# Why Complexify? Principles of Complex Systems | @pocsvox CSYS/MATH 300, Fall, 2015 | #FallPoCS2015

### Prof. Peter Dodds | @peterdodds

Dept. of Mathematics & Statistics | Vermont Complex Systems Center Vermont Advanced Computing Core | University of Vermont



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# Outline

Universality

Symmetry Breaking

The Big Theory

Final words

For your consideration

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Limits to what's possible:

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# Universality

### Sometimes details don't matter too much.

- Many-to-one mapping from micro to macro
- Suggests not all possible behaviors are available at higher levels of complexity.
- Universality means some things are fated.

### Large questions:

- How universal is universality?
- What are the possible long-time states (attractors) for a universe?



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► Kadanoff's retrospective: "Innovations in Statistics Physics" [3]

Universality 2:

### Examples:

The Central Limit Theorem:

$$P(x;\mu,\sigma)\mathrm{d}x\ = \frac{1}{\sqrt{2\pi}\sigma}e^{-(x-\mu)^2/2\sigma^2}\mathrm{d}x$$

- Navier Stokes equation for fluids.
- Nature of phase transitions in statistical mechanics.

x.

# Complex Syst

### Fluid mechanics

- ▶ Fluid mechanics = One of the great successes of understanding complex systems.
- Navier-Stokes equations: micro-macro system evolution.
- ▶ The big three: Experiment + Theory + Simulations.
- ▶ Works for many very different 'fluids':
  - the atmosphere,
  - oceans,
  - blood,
  - galaxies,
  - the earth's mantle ...
  - and ball bearings on lattices ...?



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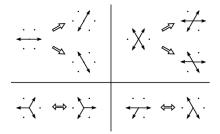
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### Lattice gas models

### Collision rules in 2-d on a hexagonal lattice:



- ▶ Lattice matters ...
- No 'good' lattice in 3-d.
- Upshot: play with 'particles' of a system to obtain new or specific macro behaviours.

### Hexagons—Honeycomb:



- Orchestrated? Or an accident of bees working hard?
- See "On Growth and Form" by D'Arcy Wentworth Thompson C. [6, 7]



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# Hexagons—Giant's Causeway:

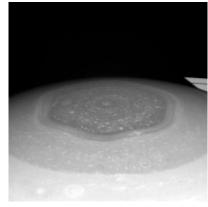


http://newdesktopwallpapers.info

### Hexagons—Giant's Causeway:

http://www.physics.utoronto.ca/

# Saturn has a hexagon:



▶ One side is longer than Earth's diameter 🗹

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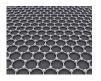
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### Hexagons run amok:



### ▶ Graphene <sup>C</sup>: single layer of carbon molecules in a perfect hexagonal lattice (super strong).

▶ Chicken wire 🗹 ...

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"More is different" P. W. Anderson, Science, 177, 393-396, 1972.<sup>[1]</sup>



scientists are those working on the fundamental laws.

Symmetry breaking  $\rightarrow$  different laws/rules at different scales ...

2006 study: "most creative physicist in the world"

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### Triumph of the Hexagon

From the remarkable Hexnet.org Z, the Global Hexagonal Awareness Resource Center.







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# Symmetry Breaking

### "Elementary entities of science X obey the laws of science Y"

- ► X
- solid state or many-body physics
- chemistry
- molecular biology
- cell biology
- psychology
- social sciences

# Symmetry Breaking

Anderson:

- ▶ [the more we know about] "fundamental laws, the less relevance they seem to have to the very real problems of the rest of science."
- Scale and complexity thwart the constructionist hypothesis.
- Accidents of history and path dependence matter.

### ► Y elementary particle physics

- solid state many-body physics
- chemistry
- molecular biology
- physiology
- psychology
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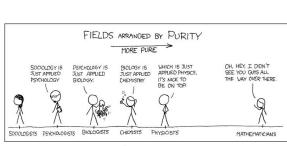
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"Critical Phenomena in Natural Sciences" 🗹 by Didier Sornette (2003).<sup>[4]</sup>

- ▶ Page 291–292 of Sornette <sup>[5]</sup>: Renormalization  $\equiv$  Anderson's hierarchy.
- But Anderson's hierarchy is not a simple one: the rules change.
- Crucial dichotomy between evolving systems following stochastic paths that lead to (a) inevitable or (b) particular destinations (states).

*	Poccs Principles of Complex Systems @pocswox What's the Story?



http://xkcd.com/435/

More is different:





### A real theory of everything anything:

- 1. Is not just about the ridiculously small stuff ...
- 2. It's about the increase of complexity

Symmetry breaking/ VS. Accidents of history

Universality

- Second law of thermodynamics: we're toast in the long run.
- So how likely is the local complexification of structure we enjoy?
- How likely are the Big Transitions?







Big

Replicate.

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### Why complexify?



"Why do things become more complex?" W. Brian Arthur, Scientific American, 268, 92, 1993.<sup>[2]</sup>

- Argues that evolution toward increased performance brings a ratcheting cycle of complexification and simplification.
- ▶ let engine replaced the complex piston engine and then itself became more complex.
- Complexification  $\equiv$  evolution of algorithms?
- ▶ Differential equations and stories ⊂ Algorithms.
- Life is a loaded word: The Search for Extraterrestrial Algorithms (SETA)?



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# Why complexify?

### Driving complexity's trajectory:

- Big Bang
- Randomness leads to replicating structures;
- Biological evolution;
- Sociocultural evolution;
- Technological evolution;
- Sociotechnological evolution.



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- Big Algorithm.

- Big Spread.



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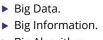
### Complexification—the Big Transitions: Big Science. Big Word. Big Bang. Big Story. ► **Big Random-**Big ness. Number. Big ► Structure.

- - Big Make.
  - ▶ Big City.
    - - ▶ Big ...?
- - ▶ Big Culture.

- Big Social.
- Big Awareness.







- Big Connection.











- Big Farm.
- ▶ Big God.



 "Heroes only win when outnumbered, and things which have a one-in-a-million chance of succeeding often do so."



Lens (for advanced users):



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# The absolute basics:

### Modern basic science in three steps:

- 1. Find interesting/meaningful/important phenomena, optionally involving spectacular amounts of data.
- 2. Describe what you see.
- 3. Explain it.

Unlocks our (limited) ability to: Create, predict, and control.

And be good people: Share.

Beware your assumptions: Don't use tools/models because they're there, or because everyone else does ...

### This is a thing that could be next:

CoNKs: The PoCS strikes back:



CSYS/MATH 303: Complex Networks 🖸 @networksvox 🗹

- Branching networks (rivers, cardiovascular systems).
- Optimal (re)distribution networks (hospitals, coffee shops, airlines, post, Internet).
- Structure detection for complex systems.
- Moar Contagion.
- Random networks-arama.
- Distributed Search.
- Organizational networks.
- Deeper investigations of scale-free networks.
- and more ...

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