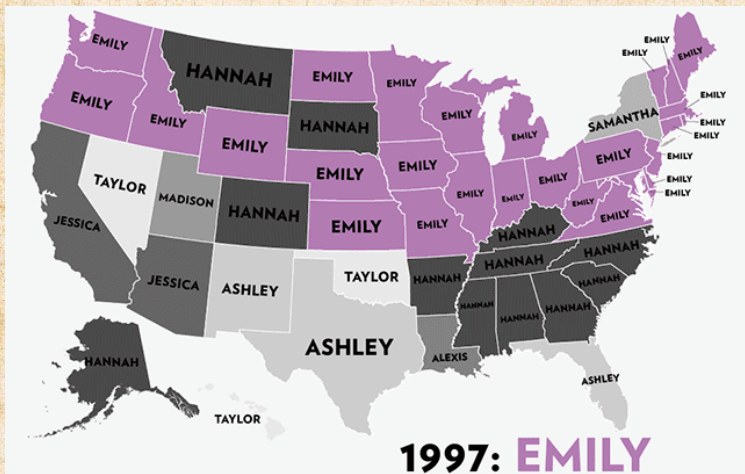
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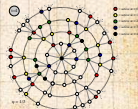


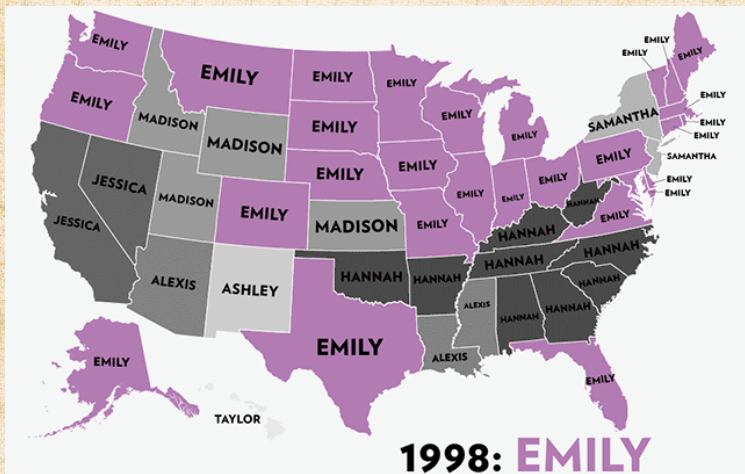
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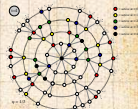


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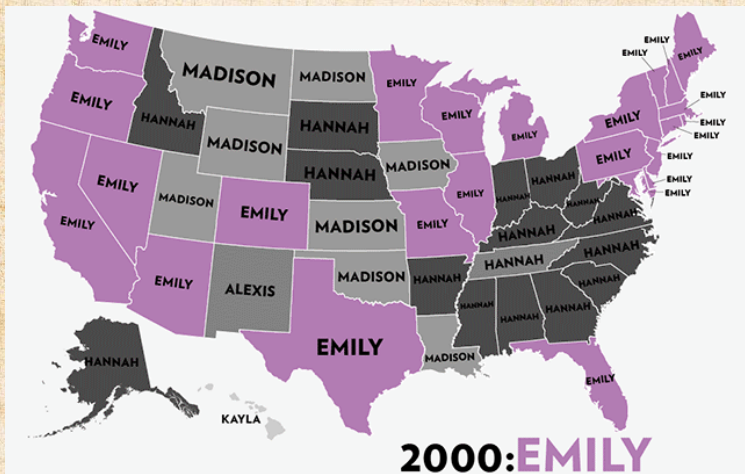
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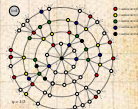


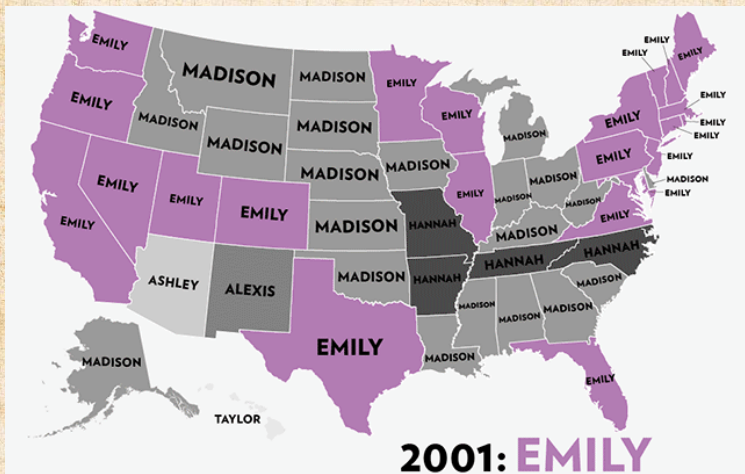
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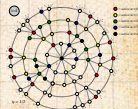


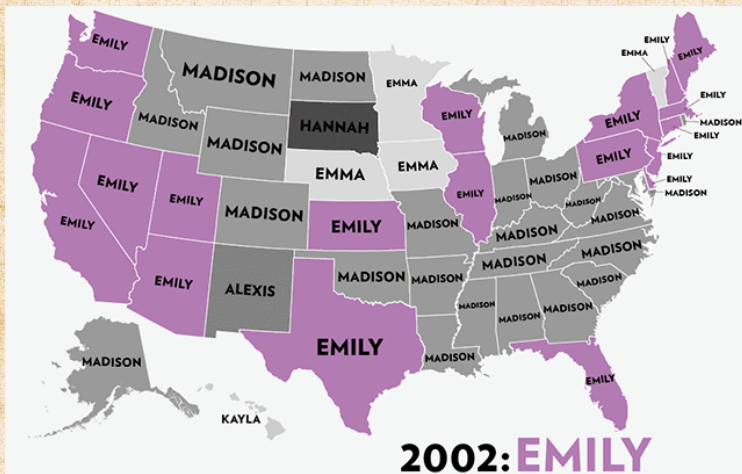
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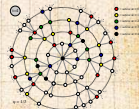


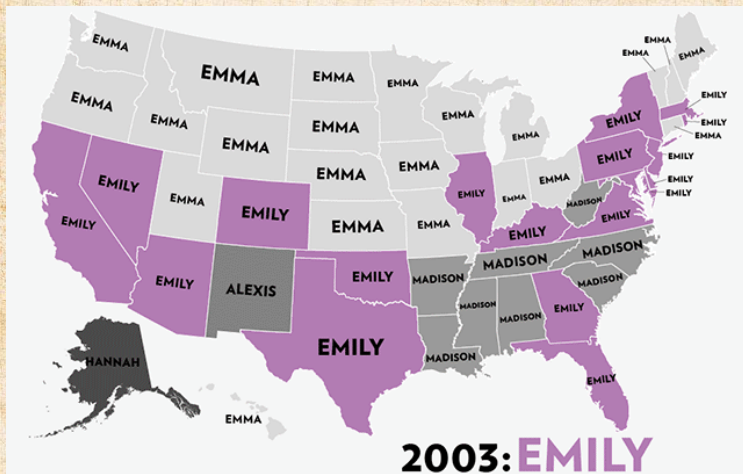
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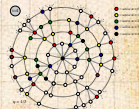


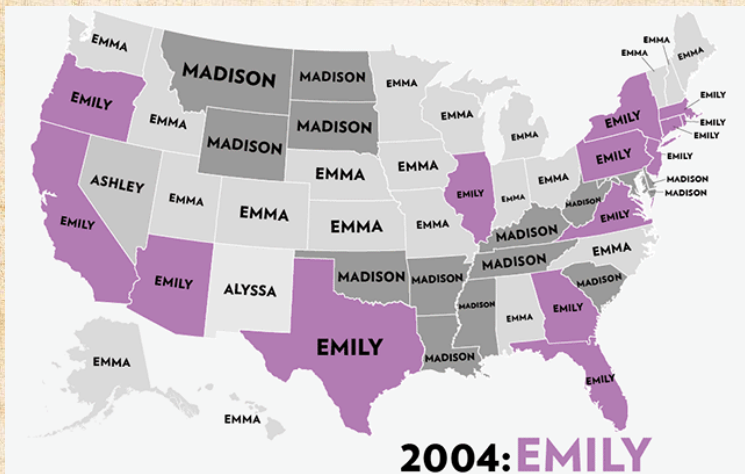
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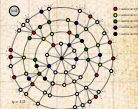


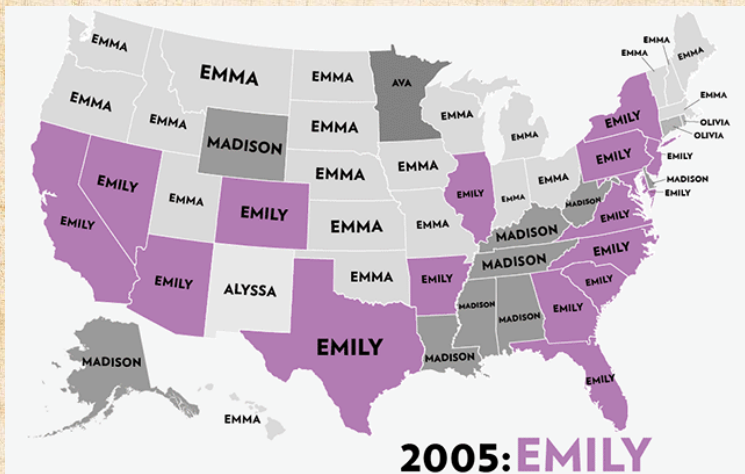
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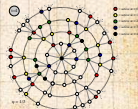


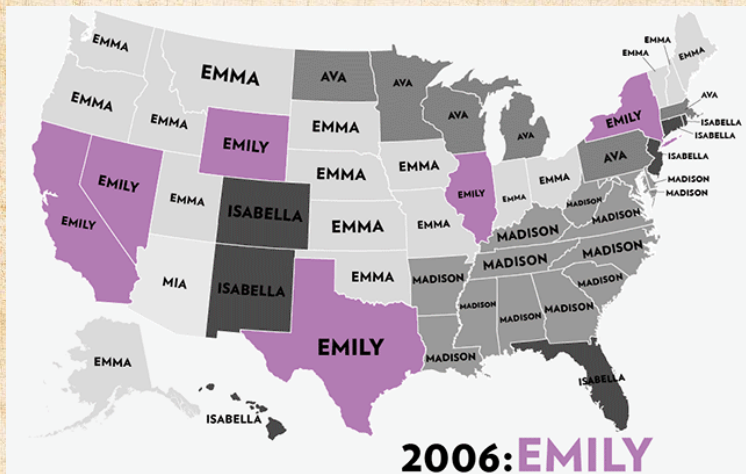
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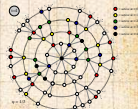


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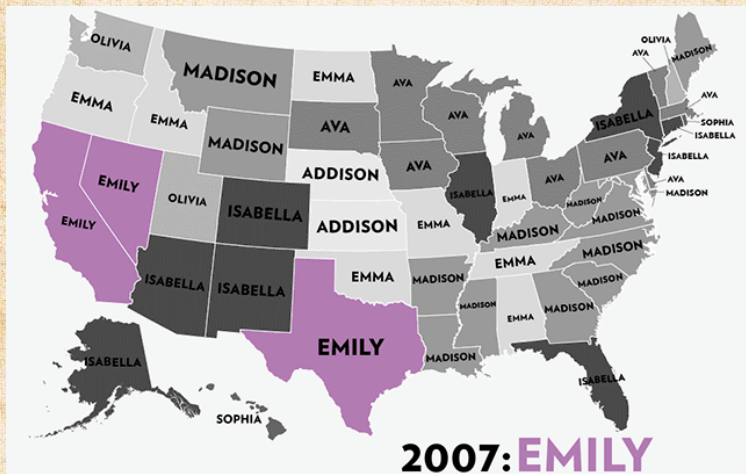
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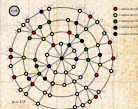


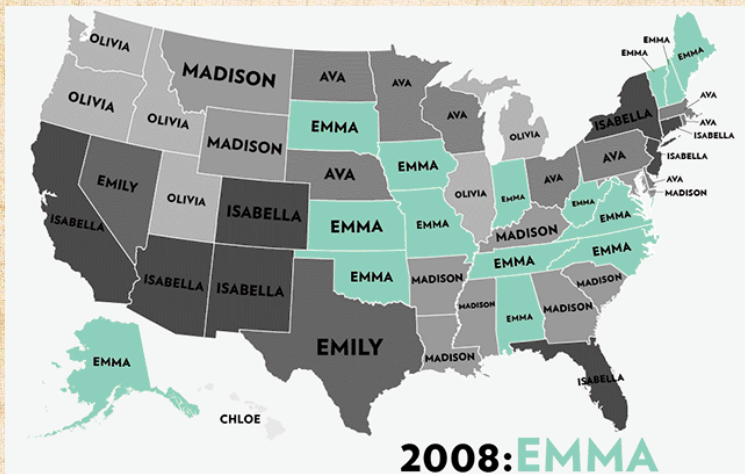
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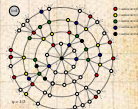


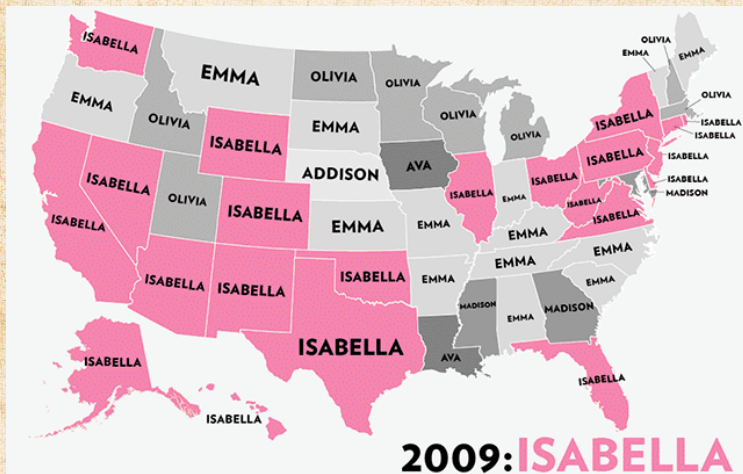
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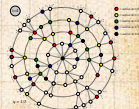


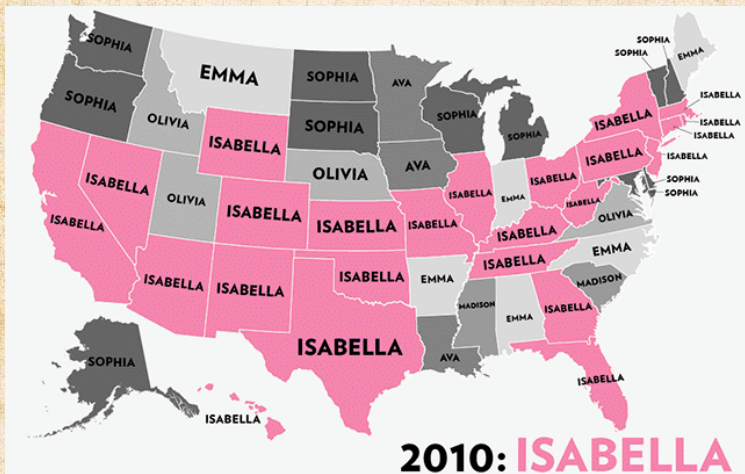
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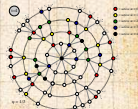


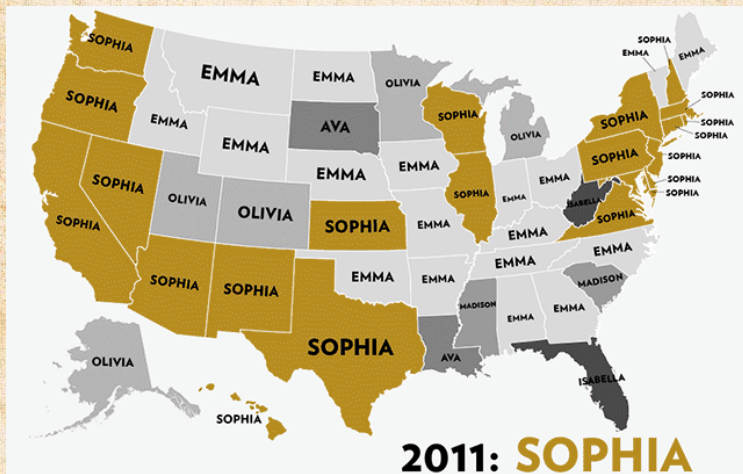
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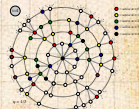


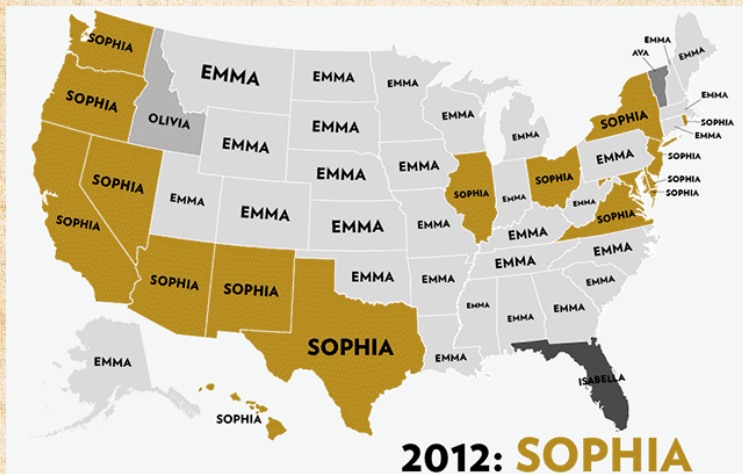
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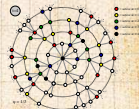


From the Atlantic 


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# Things that spread well:

[buzzfeed.com](http://buzzfeed.com) 



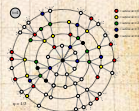
- ▶ Dangerously self aware: [11 Elements that make a perfect viral video.](#) 

+ News ...

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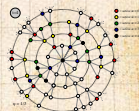
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+ News ...

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LOL + cute + fail + wtf:

PoCS | @pocsvox

Social Contagion

# Oopsie!

Social Contagion  
Models

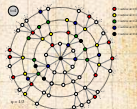
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References



**BUZZFEED FELL DOWN AND WENT BOOM.**

Please try reloading this page. If the problem persists [let us know](#).



# The whole lolcats thing:

PoCS | @pocsvox

Social Contagion

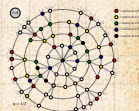


:-p

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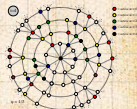
# Some things really stick:



## Social Contagion Models

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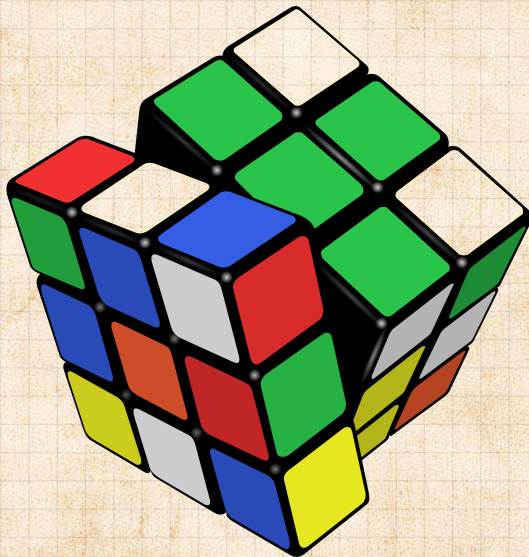
## References



wtf + geeky + omg:

PoCS | @pocsvox

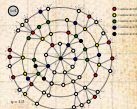
Social Contagion



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## Social Contagion Models

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Network version

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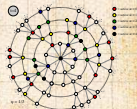
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Spreading success

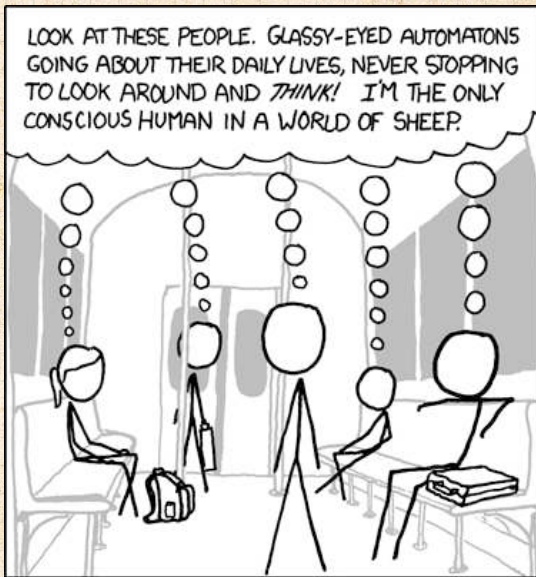
Groups

## References

## References



# Why social contagion works so well:



<http://xkcd.com/610/>

## Social Contagion Models

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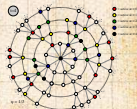
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# Social Contagion

PoCS | @pocsvox

Social Contagion



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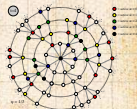
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Spreading success

Groups

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## Examples abound

- ▶ fashion
- ▶ striking
- ▶ smoking  [7]
- ▶ residential segregation [22]
- ▶ iPhones and iThings
- ▶ obesity  [6]
- ▶ Harry Potter
- ▶ voting
- ▶ gossip
- ▶ Rubik's cube 
- ▶ religious beliefs
- ▶ school shootings
- ▶ leaving lectures

## SIR and SIRS type contagion possible

- ▶ Classes of behavior versus specific behavior

## Social Contagion Models

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Granovetter's model

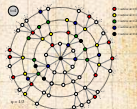
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Groups

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## Social Contagion Models

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Granovetter's model

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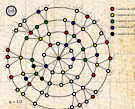
Spreading success

Groups




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- ▶ Classes of behavior versus specific behavior



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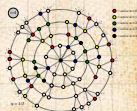
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Spreading success

Groups

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- ▶ religious beliefs
- ▶ school shootings
- ▶ **leaving lectures**

## SIR and SIRS type contagion possible

- ▶ Classes of behavior versus specific behavior :  
**dieting, horror movies, getting married, invading countries, ...**

### Social Contagion Models

#### Background

Granovetter's model

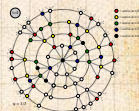
Network version

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Groups

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# Mixed messages: Please copy, but also, don't copy ...

## Social Contagion Models

### Background

Granovetter's model




Network version

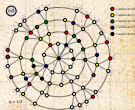
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Spreading success

Groups

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## Social Contagion Models

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Granovetter's model



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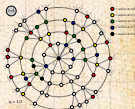
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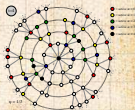
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# Market much?

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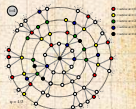
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Groups

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- ▶ The spread of quitting smoking  [7]
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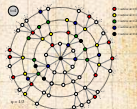
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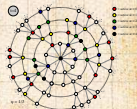
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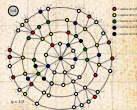
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Social Contagion  
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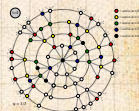
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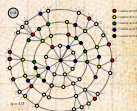
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- ▶ Widespread media influence
- ▶ Word-of-mouth influence

## We need to understand influence

- ▶ Who influences whom?
- ▶ What kinds of influence response functions are there?
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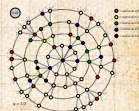
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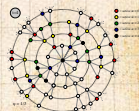
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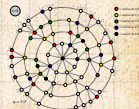
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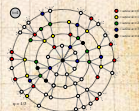
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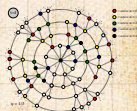
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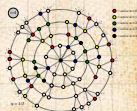
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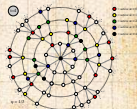
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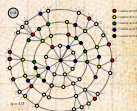
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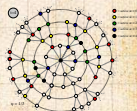
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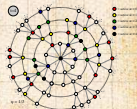
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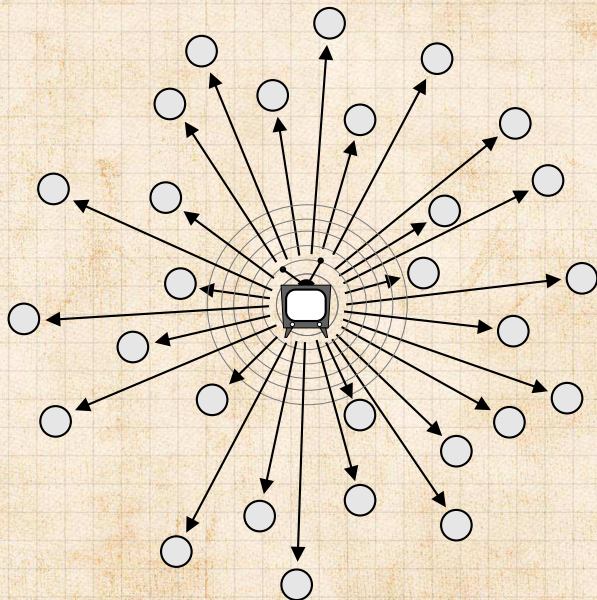
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# The hypodermic model of influence



## Social Contagion Models

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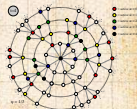
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Groups

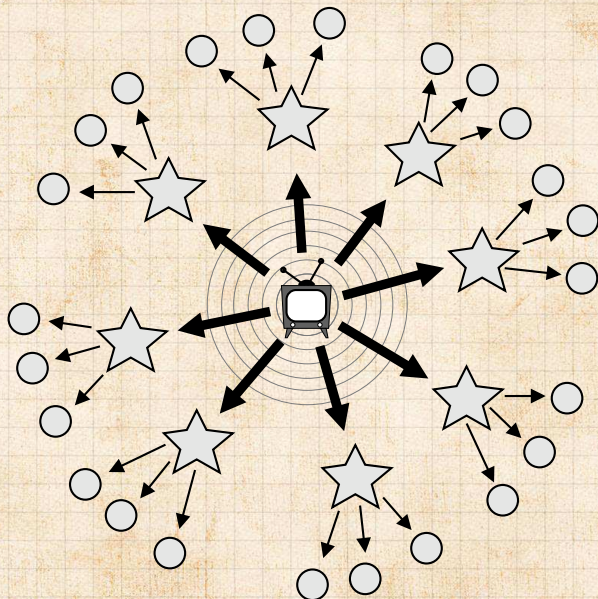
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# The two step model of influence [19]

PoCS | @pocsvox

Social Contagion



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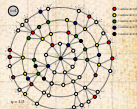
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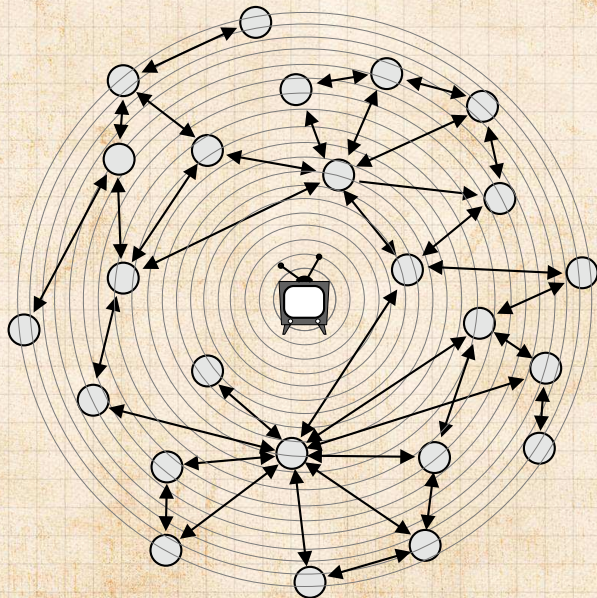
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# The general model of influence: the Social Wild



## Social Contagion Models

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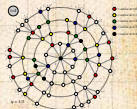
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# Talking about the social wild:

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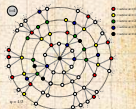
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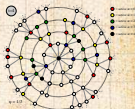
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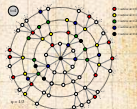
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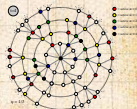
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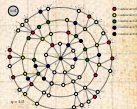
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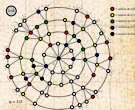
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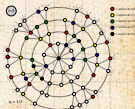
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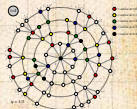
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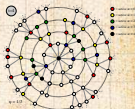
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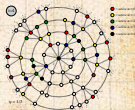
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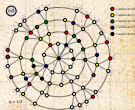
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# The Mona Lisa



## Social Contagion Models

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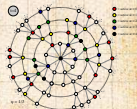
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- ▶ “Becoming Mona Lisa: The Making of a Global Icon”—David Sassoon
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# The Mona Lisa



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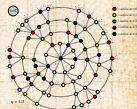
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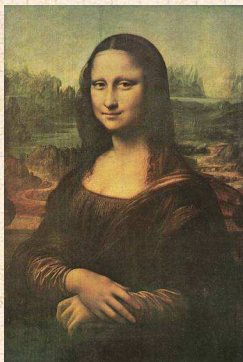
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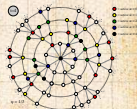
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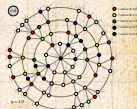
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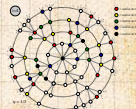
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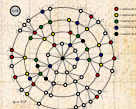
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# 'Tattooed Guy' Was Pivotal in Armstrong Case [nytimes] ↗

PoCS | @pocsvox

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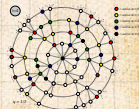
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- ▶ "... Leogrande's doping sparked a series of events ..."

# The completely unpredicted fall of Eastern Europe

PoCS | @pocsvox  
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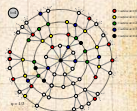


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Timur Kuran: [20, 21] "Now Out of Never: The Element of Surprise in the East European Revolution of 1989"





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### Social Contagion Models

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# Drafting success in the NFL: ↗

## Top Players by Round, 1995-2012



1ST ROUND  
**Peyton Manning**  
1ST OVER ALL, 1998



2ND ROUND  
**Drew Brees**  
32ND PICK, 2001



3RD ROUND  
**Terrell Owens**  
89TH PICK, 1996



4TH ROUND  
**Jared Allen**  
126TH PICK, 2004



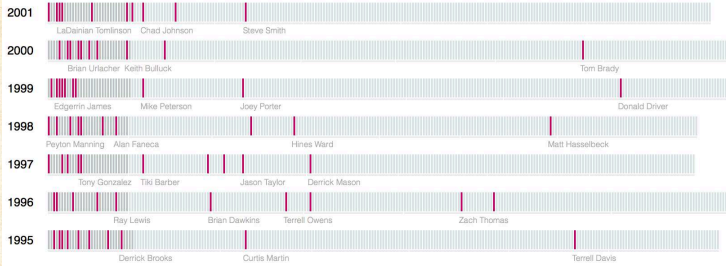
5TH ROUND  
**Zach Thomas**  
154TH PICK, 1996



6TH ROUND  
**Tom Brady**  
199TH PICK, 2000



7TH ROUND  
**Donald Driver**  
213TH PICK, 1999



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## Messaging with social connections

- ▶ Ads based on message content
- ▶ BzzAgent 
- ▶ One of Facebook's early advertising attempts: Beacon 
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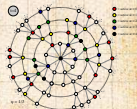
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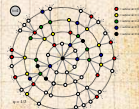
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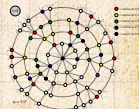
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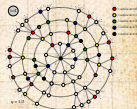
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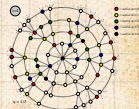
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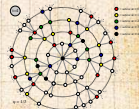
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# Getting others to do things for you

A very good book: 'Influence'<sup>[8]</sup> by Robert Cialdini 

## Six modes of influence:

1. Reciprocation: *The Old Give and Take... and Take*; e.g., Free samples, Hare Krishnas.
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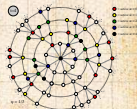
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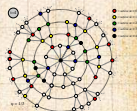
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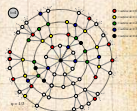
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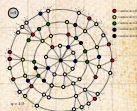
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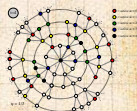
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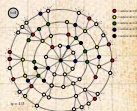
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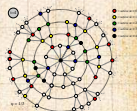
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References



# Getting others to do things for you

A very good book: 'Influence' <sup>[8]</sup> by Robert Cialdini ↗

## Six modes of influence:

1. **Reciprocation**: *The Old Give and Take... and Take*; e.g., Free samples, Hare Krishnas.
2. **Commitment and Consistency**: *Hobgoblins of the Mind*; e.g., Hazing.
3. **Social Proof**: *Truths Are Us*; e.g., Jonestown ↗, Kitty Genovese ↗ (contested).
4. **Liking**: *The Friendly Thief*; e.g., Separation into groups is enough to cause problems.
5. **Authority**: *Directed Deference*; e.g., Milgram's obedience to authority experiment. ↗
6. **Scarcity**: *The Rule of the Few*; e.g., Prohibition.

Social Contagion  
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Background

Granovetter's model

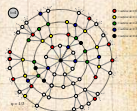
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- ▶ Cialdini's modes are heuristics that help us get through life.
- ▶ Useful but can be leveraged...

## Other acts of influence:

- ▶ Conspicuous Consumption (Veblen, 1912)
- ▶ Conspicuous Destruction (Pottlatch)

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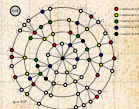
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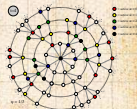
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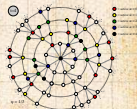
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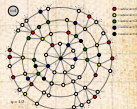
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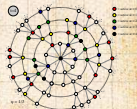
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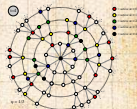
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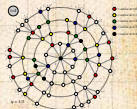
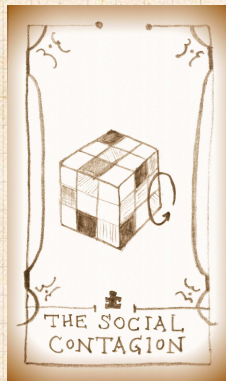
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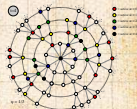
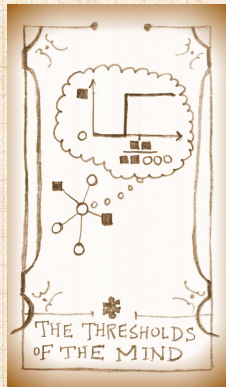
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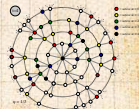
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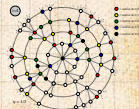
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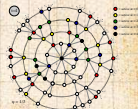
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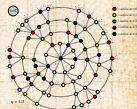
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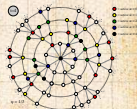
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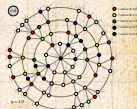
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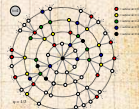
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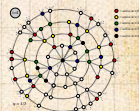
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## Thresholds

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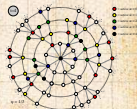
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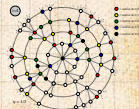
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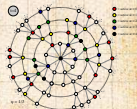
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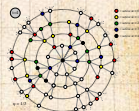
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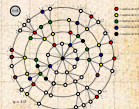
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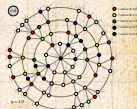
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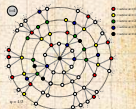
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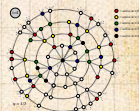
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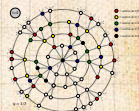
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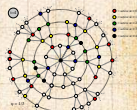
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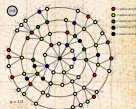
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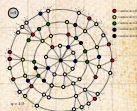
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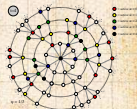
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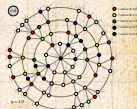
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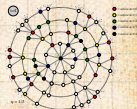
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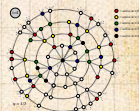
Network version

Final size

Spreading success

Groups

## References



## Shareworthy interlude

### Social Contagion Models

#### Background

Granovetter's model

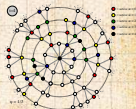
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## Social Contagion Models

Background

Granovetter's model

Network version

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Groups

## Social Contagion Models

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**Granovetter's model**

Network version

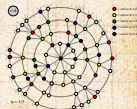
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# Threshold models—response functions

## Social Contagion Models

Background

Granovetter's model

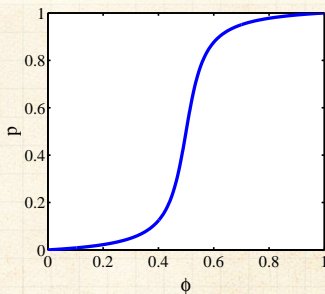
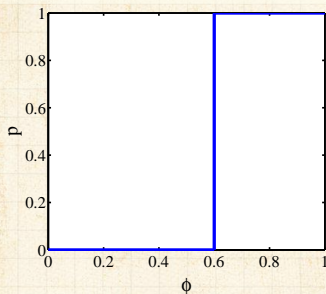
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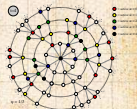
Spreading success

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- ▶ Example threshold influence response functions:  
**deterministic** and **stochastic**
- ▶  $\phi$  = fraction of contacts 'on' (e.g., rioting)
- ▶ Two states: S and I.



# Threshold models—response functions

## Social Contagion Models

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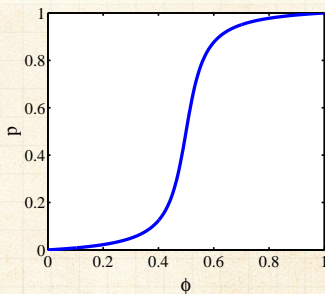
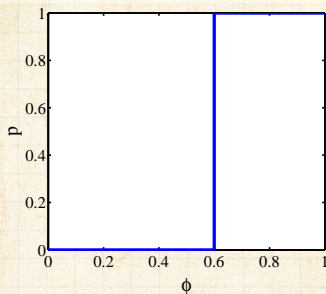
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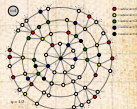
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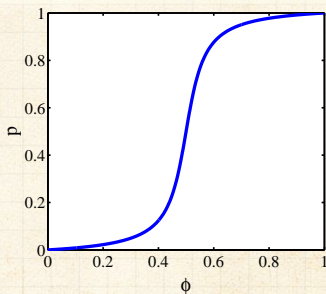
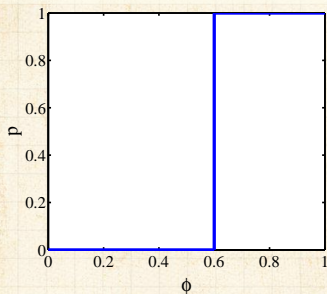
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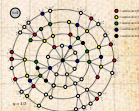
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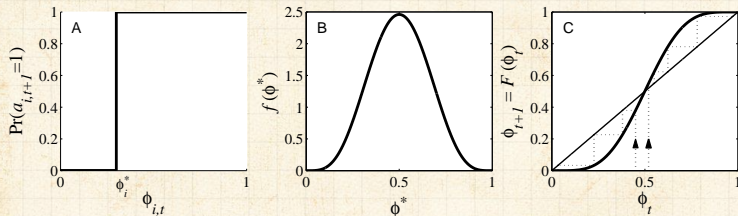
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## Action based on perceived behavior of others:



- ▶ Two states: S and I.
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- ▶ Discrete time update (strong assumption!)
- ▶ This is a **Critical mass model**

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Granovetter's model

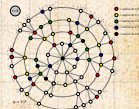
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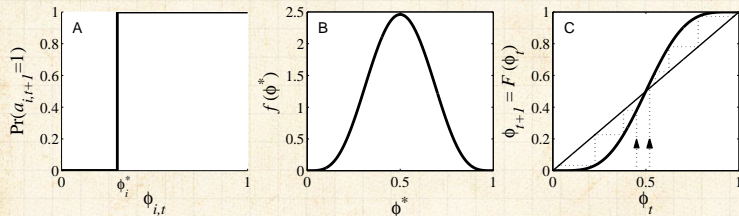
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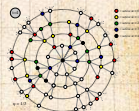
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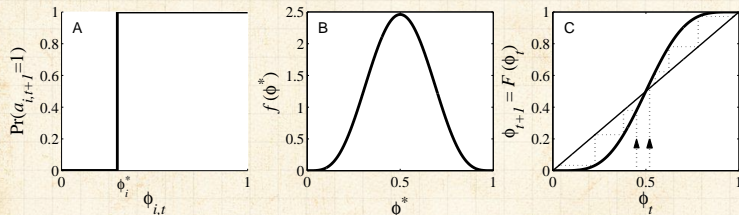
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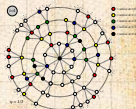
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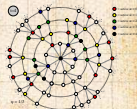
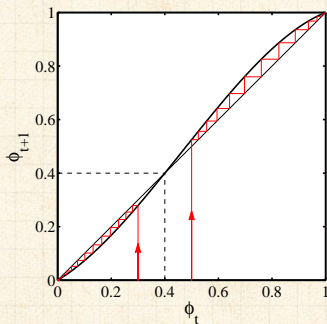
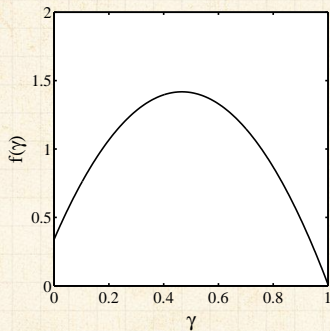
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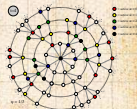
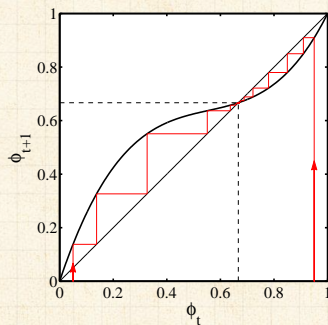
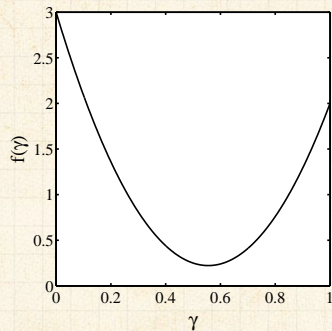
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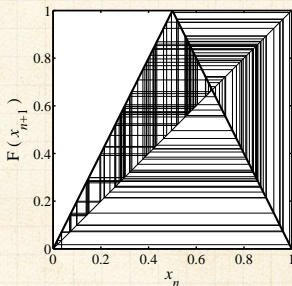
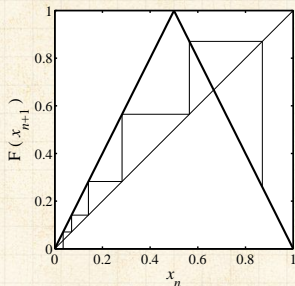
Another example of critical mass model:



Example of single stable state model:



## Chaotic behavior possible [17, 16, 9, 18]



- ▶ Period doubling arises as map amplitude  $r$  is increased.
- ▶ Synchronous update assumption is crucial

## Social Contagion Models

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Granovetter's model

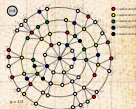
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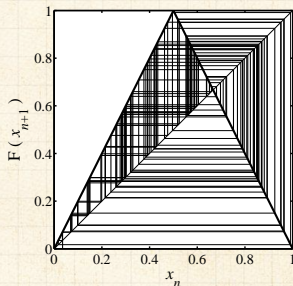
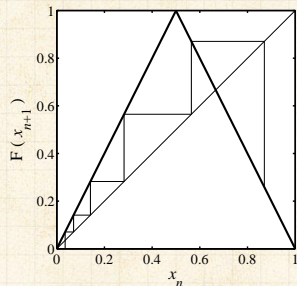
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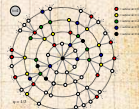
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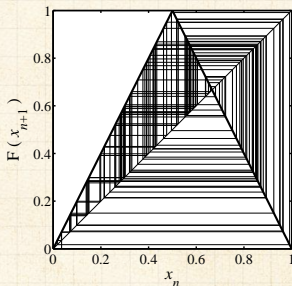
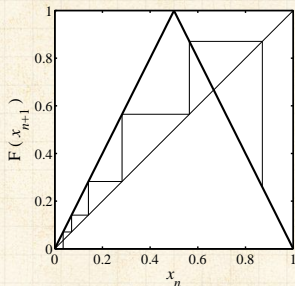
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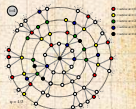
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## Implications for collective action theory:

1. Collective uniformity  $\Rightarrow$  individual uniformity
2. Small individual changes  $\Rightarrow$  large global changes
3. The stories/dynamics of complex systems are conceptually inaccessible for individual-centric narratives.
4. System stories live in left null space of our stories—we can't even see them.
5. But we happily impose simplistic, individual-centric stories—we can't help ourselves.

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**Granovetter's model**

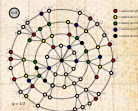
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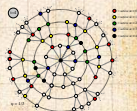
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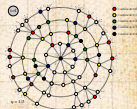
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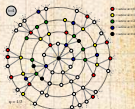
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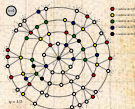
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Social Contagion  
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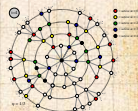
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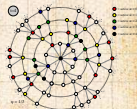
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- ▶ "A simple model of global cascades on random networks"

D. J. Watts. Proc. Natl. Acad. Sci., 2002 [26]

- ▶ Mean field model → network model
- ▶ Individuals now have a limited view of the world

## Social Contagion Models

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## We'll also explore:

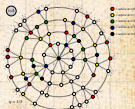
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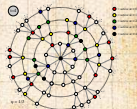
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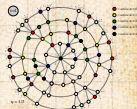
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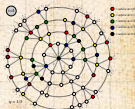
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# Threshold model on a network

- ▶ Interactions between individuals now represented by a network.
- ▶ Network is **sparse**.
- ▶ Individual  $i$  has  $k_i$  contacts.
- ▶ Influence on each link is **reciprocal** and of **unit weight**.
- ▶ Each individual  $i$  has a fixed threshold  $\phi_i$ .
- ▶ Individuals repeatedly poll contacts on network.
- ▶ Synchronous, discrete time updating.
- ▶ Individual  $i$  becomes active when fraction of active contacts  $\frac{a}{k} \geq \phi_i$ .
- ▶ Individuals remain active when switched (no recovery = SI model).

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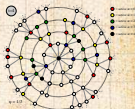
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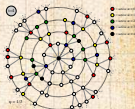
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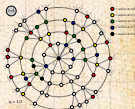
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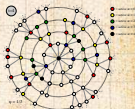
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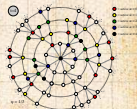
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# Threshold model on a network

- ▶ Interactions between individuals now represented by a network.
- ▶ Network is **sparse**.
- ▶ Individual  $i$  has  $k_i$  contacts.
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## Social Contagion Models

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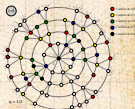
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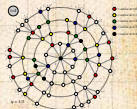
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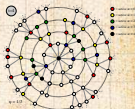
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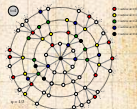
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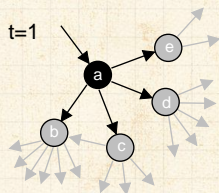
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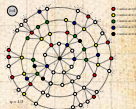
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- All nodes have threshold  $\phi = 0.2$ .



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## Social Contagion Models

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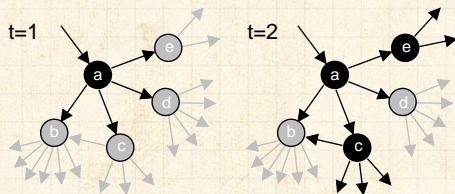
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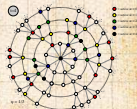
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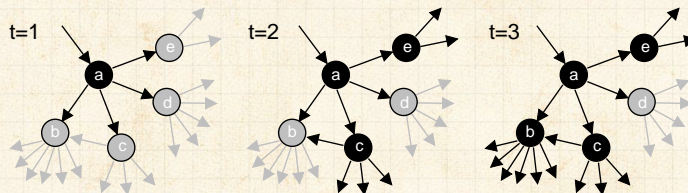
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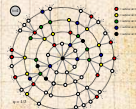
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## First study random networks:

- ▶ Start with  $N$  nodes with a degree distribution  $P_k$
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Granovetter's model

Network version

Final size

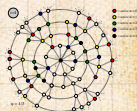
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1. If one individual is initially activated, what is the probability that an activation will spread over a network?
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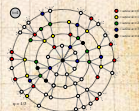
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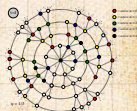
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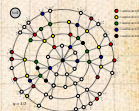
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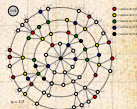
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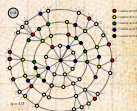
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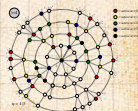
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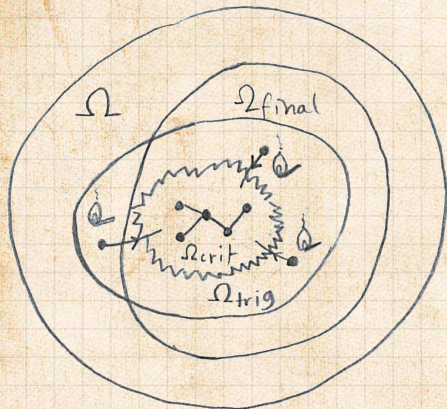
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# Example random network structure:



- ▶  $\Omega_{crit} = \Omega_{vuln} =$   
critical mass =  
global  
vulnerable  
component
- ▶  $\Omega_{trig} =$   
triggering  
component
- ▶  $\Omega_{final} =$   
potential  
extent of  
spread
- ▶  $\Omega =$  entire  
network

Social Contagion  
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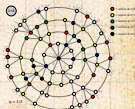
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$$\Omega_{crit} \subset \Omega_{trig}; \Omega_{crit} \subset \Omega_{final}; \text{ and } \Omega_{trig}, \Omega_{final} \subset \Omega.$$

## Follow active links

- ▶ An active link is a link connected to an activated node.
- ▶ If an infected link leads to **at least 1 more infected link**, then **activation spreads**.
- ▶ We need to understand which nodes can be activated when only one of their neighbors becomes active.

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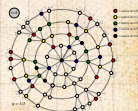
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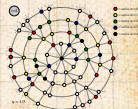
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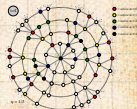
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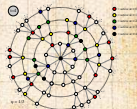
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# The most gullible

## Vulnerables:

- ▶ We call individuals who can be activated by just one contact being active **vulnerables**
- ▶ The vulnerability condition for node  $i$ :

$$1/k_i \geq \phi_i$$

- ▶ Which means # contacts  $k_i \leq \lfloor 1/\phi_i \rfloor$
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- ▶ Network story: 1 node  $\rightarrow$  critical mass  $\rightarrow$  everyone.

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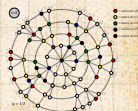
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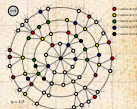
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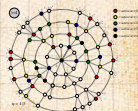
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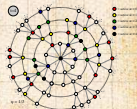
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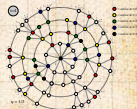
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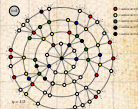
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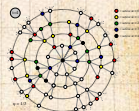
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- ▶ Normalization:

$$\sum_{k=0}^{\infty} kP_k = \langle k \rangle$$

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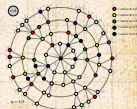
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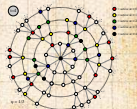
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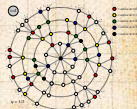
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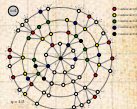
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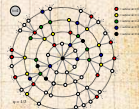
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## Next: Vulnerability of linked node

- ▶ Linked node is **vulnerable** with probability

$$\beta_k = \int_{\phi'_*=0}^{1/k} f(\phi'_*) d\phi'_*$$

- ▶ If linked node is **vulnerable**, it produces  $k - 1$  **new** outgoing active links
- ▶ If linked node is **not vulnerable**, it produces **no** active links.

### Social Contagion Models

Background

Granovetter's model

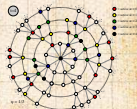
Network version

Final size

Spreading success

Groups

### References

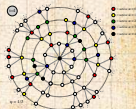


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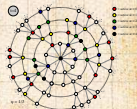


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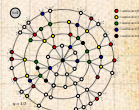
Network version

Final size

Spreading success

Groups

### References



## Putting things together:

- ▶ Expected number of active edges produced by an active edge:

$$R = \left[ \sum_{k=1}^{\infty} \underbrace{(k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle}}_{\text{success}} + \right]$$
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## Social Contagion Models

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Granovetter's model

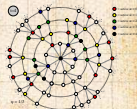
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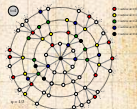
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## Social Contagion Models

[Background](#)[Granovetter's model](#)[Network version](#)[Final size](#)[Spreading success](#)[Groups](#)

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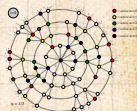
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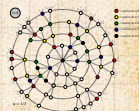
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[Background](#)[Granovetter's model](#)[Network version](#)[Final size](#)[Spreading success](#)[Groups](#)

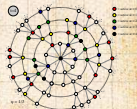
## References



So... for random networks with fixed degree distributions, cascades take off when:

$$\sum_{k=1}^{\infty} (k-1) \cdot \beta_k \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

- ▶  $\beta_k$  = probability a degree  $k$  node is vulnerable.
- ▶  $P_k$  = probability a node has degree  $k$ .



## Two special cases:

- ▶ (1) Simple disease-like spreading succeeds:  $\beta_k = \beta$

$$\beta \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

- ▶ (2) Giant component exists:  $\beta = 1$

$$1 \cdot \sum_{k=1}^{\infty} (k-1) \cdot \frac{kP_k}{\langle k \rangle} > 1.$$

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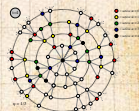
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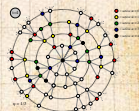
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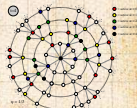
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## Social Contagion Models

Background

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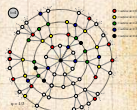
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Granovetter's model

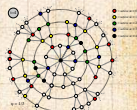
Network version

Final size

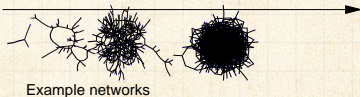
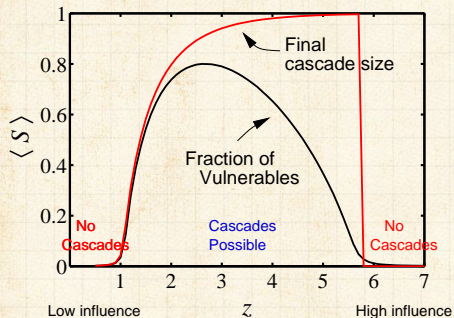
Spreading success

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# Cascades on random networks



► Cascades occur only if size of max vulnerable cluster  $> 0$ .

► System may be 'robust-yet-fragile'.

► 'Ignorance' facilitates spreading.

## Social Contagion Models

Background

Granovetter's model

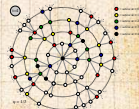
Network version

Final size

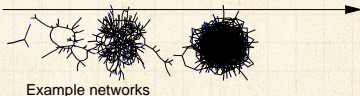
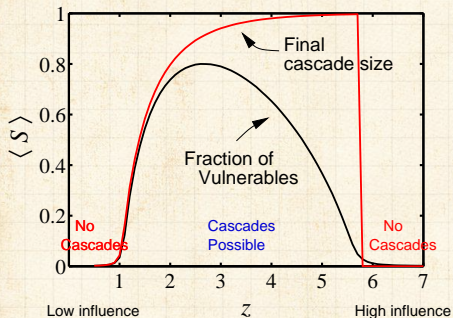
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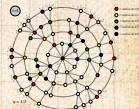


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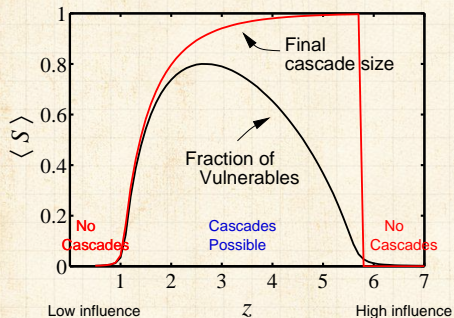
## Social Contagion Models

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- Granovetter's model
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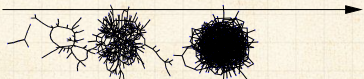
# Cascades on random networks



Low influence

$z$

High influence



Example networks

- ▶ Cascades occur only if size of max vulnerable cluster  $> 0$ .
- ▶ System may be 'robust-yet-fragile'.
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## Social Contagion Models

Background

Granovetter's model

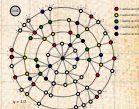
Network version

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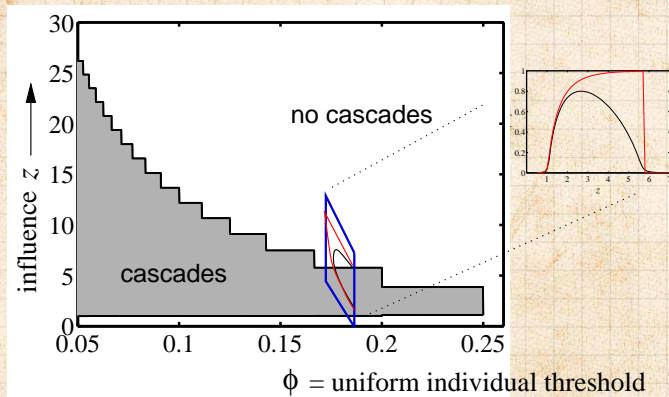
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# Cascade window for random networks



## Social Contagion Models

Background

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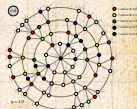
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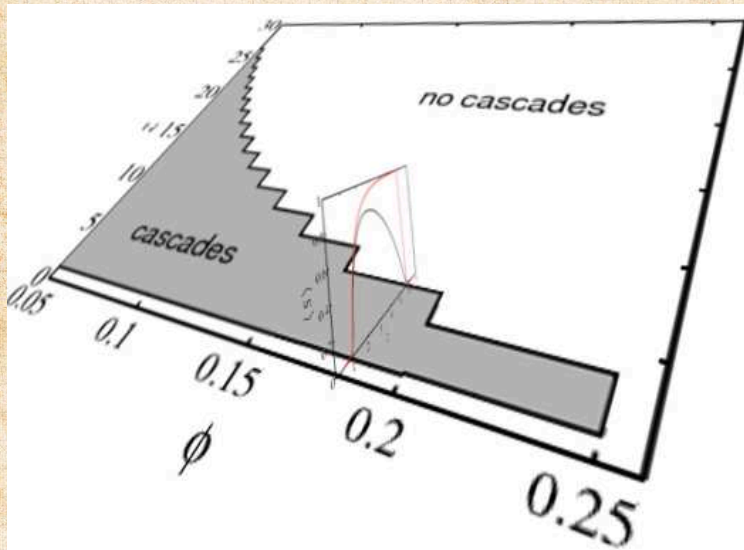
## References

- ▶ **'Cascade window'** widens as threshold  $\phi$  decreases.
- ▶ Lower thresholds enable spreading.





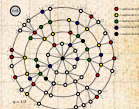
# Cascade window for random networks



## Social Contagion Models

- Background
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## References



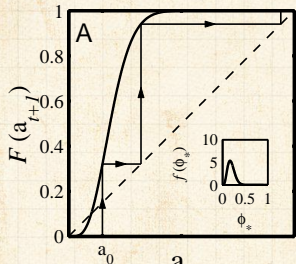
# All-to-all versus random networks

## Social Contagion Models

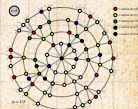
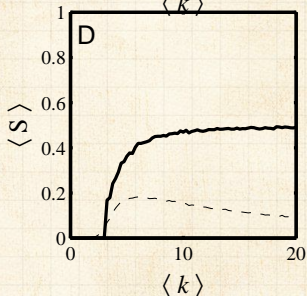
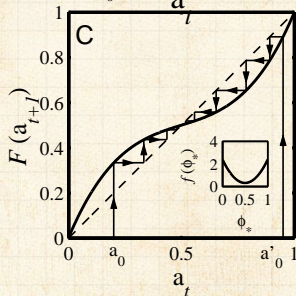
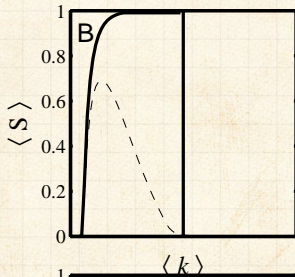
- Background
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## References

all-to-all networks



random networks



# Cascade window—summary

For our simple model of a uniform threshold:

1. Low  $\langle k \rangle$ : No cascades in poorly connected networks.  
No global clusters of any kind.
2. High  $\langle k \rangle$ : Giant component exists but not enough vulnerables.
3. Intermediate  $\langle k \rangle$ : Global cluster of vulnerables exists.  
Cascades are possible in “**Cascade window.**”

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Background

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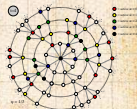
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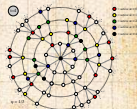
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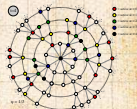
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Social Contagion  
Models

Background

Granovetter's model

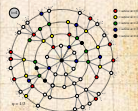
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## Social Contagion Models

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**Final size**

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## Social Contagion Models

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Granovetter's model

Network version

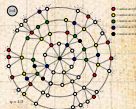
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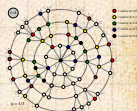
# Threshold contagion on random networks

- ▶ **Next:** Find expected fractional size of spread.
- ▶ Not obvious even for uniform threshold problem.
- ▶ Difficulty is in figuring out if and when nodes that need  $\geq 2$  hits switch on.
- ▶ Problem beautifully solved for infinite seed case by Gleeson and Cahalane:  
"Seed size strongly affects cascades on random networks," Phys. Rev. E, 2007. <sup>[14]</sup>
- ▶ Developed further by Gleeson in "Cascades on correlated and modular random networks," Phys. Rev. E, 2008. <sup>[13]</sup>

## Social Contagion Models

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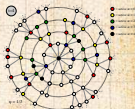
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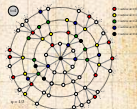
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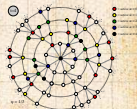
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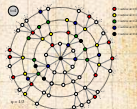
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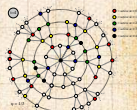
# Determining expected size of spread:

- ▶ Randomly turn on a fraction  $\phi_0$  of nodes at time  $t = 0$
- ▶ Capitalize on local branching network structure of random networks (again)
- ▶ Now think about what must happen for a specific node  $i$  to become active at time  $t$ :
  - $t = 0$ :  $i$  is one of the seeds (prob =  $\phi_0$ )
  - $t = 1$ :  $i$  was not a seed but enough of  $i$ 's friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.
  - $t = 2$ : enough of  $i$ 's friends and friends-of-friends switched on at time  $t = 0$  so that  $i$ 's threshold is now exceeded.
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## Social Contagion Models

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## References



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  - $t = 0$ :  $i$  is one of the seeds (prob =  $\phi_0$ )
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## Social Contagion Models

Background

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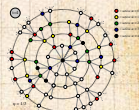
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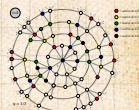
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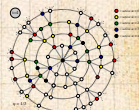
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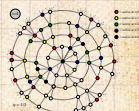
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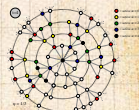
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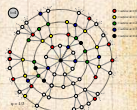
Network version

Final size

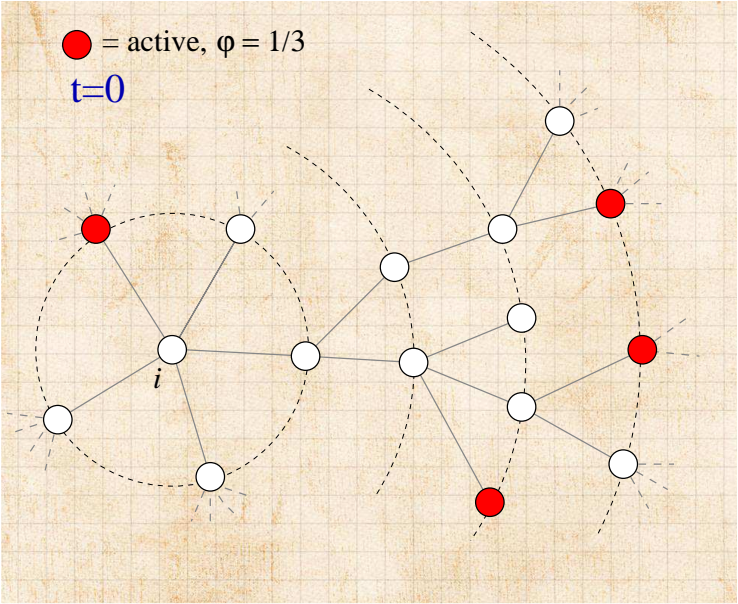
Spreading success

Groups

## References



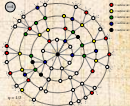
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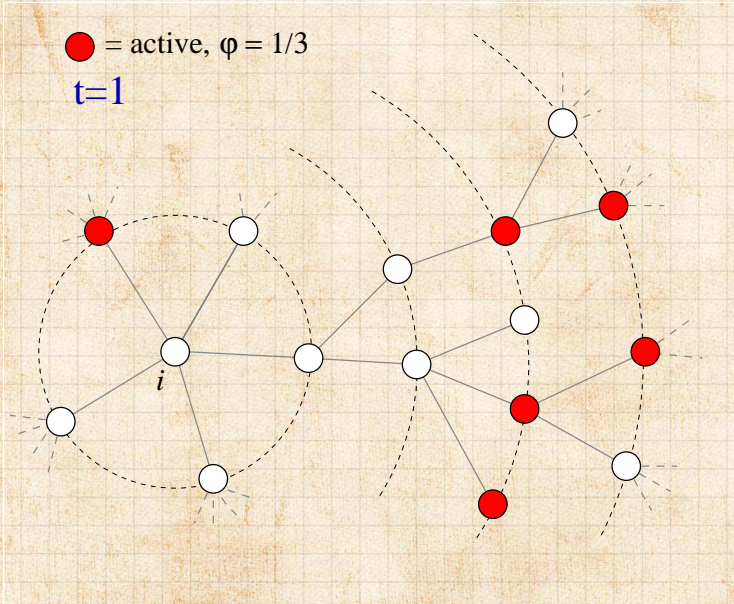
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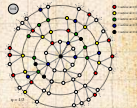
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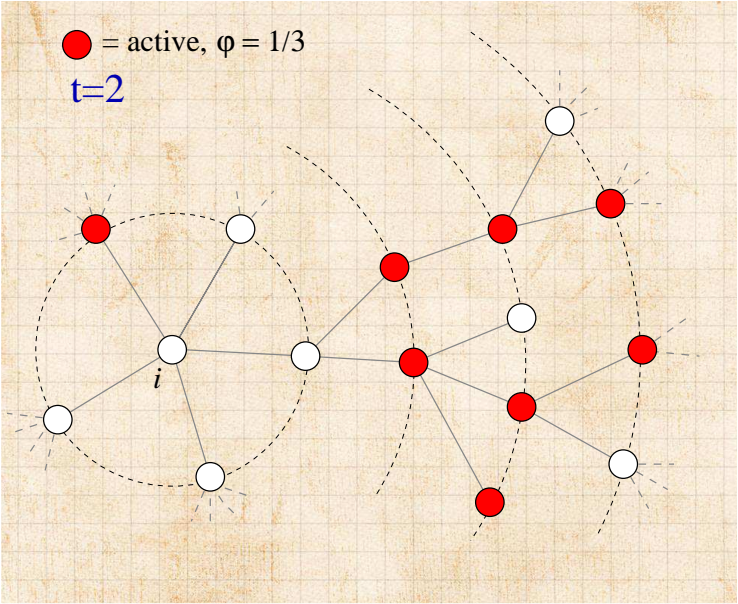
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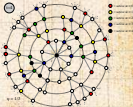
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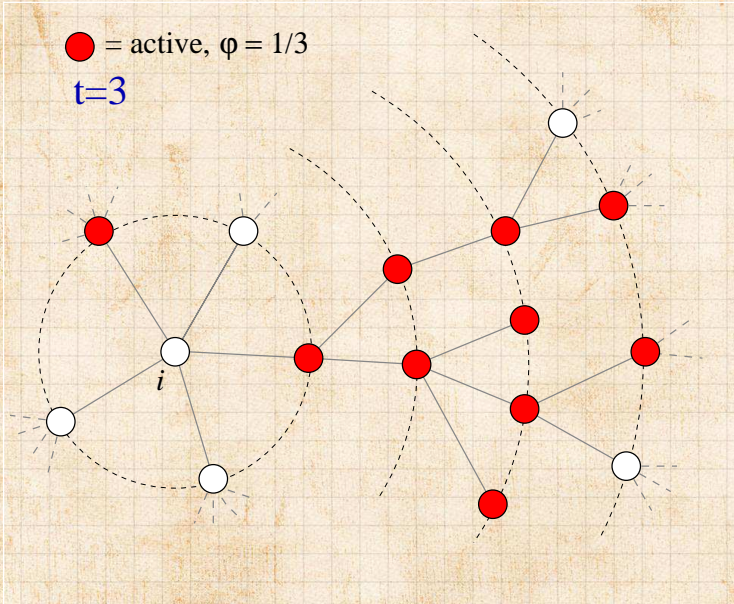
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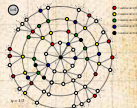
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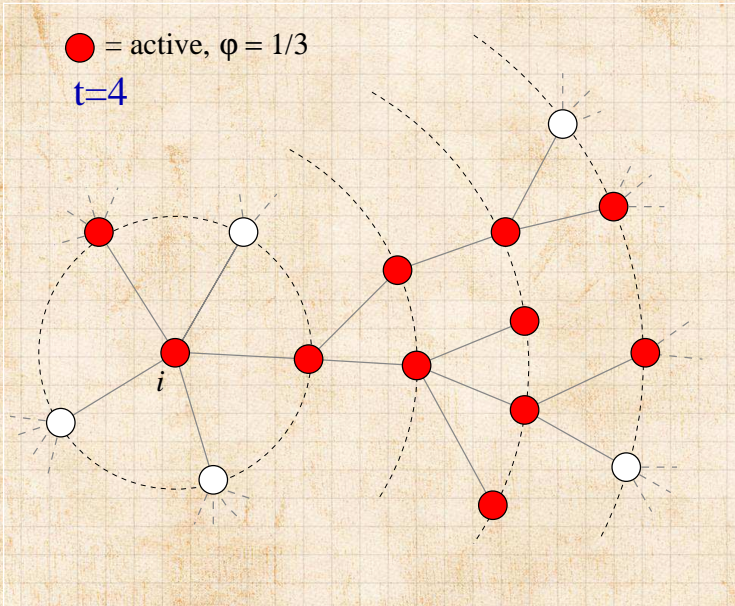
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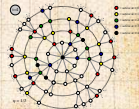
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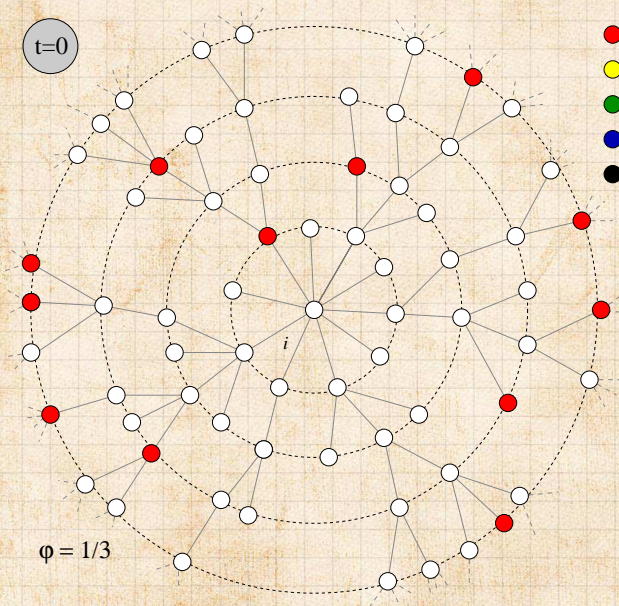
## References





# Expected size of spread

t=0



● = active at t=0

● = active at t=1

● = active at t=2

● = active at t=3

● = active at t=4

## Social Contagion Models

Background

Granovetter's model

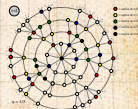
Network version

Final size

Spreading success

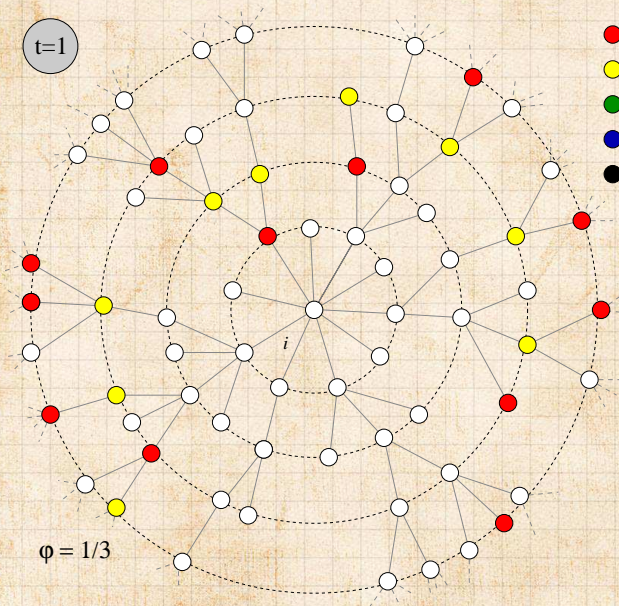
Groups

## References



# Expected size of spread

t=1



● = active at t=0

● = active at t=1

● = active at t=2

● = active at t=3

● = active at t=4

## Social Contagion Models

Background

Granovetter's model

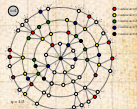
Network version

Final size

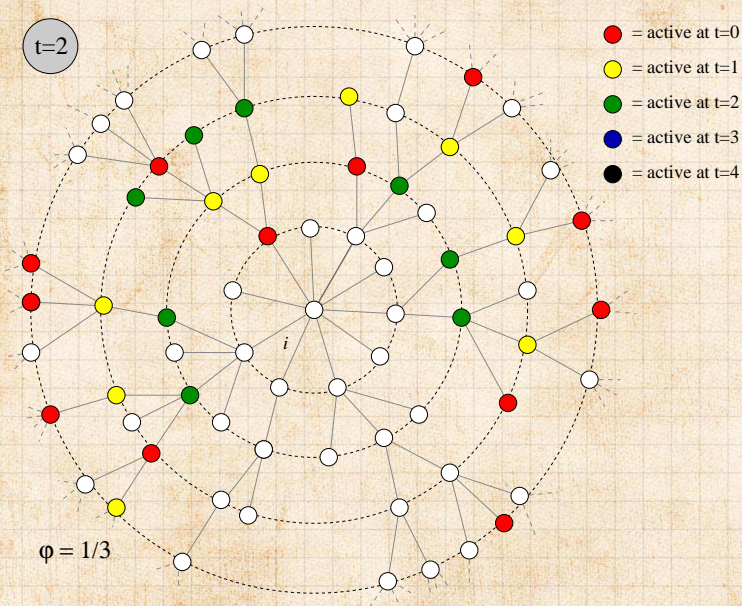
Spreading success

Groups

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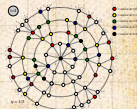
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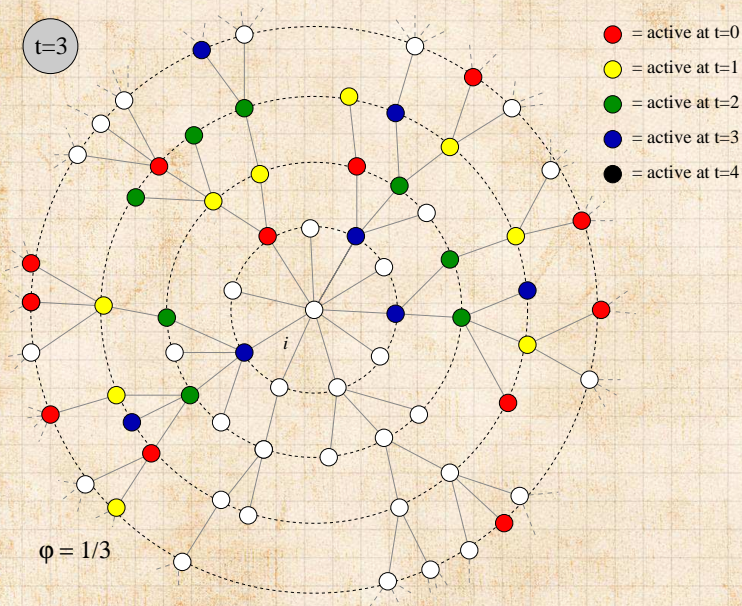
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# Expected size of spread



## Social Contagion Models

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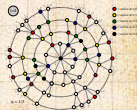
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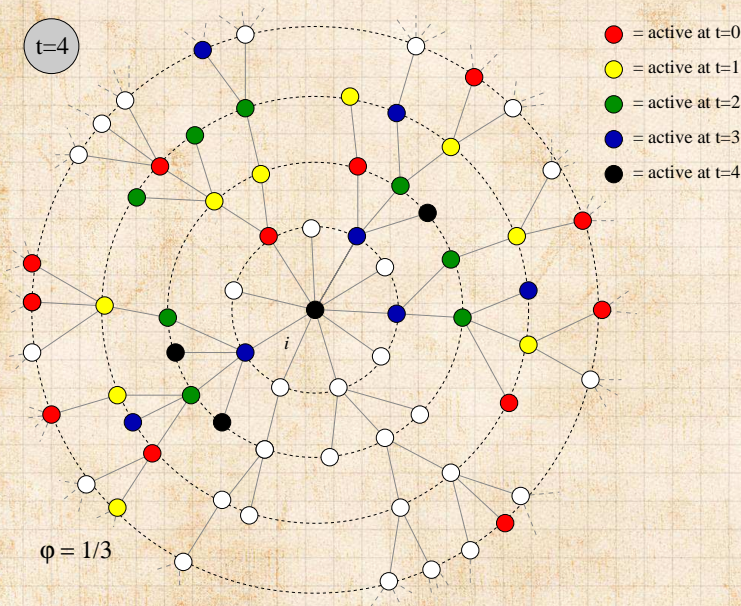
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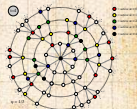
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## Social Contagion Models

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## Notes:

- ▶ Calculations are possible if nodes do not become inactive (strong restriction).
- ▶ Not just for threshold model—works for a wide range of contagion processes.
- ▶ We can analytically determine the entire time evolution, not just the final size.
- ▶ We can in fact determine  $\Pr(\text{node of degree } k \text{ switching on at time } t)$ .
- ▶ Asynchronous updating can be handled too.

## Social Contagion Models

Background

Granovetter's model

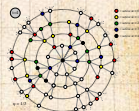
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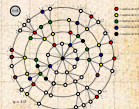
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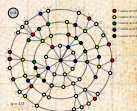
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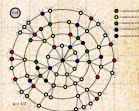
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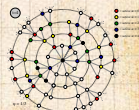
Network version

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# Expected size of spread

## Pleasantness:

- ▶ Taking off from a single seed story is about **expansion** away from a node.
- ▶ Extent of spreading story is about **contraction** at a node.

## Social Contagion Models

Background

Granovetter's model

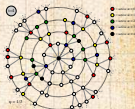
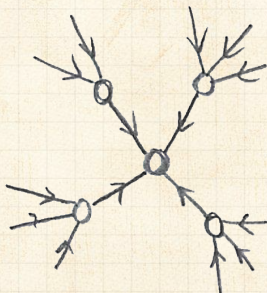
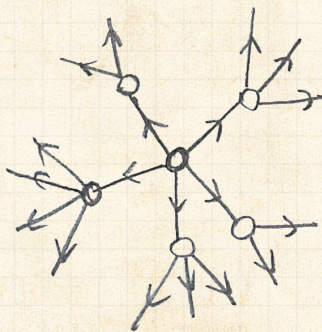
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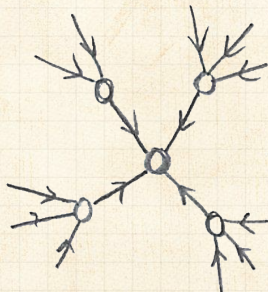
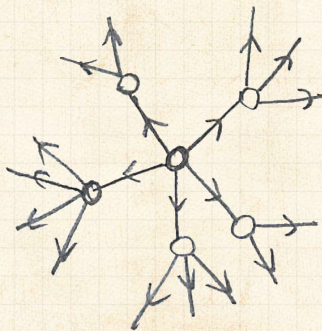
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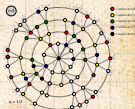
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# Expected size of spread

## ► Notation:

$\phi_{k,t} = \Pr(\text{a degree } k \text{ node is active at time } t).$

► Notation:  $B_{kj} = \Pr(\text{a degree } k \text{ node becomes active if } j \text{ neighbors are active}).$

► Our starting point:  $\phi_{k,0} = \phi_0.$

►  $\binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} = \Pr(j \text{ of a degree } k \text{ node's neighbors were seeded at time } t = 0).$

► Probability a degree  $k$  node was a seed at  $t = 0$  is  $\phi_0$  (as above).

► Probability a degree  $k$  node was not a seed at  $t = 0$  is  $(1 - \phi_0).$

► Combining everything, we have:

$$\phi_{k,1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^k \binom{k}{j} \phi_0^j (1 - \phi_0)^{k-j} B_{kj}.$$

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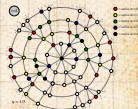
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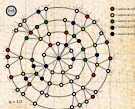
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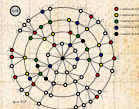
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► Probability a degree  $k$  node was a seed at  $t = 0$  is  $\phi_0$  (as above).

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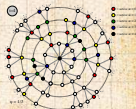
► Combining everything, we have:

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# Expected size of spread

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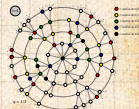
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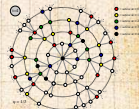
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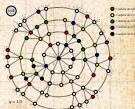
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▶ Story analogous to  $t = 1$  case. For node  $i$ :

$$\phi_{i,t+1} = \phi_0 + (1 - \phi_0) \sum_{j=0}^{k_i} \binom{k_i}{j} \theta_t^j (1 - \theta_t)^{k_i - j} B_{k_i j}.$$

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▶ So we need to compute  $\theta_t$ ...

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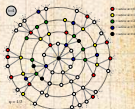
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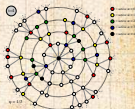
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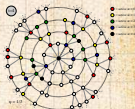
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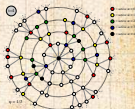
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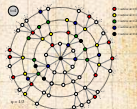
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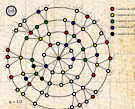
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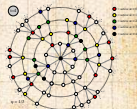
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- ▶ So we need to compute  $\theta_t$ ... massive excitement...



# Expected size of spread

First connect  $\theta_0$  to  $\theta_1$ :

▶  $\theta_1 = \phi_0 +$

$$(1 - \phi_0) \sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_0^j (1 - \theta_0)^{k-1-j} B_{kj}$$

- ▶  $\frac{k P_k}{\langle k \rangle} = R_k = \mathbf{Pr}$  (edge connects to a degree  $k$  node).
- ▶  $\sum_{j=0}^{k-1}$  piece gives  $\mathbf{Pr}$ (degree node  $k$  activates) of its neighbors  $k - 1$  incoming neighbors are active.
- ▶  $\phi_0$  and  $(1 - \phi_0)$  terms account for state of node at time  $t = 0$ .
- ▶ See this all generalizes to give  $\theta_{t+1}$  in terms of  $\theta_t \dots$

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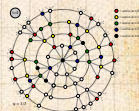
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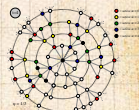
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# Expected size of spread

Two pieces: edges first, and then nodes

$$1. \theta_{t+1} = \underbrace{\phi_0}_{\text{exogenous}}$$

$$+(1 - \phi_0) \underbrace{\sum_{k=1}^{\infty} \frac{k P_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_t^j (1 - \theta_t)^{k-1-j} B_{kj}}_{\text{social effects}}$$

with  $\theta_0 = \phi_0$ .

$$2. \phi_{t+1} =$$

$$\underbrace{\phi_0}_{\text{exogenous}} + (1 - \phi_0) \underbrace{\sum_{k=0}^{\infty} P_k \sum_{j=0}^k \binom{k}{j} \theta_t^j (1 - \theta_t)^{k-j} B_{kj}}_{\text{social effects}}$$

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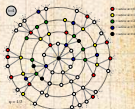
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# Expected size of spread

Iterative map for  $\theta_t$  is key:

$$\theta_{t+1} = \underbrace{\phi_0}_{\text{exogenous}}$$

$$+(1 - \phi_0) \underbrace{\sum_{k=1}^{\infty} \frac{kP_k}{\langle k \rangle} \sum_{j=0}^{k-1} \binom{k-1}{j} \theta_t^j (1 - \theta_t)^{k-1-j} B_{kj}}_{\text{social effects}}$$

$$= G(\theta_t; \phi_0)$$

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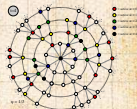
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# Expected size of spread:

- ▶ Retrieve cascade condition for spreading from a single seed in limit  $\phi_0 \rightarrow 0$ .
- ▶ Depends on map  $\theta_{t+1} = G(\theta_t; \phi_0)$ .
- ▶ First: if self-starters are present, some activation is assured:

$$G(0; \phi_0) = \sum_{k=1}^{\infty} \frac{kP_k}{\langle k \rangle} \cdot B_{k0} > 0.$$

meaning  $B_{k0} > 0$  for at least one value of  $k \geq 1$ .

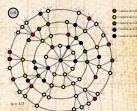
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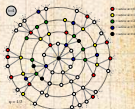
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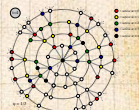
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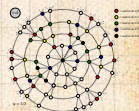
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# Expected size of spread:

In words:

- ▶ If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.
- ▶ If  $G$  has an **unstable fixed point** at  $\theta \equiv 0$ , then cascades are also always possible.

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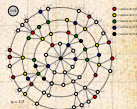
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Non-vanishing seed case:

- ▶ Cascade condition is more complicated for  $\phi_0 > 0$ .
- ▶ If  $G$  has a stable fixed point at  $\theta = 0$ , and an unstable fixed point for some  $0 < \theta_* < 1$ , then for  $\phi_0 > \theta_*$ , spreading takes off.
- ▶ Tricky point:  $G$  depends on  $\phi_0$ , so as we change  $\phi_0$ , we also change  $G$ .
- ▶ A version of a critical-mass model again.



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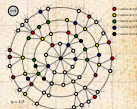
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- ▶ Tricky point:  $G$  depends on  $\phi_0$ , so as we change  $\phi_0$ , we also change  $G$ .
- ▶ A version of a critical mass model again.

Social Contagion  
Models

Background

Granovetter's model

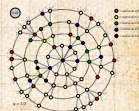
Network version

Final size

Spreading success

Groups

References



# Expected size of spread:

## In words:

- ▶ If  $G(0; \phi_0) > 0$ , spreading must occur because some nodes turn on for free.
- ▶ If  $G$  has an **unstable fixed point** at  $\theta = 0$ , then cascades are also always possible.

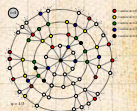
## Non-vanishing seed case:

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## Social Contagion Models

[Background](#)[Granovetter's model](#)[Network version](#)[Final size](#)[Spreading success](#)[Groups](#)

## References



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Social Contagion  
Models

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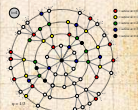
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Final size

Spreading success

Groups

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Social Contagion Models

Background

Granovetter's model

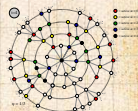
Network version

Final size

Spreading success

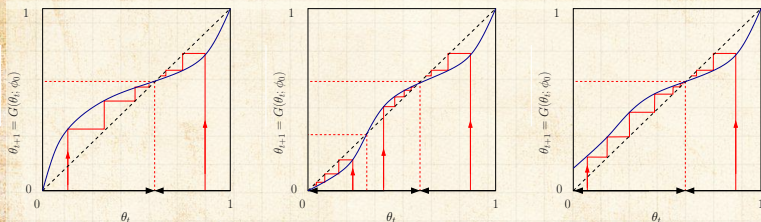
Groups

References





# General fixed point story:

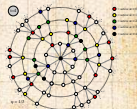


- ▶ Given  $\theta_0 (= \phi_0)$ ,  $\theta_\infty$  will be the nearest stable fixed point, either above or below.
- ▶ n.b., adjacent fixed points must have opposite stability types.
- ▶ **Important:** Actual form of  $G$  depends on  $\phi_0$ .
- ▶ So choice of  $\phi_0$  dictates both  $G$  and starting point—can't start anywhere for a given  $G$ .

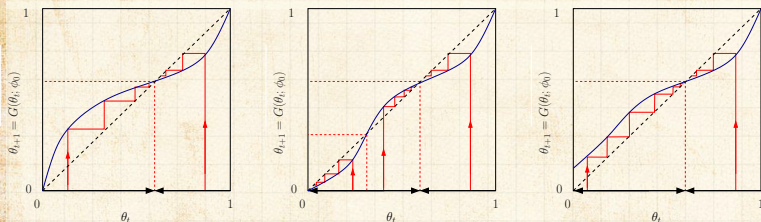
## Social Contagion Models

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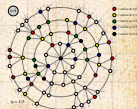


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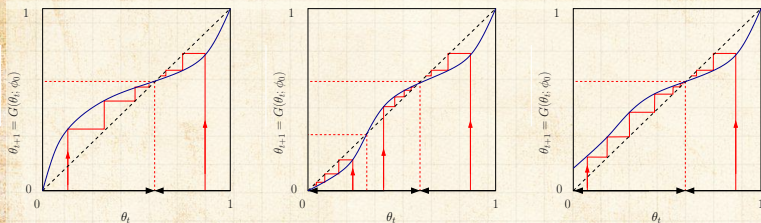
## Social Contagion Models

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- Granovetter's model
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## Social Contagion Models

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Granovetter's model

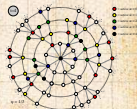
Network version

Final size

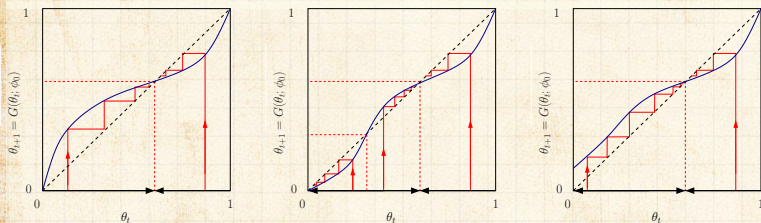
Spreading success

Groups

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## Social Contagion Models

Background

Granovetter's model

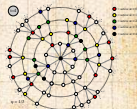
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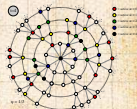
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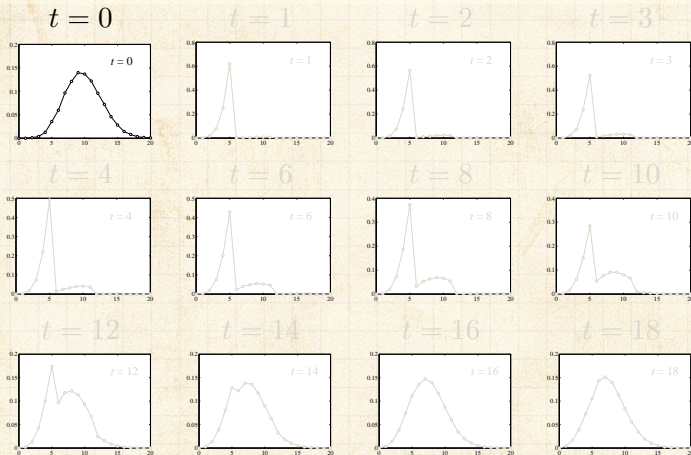


# Early adopters—degree distributions

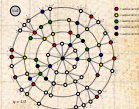
## Social Contagion Models

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$P_{k,t}$  versus  $k$

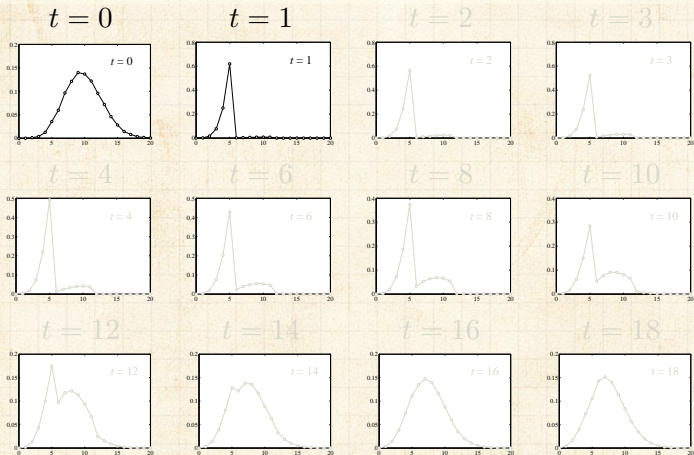


# Early adopters—degree distributions

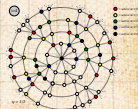
## Social Contagion Models

- Background
- Granovetter's model
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$P_{k,t}$  versus  $k$

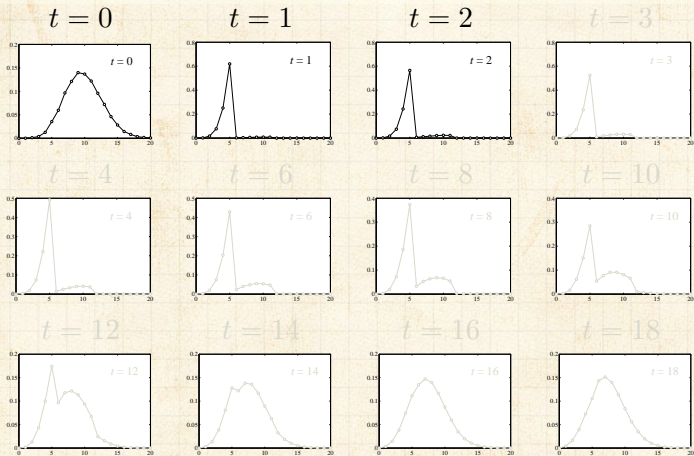


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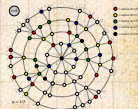
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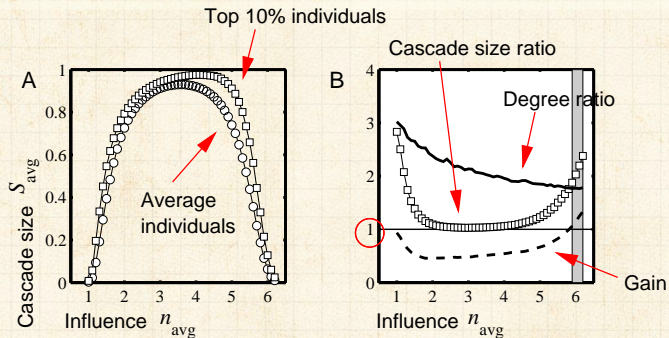
$P_{k,t}$  versus  $k$







# The multiplier effect:

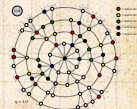


- ▶ Fairly uniform levels of individual influence.
- ▶ Multiplier effect is mostly below 1.

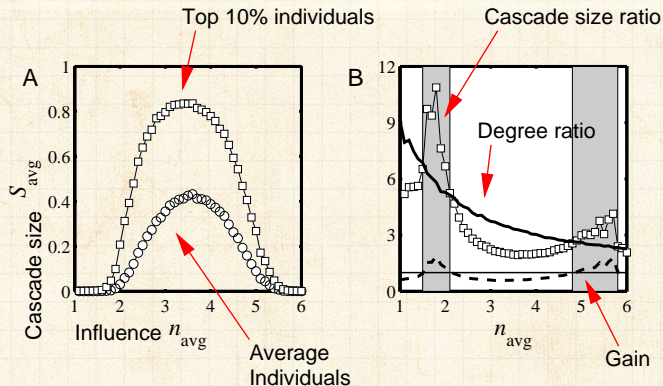
## Social Contagion Models

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Granovetter's model  
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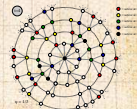


► Skewed influence distribution example.

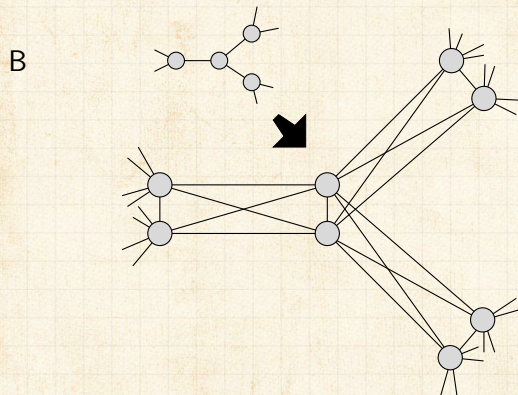
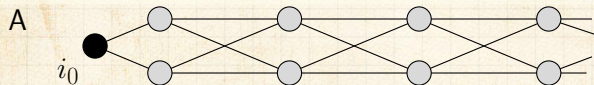
## Social Contagion Models

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# Special subnetworks can act as triggers

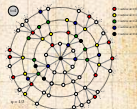


►  $\phi = 1/3$  for all nodes

## Social Contagion Models

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## References



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## Social Contagion Models

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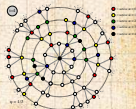
Final size

Spreading success

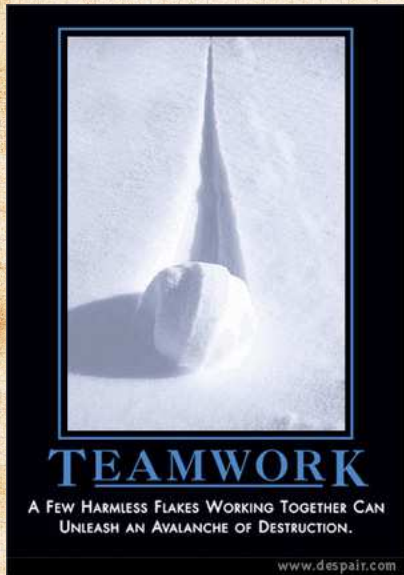
Groups

## References

## References



# The power of groups...

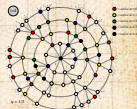


“A few harmless flakes working together can unleash an avalanche of destruction.”


## Social Contagion Models

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## References





“Threshold Models of Social Influence”   
Watts and Dodds,  
The Oxford Handbook of Analytical  
Sociology, , 475–497, 2009. [28]

Social Contagion  
Models

Background

Granovetter's model

Network version

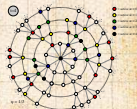
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Spreading success

Groups

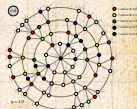
References

- ▶ Assumption of sparse interactions is good
- ▶ Degree distribution is (generally) key to a network's function
- ▶ Still, random networks don't represent all networks
- ▶ Major element missing: **group structure**




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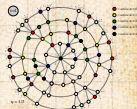







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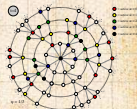
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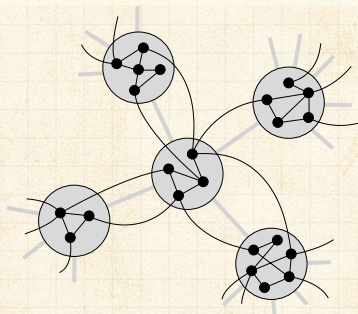


# Group structure—Ramified random networks

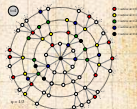
## Social Contagion Models

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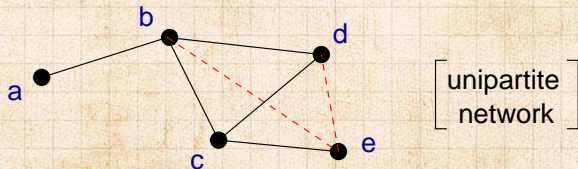
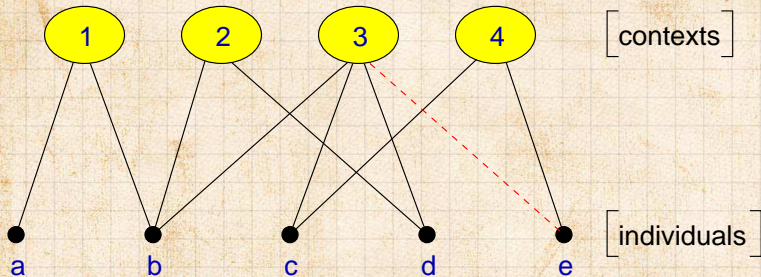
## References



$p$  = intergroup connection probability  
 $q$  = intragroup connection probability.



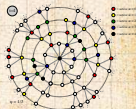
# Bipartite networks



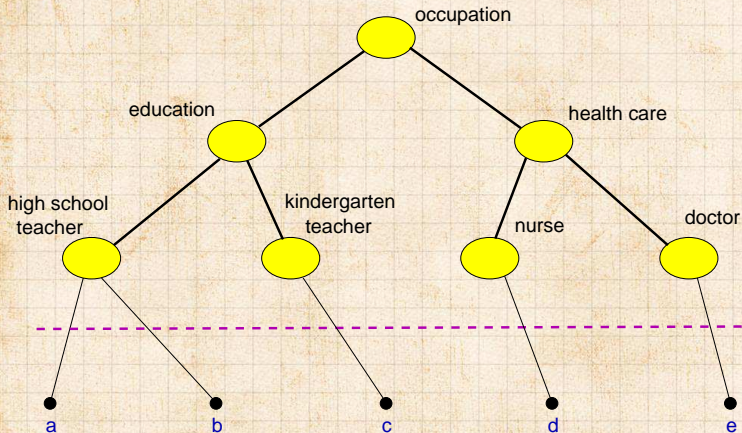
Social Contagion Models

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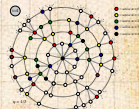
# Context distance



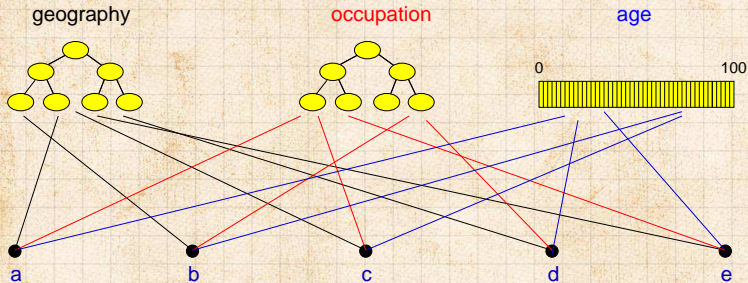
## Social Contagion Models

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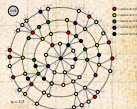
# Generalized affiliation model



(Blau & Schwartz, Simmel, Breiger)

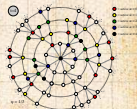
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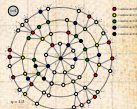
# Generalized affiliation model networks with triadic closure

- ▶ Connect nodes with probability  $\propto \exp^{-\alpha d}$  where
  - $\alpha$  = homophily parameter
  - and
  - $d$  = distance between nodes (height of lowest common ancestor)
- ▶  $\tau_1$  = intergroup probability of friend-of-friend connection
- ▶  $\tau_2$  = intragroup probability of friend-of-friend connection



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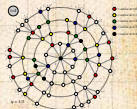
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# Cascade windows for group-based networks

## Social Contagion Models

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Granovetter's model

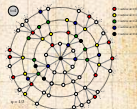
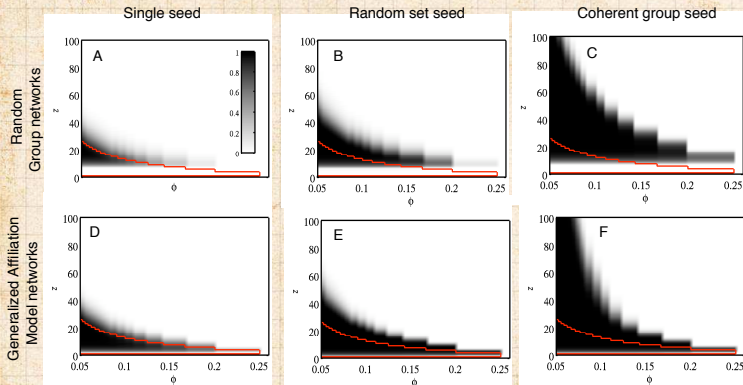
Network version

Final size

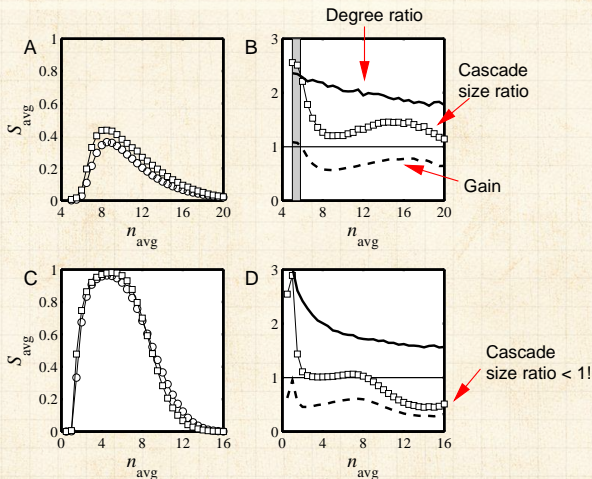
Spreading success

Groups

## References



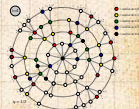
# Multiplier effect for group-based networks:



## Social Contagion Models

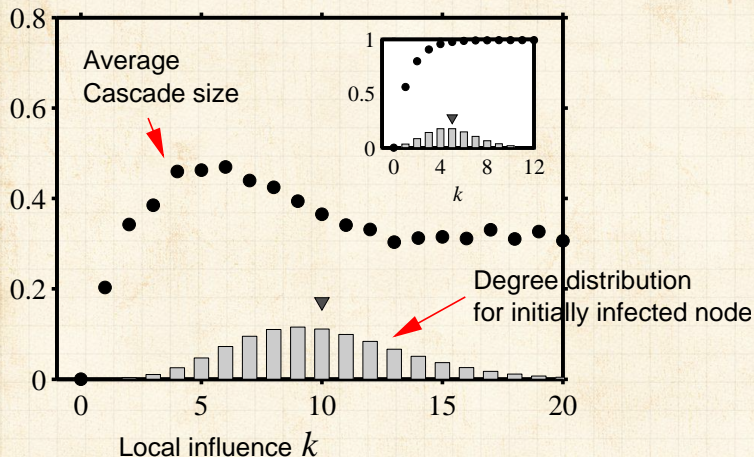
- Background
- Granovetter's model
- Network version
- Final size
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## References



► Multiplier almost always below 1.

# Assortativity in group-based networks

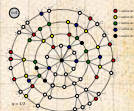


- ▶ The most connected nodes aren't always the most 'influential.'
- ▶ Degree assortativity is the reason.

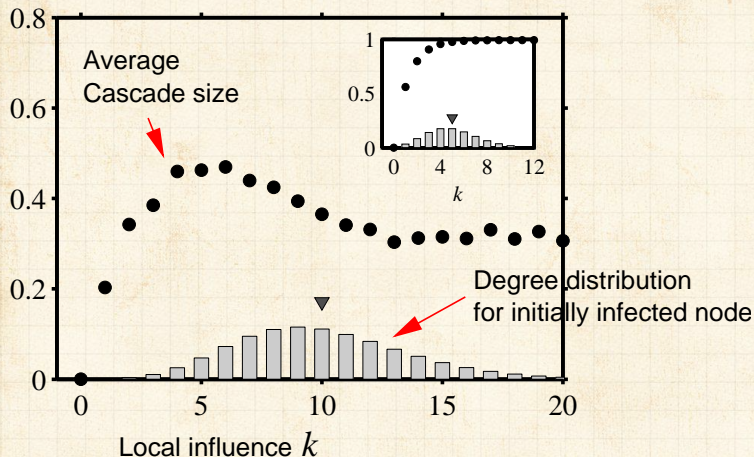
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# Assortativity in group-based networks

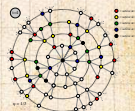


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## Social Contagion Models

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## Summary

- ▶ **'Influential vulnerables'** are key to spread.
- ▶ Early adopters are mostly vulnerables.
- ▶ Vulnerable nodes important but not necessary.
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## Social Contagion Models

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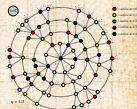
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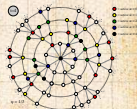
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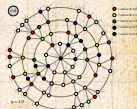
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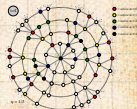
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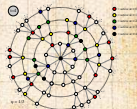
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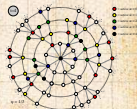
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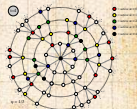
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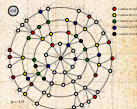
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## Implications

- ▶ Focus on the influential vulnerables.
- ▶ Create entities that can be transmitted successfully through many individuals rather than broadcast from one 'influential.'
- ▶ Only simple ideas can spread by word-of-mouth. (Idea of opinion leaders spreads well...)
- ▶ Want enough individuals who will adopt and display.
- ▶ Displaying can be passive = free (yo-yo's, fashion), or active = harder to achieve (political messages).
- ▶ Entities can be novel or designed to combine with others, e.g. block another one.

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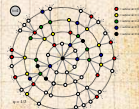
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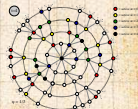
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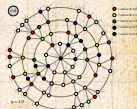
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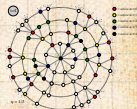
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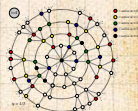
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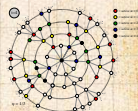
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# Spreading and unspreading: Empires

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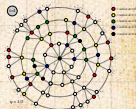
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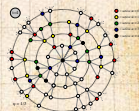
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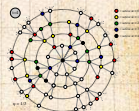




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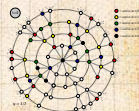
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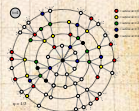
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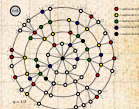
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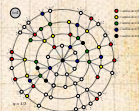


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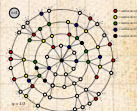
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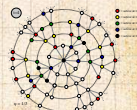


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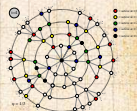
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