

Biological Contagion

Last updated: 2024/11/12, 10:03:54 EST

Principles of Complex Systems, Vols. 1, 2, & 3D
CSYS/MATH 6701, 6713, & a pretend number, 2024–2025

Prof. Peter Sheridan Dodds

Computational Story Lab | Vermont Complex Systems Center
Santa Fe Institute | University of Vermont

Licensed under the [Creative Commons Attribution 4.0 International](https://creativecommons.org/licenses/by/4.0/)

- The PoCSverse
- Biological Contagion 1 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

Contagion

A confusion of contagions:

- Did Harry Potter spread like a virus?
- Can disinformation be “infectious”?
- Suicide, violence?
- Morality? Evil? Laziness? Stupidity? Happiness?
- Religion?
- Democracy ...?
- Language? The alphabet? ^[10]
- Stories?

- The PoCSverse
- Biological Contagion 7 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

The spread of fanaticism

Hoffer’s most famous work: “**The True Believer:**
Thoughts On The Nature Of Mass Movements” (1951) ^[12]

Aphorisms-aplenty:

- “We can be absolutely certain only about things we do not understand.”
- “Mass movements can rise and spread without belief in a God, but never without belief in a devil.”
- “Where freedom is real, equality is the passion of the masses. Where equality is real, freedom is the passion of a small minority.”

- The PoCSverse
- Biological Contagion 10 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

Outline

Introduction

Simple disease spreading models

- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus

References

- The PoCSverse
- Biological Contagion 2 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

Contagion

Naturomorphisms

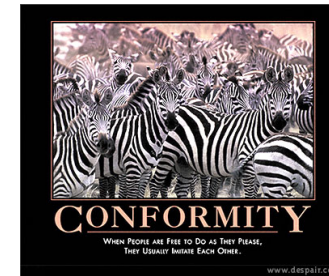
- “The feeling was contagious.”
- “The news spread like wildfire.”
- “Freedom is the most contagious virus known to man.”
—Hubert H. Humphrey, Johnson’s vice president
- “Nothing is so contagious as enthusiasm.”
—Samuel Taylor Coleridge

Optimism according to Ambrose Bierce:

The doctrine that everything is beautiful, including what is ugly, everything good, especially the bad, and everything right that is wrong. ... **It is hereditary, but fortunately not contagious.**

- The PoCSverse
- Biological Contagion 8 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

Imitation



despair.com

“When people are free to do as they please, they usually imitate each other.”

—Eric Hoffer
“The Passionate State of Mind” ^[13]

- The PoCSverse
- Biological Contagion 11 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

An awful recording: Wikipedia’s list of epidemics from 430 BC on.

WIKIPEDIA: List of epidemics

This article is a list of epidemics of infectious disease. Widespread and chronic complaints such as heart disease and ulcers are not included if they are not thought to be infectious.

Death toll (estimate)	Location	Date	Comment	Disease	Reference
ca. 175,000–190,000	Greece	430–404 BC	Known as Plague of Athens, believed to have originated in Athens.	unknown, similar to typhoid	
ca. 30% of population	Europe, Western Asia, Northern Africa	180–180	Known as Antonine Plague, said to be the cause of the Roman emperor's premature death.	unknown, symptoms similar to smallpox	
250,000–300,000 AD	Europe	541–542	Known as Plague of Justinian, due to the capture of the Byzantine emperor Justinian at the time.	unknown, possibly anthrax	
ca. 40% of population	Europe	1418–1420	Known as Plague of London, due to the capture of the English emperor at the time.	Bubonic plague	[1]
20% to 70% of population	Europe	1346–1350	Known as Black Death or Decembris pluvium, first major of the plague to Europe after the Justinian plague of the 6th century.	plague	[2]
1–1.5 million (80% of population)	Mexico	1545–1548	Cocoltli	viral hemorrhagic fever	[3][4]
2–2.5 million (80% of population)	Mexico	1576	Cocoltli	viral hemorrhagic fever	[5][6]
Severe ration	Seneca nation	1582–1584		measles	[7]

- The PoCSverse
- Biological Contagion 5 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

Social contagion

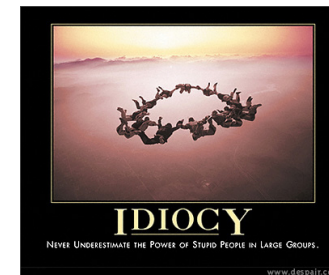
Eric Hoffer, 1902–1983

There is a grandeur in the uniformity of the mass. When a fashion, a dance, a song, a slogan or a joke sweeps like wildfire from one end of the continent to the other, and a hundred million people roar with laughter, sway their bodies in unison, hum one song or break forth in anger and denunciation, there is the overpowering feeling that in this country we have come nearer the brotherhood of man than ever before.

Hoffer was an interesting fellow...

- The PoCSverse
- Biological Contagion 9 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

The collective...



despair.com

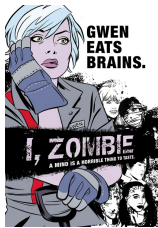
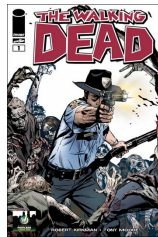
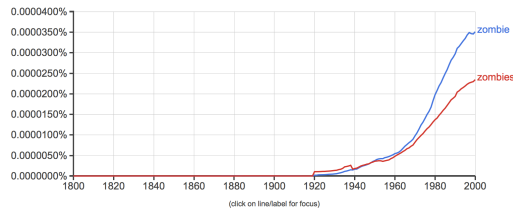
“Never Underestimate the Power of Stupid People in Large Groups.”

- The PoCSverse
- Biological Contagion 12 of 92
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models
- Model output
- Nutshell
- Other kinds of prediction
- SIR is the virus
- References

The most terrifying contagious outbreak?

Google books Ngram Viewer

Graph these comma-separated phrases: case-insensitive
 between and from the corpus with smoothing of [Search lots of books](#)



Contagion

Definitions

- ☼ (1) The spreading of a quality or quantity between individuals in a population.
- ☼ (2) A disease itself: the plague, a blight, the dreaded lurgi, ...
- ☼ from Latin: *con* = 'with' + *tangere* 'to touch.'
- ☼ Contagion has unpleasant overtones...
- ☼ Just **Spreading** might be a more neutral word
- ☼ But contagion is kind of exciting...

The PoCSverse
Biological Contagion
13 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

Contagions

Two main classes of contagion

1. **Infectious diseases:**
tuberculosis, HIV, ebola, SARS, influenza, zombification, ...
2. **Social contagion:**
fashion, word usage, rumors, uprisings, religion, stories about zombies, ...

The PoCSverse
Biological Contagion
16 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

Mathematical Epidemiology

Original models attributed to

- ☼ 1920's: Reed and Frost
- ☼ 1920's/1930's: Kermack and McKendrick [14, 16, 15]
- ☼ Coupled differential equations with a mass-action principle

The PoCSverse
Biological Contagion
21 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

The PoCSverse
Biological Contagion
14 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

Mathematical Epidemiology

The standard SIR model [18]

- ☼ = basic model of disease contagion
- ☼ Three states:
 1. S = Susceptible
 2. I = Infective/Infectious
 3. R = Recovered or Removed or Refractory
- ☼ $S(t) + I(t) + R(t) = 1$
- ☼ Presumes random interactions (mass-action principle)
- ☼ Interactions are independent (no memory)
- ☼ Discrete and continuous time versions

The PoCSverse
Biological Contagion
19 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

Independent Interaction models

Differential equations for continuous model

$$\frac{d}{dt}S = -\beta IS + \rho R$$

$$\frac{d}{dt}I = \beta IS - rI$$

$$\frac{d}{dt}R = rI - \rho R$$

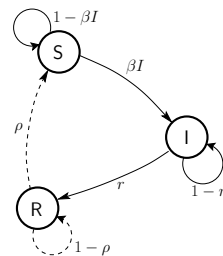
β , r , and ρ are now **rates**.

The PoCSverse
Biological Contagion
22 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

The PoCSverse
Biological Contagion
15 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

Mathematical Epidemiology

Discrete time automata example:



Transition Probabilities:
 β for being infected given contact with infected
 r for recovery
 ρ for loss of immunity

The PoCSverse
Biological Contagion
20 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

Reproduction Number R_0

Reproduction Number R_0

- ☼ R_0 = expected number of infected individuals resulting from a single initial infective
- ☼ Epidemic threshold: If $R_0 > 1$, 'epidemic' occurs.
- ☼ Exponential take off: R_0^n where n is the number of generations.
- ☼ Fantastically awful notation convention: R_0 and the R in *SIR*.

The PoCSverse
Biological Contagion
23 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References

Reproduction Number R_0

Discrete version:

- ☞ Set up: One Infective in a randomly mixing population of Susceptibles
- ☞ At time $t = 0$, single infective random bumps into a Susceptible
- ☞ Probability of transmission = β
- ☞ At time $t = 1$, single Infective remains infected with probability $1 - r$
- ☞ At time $t = k$, single Infective remains infected with probability $(1 - r)^k$

Reproduction Number R_0

Discrete version:

- ☞ Expected number infected by original infective:

$$R_0 = \beta + (1 - r)\beta + (1 - r)^2\beta + (1 - r)^3\beta + \dots$$

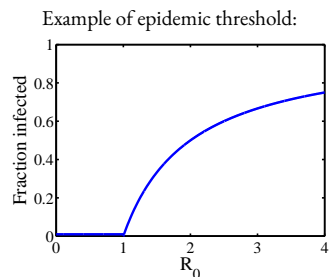
$$= \beta(1 + (1 - r) + (1 - r)^2 + (1 - r)^3 + \dots)$$

$$= \beta \frac{1}{1 - (1 - r)} = \beta/r$$

For $S(0) \approx 1$ initial susceptibles
 $(1 - S(0) = R(0) = \text{fraction initially immune})$:

$$R_0 = S(0)\beta/r$$

Independent Interaction models



- ☞ Continuous phase transition.
- ☞ Fine idea from a simple model.

Independent Interaction models

For the continuous version

- ☞ Second equation:

$$\frac{d}{dt} I = \beta SI - rI$$

$$\frac{d}{dt} I = (\beta S - r)I$$

- ☞ Number of infectives grows initially if

$$\beta S(0) - r > 0 \Rightarrow \beta S(0) > r \Rightarrow \beta S(0)/r > 1$$

where $S(0) \approx 1$.

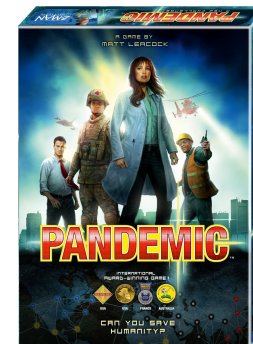
- ☞ Same story as for discrete model.

Independent Interaction models

Many variants of the SIR model:

- ☞ SIS: susceptible-infective-susceptible
- ☞ SIRS: susceptible-infective-recovered-susceptible
- ☞ compartment models (age or gender partitions)
- ☞ more categories such as 'exposed' (SEIRS)
- ☞ recruitment (migration, birth)

Save the world yourself:



- ☞ And you can be the virus.
- ☞ Also contagious?: Cooperative games ...

Neural reboot—Save another pretend world with Vax:

Lesson 4: Quarantine

Vaccines take time to 'kick in' so they're ineffective if an infection has already begun to spread.

Start >

VAX! Networks Epidemics Vaccines Quarantine

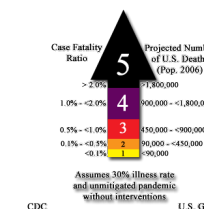
Independent Interaction models

Watch someone else pretend to save the world:



Pandemic severity index (PSI)

- ☞ Classification during/post pandemic:



- ☞ Category based.
- ☞ 1-5 scale.
- ☞ Modeled on the Saffir-Simpson hurricane scale .

The PoCSverse
 Biological Contagion
 24 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 27 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 30 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 25 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 28 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 31 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 26 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 29 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

The PoCSverse
 Biological Contagion
 33 of 92
 Introduction
 Simple disease spreading models
 Background
 Prediction
 More models
 Try metapopulation models
 Model output
 Numbell
 Other kinds of prediction
 SIR is the virus
 References

For novel diseases:

1. Can we predict the size of an epidemic?
2. How important is the reproduction number R_0 ?

R_0 approximately same for all of the following:

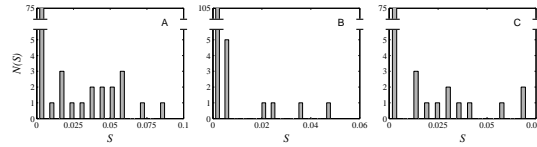
- 1918-19 “Spanish Flu” ~ 75,000,000 world-wide, 500,000 deaths in US.
- 1957-58 “Asian Flu” ~ 2,000,000 world-wide, 70,000 deaths in US.
- 1968-69 “Hong Kong Flu” ~ 1,000,000 world-wide, 34,000 deaths in US.
- 2003 “SARS Epidemic” ~ 800 deaths world-wide.

The PoCSverse
Biological Contagion
34 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Really not so good at all in Iceland

Epidemic size distributions $N(S)$ for Measles, Rubella, and Whooping Cough.

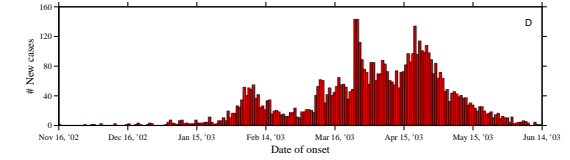


Spike near $S = 0$, relatively flat otherwise.

The PoCSverse
Biological Contagion
37 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Resurgence—example of SARS



- Epidemic slows... then an infective moves to a new context.
- Epidemic discovers new ‘pools’ of susceptibles: **Resurgence**.
- Importance of rare, stochastic events.**

The PoCSverse
Biological Contagion
40 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Size distributions

As we know, heavy-tailed size distributions are somewhat prevalent in complex systems:

- earthquakes (Gutenberg-Richter law)
- city sizes, forest fires, war fatalities
- wealth distributions
- ‘popularity’ (books, music, websites, ideas)
- Epidemics?**

Power law distributions are common but not obligatory...

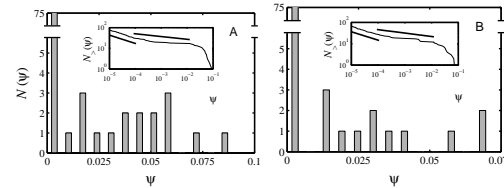
Really, what about epidemics?

- Simply hasn’t attracted much attention.
- Data not as clean as for other phenomena.

The PoCSverse
Biological Contagion
35 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Measles & Pertussis



Insert plots:
Complementary cumulative frequency distributions:

$$N(\Psi' > \Psi) \propto \Psi^{-\gamma+1}$$

Limited scaling with a possible break.

The PoCSverse
Biological Contagion
38 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

The challenge

So... can a simple model produce

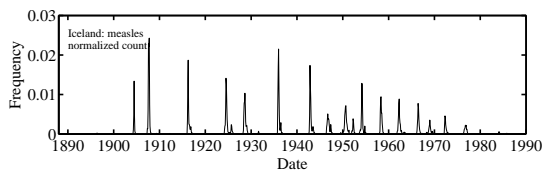
1. **broad epidemic distributions** and
2. **resurgence ?**

The PoCSverse
Biological Contagion
42 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Feeling Ill in Iceland

Caseload recorded monthly for range of diseases in Iceland, 1888-1990



Treat outbreaks separated in time as ‘novel’ diseases.

The PoCSverse
Biological Contagion
36 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Power law distributions

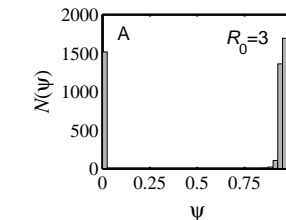
Measured values of γ :

- measles: **1.40** (low Ψ) and **1.13** (high Ψ)
- pertussis: **1.39** (low Ψ) and **1.16** (high Ψ)
- Expect $2 \leq \gamma < 3$ (finite mean, infinite variance)
- When $\gamma < 1$, can’t normalize
- Distribution is quite **flat**.

The PoCSverse
Biological Contagion
39 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Size distributions



Simple models typically produce **bimodal** or **unimodal** size distributions.

- This **includes** network models: random, small-world, scale-free, ...
- Exceptions:
 1. Forest fire models
 2. Sophisticated metapopulation models

The PoCSverse
Biological Contagion
43 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Try metapopulation models
- Model output
- Nanshell
- Other kinds of prediction
- SIR is the virus
- References

Burning through the population

Forest fire models: [19]

Rhodes & Anderson, 1996

The physicist's approach:

“if it works for magnets, it'll work for people...”

A bit of a stretch:

1. Epidemics ≡ forest fires spreading on 3-d and 5-d lattices.
2. Claim Iceland and Faroe Islands exhibit power law distributions for outbreaks.
3. Original forest fire model not completely understood.

The PoCSVerse
Biological Contagion
44 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

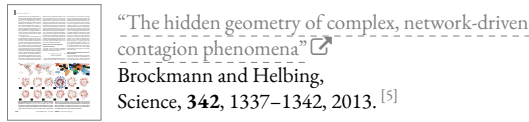
Model output

Nonhall

Other kinds of prediction

SIR is the virus

References



The PoCSVerse
Biological Contagion
47 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

Model output

Nonhall

Other kinds of prediction

SIR is the virus

References

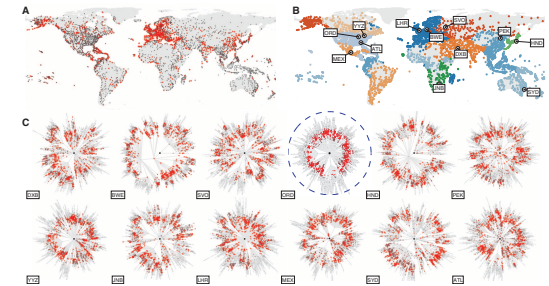


Fig. 3. Qualitative outbreak reconstruction based on effective distance. (A) Spatial distribution of prevalence $I(t)$ at time $T = 21$ days for OL Chicago (parameters $\beta = 0.28 \text{ day}^{-1}$, $R_0 = 1.5$, $\gamma = 2.8 \times 10^{-4} \text{ day}^{-1}$, and $\epsilon = 10^{-4}$). After this time, it is difficult, if not impossible, to determine the correct OL from snapshots of the dynamics. (B) Candidate OUs chosen from different geographic regions. (C) Panels depict the state of the system shown in (A) from the perspective of each candidate OU, using each OU's shortest path tree representation. Only the actual OL (OR), circled in blue, produces a circular wavefront. Even for comparable North American airports (Atlanta (ATL), Toronto (YYZ), and Mexico City (MEX)), the wavefronts are not nearly as concentric. Effective distances thus permit the extraction of the correct OL, based on information on the mobility network and a single snapshot of the dynamics.

The PoCSVerse
Biological Contagion
50 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

Model output

Nonhall

Other kinds of prediction

SIR is the virus

References



Size distributions

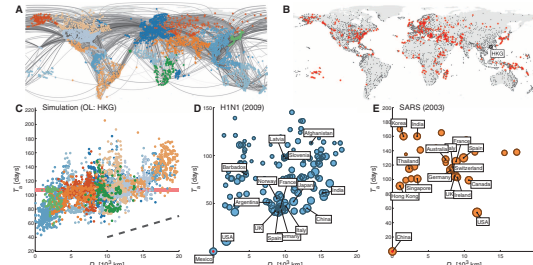
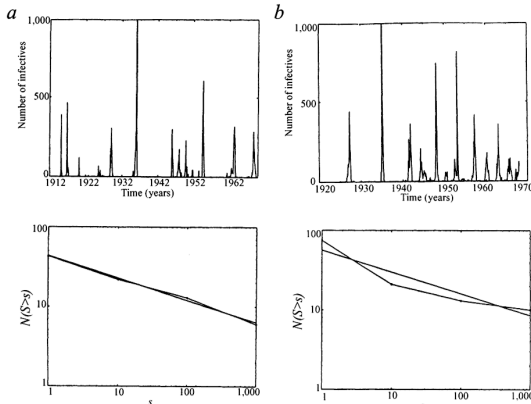


Fig. 1. Complexity in global, network-driven contagion phenomena. (A) The global mobility network (GMN). Gray lines represent passenger flows along direct connections between 4069 airports worldwide. Geographic regions are distinguished by color (classified according to network modularity maximization (99)). (B) Temporal snapshot of a simulated global pandemic with initial outbreak location (OL) in Hong Kong (HKG). The simulation is based on the metapopulation model defined by Eq. 3 with parameters $\beta_0 = 1.5$, $\beta = 0.285 \text{ day}^{-1}$, $\gamma = 2.8 \times 10^{-4} \text{ day}^{-1}$, $\epsilon = 10^{-4}$. Red symbols depict locations with epidemic arrival times in the time window $105 \text{ days} \leq T_i \leq 110 \text{ days}$. Because of the multiscale structure of the underlying network, the spatial distribution of disease prevalence (i.e., the fraction of infected individuals) lacks geometric coherence. No clear wavefront is visible, and based on this dynamic state, the OL cannot be easily deduced. (C) For the same simulation as in (B), the panel depicts arrival times T_i as a function of geographic distance $D_{i,OL}$ from the OL. Nodes are colored according to geographic region as in (A) for each of the 4069 nodes in the network. On a

The PoCSVerse
Biological Contagion
48 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

Model output

Nonhall

Other kinds of prediction

SIR is the virus

References



Size distributions

- Vital work but perhaps hard to generalize from... ⇒ Create a simple model involving multiscale travel
- Very big question: **What is N?**
- Should we model SARS in Hong Kong as spreading in a neighborhood, in Hong Kong, Asia, or the world?
- For simple models, we need to know the final size beforehand...

The PoCSVerse
Biological Contagion
51 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

Model output

Nonhall

Other kinds of prediction

SIR is the virus

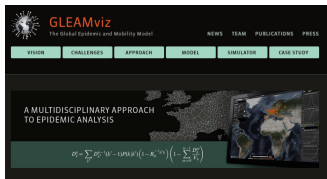
References



From Rhodes and Anderson, 1996.

Sophisticated metapopulation models:

- Multiscale models suggested earlier by others but not formalized (Bailey [1], Cliff and Haggett [6], Ferguson et al.)
- Community based mixing (two scales)—Longini. [17]
- Eubank et al.'s EpiSims/TRANSIMS—city simulations. [9]
- Spreading through countries—Airlines: Germann et al., Colizza et al. [7]



GLEAM: Global pandemic simulations by Vespignani et al.

The PoCSVerse
Biological Contagion
46 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

Model output

Nonhall

Other kinds of prediction

SIR is the virus

References

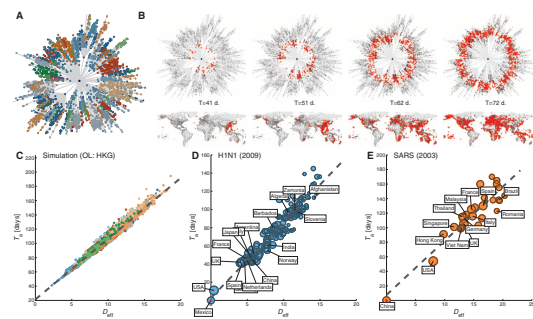


Fig. 2. Understanding global contagion phenomena using effective distance. (A) The structure of the shortest path tree in gray from Hong Kong (central node). Radial distance represents effective distance $D_{i,OL}$ as defined by Eq. 4 and 5. Nodes are colored according to the same scheme as in Fig. 1A. (B) The sequence from left to right of panels depicts the time course of a simulated disease with initial outbreak in Hong Kong (HKG), for the same parameter set as used in Fig. 1B. Prevalence is reflected by the redness of the symbols. Each panel compares the state of the system in the conventional geographic representation (bottom) with the effective distance representation (top). The complex spatial pattern in the conventional view is equivalent to a homogeneous wave that propagates outward, at constant effective speed in the effective distance representation. (C) Epidemic arrival time T_i versus effective distance $D_{i,OL}$ for the same simulated epidemic as in (B). In contrast to geographic distance (Fig. 1C), effective distance correlates strongly with arrival times ($R^2 = 0.973$). I.e., effective distance is an excellent predictor of arrival times. (D and E) Linear relationship between effective distance and arrival time for the 2009 H1N1 pandemic (D) and the 2003 SARS epidemic (E). The arrival time data are the same as in Fig. 1D and E. The effective distance was computed from the projected global mobility network between countries. As in the model system, we observe a strong correlation between arrival time and effective distance.

The PoCSVerse
Biological Contagion
49 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

Model output

Nonhall

Other kinds of prediction

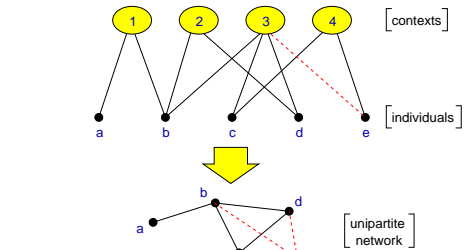
SIR is the virus

References



Improving simple models

Contexts and Identities—Bipartite networks



- boards of directors
- movies
- transportation modes (subway)

The PoCSVerse
Biological Contagion
53 of 92

Introduction

Simple disease spreading models

Background

Prediction

More models

Try metapopulation models

Model output

Nonhall

Other kinds of prediction

SIR is the virus

References



Improving simple models

Idea for social networks: incorporate identity

Identity is formed from attributes such as:

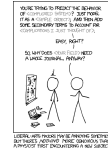
- Geographic location
- Type of employment
- Age
- Recreational activities

Groups are crucial...

- formed by people with at least one similar attribute
- Attributes ⇔ Contexts ⇔ Interactions ⇔ Networks. [23]

The PoCSverse
Biological Contagion
54 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References



A toy agent-based model:



“Multiscale, resurgent epidemics in a hierarchical metapopulation model”
Watts et al.,
Proc. Natl. Acad. Sci., **102**, 11157–11162, 2005. [24]

Geography: allow people to move between contexts

- Locally: standard SIR model with random mixing
- discrete time simulation
- β = infection probability
- γ = recovery probability
- P = probability of travel
- Movement distance:** $\Pr(d) \propto \exp(-d/\xi)$
- ξ = typical travel distance

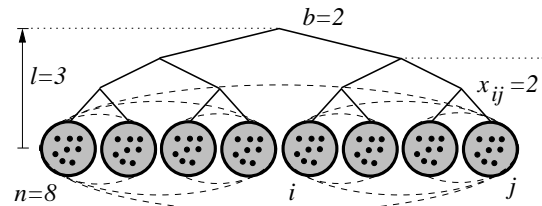
The PoCSverse
Biological Contagion
55 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References



A toy agent-based model

Schematic:



The PoCSverse
Biological Contagion
56 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References



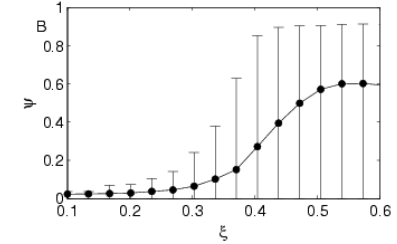
Model output

- Define P_0 = Expected number of infected individuals leaving initially infected context.
- Need $P_0 > 1$ for disease to spread (independent of R_0).
- Limit epidemic size by restricting frequency of travel and/or range

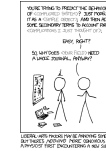


Model output

Varying ξ :



- Transition in expected final size based on typical movement distance (**sensible**)

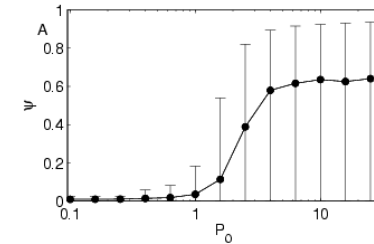


The PoCSverse
Biological Contagion
58 of 92

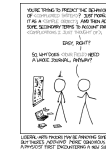
- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References

Model output

Varying P_0 :



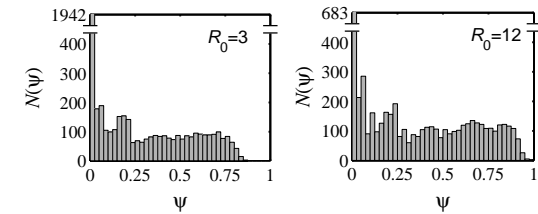
- Transition in expected final size based on typical number of infectives leaving first group (**also sensible**)
- Travel advisories: ξ has larger effect than P_0 .



The PoCSverse
Biological Contagion
60 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References

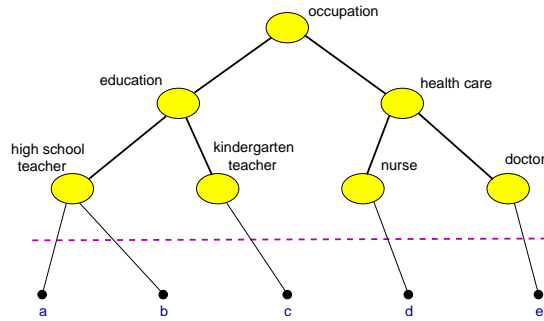
Example model output: size distributions



- Flat distributions are possible for certain ξ and P .
- Different R_0 's may produce similar distributions
- Same epidemic sizes may arise from different R_0 's

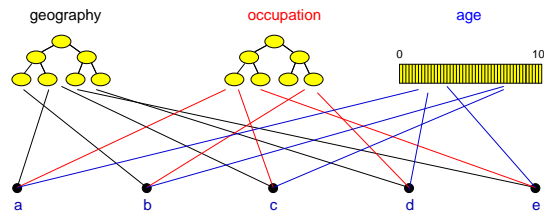


Infer interactions/network from identities



Distance makes sense in identity/context space.

Generalized context space



(Blau & Schwartz [3], Simmel [20], Breiger [4])



The PoCSverse
Biological Contagion
61 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References



The PoCSverse
Biological Contagion
62 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References



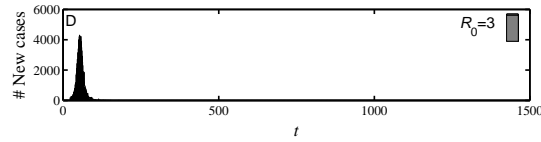
The PoCSverse
Biological Contagion
63 of 92

- Introduction
- Simple disease spreading models
- Background
- Prediction
- More models
- Toy metapopulation models**
- Model output
- Nullshell
- Other kinds of prediction
- SIR is the virus
- References



Model output—resurgence

Standard model:

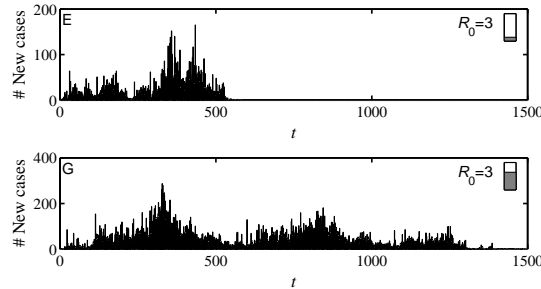


The PoCSverse
Biological Contagion
64 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



Model output—resurgence

Standard model with transport:



The PoCSverse
Biological Contagion
65 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



The upshot

Simple multiscale population structure
+
stochasticity

leads to

resurgence

+
broad epidemic size distributions

The PoCSverse
Biological Contagion
66 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



The Last of Us: Groups



The PoCSverse
Biological Contagion
67 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



The Last of Us: Groups



The PoCSverse
Biological Contagion
70 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



Nutshelling

- ☞ For the hierarchical movement model, epidemic size is highly unpredictable
- ☞ Model is more complicated than SIR but still simple.
- ☞ We haven't even included normal social responses such as travel bans and self-quarantine.
- ☞ The reproduction number R_0 is not terribly useful.
- ☞ R_0 , however measured, is not informative about
 1. how likely the observed epidemic size was,
 2. and how likely future epidemics will be.
- ☞ Problem: R_0 summarises one epidemic after the fact and unfolds movement, the price of bananas, everything.

The PoCSverse
Biological Contagion
72 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



Conclusions

- ☞ Disease's spread is highly sensitive to population structure.
- ☞ Rare events may matter enormously: e.g., an infected individual taking an international flight.
- ☞ More support for controlling population movement: e.g., travel advisories, quarantine

The PoCSverse
Biological Contagion
73 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



Nutshelling

What to do:

- ☞ Need to separate movement from disease
- ☞ R_0 needs a friend or two.
- ☞ Need $R_0 > 1$ and $P_0 > 1$ and ξ sufficiently large for disease to have a chance of spreading
- ☞ And in general: keep building up the kitchen sink models.

More wondering:

- ☞ Exactly how important are rare events in disease spreading?
- ☞ Again, what is N ?

The PoCSverse
Biological Contagion
74 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



Krugman, 1998: "Why most economists' predictions are wrong."



"The growth of the Internet will slow drastically, as the flaw in "Metcalfe's law"—which states that the number of potential connections in a network is proportional to the square of the number of participants—becomes apparent: most people have nothing to say to each other! By 2005 or so, it will become clear that the Internet's impact on the economy has been no greater than the fax machine's."¹

The PoCSverse
Biological Contagion
77 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Try metapopulation models
Model output
Nashell
Other kinds of prediction
SIR is the virus
References



¹<http://www.redherring.com/mag/issue55/economics.html>

Alan Greenspan (September 18, 2007):

“I’ve been dealing with these big mathematical models of forecasting the economy ...

If I could figure out a way to determine whether or not people are more fearful or changing to more euphoric,

I don’t need any of this other stuff.

I could forecast the economy better than any way I know.”



http://wikipedia.org

- The PoCSverse Biological Contagion 78 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



Greenspan continues:

“The trouble is that we can’t figure that out. I’ve been in the forecasting business for 50 years. I’m no better than I ever was, and nobody else is. Forecasting 50 years ago was as good or as bad as it is today. And the reason is that human nature hasn’t changed. We can’t improve ourselves.”

Jon Stewart:

“You just bummed the @!# out of me.”



wildbluffmedia.com

From the Daily Show (September 18, 2007)

The full episode is here: http://www.cc.com/video-clips/cenr5/the-daily-show-with-jon-stewart-alan-g

- The PoCSverse Biological Contagion 79 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References

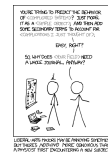


“Greenspan Concedes Error on Regulation”

- ...humbled Mr. Greenspan admitted that he had put too much faith in the self-correcting power of free markets ...
“Those of us who have looked to the self-interest of lending institutions to protect shareholders’ equity, myself included, are in a state of shocked disbelief”
Rep. Henry A. Waxman: “Do you feel that your ideology pushed you to make decisions that you wish you had not made?”
Mr. Greenspan conceded: “Yes, I’ve found a flaw. I don’t know how significant or permanent it is. But I’ve been very distressed by that fact.”

New York Times, October 23, 2008

- The PoCSverse Biological Contagion 80 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



James K. Galbraith:

NYT But there are at least 15,000 professional economists in this country, and you’re saying only two or three of them foresaw the mortgage crisis? [JKG] Ten or 12 would be closer than two or three.

NYT What does that say about the field of economics, which claims to be a science? [JKG] It’s an enormous blot on the reputation of the profession. There are thousands of economists. Most of them teach. And most of them teach a theoretical framework that has been shown to be fundamentally useless.

From the New York Times, 11/02/2008

“Waiter! There’s an SIR model ramdomly mixing in my soup.”¹

Other attempts to use SIR elsewhere:

- Adoption of ideas/beliefs (Goffman & Newell, 1964)
Spread of rumors (Daley & Kendall, 1965)
Diffusion of innovations (Bass, 1969)
Spread of fanatical behavior (Castillo-Chávez & Song, 2003)
Spread of Feynmann diagrams (Bettencourt et al., 2006)

Social contagion:

- SIR may apply sometimes ...
But we need new fundamental models.
Next up: Thresholds.

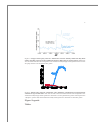
¹Apologies sir, I’m afraid our chefs can’t help themselves

We really should know social contagion is different but ...



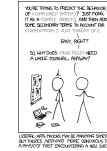
“It’s contagious: Rethinking a metaphor dialogically” Warren and Power, Culture & Psychology, 21, 359–379, 2015.

“Facebook will lose 80% of users by 2017, say Princeton researchers” (Guardian, 2014)



“Epidemiological modeling of online social network dynamics” Spechler and Cannarella, Available online at https://arxiv.org/abs/1401.4208, 2014.

- The PoCSverse Biological Contagion 81 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



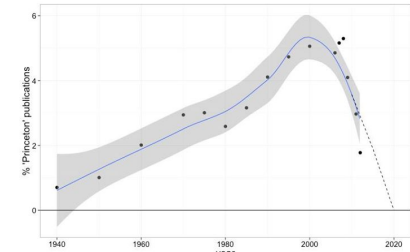
- The PoCSverse Biological Contagion 83 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



- The PoCSverse Biological Contagion 84 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



The Facebook Data Science team’s response



Mike Develin, Lada Adamic, and Sean Taylor.

- N. T. J. Bailey. The Mathematical Theory of Infectious Diseases and Its Applications. Griffin, London, Second edition, 1975.
F. Bass. A new product growth model for consumer durables. Manage. Sci., 15:215–227, 1969. pdf
P. M. Blau and J. E. Schwartz. Crosscutting Social Circles. Academic Press, Orlando, FL, 1984.
R. L. Breiger. The duality of persons and groups. Social Forces, 53(2):181–190, 1974. pdf

- D. Brockmann and D. Helbing. The hidden geometry of complex, network-driven contagion phenomena. Science, 342:1337–1342, 2013. pdf
A. D. Cliff, P. Haggett, J. K. Ord, and G. R. Versey. Spatial diffusion: an historical geography of epidemics in an island community. Cambridge University Press, Cambridge, UK, 1981.
V. Colizza, A. Barrat, M. Barthelmy, A.-J. Valleron, and A. Vespignani. Modeling the worldwide spread of pandemic influenza: Baseline case and containment interventions. PLoS Med., 4:e13, 2007. pdf

- The PoCSverse Biological Contagion 85 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



- The PoCSverse Biological Contagion 86 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



- The PoCSverse Biological Contagion 87 of 92 Introduction Simple disease spreading models Background Prediction More models Try metapopulation models Model output Nuts&shell Other kinds of prediction SIR is the virus References



References III

- [8] D. J. Daley and D. G. Kendall.
Stochastic rumours.
[J. Inst. Math. Appl.](#), 1:42–55, 1965.
- [9] S. Eubank, H. Guclu, V. S. A. Kumar, M. V. Marathe, A. Srinivasan, Z. Toroczka, and N. Wang.
Modelling disease outbreaks in realistic urban social networks.
[Nature](#), 429:180–184, 2004. [pdf](#)
- [10] J. Gleick.
The Information: A History, A Theory, A Flood.
Pantheon, 2011.
- [11] W. Goffman and V. A. Newill.
Generalization of epidemic theory: An application to the transmission of ideas.
[Nature](#), 204:225–228, 1964. [pdf](#)

References IV

- [12] E. Hoffer.
The True Believer: On The Nature Of Mass Movements.
Harper and Row, New York, 1951.
- [13] E. Hoffer.
The Passionate State of Mind: And Other Aphorisms.
Buccaneer Books, 1954.
- [14] W. O. Kermack and A. G. McKendrick.
A contribution to the mathematical theory of epidemics.
[Proc. R. Soc. Lond. A](#), 115:700–721, 1927. [pdf](#)
- [15] W. O. Kermack and A. G. McKendrick.
A contribution to the mathematical theory of epidemics. III. Further studies of the problem of endemicity.
[Proc. R. Soc. Lond. A](#), 141(843):94–122, 1927. [pdf](#)

The PoCSverse
Biological Contagion
88 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Toy metapopulation models
Model output
Nashell
Other kinds of prediction
SER is the virus
References



The PoCSverse
Biological Contagion
89 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Toy metapopulation models
Model output
Nashell
Other kinds of prediction
SER is the virus
References



References V

- [16] W. O. Kermack and A. G. McKendrick.
Contributions to the mathematical theory of epidemics. II. The problem of endemicity.
[Proc. R. Soc. Lond. A](#), 138(834):55–83, 1927. [pdf](#)
- [17] I. M. Longini.
A mathematical model for predicting the geographic spread of new infectious agents.
[Math. Biosci.](#), 90:367–383, 1988.
- [18] J. D. Murray.
Mathematical Biology.
Springer, New York, Third edition, 2002.
- [19] C. J. Rhodes and R. M. Anderson.
Power laws governing epidemics in isolated populations.
[Nature](#), 381:600–602, 1996. [pdf](#)

References VI

- [20] G. Simmel.
The number of members as determining the sociological form of the group. I.
[American Journal of Sociology](#), 8:1–46, 1902.
- [21] J. A. Spechler and J. Cannarella.
Epidemiological modeling of online social network dynamics.
Available online at <https://arxiv.org/abs/1401.4208>, 2014. [pdf](#)
- [22] Z. J. Warren and S. A. Power.
It's contagious: Rethinking a metaphor dialogically.
[Culture & Psychology](#), 21:359–379, 2015. [pdf](#)
- [23] D. J. Watts, P. S. Dodds, and M. E. J. Newman.
Identity and search in social networks.
[Science](#), 296:1302–1305, 2002. [pdf](#)

The PoCSverse
Biological Contagion
90 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Toy metapopulation models
Model output
Nashell
Other kinds of prediction
SER is the virus
References



The PoCSverse
Biological Contagion
91 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Toy metapopulation models
Model output
Nashell
Other kinds of prediction
SER is the virus
References



References VII

- [24] D. J. Watts, R. Muhamad, D. Medina, and P. S. Dodds.
Multiscale, resurgent epidemics in a hierarchical metapopulation model.
[Proc. Natl. Acad. Sci.](#), 102(32):11157–11162, 2005. [pdf](#)

The PoCSverse
Biological Contagion
92 of 92
Introduction
Simple disease spreading models
Background
Prediction
More models
Toy metapopulation models
Model output
Nashell
Other kinds of prediction
SER is the virus
References

